

# CS1332 Campus Spring 2023 Exam 2 Version C2

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TOTAL POINTS

**82 / 100**

QUESTION 1

Efficiency - Multiple Choice 14 pts

1.1 Part A 2 / 2

- + 0 pts \$\$O(1)\$\$
- + 0 pts \$\$O(\log n)\$\$
- ✓ + 2 pts \$\$O(n)\$\$
- + 0 pts \$\$O(n \log n)\$\$
- + 0 pts \$\$O(n^2)\$\$

1.2 Part B 2 / 2

- + 0 pts \$\$O(1)\$\$
- ✓ + 2 pts \$\$O(\log n)\$\$
- + 0 pts \$\$O(n)\$\$
- + 0 pts \$\$O(n \log n)\$\$
- + 0 pts \$\$O(n^2)\$\$

1.3 Part C 0 / 2

- + 0 pts \$\$O(1)\$\$
- + 0 pts \$\$O(\log n)\$\$
- + 2 pts \$\$O(n)\$\$
- ✓ + 0 pts \$\$O(n \log n)\$\$
- + 0 pts \$\$O(n^2)\$\$

1.4 Part D 0 / 2

- ✓ + 0 pts \$\$O(1)\$\$
- + 0 pts \$\$O(\log n)\$\$
- + 2 pts \$\$O(n)\$\$

+ 0 pts \$\$O(n \log n)\$\$

+ 0 pts \$\$O(n^2)\$\$

1.5 Part E 0 / 2

- + 2 pts \$\$O(1)\$\$
- ✓ + 0 pts \$\$O(\log n)\$\$
- + 0 pts \$\$O(n)\$\$
- + 0 pts \$\$O(n \log n)\$\$
- + 0 pts \$\$O(n^2)\$\$

1.6 Part F 2 / 2

- ✓ + 2 pts \$\$O(1)\$\$
- + 0 pts \$\$O(\log n)\$\$
- + 0 pts \$\$O(n)\$\$
- + 0 pts \$\$O(n \log n)\$\$
- + 0 pts \$\$O(n^2)\$\$

1.7 Part G 2 / 2

- + 0 pts \$\$O(1)\$\$
- + 0 pts \$\$O(\log n)\$\$
- + 0 pts \$\$O(n)\$\$
- ✓ + 2 pts \$\$O(n \log n)\$\$
- + 0 pts \$\$O(n^2)\$\$
- + 0 pts blank

QUESTION 2

Code ID - Multiple Choice 8 pts

2.1 Part 1 4 / 4

+ 0 pts `peek()`	+ 2.5 pts Fully Correct
+ 0 pts `enqueue(T data)`	Partial Credit
+ 0 pts `pop()`	✓ + 0.5 pts <i>Binary Tree</i>
✓ + 4 pts `push(T data)`	✓ + 0.75 pts <i>MaxHeap</i>
+ 0 pts no answer/incorrect	+ 0 pts Incorrect

## 2.2 Part 2 4 / 4

+ 0 pts `add(T data)`
+ 0 pts `enqueue(T data)`
+ 0 pts `pop()`
✓ + 4 pts `dequeue()`
+ 0 pts no answer/incorrect

## QUESTION 3

### Tree Identification - Multiple Select 10 pts

#### 3.1 Part 1 0.5 / 2.5

+ 2.5 pts Fully Correct - Binary Tree Only

Partial Credit

✓ + 0.25 pts *Binary Tree*

✓ + 0.25 pts *MinHeap*

+ 0 pts Incorrect

#### 3.2 Part 2 1.25 / 2.5

+ 2.5 pts Fully Correct

Partial Credit

✓ + 0.5 pts *Binary Tree*

+ 0.75 pts BST

✓ + 0.75 pts AVL

+ 0 pts Incorrect

#### 3.3 Part 3 1.25 / 2.5

## 3.4 Part 4 0.5 / 2.5

+ 2.5 pts Fully Correct
Partial Credit
✓ + 0.5 pts <i>Binary Tree</i>
+ 0.75 pts BST

## QUESTION 4

### 4 HashMap - Diagramming 5.5 / 12

+ 12 pts Completely Correct:

