# Neuralizing Regular Expressions

Extracurricular Material



#### Outline

Chengyue Jiang, Yinggong Zhao, Shanbo Chu, Libin Shen, and Kewei Tu, "Cold-start and Interpretability: Turning Regular Expressions into Trainable Recurrent Neural Networks", EMNLP 2020.



# Regular Expressions (RE)

- One of the most representative and useful forms of symbolic rules
- Widely used in practice: text classification, slot filling, etc.

Label	[distance]
RE	\$*(how (far   long )   distance) \$*
Matched	(BOS) tell me how far is oakland air-
Text	port from downtown (EOS)



# Regular Expressions (RE)

- Pros
  - Highly interpretable
  - Support fine-grained diagnosis and manipulation
    - Easy to add/delete/revise rules to quickly adapt to changes in task specification
  - No need for training
    - Hence no need for data annotation, less computational cost
    - Good for cold-start scenarios
- Cons
  - Rely on human experts to write
  - Often: high precision but low recall
  - Cannot evolve by training on labeled data when available
    - Underperform neural approaches in rich-resource scenarios

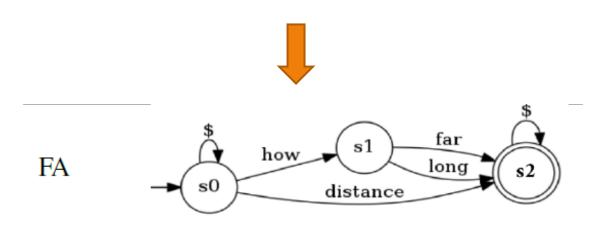
#### Our Idea

- Convert a RE to a new form of recurrent neural networks
  - Roughly equivalent to RE
    - ✓ Can still be used in cold-start scenarios
  - Trainable on labeled data
    - Can outperform REs and compete with neural approaches in rich-resource scenarios
  - Can be converted back to RE
    - ✓ Possibility of fine-grained manipulation
- Let's start with classification...

# Step 1. RE to Finite Automaton (FA)

Any RE can be converted into a FA that expresses the same language

Label	[distance]
RE	<b>\$*(how ( far   long )   distance) \$*</b>



#### FA parameters

 Binary transition tensor:

$$T \in \mathbb{R}^{V \times K \times K}$$

Binary start vector:

$$\alpha_0 \in \mathbb{R}^K$$

Binary final vector:

$$\alpha_{\infty} \in \mathbb{R}^K$$

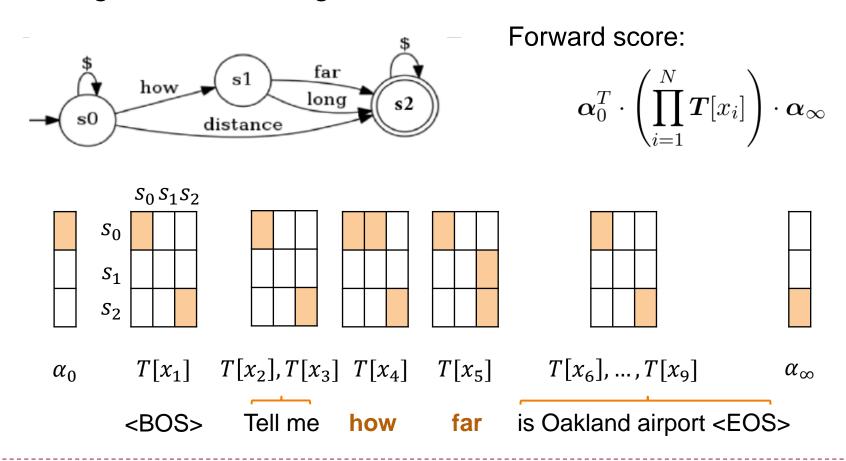
V: vocabulary size

*K*: state number



# Step 2. FA as Recurrent Neural Network (RNN)

 Score of a FA accepting a sentence can be calculated using the forward algorithm



# Step 2. FA as Recurrent Neural Network (RNN)

The computation can be rewritten into a recurrent form

$$oldsymbol{lpha}_0^T \cdot \left(\prod_{i=1}^N oldsymbol{T}[x_i]
ight) \cdot oldsymbol{lpha}_{\infty}$$



$$m{h_0} = m{lpha}_0^T$$
  $m{h_t} = m{h_{t-1}} \cdot m{T}[x_t], \ 1 \leq t \leq N$  (recurrent step)

$$\mathcal{B}_{ ext{forward}}(\mathcal{A}, oldsymbol{x}) = oldsymbol{h}_N \cdot oldsymbol{lpha}_{\infty}$$

