

```

void function_iterative(int n)
{
    while (n >= 1)
    {
        for (int i = 1; i <= n; i++)
            for (int j = 1; j <= n; j++)
                printf("*");
        n -= 3;
    }
}

```

$$T(n) = T(n-3) + O(n^2)$$

nr. de apeluri recursive $\approx k = \frac{n}{3}$

$$\Rightarrow T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots =$$

$$= \sum_{k=0}^{\frac{n}{3}} (n-3k)^2 = \sum_{k=0}^{\frac{n}{3}} (n^2 - 6kn + 9k^2) =$$

$$= \sum_{k=0}^{\frac{n}{3}} n^2 - \sum_{k=0}^{\frac{n}{3}} 6kn + \sum_{k=0}^{\frac{n}{3}} 9k^2$$

$$\sum_{k=0}^{\frac{n}{3}} n^2 = \left(\frac{n}{3} + 1\right) \cdot n^2 \Rightarrow O(n^3)$$

$$\sum_{k=0}^{\frac{n}{3}} 6kn = 6n \cdot \sum_{k=0}^{\frac{n}{3}} k = 6n \cdot \frac{\frac{n}{3} \left(\frac{n}{3} + 1\right)}{2}$$

$$\sum_{k=0}^{\frac{n}{3}} 9k^2 = 9 \cdot \frac{\frac{n}{3} \left(\frac{n}{3} + 1\right) \left(2 \cdot \frac{n}{3} + 1\right)}{6} \Rightarrow O(n^3)$$

Cum fiecare termen are $O(n^3) \Rightarrow$ și suma va
avea $O(n^3)$

$$T(n) \in O(n^3), T(n) \in \Omega(n^3) \Rightarrow T(n) = \Theta(n^3)$$