

# Effectiveness of Belleville Washers for Seismic Retrofit of Substation Equipment

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## Abstract

Seattle City Light (SCL), a power utility in the Pacific Northwest where there is potential for large earthquakes, has retrofitted several Capacitive Voltage Transformers (CVT) in their substations with Belleville washer arrangements at the bases to improve seismic performance. The strategy is simple and relatively low-cost to implement, and preliminary testing at SCL has demonstrated improved seismic performance. The washer arrangements essentially function as seismic isolators, reducing the frequency and increasing damping. To expand the implementation of this strategy more broadly for other equipment and at other utilities' substations, this project systematically characterizes the stiffness and damping mechanisms of Belleville washer arrangements and tests a retrofitted 230kV CVT on an earthquake simulator. Special instrumentation is developed to monitor the mechanics of the Belleville washer arrangements including force, deformation and equipment base moment measurements. A detailed modeling and analysis procedure is developed, allowing for either a nonlinear dynamic approach or an equivalent linear dynamic approach, to predict the response of equipment such as CVTs outfitted with Belleville washer stacks for seismic protection. The analysis procedure has been validated with experimental measurements. Essentially, knowing the force-deformation response of a washer configuration, obtained for example by cyclic loading in a material testing machine, together with the inertia characteristics of the equipment, the seismic response of the equipment can be predicted. This will enable washer configurations to be designed and deployed readily for seismic protection of various equipment.

**Keywords:** Substation equipment, seismic performance improvement, nonlinear and linear dynamic analysis, Belleville washers (disc springs), damping, experimental validation

## 1 Introduction

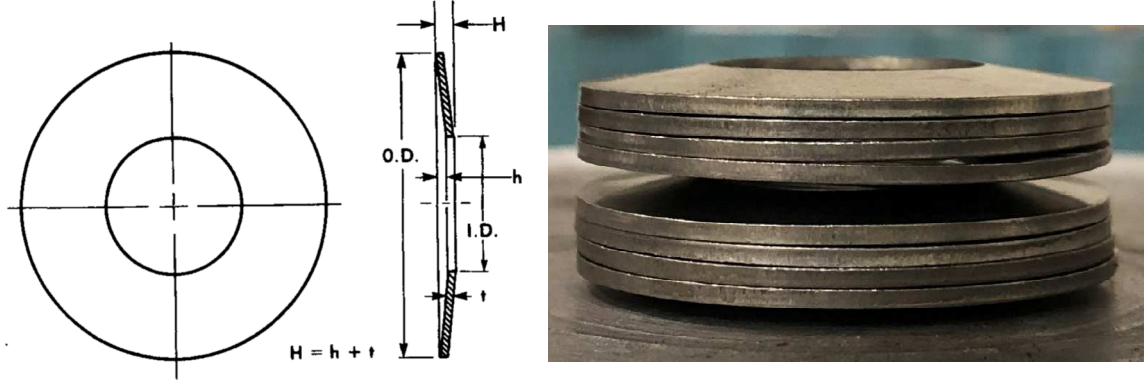
### 1.1 Background and objectives

Base isolation and supplemental damping systems are now widely used as seismic protective systems in structures. They represent a design philosophy that seeks to reduce seismic demand on functional structural components, and to minimize if not eliminate damage and permanent deformation even under large earthquakes. This is in contrast to the conventional seismic design philosophy, wherein structural components are designed to be ductile, and undergo permanent deformation without failure. For critical structures and equipment, such as in electrical substations, the approach of reducing seismic demand and permanent deformations is more attractive to ensure continued functioning of such structures and equipment post-earthquake. The concept of frequency modification for substation equipment was recommended as early as 1973 in a report prepared for Bonneville Power Administration (BPA) [1]. Base isolation and supplemental damping systems are being increasingly deployed in substations for seismic protection [2–5].