# Step 3. Decomposing the Parameter Tensor

 Goal: reduce the computational complexity to match that of traditional RNN

Tensor Rank
Decomposition

$$m{T} \in \mathbb{R}^{V imes K imes K} m{E}_{\mathcal{R}} \in \mathbb{R}^{V imes r}, m{D}_1 \in \mathbb{R}^{K imes r}, m{D}_2 \in \mathbb{R}^{K imes r}$$
 (word embedding) (state embeddings)

Now the recurrent step becomes:

$$egin{aligned} oldsymbol{v}_t &= oldsymbol{E}_{\mathcal{R}}(x_t) \ oldsymbol{h}_t &= oldsymbol{h}_{t-1} \cdot oldsymbol{T}[x_t] & \longrightarrow & oldsymbol{a} &= (oldsymbol{h}_{t-1} \cdot oldsymbol{D}_1) \circ oldsymbol{v}_t \ oldsymbol{h}_t &= oldsymbol{a} \cdot oldsymbol{D}_2^T \end{aligned}$$



### Step 4. Integrating Pretrained Word Embedding

- Goal: bringing external lexical knowledge into our model
- Method:
  - Approximate  $E_{\mathcal{R}}$  with  $E_{w}G$  external word embedding
- initialized with  $E_w^{\dagger} E_{\mathcal{R}}$  $E_w^{\dagger}$  is the pseudo-inverse of  $E_w$

- Interpolate  $E_{\mathcal{R}}$  and  $E_{\mathcal{W}}G$
- The recurrent step becomes:

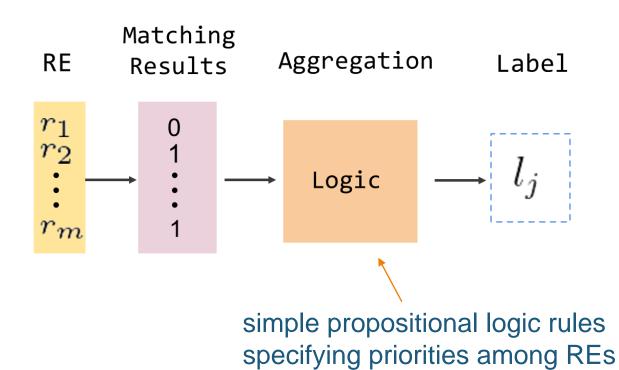
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$$egin{aligned} oldsymbol{v}_t &= oldsymbol{E}_{\mathcal{R}}(x_t) & oldsymbol{u}_t &= oldsymbol{E}_w(x_t) \ oldsymbol{z}_t &= eta oldsymbol{v}_t + (1-eta) oldsymbol{u}_t oldsymbol{G} \ oldsymbol{a} &= (oldsymbol{h}_{t-1} \cdot oldsymbol{D}_1) \circ oldsymbol{z}_t \ oldsymbol{h}_t &= oldsymbol{a} \cdot oldsymbol{D}_2^T \ oldsymbol{FA-RNN} \end{aligned}$$

