Announcement

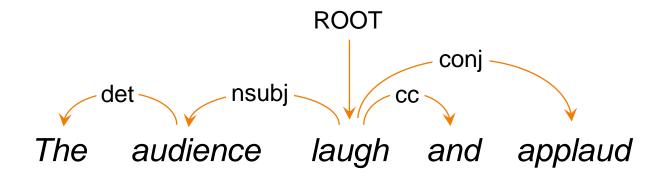
- Homework 3
 - Available in Blackboard -> Homework
 - Due: May. 1, 11:59pm (one week)

Dependency Parsing

SLP3 Ch 14; INLP Ch 11

Dependency Parse

- A dependency parse is a directed tree where
 - the nodes are the words in a sentence
 - ROOT: a special root node
 - The links between the words represent their dependency relations
 - Typically drawn as a directed arc from head to dependent
 - Dependency arcs may be typed (labeled)



Dependency Relations

Argument Dependencies	Description
nsubj	nominal subject
csubj	clausal subject
dobj	direct object
iobj	indirect object
pobj	object of preposition
Modifier Dependencies	Description
tmod	temporal modifier
appos	appositional modifier
det	determiner
prep	prepositional modifier

Dependency Parsing

Advantages

- Deals well with free word order languages where the constituent structure is quite fluid
 - ▶ Ex: Czech, Turkish
- Dependency parses of sentences having the same meaning are more similar across languages than constituency parses
- Dependency structure often captures the syntactic relations needed by downstream applications
- Parsing can be faster than CFG-bases parsers

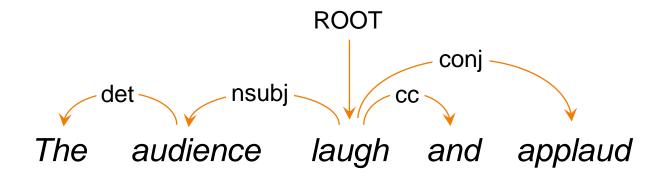
Disadvantages

- There is little agreement about what constitutes a dependency relation.
 - In contrast, there are widely agreed-upon tests for constituency.
- Dependency maps less cleanly to formal semantic representations than constituency



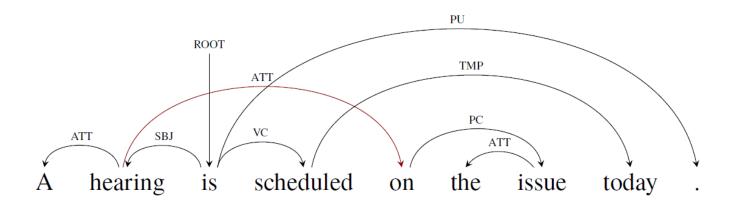
Projectivity

Projective parse: There are no crossing dependency arcs when the words are laid out in their linear order, with all arcs above the words



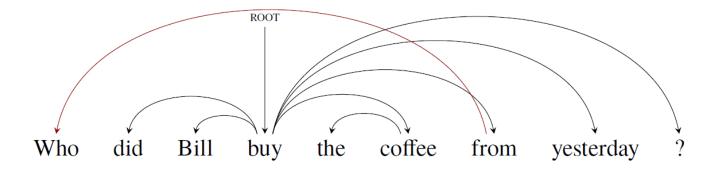
Projectivity

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- Most syntactic structures are projective, but some are non-projective.

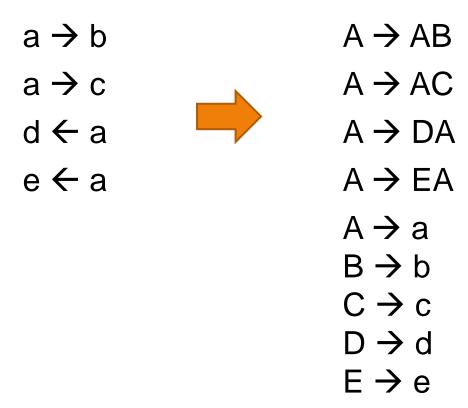


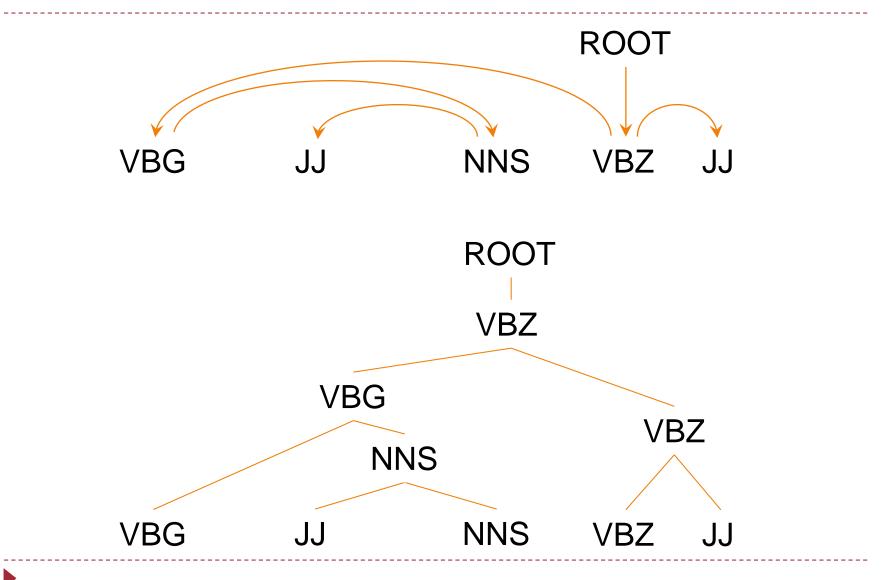
Projectivity

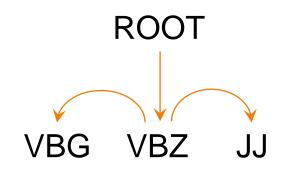
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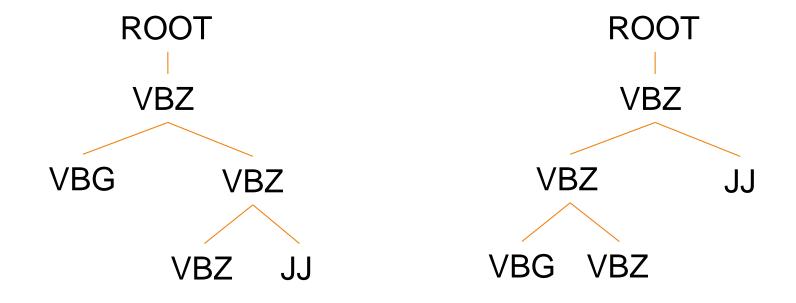