![VC\_answer.png](/files/48bb3aec-3bd4-4340-9ab1-e150417dec04)

Partial

+ 1 pts Key `19` appears once, and is updated with value `a`

+ 1 pts Key `19` appears once, and is at index 1

+ 0.5 pts `<17, k>` is added

+ 2 pts Key `17` is at index 7

+ 0.5 pts `<7, g>` is added

+ 2 pts Key `7` is at index 9

+ 0.5 pts Key `8` is present in the hashmap

+ 0.5 pts Key `8` has value `f`

+ 2 pts Key `8` is at index 2

+ 1 pts key `8` can be probed to from index 8

+ 1 pts No other data has been added, removed,

or moved, and there are no duplicate keys

Partial - Resized Backing Array

✓ + 1 pts *Backing array is resized to correct length:*

$21 \cdot (2 * \text{length}) + 1$

✓ + 0.5 pts *Key '10' is rehashed at correct index based on new length (index 10 for length 21)*

✓ + 0.5 pts *Key '19' is rehashed at correct index based on new length & rehashed entries (index 19 for length 21)*

✓ + 0.5 pts *Key '4' is rehashed at correct index based on new length & rehashed entries (index 4 for length 21)*

✓ + 0.5 pts *Key '17' is rehashed at correct index based on new length & rehashed entries (index 17 for length 21)*

✓ + 0.5 pts *Key '18' is rehashed at correct index based on new length & rehashed entries (index 18 for length 21)*

✓ + 0.5 pts *Key '7' is rehashed at correct index based on new length & rehashed entries (index 7 for length 21)*

✓ + 0.5 pts *Key '8' is rehashed at correct index based on new length & rehashed entries (index 8 for length 21)*

✓ + 1 pts *'DEL' entry is not copied to new backing array*

+ 2 pts All values are correctly copied and updated (i.e. '10' has value 'o', '17' has value 'a', '7' has value 'd', etc.),

AND there are no duplicate keys

+ 0 pts Incorrect/ No Answer

## 5 SkipList - Diagramming 10 / 10

✓ + 10 pts Completely Correct: \*\*HHHT HHHT HHT HT HHHHT\*\*

Partial Credit - First Substring

+ 2 pts Completely correct HHHT

+ 1 pts Has 1 extra H: HHHHT (counting the last level as promotion)

+ 0 pts No answer / Incorrect

Partial Credit - Second Substring

+ 2 pts Completely correct HHHT

+ 1 pts Has 1 extra H: HHHHT (counting the last level as promotion)

+ 0 pts No answer / Incorrect

Partial Credit - Third Substring

+ 2 pts Completely correct: HHT

+ 1 pts Has 1 extra H: HHHT (counting the last level as promotion)

+ 0 pts No answer / Incorrect

Partial Credit - Fourth Substring

+ 2 pts Completely correct: HT

+ 1 pts Has 1 extra H: HHT (counting the last level as promotion)

+ 0 pts No answer / Incorrect

Partial Credit - Fifth Substring

+ 2 pts Completely correct: HHHHT

+ 1 pts Has 1 extra H: HHHHHT (counting the last level as promotion)

+ 0 pts No answer / Incorrect

+ 4 pts Used T instead of H for promotion. Only get credit if completely correct when replacing H with T

**+ 4 pts** String is trying to add in data from left to right. Has to be completely correct in this order to earn this credit.

**- 1 pts** Minor Error

**+ 0 pts** No answer / Incorrect

#### QUESTION 6

### 6 2-4 Tree - Diagramming 10 / 10

Add

✓ **+ 4 pts**

![add59.png](/files/471710d9-fcff-44aa-b2dd-71560d20bbe8)

*Completely Correct*

**+ 3 pts**

![wrAdd59.jpeg](/files/59b296bc-4a2d-4003-9441-2a72fe94a807)

Promoted the wrong element

**+ 1 pts** Valid 2-4 Tree

**+ 1 pts** 59 has been added

**+ 1 pts** Resulting tree has 3 levels

**- 1 pts** Minor Error (an element is in the wrong node)

**+ 0 pts** Incorrect

Remove

✓ **+ 6 pts**

![remove5.png](/files/58f5cf79-4159-480f-9119-de92ed5041be) Completely correct

**+ 4 pts**

![wrRem5.jpeg](/files/4ae04bda-2bd0-4113-94c3-5747f3c4b808) Uses wrong successor/predecessor Fuses with the wrong parent data

