

Radiative pyrolysis of wet wood under intermediate heat flux: experiments and modelling

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An experimental study of thermally thick biomass (beech wood spheres) pyrolysis under high radiative heat flux was performed. The influence of sample diameter (5 to 20 mm), incident heat flux (60 to 180 kW/m²) and initial moisture content (1 to 50 wt%) was studied. Char yields and temperature histories were monitored. Initial moisture content impact was highlighted. Indeed, steam coming from the sample core drying can gasify the external char layer, reducing therefore the char yield and increasing syngas production. This study was supported by a 2D unsteady numerical model of biomass degradation (mass, momentum and heat conservation coupled with Broido-Shafizadeh reaction scheme). This model gave more insight about phenomena occurring inside the degrading sample. It revealed that a pyrolysis front follows up a drying one. Therefore, steam is forced out of the sample through a high temperature char layer, making char steam gasification chemically possible.

Biomass | Pyrolysis | Radiative | Thermally thick | Steam gasification | Experiment| Modelling
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1. Introduction

With the increase in energy cost, mankind is looking for new and renewable energy sources. Among the different alternatives, biomass and solar energy emerge. Biomass is the fourth wider energy source available, after coal, oil and natural gas (1). It can be used to produce heat via combustion, methane via methanation or syngas via gasification. Furthermore, biomass is a renewable source of energy and its use has a near zero green house effect. There also are several ways of producing power thanks to solar energy. Without a concentration step, electricity is produced using photovoltaic modules. With a concentration step, extremely high temperatures are reached and thermally activated chemical reactions can be led, such as water cracking (2).

The combination of these two energy sources seems promising, more specifically, the combination of lignocellulosic biomass gasification and concentrated solar energy. Indeed, liquid fuel can be produced using syngas coming from biomass gasification. This syngas is produced at around 800 °C by gasifying char produced during biomass pyrolysis. Biomass transformation into syngas is currently performed in autothermal reactors. The needed heat for this endothermal process is classically produced by burning a fraction of biomass which results in a decrease of the conversion effi-

ciency to syngas. Gasification temperature are reachable using concentrated solar energy. Thus, gasification process can be powered thanks to solar energy.

Two major advantages come from this combination: syngas is free of combustion fumes and therefore not diluted by nitrogen and carbon dioxide. The produced fuel can be used on demand and therefore solar energy captured during the day is available at any time. Other advantages can be listed: syngas yield is higher than classical processes with respect to the inlet biomass (the currently burnt biomass would be gasified). The produced gas may be processed to obtain liquid fuel that is highly useful in transport applications.

The pyrolysis step which predates gasification or combustion, is important to understand, because the main products yields (gas, tar and char) dramatically depend on the pyrolysis condition. A high biomass heating rate will favor tar over char, as to a high final temperature will do the opposite. Char yield is a key feature to design a gasification process. It dictates the required quantity of heat and oxidizing agent to convert the biomass. The influence of pyrolysis conditions can be very subtle. Depending on its history, the produced char exhibits different chemical composition (1), chemical reactivity (3) or physical shape (porosity, mechanical failure, ...).

The number of studies on lignocellulosic biomass solar gasification increases. But, it remains low. First, image furnaces (either lamp or solar) have only been seen as a way to achieve very high heating rates through high radiative heat flux, e.g. 800 kW/m² (4–7). Nowadays, radiation is considered as a heat source by itself. The potential of several solar receivers for lignocellulosic biomass gasification has been assessed (8). Fluidized beds seem to be a promising technology (9, 10), but, small and similar particles are required (11, 12). Consequently, this process needs a well controlled grinding step. Dense packed bed reactors allow the use of larger biomass feedstock. In the case of fixed bed solar receiver, ash may turn out to be a real problem. Indeed they may form a radiative shield because of their high emissivity (10). Cyclonic (13) and tubular (14) reactors as well as rotating kilns (15) have also been tested. In order to design such reactors on a large scale, there is a need for characterizing single piece biomass behavior under high radiative power.

This paper presents an experimental and a numerical ap-

proach of thermally thick beech wood samples pyrolysis under radiant power. The influence of key parameters has been investigated. Beech samples, with diameters from 5 to 20 mm, have been exposed to mean incident heat flux ranging from 60 to 180 kW/m². Initial moisture content, ranging from 1 to 50 wt%, is demonstrated to have a major impact on sample temperature history and char yield. Thanks to sample final mass measurement and core temperature monitoring, char yield, drying, pyrolysis and heating times have been calculated.

2. Experimental

An image furnace was used to submit spherical wood samples with different diameters and different initial moisture contents to high radiative heat flux (5, 16). Two parameters were monitored: the final char mass and the core temperature history.

2.1. Experimental device

The used image furnace (Fig. 1 and Fig. 2) was first developed to study solids radiative properties at high temperature (17). This furnace consists of an elliptical mirror ($a = 150$ mm, $b = 50$ mm) which directs every ray coming from the 750 W tungsten lamp at first focus to the sample at second focus. The heat flux on the sample surface is theoretically not uniform because the elliptical reflector is a non imaging optical device. This device allows to reach average heat flux as high as 180 kW/m² on 5 mm diameter samples. Wood samples can reach 1000 K at the center with a 25 K/s heating rate.



Fig. 1. Experimental device. (1) power supply, (2) image furnace

Samples are placed so that the wood fiber direction are parallel to the ellipse semi-major axis. They are held by a 1 mm diameter K type thermocouple which monitors the sample core temperature. Lamp power can be adjusted to achieve heat flux ranging from 60 to 180 kW/m². The mirror walls are water cooled in order to control boundary conditions. A 400 ml/mn nitrogen sweep is used to ensure that the sample atmosphere is inert and to prevent tars from soiling the mirror.

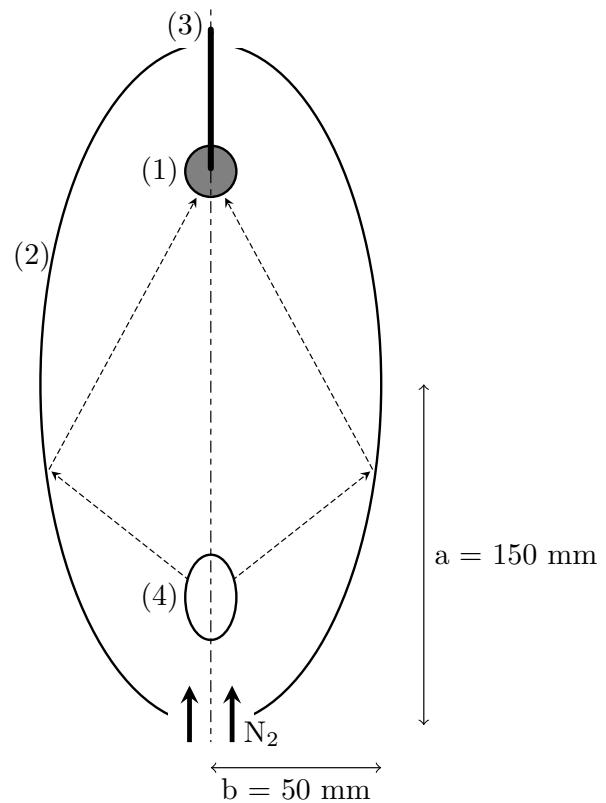


Fig. 2. Image furnace scheme. (1) sample, (2) mirror, (3) thermocouple, (4) lamp

2.2. Calibration

Thermally thin (Biot number of the steel sphere = 0.046) stainless steel spheres with a diameter of 5, 10 and 20 mm, were used to lead a calibration campaign. Thermal balance may be written as in Eq. 1 for a small Biot number body. Once steady state is reached, assuming that heat transfer is mainly radiative, equilibrium temperature can be linked to the mean incident heat flux as written in Eq. 2.

