

## Homework 3

Due data: Mar.28<sup>th</sup>

Turn in your homework in class

Rules:

- Please work on your own. Discussion is permissible, but extremely similar submissions will be judged as plagiarism!
- Please show all intermediate steps: a correct solution without an explanation will get zero credit.
- Please submit on time. No late submission will be accepted.
- Please prepare your submission in English only. No Chinese submission will be accepted.

**1**

[10 points] Known capacitance  $C=2\text{pF}$ , and  $u_c(0_-) = -1\text{mV}$ , its current waveform is shown in Figure 1. Find the capacitor voltage as a function of time, and draw its waveform.

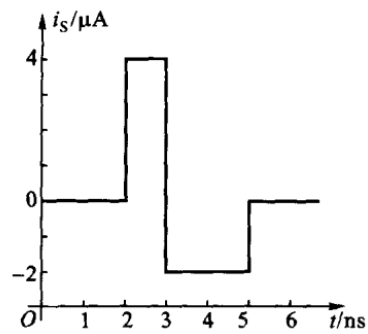


Figure 1

**2**

[10 points] With a and b as circuit terminals, please make the circuit diagram shown in Figure 2 equivalent to the series connection of a capacitor and an inductor. Find the values of the equivalent inductance  $L$  and the equivalent capacitance  $C$ .

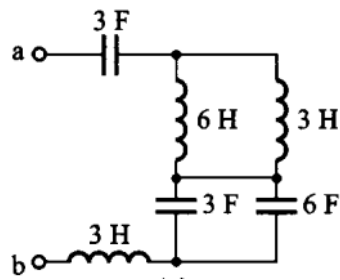


Figure 2

**3**

[10 points] The circuit in the Figure 3 has reached steady state before  $t=0$ . The switch S is closed when  $t=0$ . Known that:  $U_{S1} = 6V$ ,  $U_{S2} = 24V$ ,  $R_1 = 3\Omega$ ,  $R_2 = 6\Omega$ ,  $C = 0.5\mu F$ , find  $u_c(t)$  after S is closed ( $t \geq 0$ ).

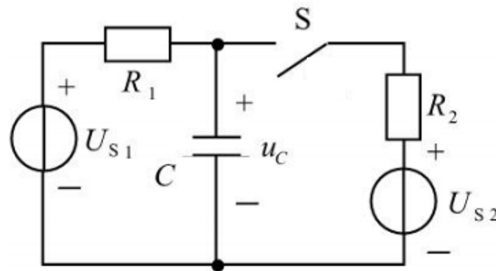


Figure 3

## 4

[12 points] Known that  $L_1 = 6H$ ,  $i_1(0) = 2A$ ,  $L_2 = 1.5H$ ,  $i_2(0) = -2A$ ,  $u = 6e^{-2t}V$ .

- (a). Find the expression of equivalent inductance  $L$  and the equivalent initial current  $i(0)$ .
- (b). Considering the equivalent inductor, find  $i(t)$ .
- (c). Considering two separate inductors, find  $i_1(t)$  and  $i_2(t)$ . Check whether the KCL holds, i.e., whether  $i(t)$  equals to  $i_1(t) + i_2(t)$ .

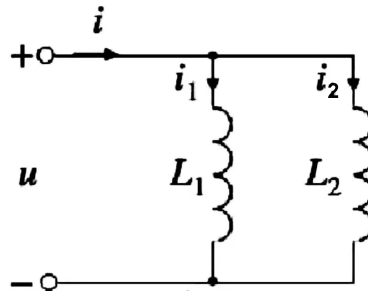


Figure 4

## 5

[12 points] The circuit is shown in the Figure 5. Write the first-order differential equation with the inductor current  $i_L$  as the variable (you don't have to solve it). The values of  $u_s$ ,  $i_s$ ,  $R_1$ ,  $R_2$ , and  $L$  are known.

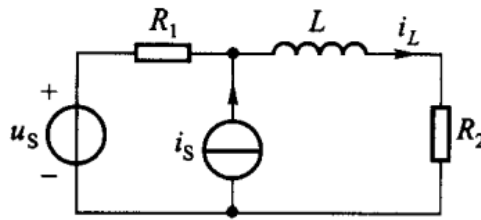


Figure 5

## 6

[14 points] The circuit is shown in the Figure 6. Write the first-order differential equation with the inductor current  $i_L$  as the variable (you don't have to solve it). The values of  $u_s, L, R_1, \mu, R_2, R_3$  are known.

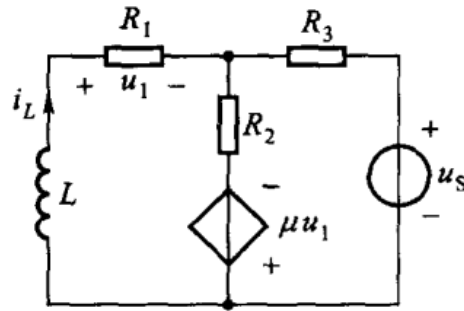


Figure 6

## 7

[16 points] The circuit is shown in the Figure 7. The switch is at position 1 and the circuit has reached steady state before  $t = 0$ . When  $t=0$ , the switch changes from position 1 to position 2. Find the inductor voltage  $u_L(t)$  when  $t \geq 0$ .

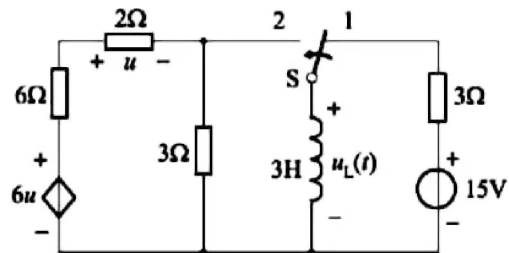


Figure 7



## 8

[16 points] At  $t=0$ , the double-pole switch in the circuit shown in figure is closed. The initial voltages on the capacitors are 12V and 4V, as shown in Figure 8. Find the numerical expressions for  $v_o(t)$ ,  $v_2(t)$  and  $v_f(t)$ . Assume the operational amplifier is ideal (Hint the operational amplifier can work in either linear region or saturation region, based on the rest of the circuit)

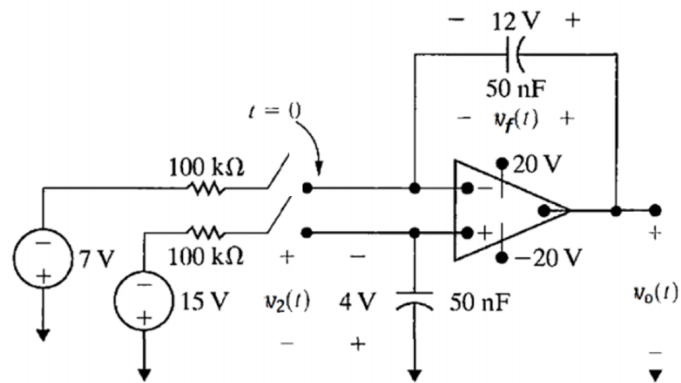


Figure 8