**+ 1 pts** Valid 2-4 tree

**+ 1 pts** 5 has been removed

**+ 1 pts** Tree has 2 levels

**- 1 pts** Minor Error (an element is in the wrong node)

**+ 0 pts** Incorrect

**+ 0 pts** Incorrect

#### QUESTION 7

### 7 AVL - Diagramming 12 / 12

add

✓ **+ 6 pts** completely correct

![Screenshot\_2023-03-

08\_at\_10.55.50\_PM.png](/files/19c84e6d-78c3-4de9-8337-59e20b78e832)

**+ 1 pts** PARTIAL: '27' is added as a leaf node

**+ 1 pts** PARTIAL: tree is balanced

**+ 1 pts** PARTIAL: tree preserves order property

**+ 1 pts** PARTIAL: other than '27', no other data is added or removed

**+ 0 pts** INCORRECT/BLANK

remove

✓ **+ 6 pts** completely correct

![Screenshot\_2023-03-

08\_at\_10.55.55\_PM.png](/files/66326661-c0bd-4f97-b7d1-1722a2a34b8d)

**+ 1 pts** PARTIAL: '75' is not present in tree

**+ 1 pts** PARTIAL: tree is balanced

- + 1 pts PARTIAL: tree preserves order property
- + 1 pts PARTIAL: other than '75', no other data is added or removed
- + 0 pts INCORRECT/BLANK

QUESTION 8

## 8 MaxHeap - Coding 9 / 9

- ✓ + 1.5 pts Throws `IndexOutOfBoundsException` when  $A$  or  $B$  is  $\leq 0$
- ✓ + 1 pts Returns a boolean
- ✓ + 1 pts Correctly returns `isParent/isChild` (single if-statement or part of loop)
- ✓ + 1.5 pts Has a while loop or uses recursion
- ✓ + 1 pts Loop/recursion is not infinite
- ✓ + 1 pts Loop/recursion breaks as soon as `isAncestor/isDescendant` is determined
- ✓ + 1 pts Correctly handles case  $A == B$  (can be implicit)
- ✓ + 1 pts Correctly returns `isAncestor/isDescendant` in all other cases
- 1 pts Efficiency: i.e. Checks `'index*2'` and `'index*2 +1'` recursively, unnecessary operations
- 1 pts Minor error: (e.g. attempts to use size or backing array)
- 0.5 pts Syntax
- + 0 pts Incorrect/No Answer
- + 0 pts

![Screenshot\_2023-03-09\_at\_5.16.08\_PM.png](/files/f0153828-5d9e-43d8-94f0-6ddb9fdd23ba)

QUESTION 9

## 9 BST - Coding 15 / 15

- + 0 pts
- ![Screen\_Shot\_2023-03-08\_at\_6.23.06\_PM.png](/files/c23d8c69-054a-4773-bf77-989a9be8aeda)
- ✓ + 1 pts Attempts to initialize a list
- ✓ + 1 pts Correctly initializes an arraylist or linkedlist in the public method given in the question
- ✓ + 1 pts Returns something
- ✓ + 1 pts Returns the list
- ✓ + 1 pts Has a helper method
- ✓ + 1 pts Throws an exception somewhere
- ✓ + 1 pts Correctly throws `NoSuchElementException` if data is not in the tree
- ✓ + 1 pts Returns without adding to the list if found data
- ✓ + 1 pts Attempts to check if current node's data is even
- ✓ + 1 pts Correctly checks if current node's data is even
- ✓ + 1 pts Adds to the list if current node's data is even
- ✓ + 1 pts There is a recursive call somewhere
- ✓ + 1 pts Attempts to compare `curr.data` and `data`
- ✓ + 1 pts If `curr.data` is less than `data` recurse to the right
- ✓ + 1 pts Else if `curr.data` is greater than `data` recurse to the left
- 1 pts Efficiency
- 1 pts Minor Error
- 1 pts Syntax Error
- + 0 pts Incorrect/No answer