$$\rho V C p \frac{dT}{dt} = \alpha \phi S - \epsilon \sigma S (T^4 - T_{sur}^4) - h S (T - T_{nit}) \quad (1)$$

$$\epsilon \sigma S (T^4 - T_{sur}^4) = \alpha \phi S \quad (2)$$

In all radiative problem, emissivity and absorptivity are of great influence on the thermal behavior of the bodies. Oxidized stainless steel emissivity is 0.8 and does not vary much with temperature (18). Its absorptivity was measured using an integrating sphere from 530 nm to 25 μm mounted on a Bruker Vertex FTIR spectrometer; it is 0.80. The lamp spectrum was established in former work (19). It is distributed equally among the near infrared and the visible range. Beech wood and char reflectivities were also measured (Fig. 3) and their absorptivities with respect to the lamp spectrum were calculated. Beech wood absorptivity is 0.37 and char absorptivity is 0.88. Both measurements are in good agreement with reported values (20–23).

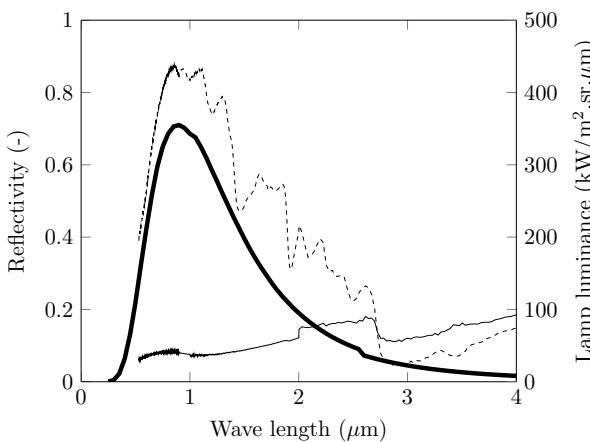


Fig. 3. Beech wood (dashed) and char (solid) infrared reflectivities. Tungsten lamp power spectral distribution (thick)

2.3. Sample characterization

A pack of beech wood spheres calibrated 10 and 20 mm diameter was purchased. Due to the impossibility to manufacture 5 mm diameter beech sphere, cylinders (height 5 mm, diameter 5mm) were used instead (Fig. 4). The wood spheres mass distribution and moisture were characterized. The mean density of the pack of sphere was $701 (\pm 59) \text{ kg/m}^3$. The initial wood moisture content was 9 wt%. It was modified in two ways. To reach 50 wt% moisture (close to the one when the wood is harvested) some of the spheres were immersed for 6 weeks in demineralized water. To reach almost zero moisture several spheres were dried out for 24 hours at 105 °C in a drying apparatus. Both batches were followed and mass was monitored until it reached a steady value.



Fig. 4. Samples before and after exposure. From left to right: 5 mm cylinder, 10 mm sphere and 20 mm sphere

2.4. Experimental procedure

The following procedure was strictly followed for every run:

- the virgin sample was drilled along wood fibers
- the virgin sample was weighted
- the lamp power was pre-tuned to set the desired incident heat flux, the sample was placed in the furnace, nitrogen flow rate was set
- oxygen was purged
- temperature monitoring and lamp power were turned on

- once the core temperature stabilized, power and temperature recording were turned off
- once the core temperature settled below 40 °C, the sample was taken out of the furnace
- the pyrolyzed sample was weighted and stored
- the furnace was cooled down and cleaned

Every measurement point was repeated at least three times.

2.5. Experimental results

Good repeatability can be achieved with this experimental set up as illustrated in figure 5.

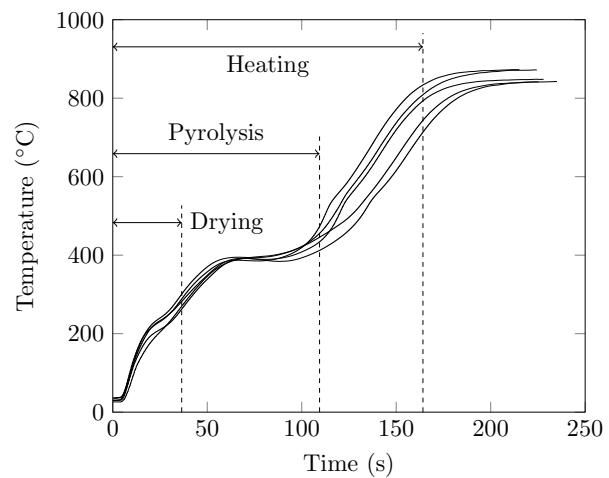


Fig. 5. Core temperature versus time. Heat flux: 120 kW/m^2 , initial moisture content: 9 wt%, sample diameter: 10 mm

This campaign has also shown that the sample position has to be accurately set. The nitrogen sweep flow rate has almost no impact on sample heating rate, which support the assumption of mainly radiative heat transfer occurs.

Let us also note that the sample geometry changes during a run. The charred sample is smaller than the initial wood one and has an oval shape (Fig. 4). Its mean diameter is 74% of the initial diameter; its volume is 40% of the initial one. These proportions are commonly found in literature (24).

2.5.1. Temperature histories. Figure 6 reports the core temperature histories. They exhibit different shapes depending on the initial moisture content. The main difference can be observed during the drying phase. Dried samples logically show no sign of deviation in the core temperature curve from 20 to 200 °C. An inflection can be found in core temperature profiles of the 9 wt% initial moisture content samples. It is due to the endothermicity of the drying process. However, there is not enough water to vaporize to create a temperature plateau. A still more pronounced plateau is found for the 50 wt% initial moisture content samples. The time required to heat and dry the 50 H₂O wt% samples is 4 times higher than the one to dry 9 H₂O wt% samples. This may have a strong impact on a large scale process.