Projective dependency parsing can be modeled with a CFG

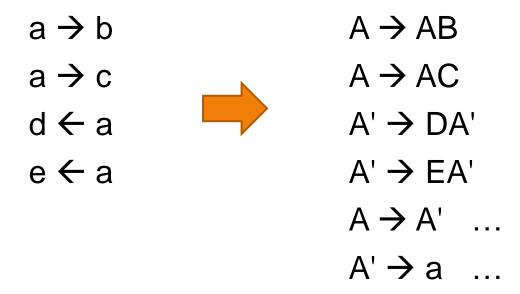




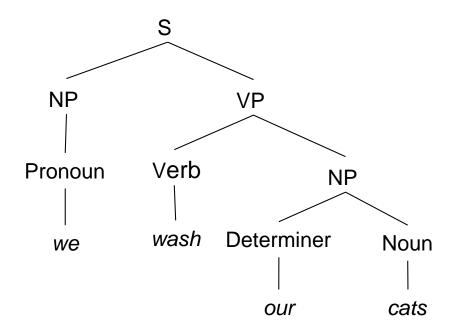




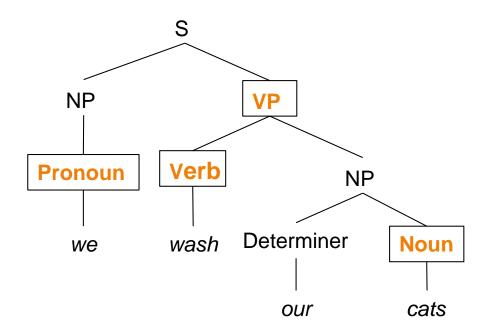
Projective dependency parsing can be modeled with a CFG



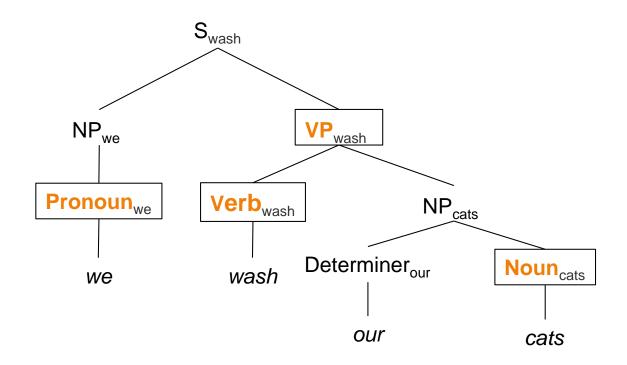
- From a constituent tree to a dependency tree
 - Constituent tree



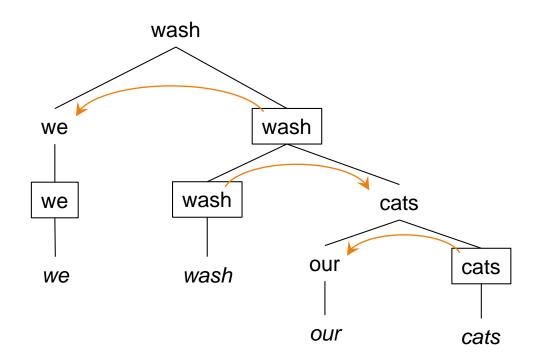
- From a constituent tree to a dependency tree
 - Constituent tree with heads



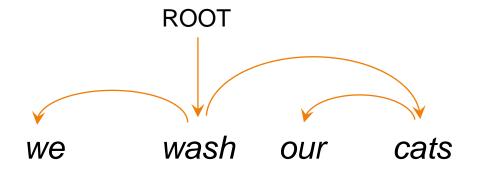
- From a constituent tree to a dependency tree
 - Constituent tree with heads, lexicalized



- From a constituent tree to a dependency tree
 - Constituent tree with heads, lexicalized



- From a constituent tree to a dependency tree
 - Dependency tree



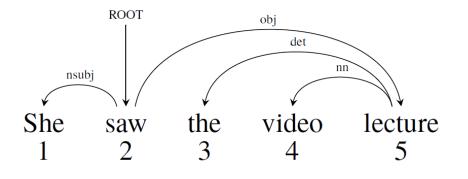
Parsing

- Parsing: taking a string and returning the (best) parse tree for that string
- Algorithms
 - Graph-based parsing: MST, Eisner, etc.
 - can find the global optimum
 - Transition-based parsing: arc-standard, arc-eager, archybrid
 - ▶ local optimum, fast
 - Parsing as sequence labeling
 - Headed-span-based parsing

Evaluating dependency parsing

Go	old	
1	2	nsubj
2	0	root
3	5	det
4	5	nn
5	2	obj

Pa	rsed	
1	2	nsubj
2	0	root
3	4	det
4	5	nsubj
5	2	ccomp



$$Acc = \frac{\# \ correct \ deps}{\# \ of \ deps}$$
, $UAS = 4/5 = 80\%$, $LAS = 2/5 = 40\%$

Resource

- Universal Dependencies (UD) Treebanks
 - ▶ As of 2022, nearly 200 treebanks in over 100 languages

Current UD Languages

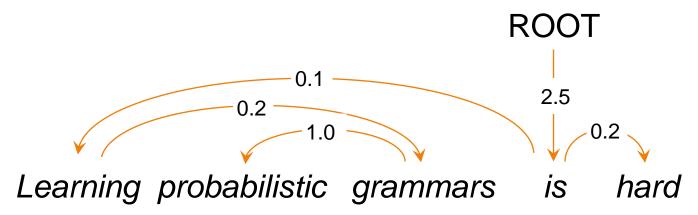
Information about language families (and genera for families with multiple branches) is mostly taken from WALS Online (IE = Indo-European).