QUESTION 10

10 Bonus 1 / 0

✓ + 1 pts Correct

+ 0 pts Incorrect

# CS 1332 Exam 2 - Version C2

## Spring Semester 2023 - March 8, 2022

Name (print clearly including your first and last name): Vudit Pokharna

Section (8:25 am - A, 9:30 am - B, 2:00 pm D, 3:30 pm - C, Online - O): C

Signature: vuditpokharna

GT account username (msmith3, etc): vpokharna3

GT account number (903000000, etc): 903772087

- ⌚ You must have your BuzzCard or other form of identification on the table in front of you during the exam. It is your responsibility to have your ID prior to beginning the exam.
- ⌚ You are not allowed to leave the exam room and return. If you leave the room for any reason, then you must turn in your exam as complete.
- ⌚ Signing and/or taking this exam signifies you are aware of and in accordance with the Academic Honor Code of Georgia Tech and the Georgia Tech Code of Conduct.
- ⌚ Notes, books, calculators, phones, laptops, smart watches, headphones, etc. are not allowed. Extra paper is not allowed. If you have exhausted all space on this test, talk with your instructor. There are extra blank pages in the exam for extra space.
- ⌚ If you plan on using ear plugs (foam or silicone, NOT AirPods) during the exam, you must show them to the instructor for approval.
- ⌚ Pens/pencils and erasers are allowed. Do not share.
- 🦆 If you brought a duck with you to the exam, you may silently consult with it at any time.
- ⌚ All work entered on this exam, whether code, diagrams or multiple choice, must be implemented as was presented in lecture and recitation.
- ⌚ All code must be in Java.
- ⌚ Efficiency matters. For example, if you code something that uses  $O(n)$  time when there is a way to do it in  $O(1)$  time, your solution may lose credit. If your code traverses data 5 times when once would be sufficient, this also is considered poor efficiency even though both are  $O(n)$ .
- ⌚ Comments are not required unless a question explicitly asks for them.

**This page is intentionally left almost blank.**

(If you use this page for your work, please reference this page number on the question you are answering so we can find your response)

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Question	Points
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9) BST - Coding	9
10) Bonus	1

## 1) Efficiency - Multiple Choice [14 points]

For each of the operations listed below, determine the time complexity of the operation as it pertains to the data structure. Select the bubble corresponding to your choice in the space provided, and completely fill in the bubble. Unless otherwise stated, assume the **worst-case** time complexity. However, make sure you choose the tightest Big-O upper bound possible for the operation. **Do not use an amortized analysis for these operations unless otherwise specified.**

A) **Average** case of finding data in a Skiplist where the coin flips only to tails. In this skiplist, tails trigger additions.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

B) Adding an element in a 2-4 tree given that the operation is guaranteed to not cause an overflow in a node.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

C) Adding to a MaxHeap assuming that the size of the heap before the operation is exactly one less than the length of the backing array.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

D) Calling add() on a Hashmap that uses external chaining and has no chains with multiple elements.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

E) Given an AVL node on the lowest level, finding the length of the path between that node and the root.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

F) **Average** case of adding to a Hashmap that uses linear probing and has a good hash function given that the operation will not trigger a resize.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

G) Clearing an AVL by repeatedly calling remove for each of the n elements in the AVL.

- O(1)       O(log n)       O(n)       O(n log n)       O(n<sup>2</sup>)

## 2) Code ID - Multiple Choice [8 points]

Choose the correct name for the method which is described by a provided code snippet. The methods given below apply to the following data structures based on implementations taught in class - **Stack**, **Queue**, **Heap**, **BST**.

```
if (data == null) {  
    throw new IllegalArgumentException("Data cannot be null");  
}  
if (size == backingArray.length) {  
    resize();  
}  
backingArray[size] = data;  
size++;
```

- peek()
- enqueue(T data)
- pop()
- push(T data)

```
if (size == 0) {  
    throw new java.util.NoSuchElementException("Empty");  
}  
T result = backingArray[front];  
backingArray[front] = null;  
front = (front + 1) % backingArray.length;  
size--;  
return result;
```

- add(T data)
- enqueue(T data)
- pop()
- dequeue()

### 3) Tree Identification - Multiple Select [10 points]

For each of the given trees, **select all** tree type(s) that apply to the given tree. There are 4 tree types to choose from. For selected answers please completely fill the squares.