Around 400 °C, temperature histories exhibit another variation (Fig. 7). These variations range from a temperature profile inflection point for 5 mm sample to a temperature plateau

for 10 and 20 mm samples. These behaviors are due to the pyrolysis endothermic reactions. At the end of the run, temperature histories also reach the same final core temperature. This may be explained by the fact that the final temperature only depends on the incident heat flux, the sample size and not on the initial moisture content.

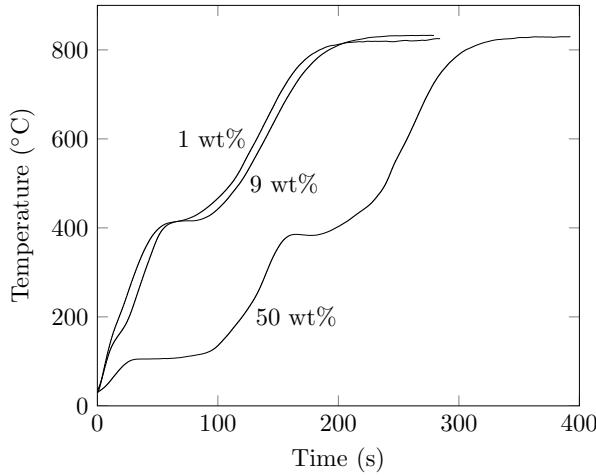


Fig. 6. Core temperature versus time for different initial moisture. Heat flux: 120 kW/m^2 , sample diameter: 10 mm

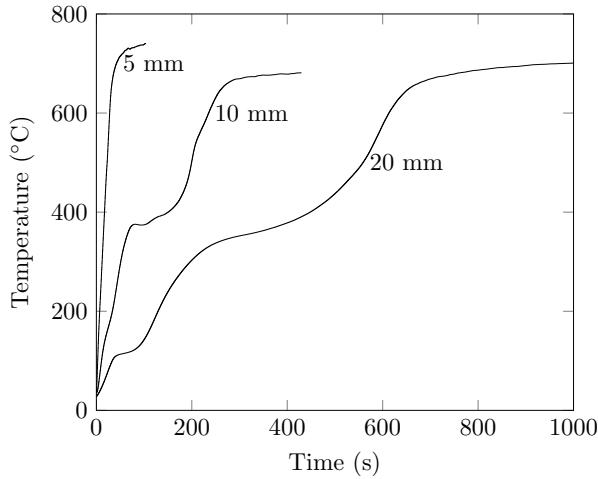


Fig. 7. Core temperature versus time for different sample diameter. Heat flux: 60 kW/m^2 , initial moisture content: 9 wt%

2.5.2. Final char yields analysis. The final char mass is the resulting sample mass minus ash. It is commonly divided by the initial wood mass to derive the char yield which is an important data for process design.

Final char yield analysis reveals an interesting behavior. First as one can see in figure 8, the larger the sphere size, the more char is produced. This results from the fact that larger sample diameter results in a lower heating rate. The char yield of a 20 mm diameter sample is twice that of a 5 mm sample. It may have an impact on large scale process feed preparation. The difference between heating rate also explains the fact that for a given sample diameter, the higher the incident heat flux, the less char is produced, as reported in

figure 9. This trend is in agreement with standard literature: a high heating rate leads to a small char yield.

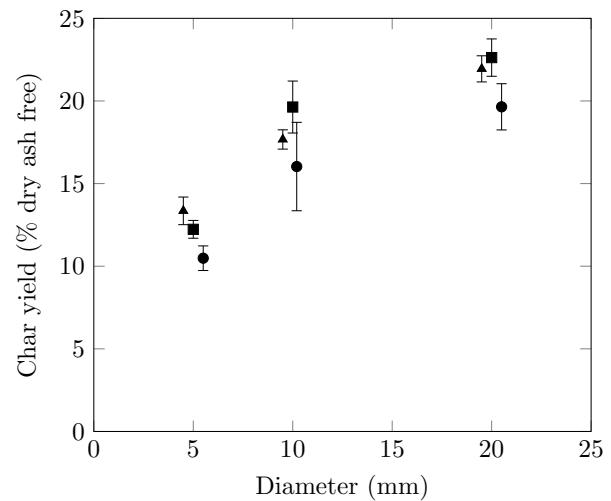


Fig. 8. Final char yield versus sample diameter. Heat flux: 60 kW/m^2 , initial moisture content: triangle = 0 wt%, square = 9 wt%, disk = 50 wt%

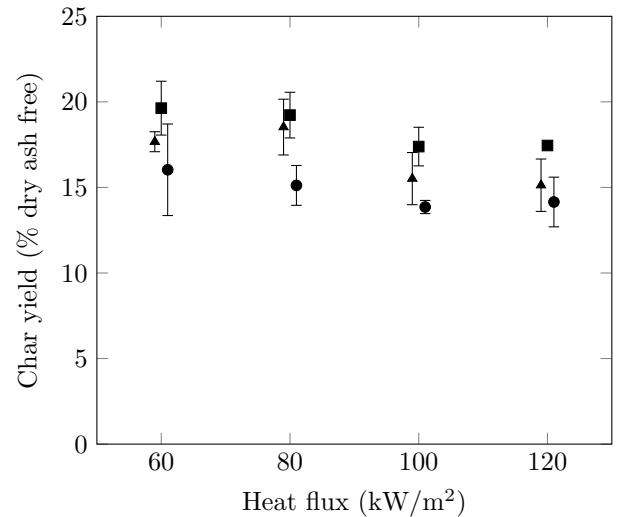


Fig. 9. Final char yield versus heat flux. Heat flux: varying, initial moisture content: triangle = 0 wt%, square = 9 wt%, disk = 50 wt%, sample diameter: 10 mm

One can note that the highest char yield is surprisingly obtained for the intermediate 9 wt% initial moisture content (Fig. 10): 1 wt% moisture sample exhibits lower char residues and 50 wt% moisture samples produce even less char residues.