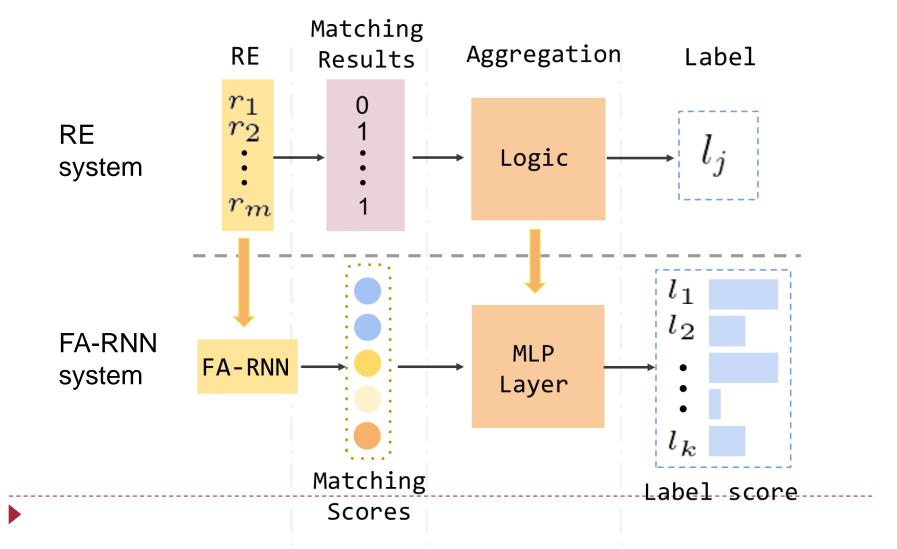
#### **FA-RNN Extensions**

- Gated extension
  - Add forget gate and reset gate like in GRU
  - Initialize parameters to make the gates inactive initially
- Combine two FA-RNNs of opposite directions
  - Create a left-to-right FA-RNN from the RE
  - Create a right-to-left FA-RNN from the reversed RE
  - Output the average score of the two FA-RNNs

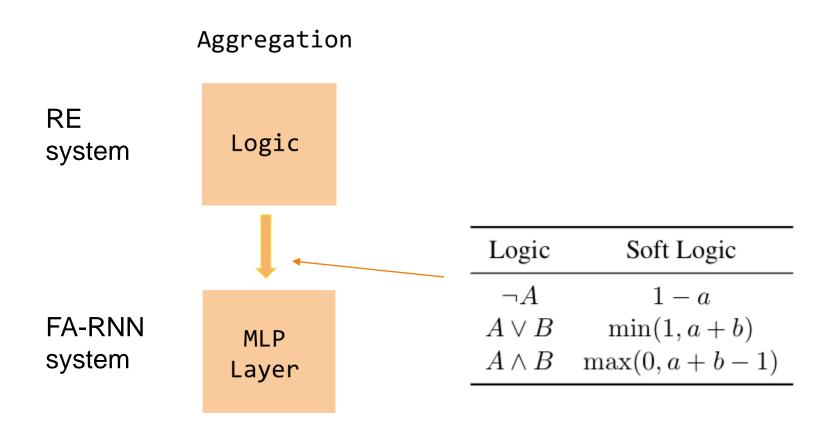
- An RE system for text classification:
  - Aggregating results from multiple REs to form a prediction



From a RE system to a FA-RNN system

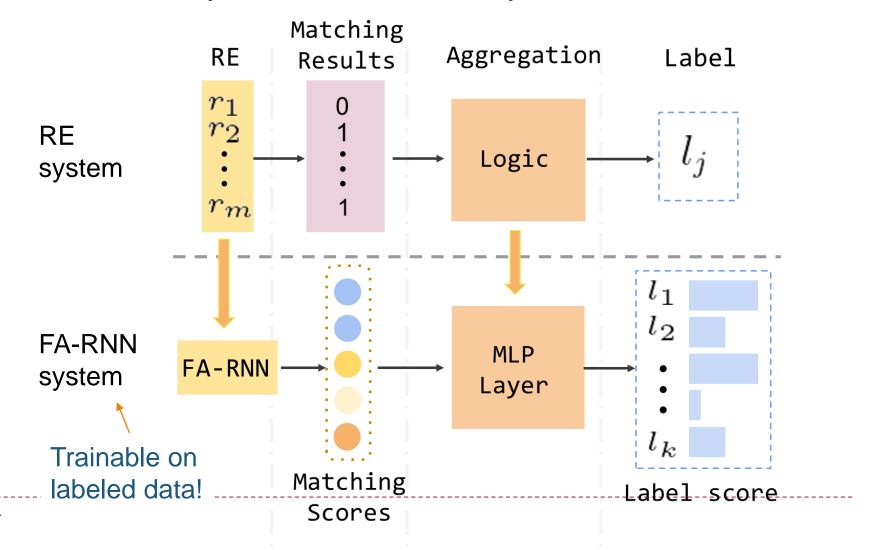


From a RE system to a FA-RNN system





From a RE system to a FA-RNN system



### Experiments

- Three intent classification datasets:
  - ATIS, QC (TREC-6), SMS
- Baselines
  - Bi-RNN/GRU/LSTM, CNN, DAN
  - RE-enhanced NN (+i, +o, +io) [Luo et al., 2016]
  - Knowledge Distillation (+kd, +pr) [Hinton et al,.2015; Hu et al,. 2016]