Given Tree	Tree Type (Select all that apply)
A binary search tree with root 10. The tree structure is as follows: <pre>graph TD; 10 --&gt; 17; 10 --&gt; 23; 17 --&gt; 18; 17 --&gt; 21; 21 --&gt; 22; 23 --&gt; 34; 23 --&gt; 26; 34 --&gt; 44; 34 --&gt; 40; 26 --&gt; 29; 26 --&gt; 90;</pre>	<input checked="" type="checkbox"/> Binary Tree <input type="checkbox"/> Binary Search Tree <input checked="" type="checkbox"/> MinHeap <input checked="" type="checkbox"/> AVL
A binary search tree with root 32. The tree structure is as follows: <pre>graph TD; 32 --&gt; 22; 32 --&gt; 38; 22 --&gt; 7; 22 --&gt; 26; 7 --&gt; 5; 7 --&gt; 8; 26 --&gt; 24; 38 --&gt; 34; 38 --&gt; 56; 34 --&gt; 33;</pre>	<input checked="" type="checkbox"/> Binary Tree <input type="checkbox"/> Binary Search Tree <input type="checkbox"/> MaxHeap <input checked="" type="checkbox"/> AVL

<pre>graph TD; 67((67)) --&gt; 45((45)); 67 --&gt; 32((32)); 45 --&gt; 9((9)); 45 --&gt; 15((15)); 9 --&gt; 5((5)); 9 --&gt; 6((6)); 15 --&gt; 11((11)); 15 --&gt; 12((12)); 12 --&gt; 1((1)); 8 --&gt; 22((22));</pre>	<ul style="list-style-type: none"><li><input checked="" type="checkbox"/> Binary Tree</li><li><input type="checkbox"/> Binary Search Tree</li><li><input checked="" type="checkbox"/> MaxHeap</li><li><input checked="" type="checkbox"/> AVL</li></ul>
<pre>graph TD; 14((14)) --&gt; 10((10)); 14 --&gt; 22((22)); 10 --&gt; 3((3)); 10 --&gt; 0((0)); 10 --&gt; 7((7)); 22 --&gt; 17((17)); 17 --&gt; 15((15));</pre>	<ul style="list-style-type: none"><li><input checked="" type="checkbox"/> Binary Tree</li><li><input type="checkbox"/> Binary Search Tree</li><li><input type="checkbox"/> MaxHeap <input checked="" type="checkbox"/></li><li><input type="checkbox"/> AVL <input checked="" type="checkbox"/></li></ul>

## 4) HashMap – Diagramming [12 points]

**Goal:** The HashMap below is backed by an array of capacity 10. Perform all of the below operations in order on the HashMap and draw the final backing array at the bottom of the page. The maximum load factor for this HashMap is 0.85. Circle the final answer if you draw multiple arrays.

**Requirements:** If you need a collision resolution strategy, use **Linear Probing** as taught in lecture. The hashCode of a particular number is the absolute value of the number itself. The compression function is to mod by the table length. If an element is deleted, represent it by writing "DEL" for the deleted element's index.

0.85

8.5  
15

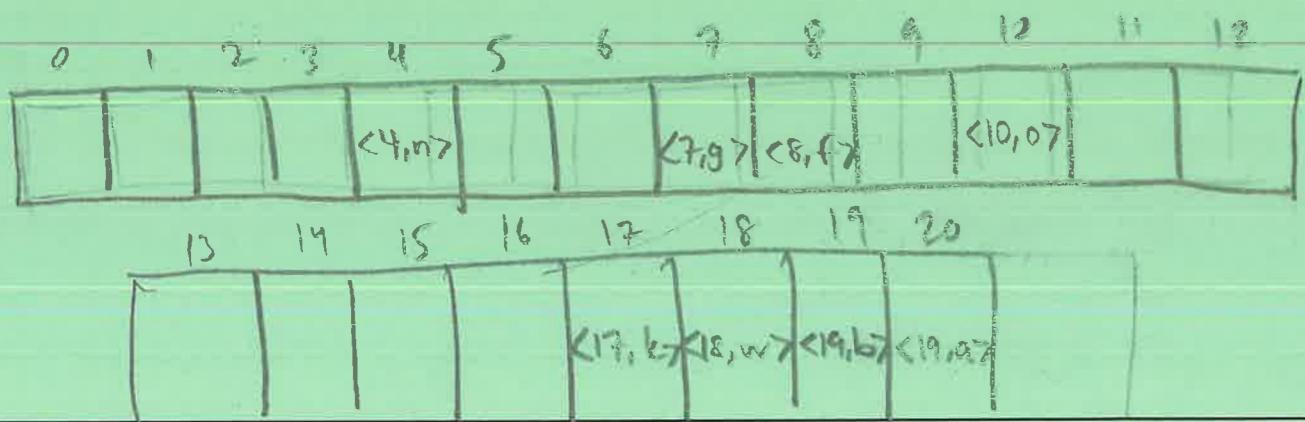
Initial Backing Array:

0	1	2	3	4	5	6	7	8	9
<10, o>	<19, b>	<19, a>	7	DEL	<4, n>	11	<17, e>	<18, w>	s8, h> DEL

Operations:

- put(19, "a")
- remove(8)
- put(17, "k")
- put(7, "g")
- put(8, "f")

Final Backing Array:



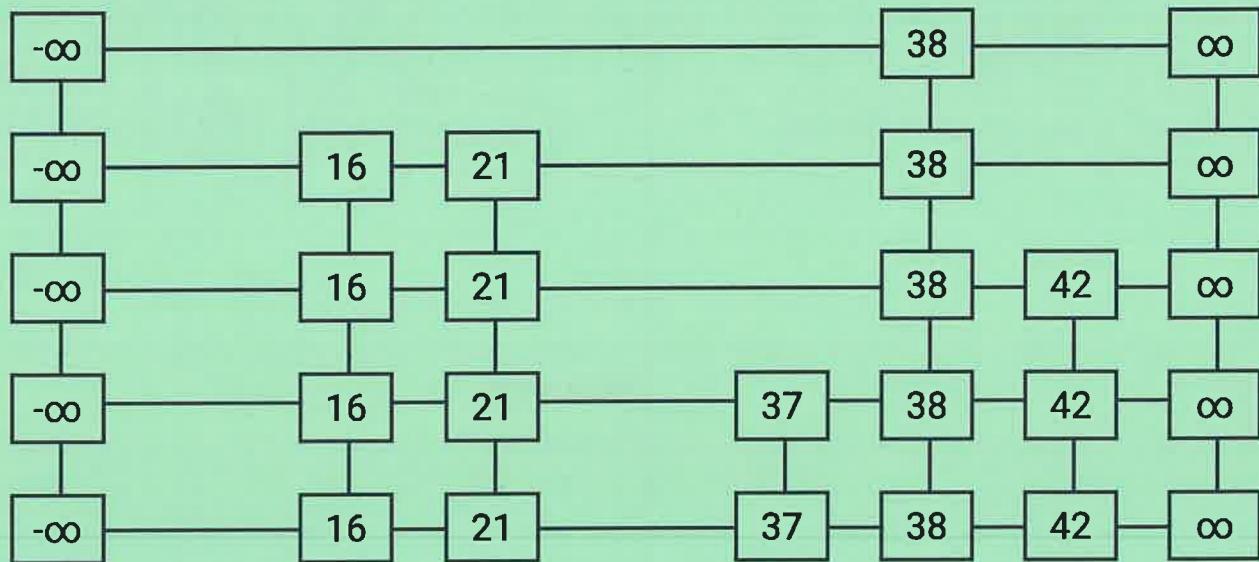
## 5) Skiplist Diagramming [10 points]

**Description:** Starting with an empty skiplist, after the series of **add()** operations below, the resulting Skiplist is as illustrated.