One approach to modifying frequency and adding damping is using stacks of Belleville washers. Belleville washers, named after Julian Belleville, who patented them in 1867, are circular washers given a taper to form a conical shape (Figure 1a). They are also known as a disc springs or conical spring washers, although the term “disc springs” may be more appropriate [6] for the type of dynamic application considered in this report. When a compressive load is applied along the axis, the washer flattens by way

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(a) Shape and dimension specifications (source: [7]) (b) Example of a stack with series-parallel arrangement

Figure 1: Belleville washer shape, dimensions and stack consisting of series-parallel arrangement

of elastic deformation, resulting in spring action [7]. When washers are nested such that the bottom surface of one is placed on the top surface of the next, frictional rubbing between these surfaces results in hysteretic behavior (see section 3), and hence energy dissipation. The washers can also be stacked in different ways as illustrated in Figure 1 and Table 1-2. Thus the stiffness and dissipation of a stack of Belleville washers can be tuned. Testing discussed further in section 3 has shown that the force-displacement hysteresis of washer stacks is stable and repeatable. These stacks therefore lend themselves to modeling, and use as engineered frequency modification and energy dissipation devices. For early analyses of the mechanical behavior of Belleville washers, see [8,9], considering both single washer and nesting. For a more recent study on the analysis of washer mechanical behavior, see [10] and the references therein. The force-displacement behavior of a single washer is given by [7,9]

$$F = \frac{E\delta}{(1-\mu^2)Ma^2} \left[ (h-\delta) \left( h - \frac{\delta}{2} \right) t + t^3 \right] \quad (1)$$

where  $F$  and  $\delta$  are the force in the washer and deflection,  $E$  and  $\mu$  are the Young's modulus and Poisson ratio of the washer material,  $M$  is a constant that depends on the ratio of outer to inner diameters (see [7] for a chart),  $a$  is the outer radius and  $h$  and  $t$  are the dimension shown in Figure 1-1. Depending on the  $h/t$  ratio, equation (1) implies a wide variety force-displacement behaviors as shown in Figure 2. As a point of reference, the washers used in the present project are listed in Table 1-1. The K1875-G-086 washer has a  $h/t$  ratio of 0.5, which corresponds to almost linear behavior till flattening. The K1750-J-057 washer on the other hand has a  $h/t$  ratio of 1.0 resulting in a force-displacement curve that softens significantly before flattening. These behaviors are reflected in the test results in section 3. Specific features of the force-displacement behavior can be exploited<sup>1</sup>. An even wider range of behavior has been explored using Belleville washers made of shape-memory materials [12].

Belleville washers have been used in a number of industries for vibration isolation/absorption applications (see for example [13]). This includes seismic protective systems. Use of large Belleville washers (referred to therein as coned disc springs) for vertically isolation of the reactor vessel and other components in a horizontally isolated nuclear power plant building was discussed in references [14–16]. Belleville washers have been used to maintain bolt tension in frictional sliding structural connections [17]. Shape memory Belleville washers have also been considered for energy-dissipating braces in structures [18]. The closely related concept of ring springs has been studied for seismic isolation in [19]. Use of Belleville washers for vertical isolation of buildings under train-induced vibration has been studied in [20]; in this paper, the different force-displacement responses of Figure 1-2 are properly utilized and a thorough analysis of hysteretic behavior (cf. section 3 in this report) is presented.

The first suggestion of using Belleville washers for seismic protection of substation equipment was in a report prepared for Bonneville Power Administration [1]. The suggestion was made in the context of

<sup>1</sup>for example, by preloading washers of  $h/t$  of about 1.5 have nearly zero stiffness at flattening; so by preloading such washers to flattening and providing spacing to deformed beyond flattening, an isolation system with nearly zero frequency can be achieved (see for example [11]). Such approaches are not pursued in the present project but offer possibilities to consider in the future.