# Experiments – Zero-Shot

ATIS	QC	SMS
87.01	64.40	93.20
86.53	61.95	93.00
86.81	62.90	93.20
88.10	62.90	93.00
88.63	62.90	93.20
1.34	18.75	11.90
30.74	27.50	30.40
38.69	25.70	73.25
9.94	17.70	53.00
9.94	17.70	53.00
	87.01 86.53 86.81 88.10 88.63 1.34 30.74 38.69 9.94	87.01 64.40 86.53 61.95 86.81 62.90 88.10 62.90 88.63 62.90 1.34 18.75 30.74 27.50 38.69 25.70 9.94 17.70

# Experiments – Low-Resource and Full Training

	ATIS (26-class)			Q	QC (6-class)		SMS (2-class)		
	1%	10%	100%	1%	10%	100%	1%	10%	100%
FA-RNN	90.43	90.79	96.52	67.75	79.6	91.3	93.1	96.75	98.8
FA-GRU	88.94	90.85	96.61	66.2	80.7	91.85	94.25	96.8	99.2
BiFA-RNN	89.31	90.85	96.72	57.65	81.5	91.55	91.7	96.7	99
BiFA-GRU	90.62	90.26	96.64	64.15	82.8	92.4	93.9	96.75	98.8
CNN	71.61	86.09	94.74	50.9	74.9	89.25	89.85	95.9	98.8
DAN	71.02	83.68	90.4	47.25	65.4	77.8	89.9	93.7	98.6
RNN	70.91	75.17	91.55	22.4	67.9	85	85.1	89.85	97.75
LSTM	69.37	78.14	95.72	40.45	75.75	90	86.2	95.75	97.85
GRU	70.72	88.52	96.3	42.35	79.75	91.2	86.15	95.55	98.05
BiRNN	70.72	79.98	93.39	49.35	75.95	87.35	86.75	94.9	97.8
BiLSTM	70.77	87.12	96.25	55.95	76.75	90.95	92.15	95.8	97.7
BiGRU	70.69	88.35	96.75	62.7	80.05	91.5	89.6	95.95	98.4
BiGRU +i	82.84	90.01	96.56	66.3	80.25	92	90.95	96.75	98.55
BiGRU +o	80.21	89.22	96.33	60.15	80.2	91.7	90.6	95.95	98.4
BiGRU +io	82.61	89.95	95.46	65.05	79.65	90.7	93.85	96.75	98.25
BiGRU +pr	72.4	88.89	96.5	61.6	80.45	91.85	90.9	96.05	98.45
BiGRU +kd	73.38	88.86	96.75	62.65	80.3	91.25	87.65	96	98.55

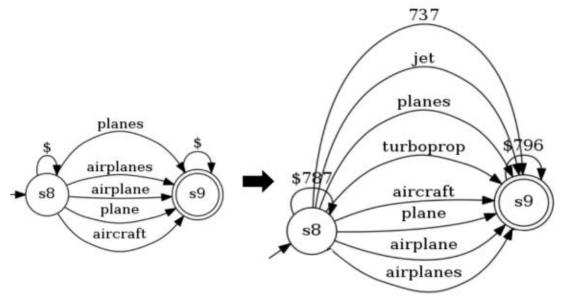
#### Conversion Back to RE

- From a FA-RNN, we can recover a WFA tensor from the model parameters
- The WFA tensor can be rounded to a 0/1 tensor, resulting in a FA and hence a RE
- Extracted RE vs. original RE

► ATIS: +0.45%

• QC: +9.2%

▶ SMS: -1.2%



### Summary

- FA-RNN combines strengths of symbolic rules and neural networks
  - Can be converted from RE
  - Can also learn from labeled data
  - Excels in zero-shot and low-resource scenarios; competitive in rich-resource scenarios