The 1 wt% moisture behavior may be explained by the fact that there is no drying plateau (Fig. 6), so, compared to the 9 wt% sample, the sample heating rate is not lowered by the drying stage. Therefore, less char is produced. In order to explain the 50 wt% initial moisture content sample lower char yield, another mechanism can be suggested: steam gasification. The steam produced by drying would outflow through a high temperature char matrix close to the particule surface and gasify part of the char. To our knowledge, such a situation of direct char gasification by steam from drying inside a particule has not been reported in the literature before. Despite the inert atmosphere, not only pyrolysis would occur but

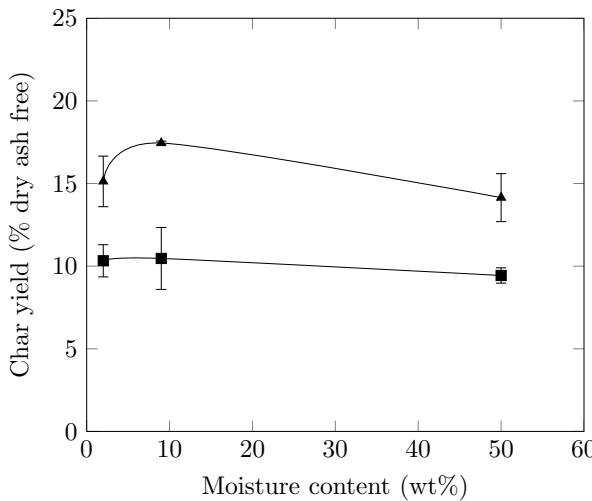


Fig. 10. Final char yield versus moisture content. Heat flux: 120 kW/m², initial moisture content: varying, sample diameter: square = 5 mm, triangle = 10 mm

coupled pyrolysis and steam gasification. Furthermore, a simple calculation shows that a 50 wt% moisture sample contains more than enough water to gasify the produced char.

2.5.3. Drying, pyrolysis and heating times. All of the results from the experimental campaign are recapitulated in table 1. One can find the char yield for every tested configuration. Whenever it was possible, we also provide the total drying, pyrolysis and heating times as defined in (Fig. 5); time evaluation method is available in appendix. Drying time is defined as the time required for the whole sample to dry. Pyrolysis time is defined as the time required for the core temperature to increase over the pyrolysis plateau temperature. One can still observe temperature inflections after the pyrolysis plateau (Fig. 5). These variations are attributed to the exothermic decomposition of lignin (25). We have decided not to take them into account when evaluating the pyrolysis time because these variations have not been always observed. Heating time is defined as the time required for the sample core to reach its maximum temperature. Table 1 also provides an indication of the data dispersion, defined as the ratio standard deviation / mean value. Data dispersion above 10% are notified. One can see that char yield is the most reliable result. Drying, pyrolysis and heating times are less reliable. The total heating time decreases with an increase of the incident heat flux. Even if expected tendencies are found, discrepancies are observed. The differences may come from several factors: sample positioning accuracy, thermocouple positioning inside the sample, sample mechanical failure. Mechanical failure during the sample heating phase (observed, but not reported here) allows radiative heat flux to penetrate inside of the sample.

3. Numerical model

A numerical model was developed in order to get more insight about radiative pyrolysis. This model includes heat and momentum balance, drying and pyrolysis chemical reactions. Steam gasification was not implemented. Solving the model

equations seemed barely feasible analytically, so a numerical approach was chosen. All the following work was realized using the opensource equation solver OpenFOAM.

3.1. Preliminary study

Some key dimensionless numbers were calculated in order to assess assumptions validity. The use of dimensionless numbers is not common in this field of research, only few authors mentioned it (4, 26, 27). The required properties values are either measured or taken from the literature (Table 2).

$$\begin{aligned} Bi &= \frac{\phi d}{\lambda \Delta T} = 4.9 \\ Re &= \frac{\rho_g \bar{u} \hat{d}_p}{\mu} = 4.6 \cdot 10^{-2} \\ Pe &= \frac{\xi \rho_g C p_g \hat{d}_p \bar{u}}{\lambda_g} = 0.18 \\ \pi &= \frac{\phi}{\rho_l w d k_{drying} \Delta h_{drying}} = 2.9 \cdot 10^{-2} \end{aligned}$$

These dimensionless numbers are used to assess the validity of key assumptions. Hence, they have been calculated in the most unfavorable cases. Biot number was assessed for wood in the longitudinal direction. The velocity used to calculate pore Reynolds and Péclet numbers is based on Darcy's law using the highest gas overpressure reported in the literature (Tab. 2).

From Biot number value, one can expect strong temperature gradient inside the sample. Reynolds number value validates the use of Darcy's law to model the flow inside the porous sample. Péclet number shows that local thermal equilibrium assumption is valid. Therefore, a unique temperature can be used to describe the problem (32). Finally π and Biot numbers show that between heat transfer and chemical kinetic, heat transfer should be the limiting step. Thus one can expect reaction fronts to appear during the process.

3.2. Physical properties values and pyrolysis reaction scheme

Being anisotropic materials, wood and char properties values should be specified in the three directions. There is no major difference between radial and azimuthal wood properties (28). Medium radial properties were determined by dividing longitudinal properties by a scalar factor: $\lambda_{radial} = \lambda_{longitudinal}/1.9$ (33) and $K_{radial} = K_{longitudinal}/9970$ (28).

Due to the large range of temperature across the sample, physical properties values should vary with temperature. It is the case for intrinsic heat capacity and thermal conductivity of both wood and char. One should note that wood and char are insulating material. Their thermal conductivities dramatically increase with the temperature due to internal radiation inside of the porous structure (34). Both wood and char thermal conductivities increase with respect to the temperature. This increase accounts for radiation contribution.

The following correlations were used to describe wood thermal conductivity and specific heat capacity:

Experimental conditions				Results		
Diameter (mm)	Moisture content (wt%)	Heat flux (kW/m ²)	Drying time (s)	Pyrolysis time (s)	Heating time (s)	Char yield (% daf)
1	60	-	29 [†]	44 [‡]	13	
	90	-	19 [†]	27 [†]	11	
	120	-	-*	28 [‡]	10	
	150	-	15 [†]	29 [‡]	10	
	180	-	16 [•]	22 [‡]	9 [†]	
5	9	60	12 [•]	27	36	12
	90	-*	19 [•]	25	10	
	120	-*	22 [•]	37 [‡]	10 [†]	
	150	6 [•]	17 [†]	30 [‡]	10	
	180	-*	18	31 [‡]	10	
50	50	60	-*	37	59 [†]	10
	90	10 [‡]	29	51 [†]	10	
	120	-*	23	36	9	
	150	7 [‡]	27 [†]	45 [†]	10	
	180	6 [†]	22	35	9	
10	1	60	-	144 [†]	198 [†]	18
	80	-	110 [†]	171 [†]	19	
	100	-	73 [‡]	110 [‡]	16	
	120	-	97	158	15 [†]	
	9	60	40 [‡]	155 [†]	231	20
50	80	31	125 [†]	185	19	
	100	26	87 [†]	142	17	
	120	24	111 [†]	189	17	
	50	60	74 [‡]	168 [‡]	225 [‡]	16 [†]
	80	126 [†]	244 [†]	341	15	
20	1	100	90	191	262	14
	9	120	102	218	286	14 [†]
	1	60	-	673	830	22
	9	60	94	525	676	23
	50	60	580	1335 [†]	1496	20

Table 1. Results summary. - data not available, * unable to extract data, • data based on a single run, † data dispersion between 10 and 20 %, ‡ data dispersion over 20 %