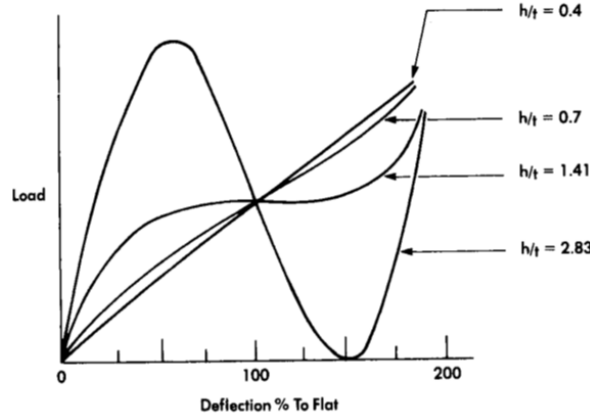


Figure 2: Force-displacement response of a single washer as a function of  $h/t$  (source [7])

Table 1: Washers used in this project [22]

Washer	Outer diameter (in)	Inner diameter (in)	$t$ (in)	$h$ (in)	Flattening load (lb)
K1875-G-086	1.875	0.656	0.086	0.043	1319
K1750-J-057	1.750	0.88	0.057	0.057	650

lightning arresters. The 1984 edition of IEEE 693 [21] briefly mentions the possibility of Belleville washers for seismic protection, but this was removed in subsequent edition. Seattle City Light has been installing Belleville washer stacks for seismic protection of their equipment; the present research was driven by this.

The goal of this project is to study the effectiveness of Belleville washers for seismic protection of equipment such as capacitive voltage transformers (CVT), capacitor banks etc. that do not have moving parts (such as in switches) and do not have complex dynamic modes of their own (such as dead tank circuit breakers). Such equipment, when mounted on support structures, essentially behave as rigid bodies rocking under horizontal ground motion due to the flexibility of the support structure. When Belleville washer stacks are installed at the base of such equipment, above the support structure, the equipment will rock under horizontal ground motion relative to the support structure. The Belleville washer stacks are expected to provide damping through frictional dissipation under such motion, resulting in reduction of equipment base moment relative when they are rigidly connected to the support structure. In deforming to provide frictional dissipation, the washer stacks will also invariably reduce the frequency; this reduction may further aid in reducing base moment. This could potentially occur at the expense of increased terminal deflection that must be accommodated.

The objectives of this project are:


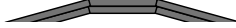


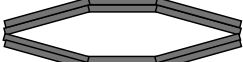
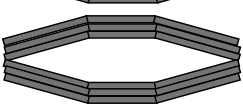
1. Develop an analysis-based systematic approach for design of a Belleville washer seismic protective system for a given equipment (together with given seismic demand and support structure).
2. Develop support for such an approach through physical experiments.

A CVT provided by Seattle City Light (see –) is used in the shake table experiments described in section 4.

## 1.2 Nomenclature for washer configurations

The specific washers used in the project are from Key Bellevilles [22] and are listed in Table 1. Table 1-2 summarizes the nomenclature used in this report for Belleville washer units, each consisting of series parallel arrangements. A stack is identified by the number and type of units, for example as illustrated in Table 1-2.

Table 2: Nomenclature used for Belleville washer units and stacks

Sr. No.	Units		Stack
	Configuration	Nomenclature	
1		1U	
2		1D	
3		1U1D	
4		2U2D	
5		3U3D	

Then washers are nested with the cones oriented in the same direction, as for example in the top or bottom half of a 2U2D unit, they act in *parallel* since when a load is applied, their deformations are the same. When the cone orientations are opposite, as for example with the two washers in a 1U1D unit, they are in series, since they see the same force and their deformations are additive. Thus, a stack can be viewed as a series-parallel arrangement of washers. If the washers were ideal springs, the stiffness of a stack can be calculated using series-parallel combinations of the stiffnesses of the constituent springs (as will be seen in section 3), washers, particularly when nested are not linear springs and exhibit hysteresis, so such a calculation of stiffness would only be approximate). The strength (flattening load) of a stack is determined by the weakest parallel combination in the stack.

### 1.3 Analysis and design questions

The findings reported here must ultimately guide the selection of washer stacks the provide the desired level of seismic protection. This is the design question, given (a) an equipment, (b) its support structure, (c) seismic input (design spectrum) and (d) performance specifications (max base moment, max terminal displacement etc.), design a Belleville washer stack so that the system response meets the specifications.