	\geq	Afrikaans	1	49K	₹ 0	IE, Germanic
•	. a. a.	Akkadian	2	25K		Afro-Asiatic, Semitic
•		Akuntsu	1	<1K		Tupian, Tupari
		Albanian	1	<1K	W	IE, Albanian
•	一卷	Amharic	1	10K		Afro-Asiatic, Semitic
-		Ancient Greek	2	416K	≜ £€	IE, Greek
-	(Apurina	1	<1K		Arawakan
•	©	Arabic	3	1,042K		Afro-Asiatic, Semitic
-		Armenian	2	55K		IE, Armenian
•	X	Assyrian	1	<1K	9	Afro-Asiatic, Semitic
-		Bambara	1	13K		Mande
•		Basque	1	121K		Basque
-		Beja	1	1K	0	Afro-Asiatic, Cushitic
-		Belarusian	1	305K		IE, Slavic
		Bengali	1	<1K	7	IE, Indic

Graph-Based Dependency Parsing

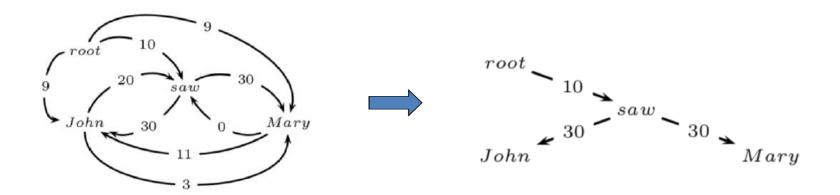
First-order graph-based dependency parsing

- Parse tree scoring
 - Each arc has a score. The tree score is the sum of arc scores.
 - An arc score is often computed from features of the two words
 - Possible features: neighboring words, their POS tags, contextual word embeddings



First-order graph-based dependency parsing

- Parse tree scoring
- Parsing
 - Maximum spanning tree (more precisely, spanning arborescence)
 - What about dependency labels?
 - For each arc, we may simply predict its label from features of the two words

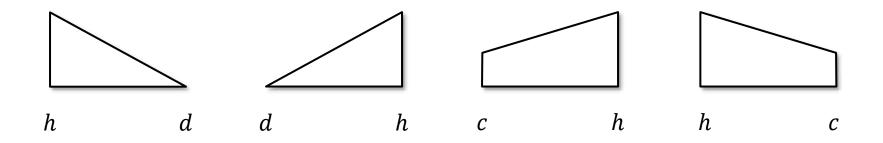


CYK

- Remember: projective dependency parsing can be modeled with a CFG
- We can run CYK for parsing
- But runtime is $O(n^5)!$
 - CYK is $O(n^3 \cdot |G|)$
 - ▶ There are n^2 rules for a sentence:

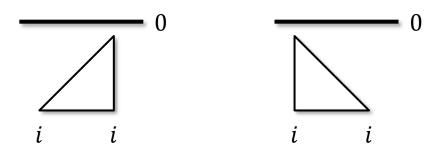
$$\forall w_1, w_2 : N_{w_1} \to N_{w_1} N_{w_2} \text{ or } N_{w_2} \to N_{w_1} N_{w_2}$$

Items:

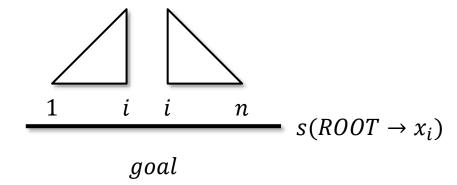


- Triangles: a partial tree whose root is x_h and no words except x_h expect more children.
- Trapezoids: x_c is a child of x_h and x_c still expects children on its side.
- In all cases, the words in between are descendants of x_h .

Initialization:

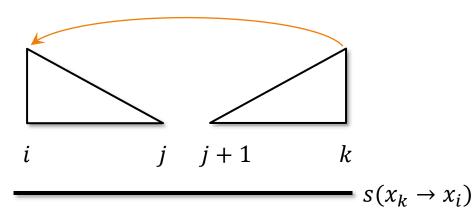


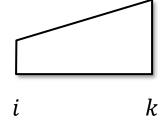
Goal:



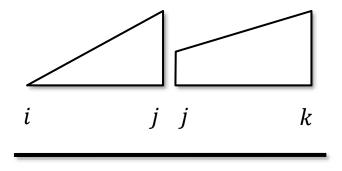


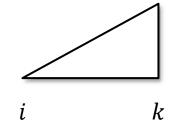
Attach a left dependent:



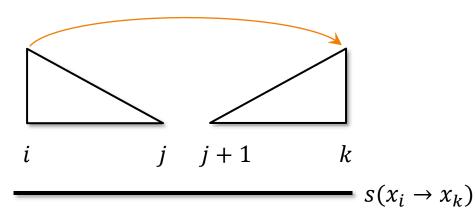


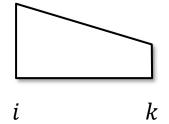
Complete a left child:



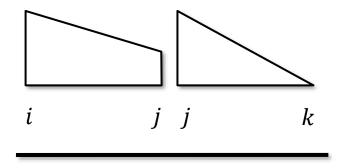


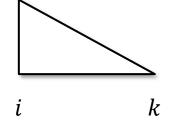
Attach a right dependent:

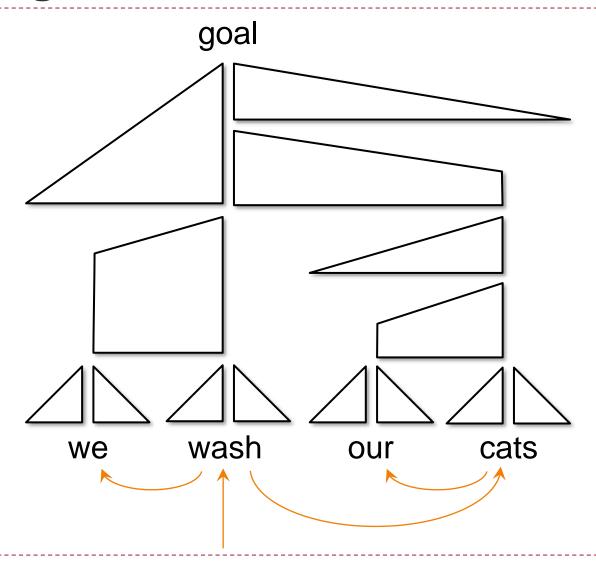




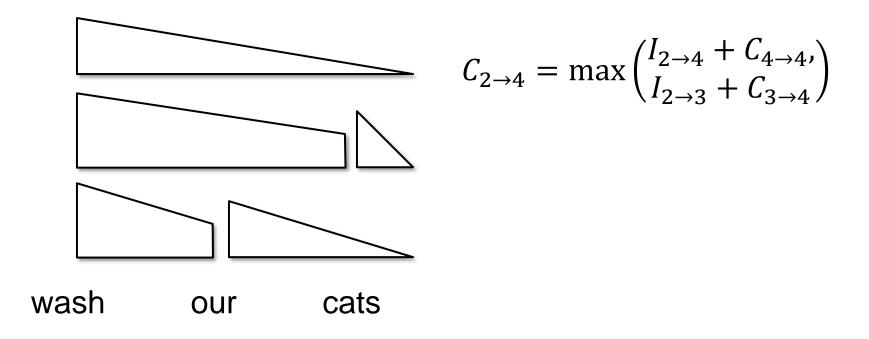
Complete a right child:



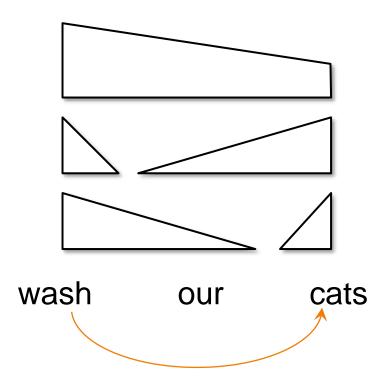




- Ambiguity
 - An item may have multiple valid compositions
 - Pick the highest scoring one



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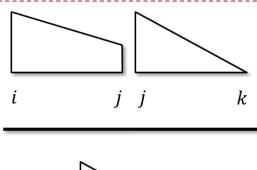


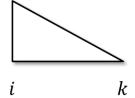
$$I_{2\to 4} = \max \begin{pmatrix} C_{2\to 2} + C_{3\leftarrow 4}, \\ C_{2\to 3} + C_{4\leftarrow 4} \end{pmatrix} + s(x_2 \to x_4)$$

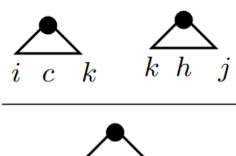
- Time complexity
 - $ightharpoonup O(n^2)$ items
 - Each item has O(n) possible compositions
 - The run time is $O(n^3)$

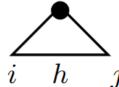


- CYK has $O(n^3)$ items, each has $O(n^2)$ possible compositions, hence the run time is $O(n^5)$
- Fisher does head-splitting to eliminate $O(n^2)$ time!







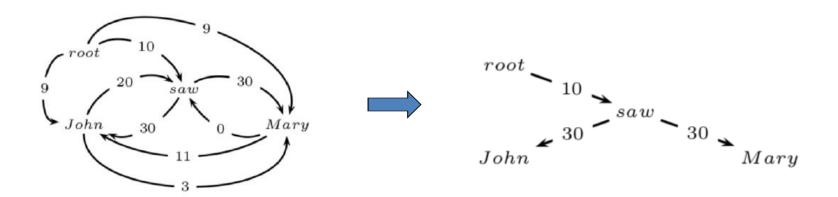


Non-projective dependency parsing

- Eisner algorithm only finds projective dependency parses
- We need a different algorithm for finding non-projective dependency parses
 - MST parser based on the Chu-Liu-Edmonds algorithm

Chu-Liu-Edmonds: Preliminary

- Maximum spanning tree (arborescence)
- Every non-root node needs exactly one incoming edge.
- In fact, every connected component that doesn't contain x_0 needs exactly one incoming edge.



Chu-Liu-Edmonds

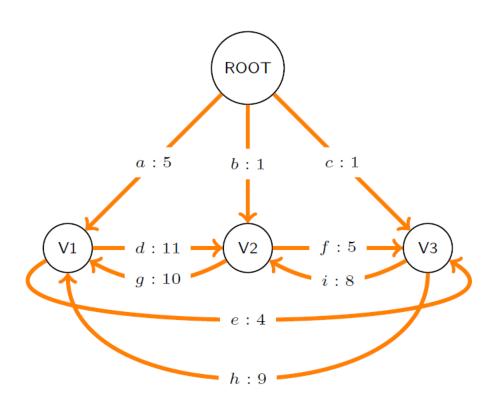
- Two stages:
 - Contraction
 - Expansion

Chu-Liu-Edmonds: Contraction

- 1. For each non-ROOT node v, pick its highest scoring incoming edge
 - Set bestInEdge[v] to be the edge
- 2. If this forms an arborescence (i.e., no cycle)
 - We are done! Go to the next stage.
- Otherwise, a cycle C is formed
 - To build an arborescence, we need to:
 - ▶ Find an incoming edge for C
 - Kick out some edge in C
 - Choosing the incoming edge for C determines which edge to kick out.