**Goal:** Write the sequence of Heads (H) and Tails (T) coin tosses that was used in the add operations below to construct the Skiplist that was drawn below. Your answer, for example, should be in the format "HHTHTT", with H representing Head and T representing Tail in the sequence of coin tosses. **Use Heads as promotion in your answer.**

The series of **add()** operations were performed **in the following order**:

**add(16) 3**  
**add(21) 3**  
**add(42) 2**  
**add(37) 1**  
**add(38) 4**



**Write the coin toss sequence used in constructing the Skiplist above in the provided table below.** You may not have to use all cells:

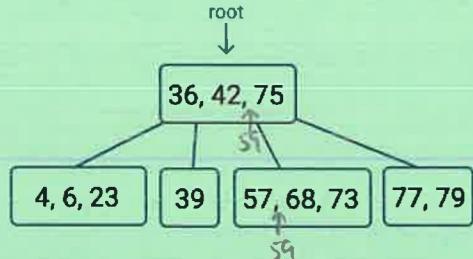
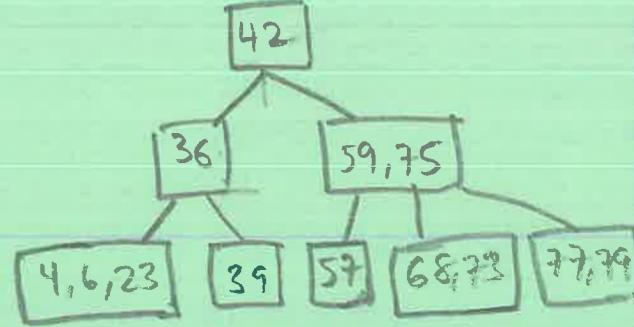
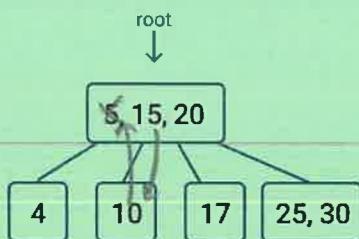
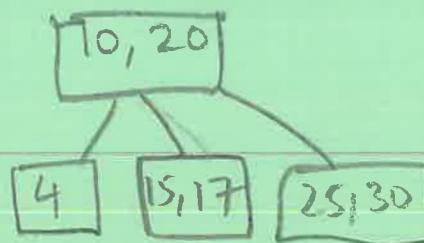
H	H	H	T	H	H	H	T	H	H	T	H	T	H	H	H	H	T		
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	--	--

## 6) 2-4 Tree - Diagramming [10 points]

Given the following initial 2-4 trees in the left column below, perform the stated operation. Draw the resulting 2-4 tree in the right column. If you want, you can draw multiple steps (circle the final step if you do so). Follow the implementation taught in the **1332 module videos** and live lectures. Please read the instructions below carefully.

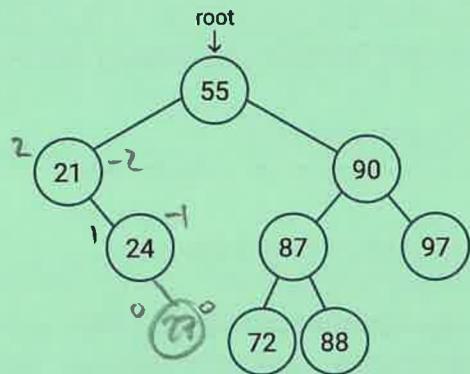
### Implementation Details:

If you need to promote an element from a node, use the **second** element. When needed, use the **successor**. When checking if a transfer is possible, check the **right** sibling before the **left** sibling. If a fusion is necessary and the node has more than one parent data, choose the **right** parent data.

