

MASTER README

Source data, Section 8 for Eggertsson, Mehrotra, & Robbins, "A Model of Secular Stagnation: Theory and Quantitative Evaluation"

DATA SOURCES

This folder contains the underlying data used to calibrate the quantitative secular stagnation model. The model requires a data series for US government debt (including state and local government debt), age-specific survival rates, total factor productivity, total fertility rate, and the age distribution of the population.

1. TOTAL FACTOR PRODUCTIVITY: (Column A, jr_tfp.xlsx) HP-filtered annual utilization adjusted total factor productivity (dtfp_util) from John G. Fernald, "A Quarterly, Utilization Adjusted Series on Total Factor Productivity." Available from <<https://www.frbsf.org/economic-research/indicators-data/total-factor-productivity-tfp/>>. This series is modified in two ways - the initial level of TFP in 1970 is set at the average from 1948-1974 and the final value of TFP is set at the average from 1975-1993. The optimistic series simply sets the terminal level of TFP to its 1948-1974 average.

2. GOVERNMENT DEBT: (Column B, jr_gdebt.xlsx) 5-year moving average of federal plus state and local government debt (% of GDP). Federal debt is FRED series, Gross Federal Debt as a Percent of Gross Domestic Product (GFDGDPA188S). State and local debt is imputed from 2012-13 data on state and local debt obtained from US Census Bureau's Survey of State and Local Governments. Available from <<https://www.census.gov/govs/local/index.html>>. The 2012 and 2013 average of state/local government debt is assumed to be a constant multiple of gross federal debt. A five-year centered moving average is taken to obtain the series in Column B.

3. TOTAL FERTILITY RATE: (Column A, jr_tfr.xlsx) 5-year centered moving average of 0.5 x US total fertility rate (births per woman). US total fertility rate from 1960-2015 obtained from World Bank World Development Indicator, series SP.DYN.TFRT.IN. Available from <<https://data.worldbank.org/indicator/SP.DYN.TFRT.IN?locations=US>>. US total fertility rate from 1945-1960 obtained from Centers for Disease Control Vital Statistics. Available from Table 1-7: <<https://www.cdc.gov/nchs/data/statab/t991x07.pdf>>.

4. SURVIVAL RATES: (Columns A-BD, jr_survival.csv) One-year age-specific survival probabilities by year (rows, 1970-2007) and columns are from age 25-80. Survival rates are obtained as 1-mortality rate within age-specific bins: 25-34, 35-44, 45-54, 55-64, 65-74, 75-84. For each year, survival rates by age are interpolated within age bins. Mortality (per 100,000 persons) within age bins by year reported by Centers for Disease Control, Vital Statistics. Available from

<<https://www.cdc.gov/nchs/nvss/mortality/gmwk23r.htm>> and
<<https://www.cdc.gov/nchs/nvss/mortality/hist290.htm>>.

5. US POPULATION PYRAMID: (Columns A-B, [us_census_pop.xlsx](#)) US population by age 25-81 in 1970 and 2015. Full population pyramid estimates by year available from US Census Bureau: <<https://www.census.gov/data/tables/time-series/demo/popest/pre-1980-national.html>>.

Instructions for running the Matlab code for Eggertsson, Mehrotra, & Robbins, "A Model of Secular Stagnation: Theory and Quantitative Evaluation"

SHORT INSTRUCTIONS FOR REPLICATION

Open the file `sec_stag_calibration_control_panel.m` in Matlab, press run. Table results will be stored in the "text_results" folder, and figure results will be stored in the "figures" folder. The exact tables and figures in Section 8 are found here:

Table 3 is replicated in `text_results/main_calib.txt`

Figure 7 is replicated in `figures/as_ad_out_main_calibration.png`

Tables 5-7 is replicated in `text_results/main_calibration_results.txt`

Figure 8 is replicated in `text_results/full_main_calibration_tables.csv`

Figure 9 is replicated in `text_results/baby_boom_main_calibration_tables.csv` and `figures/baby_boom_main_calibration_set7.png`

LONG INSTRUCTIONS FOR REPLICATION

The file `sec_stag_calibration_control_panel.m` is the master control file which does several things:

- (1) Calibrates the model for the main calibration
- (2) Runs the model, and automatically generates all tables and figures.

In order to run the model and generate all tables and figures from scratch, simply open `sec_stag_calibration_control_panel.m` in Matlab and press run.

By default the results do not produce transition dynamics given the time required. In order to run transition dynamics, set the option "run_transition" to 1 at the top of the program.

By default the program does not calibrate the model, but reads in pre-calibrated parameters. If the user wants to re-calibrate the model, simply set 'calibrate' to be 1 at the top of the program.

There are a number of additional controls that can be found in the program that control which results are run. These are controlled by the structural variable `controller_main`, and can be changed to perform a variety of different runs.

The overall structure of the program is somewhat complex; there are a variety of different functions and programs which are called by the main program. The following is a brief overview of the structure of the files.

The main function called in `sec_stag_calibration_control_panel.m` is `sec_stag_calibration.m`. This function, for a given set of parameters taken as an

argument, solves the model and returns an objective function equal to the difference between the model's moments and a set of data moments, which is a separate argument to the function.

To calibrate the model to 1970, `sec_stag_calibration_control_panel.m` optimizes over the objective function `sec_stag_calibration_1970`.

Once the model is calibrated, all the results are generated by calling the function `sec_stag_runmachine.m`. The actual results which are run are controlled by the argument (controller).

