

Discussion 2/18: LL Parsing and Earley's Algorithm

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1. **LL Parsing Ambiguities.** An LL(k) grammar is a CFG used by a parser that scans input left-to-right (“L”), leftmost derivation (“L”), and uses k tokens of lookahead to predict the correct production. We’ve previously seen that a grammar is ambiguous if it has a parse tree that is not unique. A more formal definition of LL conflicts uses FIRST and FOLLOW sets.

- **FIRST(A):** the set of all terminals that could occur first in an expansion of the terminal or nonterminal A (include ϵ if A can expand to ϵ)
- **FOLLOW(A):** the set of all terminals that could follow an occurrence of the terminal or nonterminal A in a (partial) derivation

There are two main types of LL(1) conflicts:

- **FIRST/FIRST:** The FIRST sets of two different productions for same non-terminal intersect.
- **FIRST/FOLLOW:** The FIRST set of a grammar rule contains an epsilon and the intersection with its FOLLOW set is not empty.

Is the following grammar LL(1)? Justify your answer using FIRST and FOLLOW sets.

- $S \rightarrow Xd \quad X \rightarrow C \mid Ba \quad C \rightarrow \epsilon \quad B \rightarrow d$

2. **Resolving Conflicts.**

Consider the following grammar for numerical expressions with division, addition, and unary minus:

- $E \rightarrow Num \mid E/E \mid E + E \mid - E$
- (a) Rewrite the grammar so that it is LL(1), so that ‘/’ has higher precedence than ‘+’, and so that ‘-’ has highest precedence. ‘+’ and ‘/’ should be parsed in a right-associative way.
- (b) Compute the FIRST and FOLLOW sets for your re-written LL(1) grammar.

(c) Draw the LL(1) parsing table for the grammar. You may need the following rules:

- For each production $X \rightarrow A_1 \dots A_n$:
 - For each $1 \leq i \leq n$, and for each b in **First**(A_i): Set $T[X, b] = X \rightarrow A_1 \dots A_n$. Stop when ϵ is not in **First**(A_i).
 - If $A_1 \dots A_n \rightarrow^* \epsilon$, then for each b in **Follow**(X): Set $T[X, b] = \epsilon$.

3. Earley's Algorithm.

- Consider the following grammar:

$$\begin{aligned} P &\rightarrow E \mid \\ E &\rightarrow E + E \\ E &\rightarrow E * E \\ E &\rightarrow ID \end{aligned}$$

Use Earley's algorithm to parse $ID + ID * ID$ by filling out the chart below (you may not need all of the rows).

	ID		+	ID		*	ID	
	0	1	2	3	4	5		
a								
b								
c								
d								
e								
f								
g								
h								
i								
j								
k								
l								
m								

- Draw the accepting parse tree(s) and identify whether there are ambiguities in the grammar.