A prerequisite to approaching this design question is being able to answer the analysis question, given (a) an equipment, (b), its support structure, (c) seismic input (ground motion record) and 1-6 (d) a specific Belleville washer configuration, compute the response of this system (accelerations, base moments, terminal displacements etc.). Hence the emphasis of this project is more on this analysis question and support for the analysis process from physical experimental measurements, with a focus as noted above on “rigid” structures, in particular a CVT.

### 1.4 Organization of the report

This report is organized as follows. As noted above, the main goal of this project is to develop an analysis-based systematic approach for design of a Belleville-washer seismic protective system. The report is therefore structured around an analysis procedure. This procedure is summarized upfront in section 2, and the various steps in this procedure are expounded in subsequent chapters. Characterizing the force-displacement hysteresis of a single stack of washers through cyclic loading tests is presented in section 3. Shake table experiments to characterized dynamic seismic response of a CVT equipment with Belleville washer stacks, including setup, instrumentation and specific steps for installing the washer stacks, are described in section 4. In section 5, a nonlinear dynamic model of the CVT with Belleville washer stacks is developed, and predictions from the model are compared with measurements from shake table experiments. An important note is that all the information needed for this model can be obtained from the washer characterization data from section 3, the type of information that can be readily obtained. In section 6, a linearized model based on equivalent stiffness and damping is developed that may be more conducive for practical use than the nonlinear model in section 5; this linear model can also be developed simply for the characterization data in section 3. The approach taken in this report

to analyze substation equipment with Belleville washer seismic protective systems loosely parallels that in ASCE 7 for seismically isolated structures; this is pointed out in section 6 to lend credence to the proposed approach relative to well-established procedures in seismic standards. Finally in section 7, a summary is provided, and some outstanding questions are identified.

## 2 Proposed analysis procedure

The main goal of this project is to develop an analysis-based systematic approach for design of a Belleville washer seismic protective system. Therefore, in this chapter, a proposed analysis procedure is laid out. This serves to tie together the different steps and experimental support for these steps discussed in subsequent chapters. The following is the proposed analysis procedure:

Given (a) an equipment, (b) its support structure, (c) seismic input (ground motion record), (d) Belleville washer configuration

1. Determine the force-displacement response of the stack.
  - In this project, we have done this by testing the stack in a material test machine (see section 3).
  - This is a hysteretic behavior.
2. Compute the moment-rotation behavior of the assembly of washer stacks (see section 5).
  - This can be done, for example, in an Excel spreadsheet.
  - In this project, special instrumentation has been used to experimentally verify the relationship between the stack force-displacement behavior and the system moment-rotation behavior (see section 4).
3. Model this moment-rotation behavior – two possible approaches.
  - Fit a hysteresis model (section 5).
  - Compute an “equivalent” stiffness and damping (section 6).
  - Both approaches have been verified in this project; it has also been verified that this equivalent stiffness and damping agrees well with fitting a linear model to the measured response.
4. Compute the system response – three approaches are possible.
  - Nonlinear time-history analysis with the hysteresis model for the washer arrangement (section 5).
  - Linear time history analysis with the equivalent stiffness and damping.
  - Response spectrum analysis with the equivalent stiffness and damping ((section 6). This together with the equivalent stiffness and damping resemble ASCE 7 process for base isolation (Chapter -)
  - In the project, it has been verified that the three approaches produce close responses.

## 3 Cyclic force-displacement behavior of washer stacks

This chapter is on the measurement of force-displacement behavior of Belleville washer stacks. As will be seen in sections 5 and 6, this is the primary information required to predict the seismic response of rigid equipment (besides mass, moment of inertia of the equipment itself and support structure stiffness).