Symbol	Name	Value	Dimension	Reference
α	Char surface absorptivity	0.88	-	-
ϵ	Char surface emissivity	0.88	-	-
ξ_w	Wood porosity	0.51	-	-
ξ_c	Char porosity	0.85	-	-
T_s	Typical sample surface temperature	900	°C	-
T_{sur}	Surrounding typical temperature	50	°C	-
ΔT	Typical temperature difference	850	°C	-
d	Sample diameter	0.01	m	-
$\overline{\overline{D}}$	Gas dispersion tensor typical value	$8.45 \cdot 10^{-6}$	m^2/s	(28)
ϕ	Mean incident radiative heat flux	120	kW/m^2	-
ρ_w	Wood apparent density	701	kg/m^3	-
ΔP	Overpressure across the sample	30000	Pa	(29)
$\overline{\overline{K}_w}$	Wood permeability tensor typical value	$7.52 \cdot 10^{-13}$	m^2	(28)
$\overline{\overline{K}_c}$	Char permeability tensor typical value	$1.0 \cdot 10^{-11}$	m^2	(30)
\hat{d}_p	Mean pore diameter	$55.3 \cdot 10^{-6}$	m	(31)

Table 2. Physical properties values

$$Cp_w(T) = 2300 - 1150\exp(-0.0055T), \\ 20 < T(°C) < 240 \quad (35).$$

$$\lambda_{w,longitudinal}(T) = 0.291 + 0.000836 \times 0.33T, \\ 20 < T(°C) < 500 \quad (36).$$

The following correlations were set to describe char thermal conductivity and specific heat capacity:

$$Cp_c(T) = 1430 + 0.355T - 7.3210 \cdot 10^7 T^{-2},$$

$40 < T(^{\circ}\text{C}) < 700$ (37).

$$\lambda_{c, longitudinal}(T) = 2.3584 - 1.4962 \cdot 10^{-2}T + 3.8483 \cdot 10^{-5}T^2 - 4.3292 \cdot 10^{-8}T^3 + 1.8595 \cdot 10^{-11}T^4,$$

$$20 < T(^{\circ}\text{C}) < 600$$
 (33).

Effective thermal conductivities are calculated following Gauthier recommendations (33), using Saastamoinen and Richard model:

$$\lambda_{eff} = (1 - \xi^{2/3})\lambda_s + \frac{\xi^{2/3}}{\frac{1 - \xi^{1/3}}{2\lambda_s} + \frac{\xi^{1/3}}{\lambda_g}}$$

Physical properties were either calculated or taken from literature (Table 2).

Gas phase being a complex mixture, model molecules were used to describe it. Carbon monoxide was taken as model molecule for gas and benzene for tar. Gas phases physical properties evolution versus temperature were taken from the literature (38–45). These properties evolutions versus temperature are described using high order polynomial expression (Janaf). The authors have checked that even out of their validity range, these expressions provide reasonable values with an increasing trends with temperature.

Depending on the degree of thermal degradation, one can find wood and/or char at a given point of the computational domain. Solid matrix physical properties are assumed to be the weighted average between wood and char properties. For example :

$$\overline{\overline{K}_s} = \frac{\rho_w \overline{\overline{K}_w} + \rho_c \overline{\overline{K}_c}}{\rho_w + \rho_c} \quad (3)$$

Biomass pyrolysis is a complex thermochemical process involving more than 300 molecules (46). The products yields depend on many factors such as temperature, heating rate, pressure. Three main kinds of model exist; each consider biomass from a different point of view. The simplest models consider lumped species. These models can predict char, tar and gas yields, but not individual chemical molecule production. Other models consider the biomass as a mixture of cellulose, hemicellulose and lignin. These models allow a better prediction but require to know the different product yields beforehand. The last category are capable of predicting the production of individual species considering numerous chemical reactions. Nevertheless, their use is heavy to implement and no experimental feedback would have been possible in our case. Here, a modified Broido-Shafizadeh model was used (Fig. 11) (47). It assumes that the complexity of biomass pyrolysis can be modeled using macro-components: wood, tars, gas, intermediate solid and char. Tar cracking reactions are taken into account as they have been shown not to be negligible in the case of a thermally thick sample fast pyrolysis (48). Kinetic parameters may be found in Table 3.

3.3. Assumptions

Several assumptions were made in order to simplify the problem and solve it:

- the geometry is modeled by a 2D axisymmetrical mesh

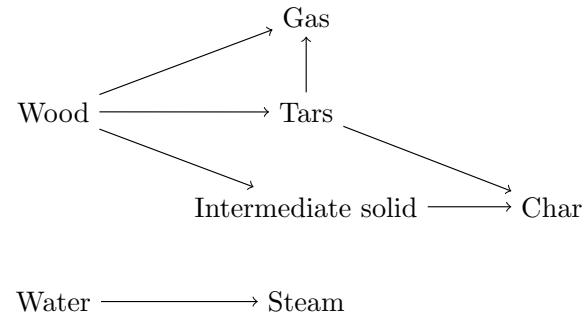


Fig. 11. Beech wood decomposition scheme (47)

(Fig. 12). As a first approach, one can assume that radial and azimuthal values are equal,

- Darcy's law is used to model the steam, gas and tar flow inside the sample,
- drying and pyrolysis reactions are modeled using first order kinetics and Arrhenius laws,
- a unique temperature will be used to describe fluid and solid temperature at a given point,
- matter diffusion heat transport and viscous dissipation heat will be neglected,
- liquid water motion will be neglected,
- gravity will be neglected,
- particle shrinkage will not be taken into account.

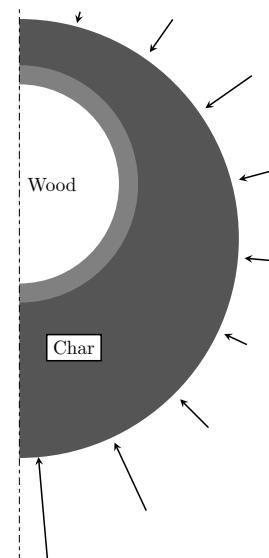


Fig. 12. Computational domain. Arrows: incident heat flux distribution

3.4. Equations and boundary conditions

Based on the former assumptions, the following coupled equations were solved.