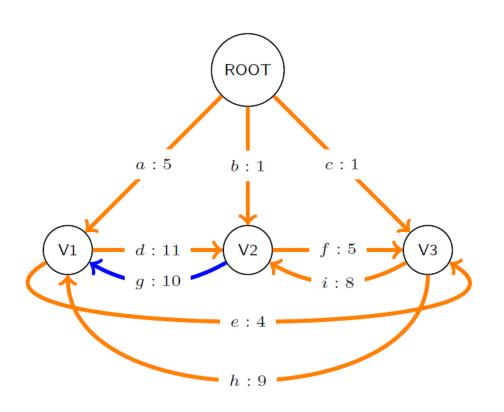
Chu-Liu-Edmonds: Contraction

- Otherwise, a cycle C is formed
 - Choosing the incoming edge for C determines which edge to kick out.
 - contract the nodes in \mathcal{C} into a new node $v_{\mathcal{C}}$ and adjust related edges:
 - \blacktriangleright Edges outgoing from any node in C now get source v_C
 - ightharpoonup Edges incoming to any node in C now get destination v_C
 - ▶ For each edge e incoming to $v \in C$ from outside of C:
 - ▶ $e.kicksOut \leftarrow bestInEdge[v]$
 - ▶ e.score $\leftarrow e$.score -e.kicksOut.score
 - This is the change in total score if we choose e and kick out the original incoming edge to v
- 4. Now we get a new graph. Go back to step 1 and repeat.



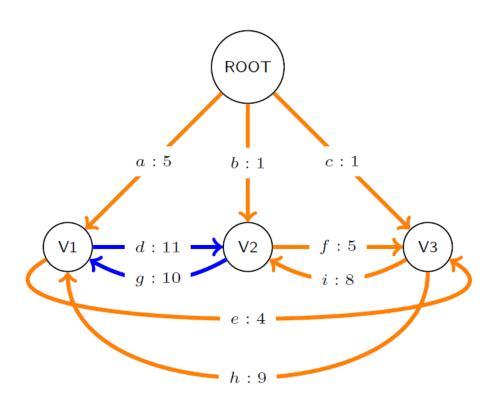
	bestInEdge
V1	
V2	
V 3	

	kicksOut
a	
a b	
c d	
d	
е	
e f	
g	
h	
i	



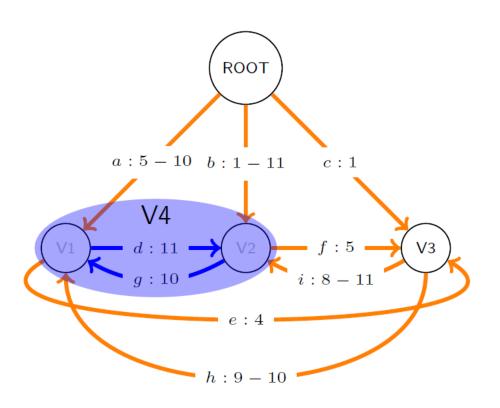
	${\tt bestInEdge}$
V1	g
V2	
V 3	

	kicksOut
a	
a b	
c d	
d	
е	
e f	
g	
h	
i	



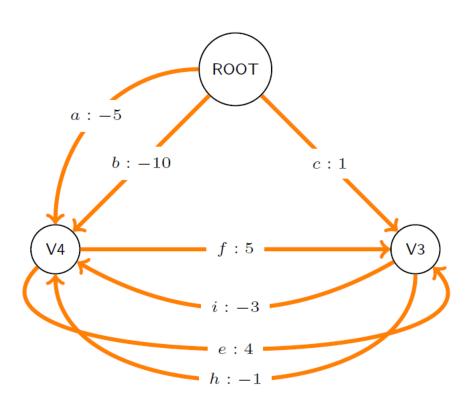
	${\tt bestInEdge}$
V1	g
V2	d
V3	

	kicksOut
a	
a b	
c d	
d	
е	
e f	
g	
h	
i	



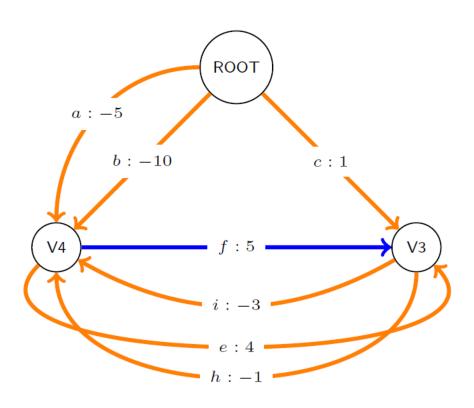
	bestInEdge
V1	g
V2	d
V3	

	kicks0ut
a	g
a b	g d
c d	
d	
е	
e f	
g	
h	g
i	g d



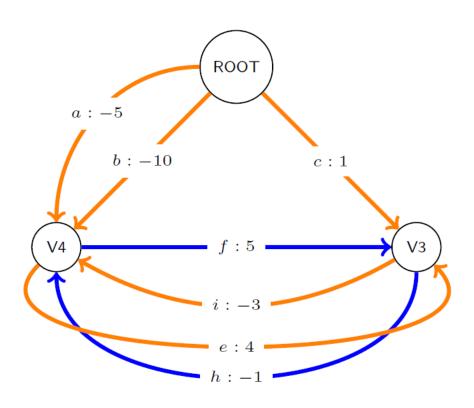
	bestInEdge
V1	g
V2	d
V3	
V4	

	kicks0ut
а	g
b	d
c d	
d	
e f	
f	
g h	
h	g
i	d



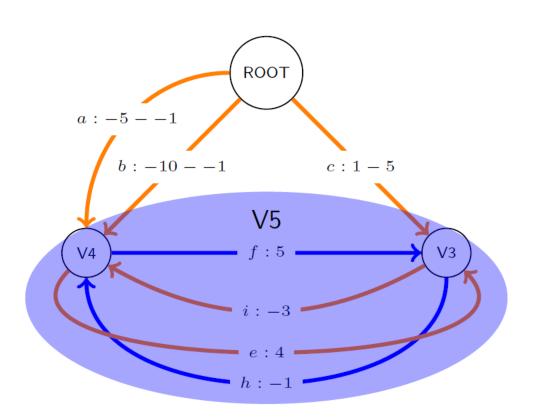
	bestInEdge
V1	g
V2	d
V3	f
V4	

	kicksOut
а	g
a b	d
c d	
1	
е	
f	
g h	
h	g
i	d



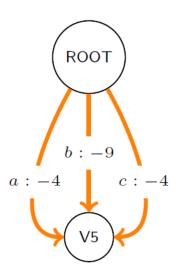
	bestInEdge
V1	g
V2	d
V3	f
V4	h

	kicks0ut
а	g
a b	d
c d	
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f	
g h	
h	g
i	d