The force displacement response of a washer stack is obtained here by applying cyclic compressive loading to the stack in a materials testing machine. At first, this was done by simply compressing the stack between loading plates as shown in Figure 3-1(a). The resulting force-displacement curves of Figure 3-1(b) showed changes in slope that weren’t observed in force-displacement measurements of the same stack in shake table tests (the special instrument designed to measure this response in situ under the equipment in the shake table test is discussed in section 4). This is likely because of slight misalignment between washers in the stack initially that corrects itself during the loading. To avoid this, an alternative

approach was devised, where the compressive loading was applied to the stack through a loading frame and guiding rod as illustrated in Figure 3-2(a). This arrangement is closer to how the washer stack is installed under the equipment. The guiding rod prevents any initial misalignment and subsequent realignment. The resulting force-displacement measurement, shown in Figure 3-2(b), does not have any unexpected changes in slope. Indeed the in situ measurements from the shake table tests follow these curves closely as seen in Figure 3-3.

Figure 3-4 shows force-displacement curves for two configurations of the K1750-J-057 washers. They exhibit the reduction in stiffness with loading noted in Figure 2 due to their higher  $h/t$  ratio.

## 4 Shake table experiments

## 5 Nonlinear modeling and analysis

## 6 Equivalent linear modeling

## 7 Summary and concluding remarks

### 7.1 Executive summary

A modeling procedure has been developed to predict the seismic response of rigid equipment such as CVTs equipped with Belleville washer stacks at the base for seismic protection. The procedure allows for nonlinear dynamic analysis or an equivalent linear analysis, and is outlined in section 2. The starting points are (a) the force-displacement hysteretic behavior of an individual stack that can be readily obtained by cyclic loading in a materials test machine, (b) inertia properties of the CVT – mass, mass moment of inertia and center of mass location. With this, the seismic response can be predicted reliably. This has been validated with experiments on an earthquake simulator (shake table). Special instrumentation was developed to obtain detailed in situ measurements of the behavior of the washer stacks in the shake table experiments. Validation using these measurements provides confidence that the analysis procedure can be used to inform decisions when installing Belleville washer devices in the field. The process also parallels procedures in ASCE 7-16 for seismic isolators.

The washer stacks essentially act as seismic isolators, reducing the frequency and increasing the damping. They are effective in reducing the insulator base moment. As is the case with seismic isolation systems, reduction in base moment has to be traded off with increase in terminal displacement.

### 7.2 Outstanding research questions

Some outstanding research questions remain:

Testing and modeling with different washer types; only one washer type has been studied completely (K1875-G-086). A second washer type has been studied partially (K1750-J-057), but some issues were discovered and are being remedied. It will be useful to complete the study with the K1750 washer type, as well as one other washer type from a different vendor.

Testing and modeling beyond flattening load: When subject to earthquake larger than what the spring washer protective system is designed for, the washer is likely to flatten, causing a different type of dynamics. It will be useful to study this performance under extreme loading. This is similar to when a base isolation system hits its displacement limit, which is considered in the design.

Testing and modeling single acting configuration: Thus far, we have only test cases with the spring washers in a single acting configuration, but that one configuration revealed promising behavior consisting of flag-shaped hysteretic behavior. It will be useful to study this further.