3.4.1. Thermal balance.

$$(\rho C_p)_{eq} \frac{\partial T}{\partial t} + \rho_g C p_g \nabla \cdot (\vec{u} T) = -\nabla \cdot (-\overline{\overline{\lambda}_{eff}} \nabla T) + Q \quad (4)$$

$$(\rho C_p)_{eq} = \rho_s C p_s + \rho_g C p_g + \rho_l w C p_l w \quad (5)$$

Reaction	$k (s^{-1})$	$E_a (kJ/mol)$	$\Delta h (kJ/kg)$	Reference
Water \mapsto steam	$5.13 \cdot 10^6$	88.0	$-2.44 \cdot 10^3$	(49)
Wood \mapsto gas	$4.38 \cdot 10^9$	152.7	-80	(47)
Wood \mapsto tars	$1.08 \cdot 10^{10}$	148.0	-80	(47)
Wood \mapsto intermediate solid	$3.75 \cdot 10^6$	111.7	-80	(47)
Intermediate solid \mapsto char	$1.38 \cdot 10^{10}$	161.0	300	(47)
Tar \mapsto gas	$4.28 \cdot 10^6$	108.0	42	(47)
Tar \mapsto char	$1 \cdot 10^5$	108.0	42	(47)

Table 3. Kinetic parameters for water vaporisation and beech wood pyrolysis

With Q the heat source term :

$$Q = - \sum \Delta h_i \omega_i \quad (6)$$

The initial and boundary conditions are:

$$T(\vec{x}, 0) = T_0 = 293K \quad (7)$$

On the external boundary:

$$-\vec{n} \cdot (-\overline{\lambda_{eff}} \nabla T) = \alpha f(\beta) - \epsilon \sigma (T^4 - T_{sur}^4) \quad (8)$$

With $f(\beta)$ the incident heat flux around the sample (Fig. 13). It was determined using a ray tracing method. It can be seen that the incident heat flux close to the south pole is approximately 3.5 times higher than the average heat flux.

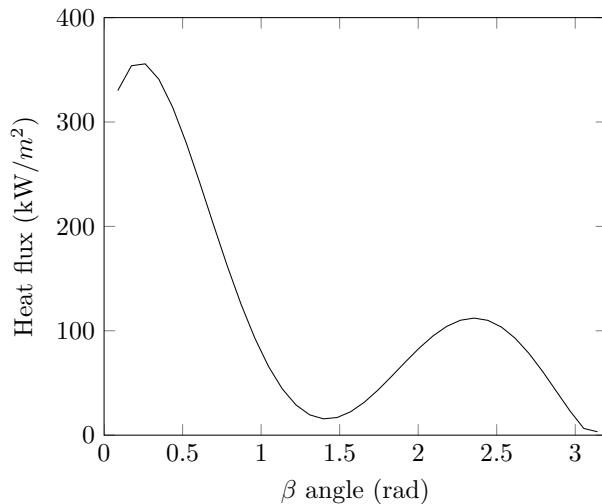


Fig. 13. Numerically calculated incident heat flux distribution around a 10 mm sample

3.4.2. Momentum balance and total gas phase mass continuity.

$$\xi \frac{M_g}{RT} \frac{\partial P}{\partial t} - \nabla \cdot (\rho_g \frac{\overline{K}}{\xi \mu} \nabla P) - \frac{\rho_g}{T} \frac{\partial T}{\partial t} = \sum_{i=1}^N \omega_i \quad (9)$$

$$\rho_g = \frac{PM_g}{RT} \xi \quad (10)$$

$$\vec{u} = -\frac{\overline{K}}{\xi \mu} \nabla P \quad (11)$$

Where $\frac{\xi \rho_g}{T} \frac{\partial T}{\partial t}$ accounts for thermal expansion pressure contribution.

The initial and boundary conditions are:

$$P(\vec{x}, 0) = 101325 Pa \quad (12)$$

On the external boundary:

$$P = 101325 Pa \quad (13)$$

3.4.3. Solid and gaseous phases continuity. The different species are modelled using density fields.

Solid (wood and char) and liquid (water) phases :

$$\frac{\partial \rho_i}{\partial t} = \omega_i \quad (14)$$

The initial and boundary conditions are (Table 4):

$$\rho_i(\vec{x}, 0) = \rho_{i0} \quad (15)$$

On the external boundary:

$$\nabla \rho_i = \vec{0} \quad (16)$$

Gaseous (steam, tars and gas) phases:

$$\frac{\partial \rho_g Y_i}{\partial t} + \nabla \cdot (\vec{u} \rho_g Y_i) = -\nabla \cdot (-\overline{D} \nabla \rho_g Y_i) + \omega_i \quad (17)$$

$$\omega_i = \sum_{j=1}^N \gamma_{ij} k_{ij} e^{-\frac{E_{a,j}}{RT}} \rho_i \rho_j \quad (18)$$

The initial and boundary conditions are (Table 4):

$$Y_i(\vec{x}, 0) = Y_{i0} \quad (19)$$

On the external boundary:

$$\nabla Y_i = \vec{0} \quad (20)$$

3.5. Results

The equations were solved using the CFD framework OpenFOAM. In this framework, partial differential equations are solved with a finite volume method. Mesh and time step convergence were checked before producing the following results.

Species	Initial apparent density (kg/m^3)	Initial mass fraction (-)
Wood	701	-
Char	0	-
Liquid water	70	-
Steam	-	0
Nitrogen	-	1
Tar	-	0
Gas	-	0

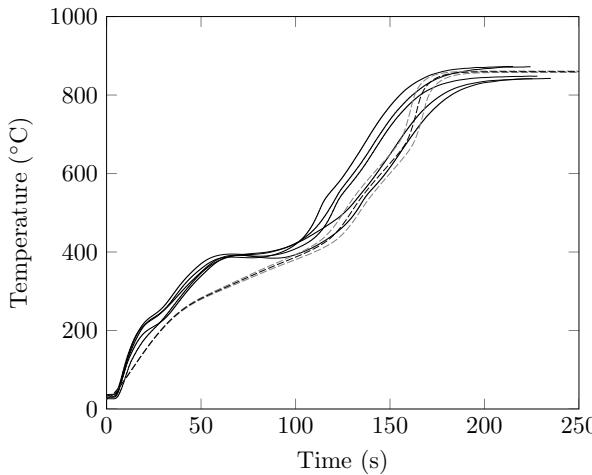
Table 4. Species initial conditions

Fig. 14. Core temperature versus time. Heat flux: 120 kW/m^2 , initial moisture content: 9 wt%, sample diameter: 10 mm. Thin lines: experimental results. Dotted line: numerical prediction (black), numerical prediction with $\pm 20\%$ on the char thermal conductivity (gray)

3.5.1. Temperature history. Figure 14 reports the predicted core temperature computed by the model and the experimentally measured one, in the case of a 10 mm diameter sample containing 9 wt% moisture exposed to a heat flux of 120 kW/m^2 .

The observed delay of the computed drying step compared to the experimental one can be explained by the simplification used in the model. Indeed, drying is a complex process (50) which was highly simplified using an Arrhenius law in this model.

The model predicts a temperature plateau around 400°C . This plateau is due to biomass endothermic degradation. It validates the choice of the kinetic parameters set to describe beech wood pyrolysis.