In order to calculate moments for a given run of the model, `set_stag_runmachine` will call the function `master_control.m`. This is a flexible program; depending on the argument given, it can calculate an initial steady state, a final steady state, or a transition.

BRIEF DESCRIPTION OF THE MAIN PROGRAMS

`ak_display.m` - Displays the output from the equilibrium.

`ak_display_control.m` - Controls the output displayed from `ak_display`.

`bequest_control.m` - Calculates bequests so the accounting is correct.

`calc_deriv.m` - Makes summary statistics.

`calc_elas.m` - Makes calculations for summary statistics.

`calculate_oldu.m` - Not used in the paper. Calculates utility for the LSRA.

`calculate_prices.m` - Updates aggregate prices, given aggregate quantities (first-order conditions for firm's problem).

`calculate_Q.m` - Calculates Tobin's Q and the interest rate.

`cb_nonl_cons.m` - When using `opt_control_matlab`, this function displays whether or not an individual satisfies the budget constraint.

`create_index.m` - Depending on whether we are running the initial steady state, transition, or final steady state, this calculates the correct index to use when looping through an individual's age.

`create_profile.m` - This program manages the equilibrium prices and quantities for a given iteration and puts them into easy to use structures and matrices.

`crrautil.m` - The CRRA utility function.

demog_comp.m - Not used in the paper. Calculates elasticity of savings with respect to population growth.

endog_fertility.m - Calculates fertility rates as in Auerbach & Kotlikoff, Chapter 11.

equil_update.m - This is a within-iteration program which calculates the equilibrium given a guess for aggregate levels of capital / labor.

genmhs.m - Calculates probability an individual survives.

gens.m - Calculates more survival probabilities.

getpv1_alt.m - Alternative way of calculating present value of income. Useful for calculating optimal consumption.

getpv1.m - Calculates present value of income. Useful for calculating optimal consumption.

getx1_alt.m, getx1.m - Calculates percentage of present value of income an individual consumes. Useful for calculating optimal consumption.

gov_dec.m - Sets the government decisions, i.e. taxes, spending, and the proportion of government revenue financed by the deficit (fiscal policy conditions).

graph_display.m - Displays graphs of the output for the transition.

initialize_iss.m - Sets the guesses for calculating the initial steady state.

initialize_fss.m - Sets the guesses for calculating the final steady state.

initialize_trans.m - Sets the guesses for calculating the transition.

kl_func.m - Only run for partial equilibrium runs. Finds the optimal capital to output ratio demanded by firms.

lsra.m - For welfare analysis, a "lump sum redistribution authority" redistributes income across generations. This is not used in the main text of the paper.

master_control.m - Program controls which equilibria are calculated.

nipa_display.m - Displays NIPA statistics from the model.

nipa_display_control.m - Controls the display of NIPA moments.

opt_control.m - Old version of calculating an individual's optimal consumption and savings decisions.

opt_control_final - Master control file for calculating an individual's consumption and savings decisions.

opt_control_matlab - Alternative way of calculating an individual's consumption and savings decisions from opt_control_final. This uses matlab's fmincon, but is much much slower than opt_control_final. These two methods yield the same results.

opt_lb.m, opt_lb_alt.m, olt_lb_final_calc.m, opt_lb_master.m - Calculate optimal consumption and bond holdings from individuals.

plot_adjust.m - Adjusts figures when plotting population and productivity growth.

pop_adjust.m - Makes adjustments to population figures.

prod_adjustment.m - Makes adjustment to productivity totals.

repeatfunc.m - Updates aggregate quantities and determines whether or not another iteration is run.

r_mult.m, r_mult_alt.m, r_mult_fin.m, r_mult_simp.m - Functions which multiplies interest rates.

recursive_solve.m, recursive_solve_alt.m - Programs to recursively solve consumption and investment problems.

set_stag_calibration.m - Calibrates the economy to the US in 2015.

sec_stag_calibration_1970.m - Calibrates the model to the US in 1970.

testing_nl.m - Tests the nonlinear budget constraint is satisfied. Called when solving optimization through MATLAB's fmincon.

test_crrautil.m - Called when solving optimization through fmincon.

ucalc.m - Calculates lifetime utility.

update_ssben.m - If a social security policy is specified, this calculates social security benefits.

update_sst.m - If a social security policy is specified, this calculates social security taxes.

Instructions for replication of Figure 5 and Appendix H in Eggertsson, Mehrotra, & Robbins, "A Model of Secular Stagnation: Theory and Quantitative Evaluation"

DATA

The underlying data in Figure 5 (blue starred lines) can be found in Figure 5.xlsx which contains separate spreadsheets for the US, Japan, and the Eurozone. The underlying data sources along with websites for downloading updated series are documented at the bottom of the spreadsheet.

MODEL

The key moments from the model used to plot the impulse response of the 3 period secular stagnation model are highlighted in light blue in the spreadsheets of Figure 5.xlsx. These moments are obtained from the matlab programs stag_US.m, stag_JP.m, and stag_EU.m. Each of these m-files numerically calibrate and solve the log-linearized three equation secular stagnation model with hysteresis. The details of the calibration are discussed in Appendix H. These m-files call the programs gx_hx.m and ir.m available from Stephanie Schmitt-Grohe and Martin Uribe <http://www.columbia.edu/~mu2166/1st_order/1st_order.htm>. The program computes the impulse response for output, inflation, and total factor productivity for each country.

The calculations in Figure 5.xlsx take these underlying moments for log-linear deviations from steady state and recover projections for output and inflation from the model.