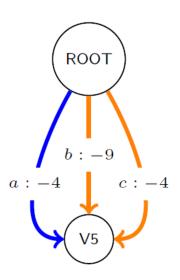
	${\tt bestInEdge}$
V1	g
V2	d
V3	f
V4	h
V5	

	kicks0ut
а	g, h
a b	d, h
c d	f
d	
е	
f	
g h	
h	g
i	d



	${\tt bestInEdge}$
V1	g
V2	d
V3	f
V4	h
V5	

	kicksOut
а	g, h
b	d, h
c d	f
е	
f	
g	
g h	g
i	g d

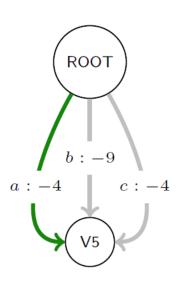


	bestInEdge
V1	g
V2	d
V3	f
V4	h
V5	a

	kicks0ut
а	g, h
a b	d, h
c d	f
d	
e f	
f	
g	
h	g
i	d

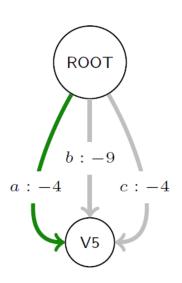
Chu-Liu-Edmonds: Expansion

- After the contraction stage, every contracted node will have exactly one bestInEdge. This edge will kick out one edge inside the contracted node, breaking the cycle.
 - Go through each bestInEdge e in the reverse order that we added them
 - Lock down e, and remove every edge in kicksOut(e) from bestInEdge.



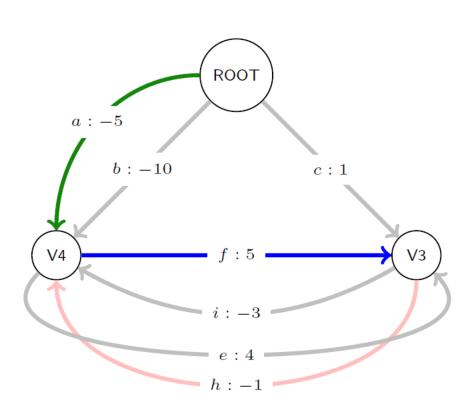
	bestInEdge
V1	g
V2	d
V3	f
V4	h
V5	a

	kicksOut
а	g, h
b	d, h
c d	f
d	
е	
f	
g	
h	g
i	d



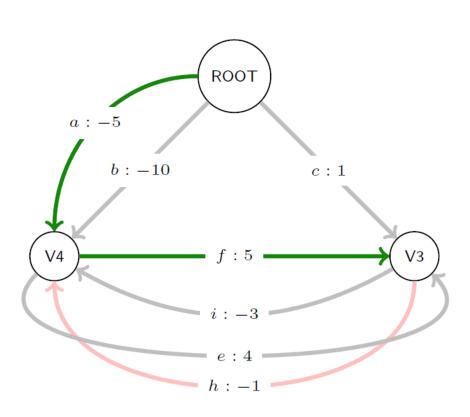
	bestInEdge
V1	a g
V2	ď
V3	f
V4	a M
V5	a

	kicksOut
а	g, h
a b	d, h
c d	f
d	
е	
f	
g	
h	g
i	g d



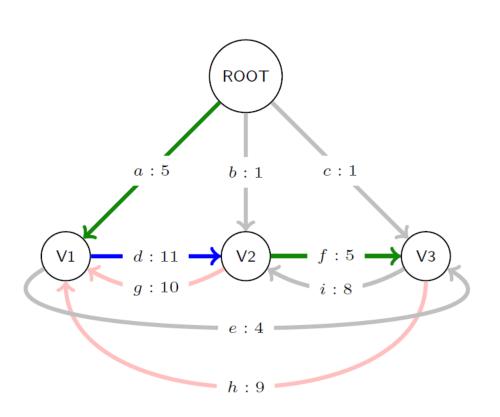
	bestInEdge
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	kicksOut
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a b	d, h
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е	
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g	
g h	g
i	d



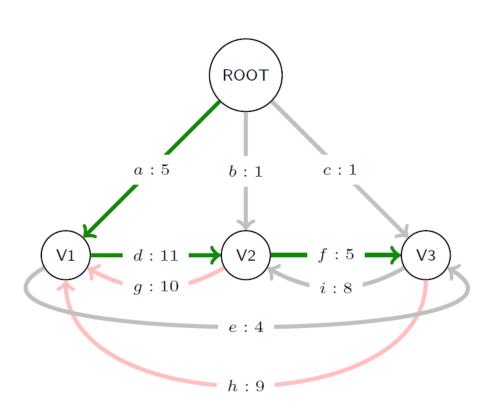
	bestInEdge
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а	g, h
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g h	g
i	g d



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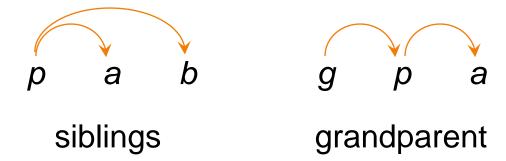
	kicksOut
а	g, h
b	d, h
С	f
d	
е	
e f	
g	
h	g
i	d

Chu-Liu-Edmonds Algorithm

- Time complexity
 - Simple implementation: $O(n^3)$
 - Fast implementation: $O(n^2 + n \log n)$
- Single-root parsing: only one word can be the root
 - Several extensions of CLE
 - A simple solution: root reweighting
 - Subtract a large constant from ROOT edges, so that any singleroot tree has a larger score than any multi-root tree
 - See https://aclanthology.org/2021.emnlp-main.823.pdf

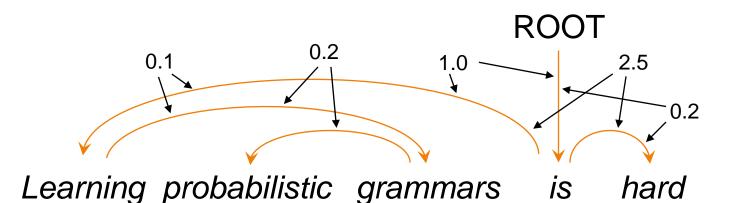
Second-order graph-based dependency parsing