The predicted final core temperature trend is in good agreement with the experimental observations. This agreement has to be analyzed carefully. Indeed, it was experimentally observed that sample shrinkage is important. Hence, the incident heat flux at the sample surface variates during a run. The surface exposed to radiation decreases while the incident heat flux increases. The geometry and heat flux modification have opposite effects: the incident energy can possibly be roughly the same during a run. It would explain why the model prediction is in good agreement with experimental observation during the heating phase following the pyrolysis plateau. The simultaneous change in geometry and incident heat flux would also explain why the model predicts properly

the final core temperature.

3.5.2. Char yield. Figure 15 reports the numerically predicted char yield versus the incident heat flux. The model succeeds in capturing the trend and the values of the final char yield for different heat fluxes.

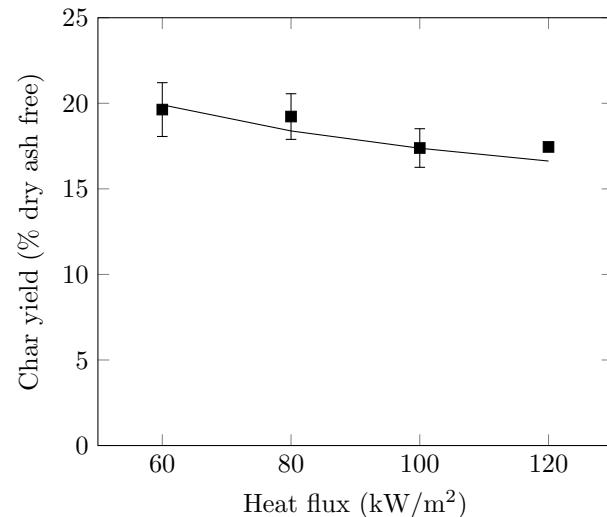


Fig. 15. Final char yield versus heat flux. Initial moisture content: 9 wt%, sample diameter: 10 mm. Square = experimental observations, solid line = numerical predictions

3.5.3. Internal fields. The model was used to predict the position of the pyrolysis front for a given time (Fig. 16 and 17): numerical front is located at 1.3 mm of the south pole and experimental one is at 1 mm of the south pole after 26 seconds of reaction. A time of 26 seconds was chosen due to technical feasibility and the fact that at this time the sample still has a spherical shape. It allows better comparison between numerical predictions and experimental observations, solid deformation not being taken into account. The discrepancy between the experimental observation and the numerical prediction has to be tempered by the fact that shrinkage was not taken into account in this numerical model. Indeed, if the numerically predicted length is corrected by the experimentally observed shrinkage factor, it becomes 0.95 mm, which is close to the experimental observation.

The model allows to investigate the eventual presence of a drying front prior to the pyrolysis front. Figure 18 plots the normal reaction rate, which is defined as: $\omega_{\text{norm}} = \omega_{lw}/\omega_{lw,\text{max}} + \omega_c/\omega_{c,\text{max}}$. From the numerical prediction, one can see a drying front followed by a pyrolysis front.

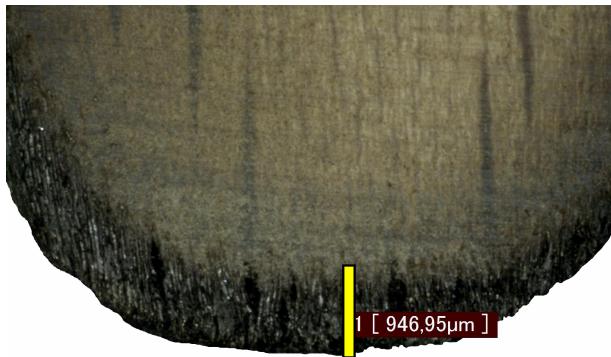


Fig. 16. Cut of a sample at south pole. Heat flux: 120 kW/m^2 , initial moisture content: 9 wt%, sample diameter: 10 mm, time: 26 s

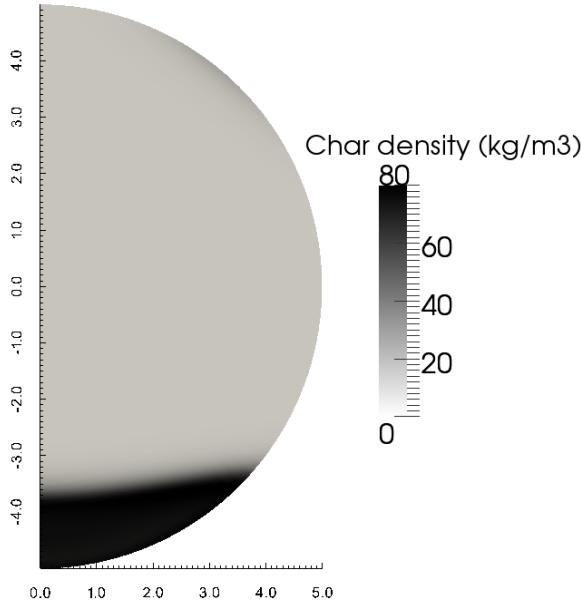


Fig. 17. Numerically predicted char density field. Heat flux: 120 kW/m^2 , initial moisture content: 9 wt%, sample diameter: 10 mm, time: 26 s

Therefore, the steam released by the drying front diffuses through the high temperature char layer produced by the pyrolysis front. This front was numerically evidenced in both 9 wt% and 50 wt% initial moisture content samples. In order to assess the validity of the experimental steam gasification of char observation, the sample south pole temperature and the steam density values were computed by the numerical model for a 50 wt% moisture sample (Fig. 19). One can see that steam is in contact with char at temperature higher than 800°C , up to 1200°C . Such temperature kinetically allows char steam-gasification reactions (not implemented in the model) to take place simultaneously with drying inside the sample. This observation correlates the former explanation.

Finally, one should note that the correlations for thermal conductivities, thermal capacities and gas phase viscosity are used out of their validity ranges. Sample core temperature reaches 900°C . At the same time, sample south pole temperature is around 1200°C . These temperatures are much higher

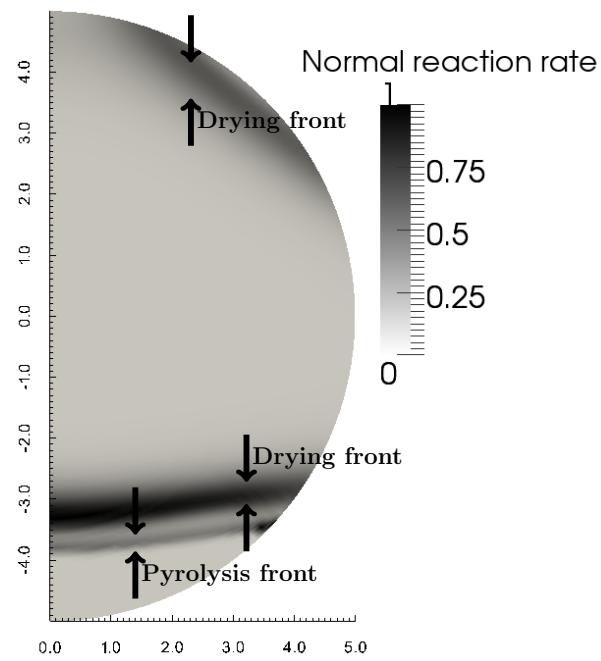


Fig. 18. Numerically predicted normal reaction rate ($\omega_{norm} = \omega_{tw}/\omega_{tw,max} + \omega_c/\omega_{c,max}$). Reaction fronts are located in the dark regions. Heat flux: 120 kW/m^2 , initial moisture content: 9 wt%, sample diameter: 10 mm, time: 26 s