## References

- [1] R. Couch and R. Deacon, "Procedures and criteria for increasing the earthquake resistance level of electrical substations and special installations," tech. rep., Agbabian Associates, El Segundo, CA (USA), 1973.
- [2] R. S. Cochran, "Seismic base isolation of a high voltage transformer," in *Electrical Transmission and Substation Structures 2015*, pp. 413–425, 2015.
- [3] L. Kempner Jr. and M. Riley, "High voltage transformer base isolation," in *Proceedings of the 11th Canadian Conference on Earthquake Engineering*, 2015.
- [4] K. Oikonomou, M. C. Constantinou, A. M. Reinhorn, and L. Kempner Jr, "Seismic isolation of high voltage electrical power transformers," *MCEER Technical Report MCEER-16*, vol. 6, 2016.
- [5] M. A. Saadeghvaziri, B. Feizi, L. Kempner Jr, and D. Alston, "On seismic response of substation equipment and application of base isolation to transformers," *IEEE Transactions on power delivery*, vol. 25, no. 1, pp. 177–186, 2009.
- [6] N. Blunt, "The Difference Between Disc Springs and Belleville Washers." [https://www.spirol.com/assets/files/disc\\_wp\\_differences\\_between\\_disc\\_springs\\_and\\_belleville\\_washers\\_us.pdf](https://www.spirol.com/assets/files/disc_wp_differences_between_disc_springs_and_belleville_washers_us.pdf). Accessed: 11-8-2025.
- [7] J. E. Shigley and C. R. Mischke, *Standard handbook of machine design*. New York, NY: McGraw-Hill, 2004.
- [8] G. Ashworth, "The disk spring or belleville washer," *Proceedings of the Institution of Mechanical Engineers*, vol. 155, no. 1, pp. 93–100, 1946.
- [9] J. O. Almen and A. Laszlo, "The uniform-section disk spring," *Journal of Fluids Engineering*, vol. 58, no. 4, pp. 305–314, 1936.
- [10] Y. Zhou, D. Wang, Z. Qiu, Z. Wei, W. Chen, and R. Zhu, "Modeling of disc springs based on energy method considering asymmetric frictional boundary," *Thin-Walled Structures*, vol. 190, p. 110971, 2023.
- [11] M. Korytov, V. Shcherbakov, V. Titenko, I. Kashapova, and V. Derkach, "Use of the belleville spring package in the vibration protection mechanism of the operator's seat," in *Journal of Physics: Conference Series*, vol. 2182, p. 012056, IOP Publishing, 2022.
- [12] C. Maletta, L. Filice, and F. Furgiuele, "Niti belleville washers: Design, manufacturing and testing," *Journal of intelligent material systems and structures*, vol. 24, no. 6, pp. 695–703, 2013.
- [13] Solon Manufacturing Co., "Belleville Spring Washer Applications & Solutions." <https://www.solonmfg.com/washer-applications>. Accessed: 11-8-2025.
- [14] T. Fujita, "Fundamental study of three-dimensional seismic isolation system for nuclear power plants," in *Proceedings of Eleventh World Conference on Earthquake Engineering, 1996-6*, vol. 5, 1996.
- [15] S. Kitamura, T. Nakatogawa, A. Miyamoto, and T. Somaki, "Experimental study on coned disk springs for vertical seismic isolation system," *Transaction of the 17th SMiRT, Prague, Czech Republic, August, Division K, Paper# K10*, vol. 2, 2003.
- [16] S. Kitamura, S. Okamura, and K. Takahashi, "Experimental study on vertical component seismic isolation system with coned disk spring," in *ASME Pressure Vessels and Piping Conference*, vol. 41936, pp. 175–182, 2005.
- [17] S. Ramhormozian, G. C. Clifton, G. A. MacRae, and G. P. Davet, "Stiffness-based approach for belleville springs use in friction sliding structural connections," *Journal of Constructional Steel Research*, vol. 138, pp. 340–356, 2017.
- [18] M. Speicher, D. E. Hodgson, R. DesRoches, and R. T. Leon, "Shape memory alloy tension/compression device for seismic retrofit of buildings," *Journal of materials engineering and performance*, vol. 18, no. 5, pp. 746–753, 2009.

- [19] K. E. Hill, *The utility of ring springs in seismic isolation systems*. Phd thesis, University of Canterbury, Department of Mechanical Engineering, Christchurch, New Zealand, 1995.
- [20] K. Ma, Y. Zhou, and D. Lu, “Theoretical and experimental investigation on disc spring isolation system with loading rings,” *Soil Dynamics and Earthquake Engineering*, vol. 165, p. 107655, 2023.
- [21] IEEE recommended practice for seismic design for substations, *IEEE Std 693-1984*, 1984.
- [22] Key Bellevilles Inc., “Belleville spring washer applications & solutions.” <https://keybellevilles.com/bellevilles/sampleCatalog>. Accessed: 11-8-2025.