

CS 131 Compilers: Discussion 3: Top-Down Parsers

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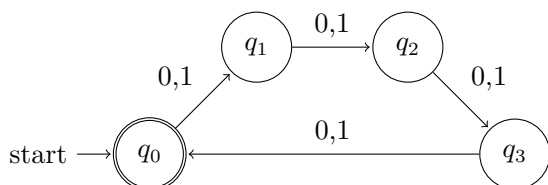
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1 DFA and NFA

1.1 Introduction

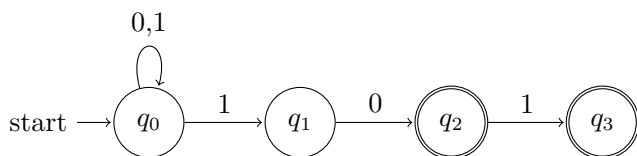
Finite state automata (FSA) are abstract machines that feature states and guarded transitions from one state to another. An FSA can only be in one state at a time, and its total number of states is finite. The machine takes transitions in response to inputs it receives sequentially; if an input matches the guard of a transition that departs from the current state that transition is said to be enabled; only enabled transitions can be taken. FSA that have an accepting state provide the machinery to determine whether an input string is in a regular language. If no transitions are enabled by a given input then the entire input string gets rejected. If all inputs are processed and the FSA is in an accepting state then the entire input string is accepted. Deterministic finite state automata (DFA) can only have one enabled transition at a time while a non-deterministic finite state automata (NFA) can have multiple.

1.2 What language is accepted by the following DFA?



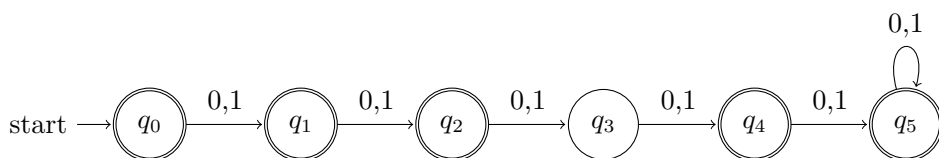
Answer:

1.3 What language is accepted by the following NFA?



Answer:

1.4 What language is accepted by the following NFA?



Answer:

1.5 Construct the NFA that accepts

1.5.1 $x(zy^?|(yz)^*)$

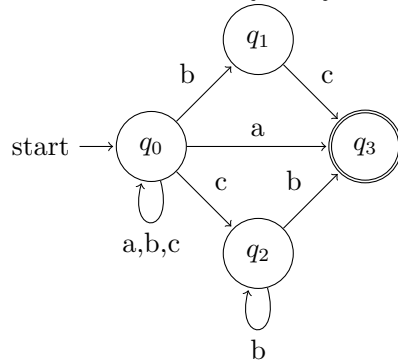
Answer:

1.5.2 $(10)^* 1^* 01^* 0$

Answer:

1.6 Minimized the NFA

1. Original NFA, $\Sigma = \{a, b, c\}$:



Answer:

2 Pumpingg Lemma

Pumping Lemma: For any DFA (or NFA or regular expression) that accepts an infinite number of strings, there is some minimum length, M , such that any string with length greater than or equal to M that the machine accepts must have the form uxv , where u, x , and v are strings, x is not empty, the length of ux is $\leq M$, and the machine accepts all strings of the form $ux^n v$, for all $n \geq 0$.

2.1 Proof of not regular

Let $A = \{1^j z \mid z \in \{0, 1\}^* \text{ and } z \text{ contains at most } j \text{ 1's, for any } j \geq 1\}$. Prove, by the pumping lemma, that A is not regular.

Answer:

<http://pfmiles.github.io/blog/left-recursion-removal-using-kleene-closure/>