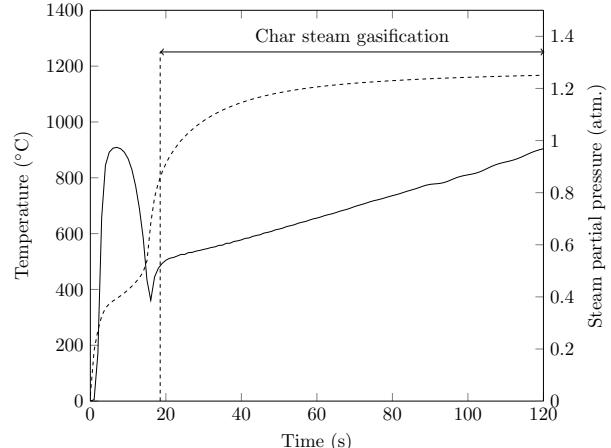


Fig. 19. Sample temperature (dashed line) and steam density (solid line) evolution versus time at south pole. The period when char steam gasification is chemically possible favored is indicated. Heat flux: 120 kW/m^2 , initial moisture content: 50 wt%, sample diameter: 10 mm

than the validity range upper limit of the used correlations. Not knowing precisely these properties is a concern because temperature controls wood degradation reactions rates, themselves controlling products yields. In order to assess the effect of the uncertainty in the key physical property value, char thermal conductivity was varied by $\pm 20\%$ (Fig. 14). Even with these variations, numerical model succeeds in capturing the core temperature trend and produces results in agreement with experimental observation.

4. Conclusion

The experimental apparatus enabled to submit beech wood particles to high radiative heat flux. The influence of sample diameter, initial moisture content and incident heat flux

on temperature history and char final yield was investigated. Wood moisture was identified as a key parameter. It has a considerable impact on the char production. Indeed, the water contained inside the sample, once vaporized, can gasify the external char layer.

The 2D unsteady numerical model predictions are in good agreement with the experimental observations. The model has also shown limitations. Shrinkage seems to be an important phenomenon that has to be taken into account. The selected biomass degradation scheme was not suited to properly predict char yield.

Nevertheless, this model evidences the presence of a drying front prior to the pyrolysis one. Its prediction lead to think that steam released during the drying step diffuses out through a high temperature char matrix and reacts with it. Therefore, numerical predictions conform the possibility of char steam-gasification by the water vapor coming from wood drying.

This particular behavior was evidenced under 120 kW/m^2 ; it can be expected to be even more important on a large scale industrial furnace reaching heat flux as high as 10 MW/m^2 . Therefore, the char production would be lowered and direct syngas production may be expected to increase. For further investigation, experimental studies under higher heat flux will be carried out. The improving of model predictions is subject to a better knowledge of char thermal properties at high temperature.

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Appendix - Time extraction method

In order to determine drying, pyrolysis and heating time, core temperature histories were analyzed. We consider that a phenomenon is over when the temperature reading at the sample core inflection stops. Indeed, for each of these phenomena an inflection in the temperature history can be observed (Fig. 20). Most of the time, drying is associated to an inflection around 300°C , pyrolysis to a plateau around 400°C and final heating time to a plateau at the end of the run. In order to have a repeatable method to determine times when phenomena were over, those times were derived from tangents crossing points. Indeed, one can draw tangents for every inflection of the temperature history (Fig. 20). The reported times are the abscissa at the tangents crossing points.

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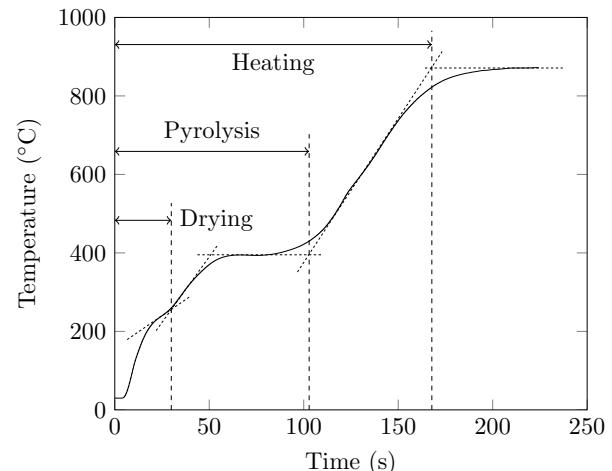


Fig. 20. Final times extraction method from a particle center time history. Heat flux: 120 kW/m^2 , initial moisture content: 9 wt%, sample diameter: 10 mm

Latin symbols

$\overline{\overline{A}}$	tensors	-
a	ellipse semi-major axis	m
b	ellipse semi-minor axis	m
C_p	specific heat capacity	J/kg/K
\overline{D}	mass diffusion tensor	m^2/s
\hat{d}_p	mean pore radius	m
d	sample diameter	m
E_a	activation energy	J/mol
$f(\beta)$	heat flux distribution around a sample	W/m^2
h	convection heat transfer coefficient	$W/m^2/K$
k	frequency factors	s^{-1}
\vec{n}	normal vector	-
K	permeability	m^2
P	pressure	Pa
Q	heat source term	W/m^3
R	ideal gas constant	J/mol/K
S	surface	m^2
V	volume	m^3
T	temperature	K
t	time	s
\vec{u}	intrinsic velocity vector	m/s
\vec{x}	position vector	m
Y	mass fraction	-

Greek symbols

α	absorptivity	-
β	angle	rad
Δh	reaction heat	J/kg
ΔP	typical pressure drop	Pa
ΔT	typical temperature difference	K
ϵ	emissivity	-
$\overline{\lambda}$	thermal conductivity tensor	$W/m/K$
μ	dynamic viscosity	Pa.s
ξ	porosity	-
ρ	apparent density	kg/m^3
σ	Stefan-Boltzmann constant	$W/m^2/K^4$
ϕ	heat flux	W/m^2
ω	reaction term	$kg/m^3/s$

Subscripts

c	char
eff	effective
g	gas phase
i,j	accounting for the different species (wood, char, liquid water, steam, tar, gas)
lw	liquid water
nit	nitrogen
p	pore
s	solid phase
sur	surrounding
w	wood

Table 5. Nomenclature

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