- Parse tree scoring:
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Second-order graph-based dependency parsing

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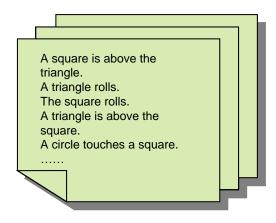


Second-order graph-based dependency parsing

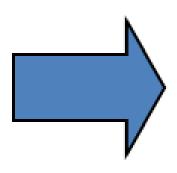
- Parse tree scoring:
 - Each connected pair of arcs has a score. The tree score is the sum of arc-pair scores.
- Parsing:
 - $O(m^4)$ time for projective dependency parsing
 - NP-hard for non-projective dependency parsing
 - Approximate algorithms exist

Learning a grammar from a corpus

Training Corpus



Induction



Grammar / Parser

```
S → NP VP

NP → Det N

VP → Vt NP (0.3)

| Vi PP (0.2)

| rolls (0.2)

| bounces (0.1)

.....
```

- Supervised Methods
 - Rely on a training corpus of sentences annotated with parses (treebank)
- Unsupervised Methods (Grammar Induction)
 - Do not require annotated data

Supervised Learning

- Objective
 - Conditional likelihood: P(gold parse | sentence)

$$P(t|x) = \frac{\exp(s(t))}{Z(x)} = \frac{\exp(\sum_{r \in (t,x)} s(r))}{Z(x)} = \frac{\prod_{r \in (t,x)} \exp(s(r))}{Z(x)}$$

- Problem: how to compute the partition function
 - Impossible to enumerate parse trees
- Projective: replace max with sum in Eisner algorithm (similar to inside algorithm)
- Non-projective: Kirchhoff's matrix tree theorem
 - The determinant of the Kirchoff (aka Laplacian) adjacency matrix of directed graph G without row and column r is equal to the sum of scores of all directed spanning trees of G rooted at node r.

Supervised Learning

- Objective
 - Conditional likelihood: P(gold parse | sentence)
 - Margin-based objective
- Optimization
 - Gradient-based methods

Unsupervised Learning

- Generative method
 - Dependency parser as a PCFG
 - Ex: Dependency Model with Valence (DMV)
 - Run EM algorithm or SGD to maximize likelihood P(sentence)
- Discriminative method
 - CRF-Autoencoder
 - Encoder: a graph-based dependency parser
 - Decoder: predict each word from its head
 - Maximize reconstruction probability using SGD

Transition-Based Dependency Parsing

Transition-Based Parsing

- Dependency tree represented as a linear sequence of transitions.
- Transitions: simple actions to be executed on a parser configuration.
- Parser configuration
 - ▶ Buffer *B*: unprocessed words of the input sentence
 - Stack S: parse tree under construction

Transition-Based Parsing

- Transitions: "arc-standard" transition set (Nivre, 2004)
 - SHIFT: move the word at the front of buffer B onto stack S.
 - ▶ RIGHT-ARC: u = pop(S); v = pop(S); $push(S, v \rightarrow u)$.
 - LEFT-ARC: u = pop(S); v = pop(S); push $(S, v \leftarrow u)$.
- For labeled parsing, add labels to the RIGHT-ARC and LEFT-ARC transitions.
 - ► Ex. LEFT-ARC-nSubj
- ▶ There are other transition sets: arc-eager, arc-hybrid, ...

Transition-Based Parsing

- Initial Configuration
 - Buffer B contains the complete input sentence and stack S only contains ROOT.
- During parsing
 - Apply a classifier to decide which transition to take next.
 - Greedy. No backtracking.
- Final Configuration
 - Buffer B is empty and stack S contains the entire parse tree.

Stack S:

Buffer B:

we
vigorously
wash
our
cats
who
stink

ROOT

Actions:

Stack S:

Buffer B:

we ROOT

vigorously
wash
our
cats
who
stink

Actions: SHIFT

Stack S:

Buffer B:

vigorously
we
ROOT

wash
our
cats
who
stink

Actions: SHIFT SHIFT

Stack S:

Buffer B:

wash
vigorously
we
ROOT

our
cats
who
stink

Actions: SHIFT SHIFT SHIFT

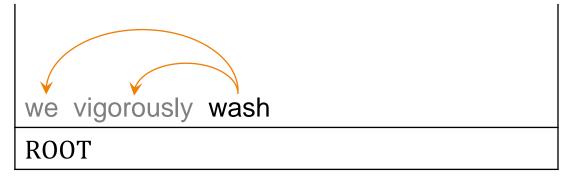
Stack *S*: Buffer *B*:

vigorously wash	
we	
ROOT	

our
cats
who
stink

Actions: SHIFT SHIFT LEFT-ARC

Stack *S*: Buffer *B*:



our
cats
who
stink

Actions: SHIFT SHIFT LEFT—ARC LEFT — ARC

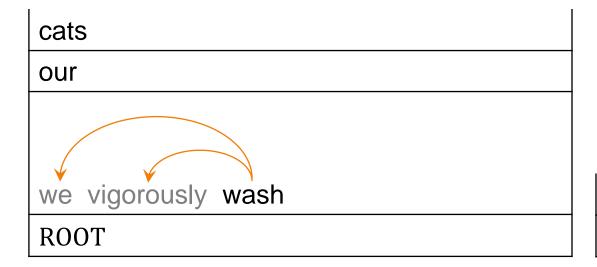
Stack *S*: Buffer *B*:



cats who stink

Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT

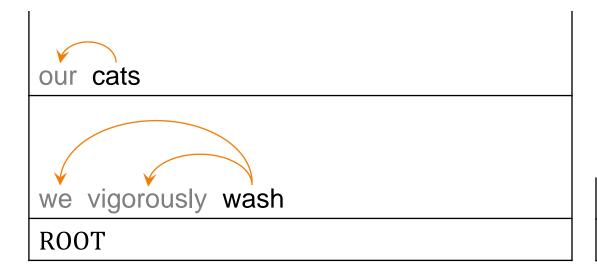
Stack *S*: Buffer *B*:



who stink

Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT

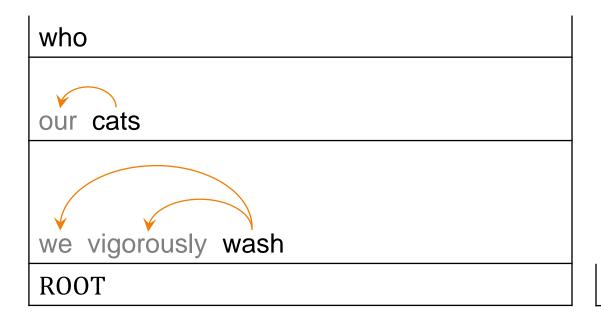
Stack *S*: Buffer *B*:



who stink

Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC

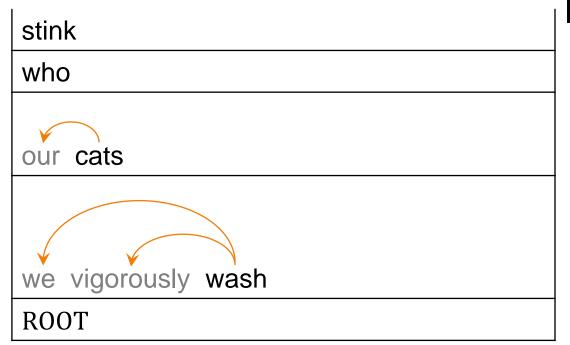
Stack *S*: Buffer *B*:



stink

Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC SHIFT

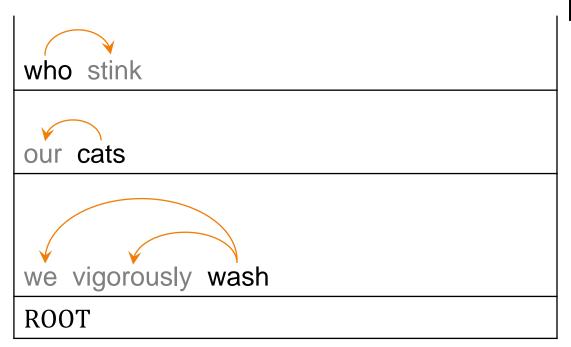
Stack S:



Buffer B:

Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC SHIFT SHIFT

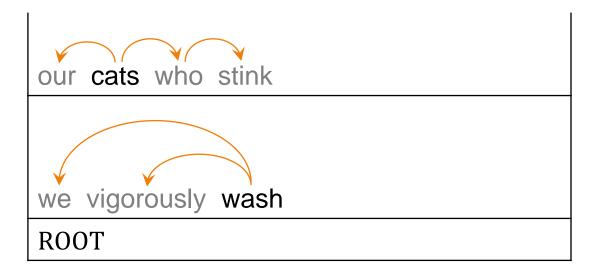
Stack S:



Buffer B:

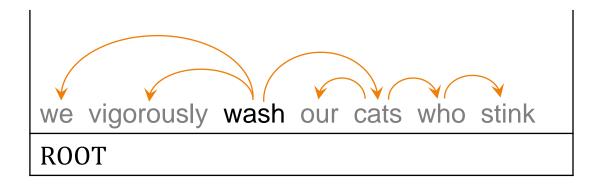
Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC SHIFT RIGHT—ARC

Stack *S*: Buffer *B*:



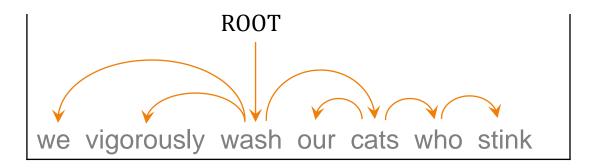
Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC SHIFT RIGHT—ARC RIGHT—ARC

Stack *S*: Buffer *B*:



Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC SHIFT RIGHT—ARC RIGHT—ARC RIGHT—ARC

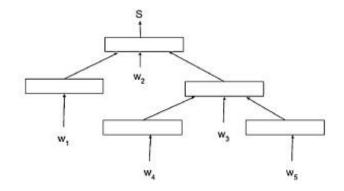
Stack *S*: Buffer *B*:



Actions: SHIFT SHIFT LEFT—ARC LEFT—ARC SHIFT SHIFT LEFT—ARC SHIFT RIGHT—ARC RIGHT—ARC RIGHT—ARC

The Core of Transition-Based Parsing: Classification

- At each iteration, choose among {SHIFT, RIGHT—ARC, LEFT—ARC}
 - Actually, among all L-labeled variants of RIGHT—ARC and LEFT—ARC
- Train a classifier to score actions
 - ▶ Input features can be extracted from stack *S*, buffer *B*, and the history *H* of past actions.
 - Can use a neural network to summarize info from S, B, H
 - ▶ LSTM over B and H
 - ▶ LSTM + <u>recursive neural net</u> over *S*



The Core of Transition-Based Parsing: Classification

Training classifier

Training data: convert "oracle" transition sequence that builds the gold parse tree into 2n pairs: (configuration, correct transition)

Potential flaw

- The classier is only trained with correct configurations (i.e., assuming all the preceding classification decisions were all correct).
- In testing, however, the classifier can make mistakes and produce incorrect configurations not seen during training.

Dynamic oracle

- Make random errors to produce incorrect configurations
- Find transitions (e.g., using rules) that can change these configurations to a gold configuration in the fastest possible way
- Train the classifier to predict these transitions



Transition-Based Parsing: Remarks

- Action selection
 - Greedy: pick the highest scoring predicted action
 - Beam search: pick multiple actions, maintain multiple hypotheses
- Time complexity
 - Each word gets SHIFTed once and participates as a child in one ARC.
 - Linear time!
- Can also be applied to constituency parsing ("shiftreduce" parsing)



Summary

Dependency Parsing

- Dependency Parsing
 - Projectivity
 - Relation to constituency parsing
- Graph-based parsing
 - ▶ 1st-order: Eisner, MST
 - Learning
- Transition-based parsing
 - Arc-standard