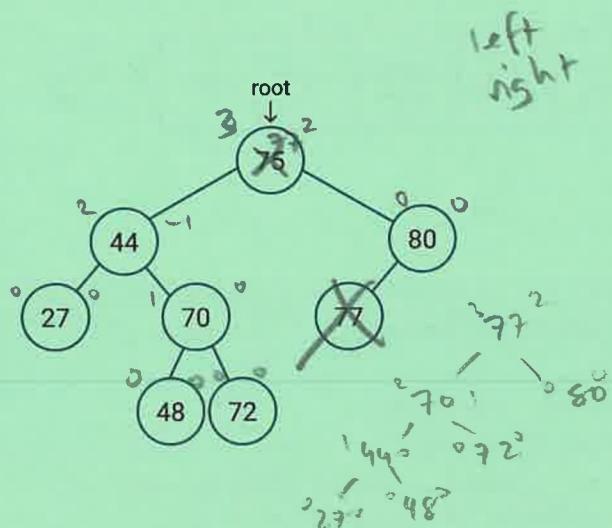
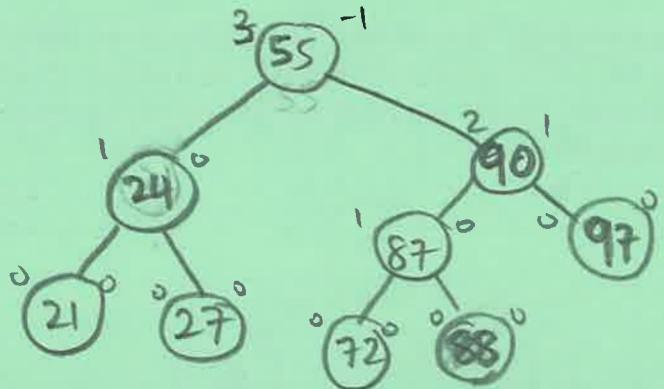
	<p><b>add(59)</b></p> 
	<p><b>remove(5)</b></p> 

## 7) AVL - Diagramming [12 points]

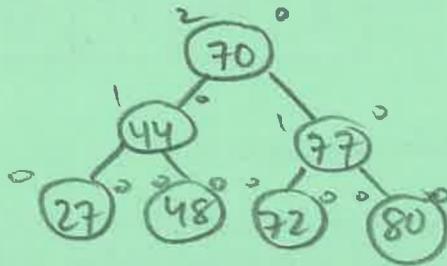
Given the following initial AVL, perform the stated operation and draw your final answer in the box provided. If necessary for any operation, use the **successor node**.



add(27)



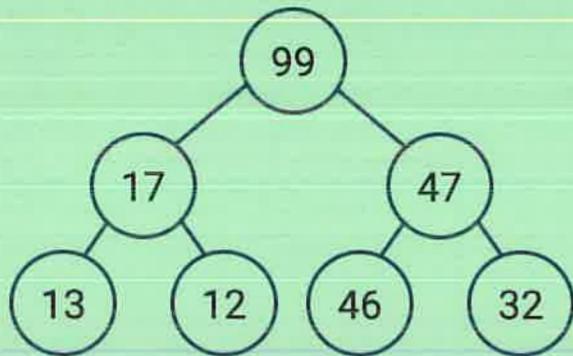
remove(75)



## 8) MaxHeap - Coding [9 points]

**Goal:** Given two integers, **indexA** and **indexB**, that represent the **indices** of data in a maxheap, write a method that determines if the node at **indexA** is a descendant of the node at **indexB**. An element in a heap is considered a **descendant** of another element if it exists in the subtree of the parent element (see example below). An element is also considered a descendant of itself.

**Requirements:** The method should throw an **IndexOutOfBoundsException** if **indexB** or **indexA** is less than the start index of the heap. The method should return **true** if A is a descendant of B, and false otherwise. You do not have access to the backing array. Remember, **indexA** and **indexB** are indices in the array!



**Examples** (With tree and array representations of a heap for reference):

- `isDescendant(5, 1)` returns `true`
  - Index 5 (12) is a descendant of Index 1 (99)
- `isDescendant(4, 3)` returns `false`
  - Index 4 (13) is NOT a descendant of index 3 (47)
- `isDescendant(1, 1)` returns `true`

	0	1	2	3	4	5	6	7	8	9
	X	99	17	47	13	12	46	32	X	X

```
public class Solution {  
  
    /**  
     * Returns a boolean value representing whether or not  
     * index a is a descendant of index b.  
     * @param indexA The index of the descendant element.  
     * @param indexB The index of the ancestor element.  
     * @return true if indexA is descendant of indexB, false otherwise.  
     * @throws java.lang.IndexOutOfBoundsException if indexB <= 0 or  
     * indexA <= 0  
    */  
    public boolean isDescendant(int indexA, int indexB) {  
        //WRITE YOUR METHOD HERE  
        if(indexA <= 0 || indexB <= 0){  
            throw new IndexOutOfBoundsException("One or more indices is less than 0");  
        }  
    }  
}
```

```
if(indexA < indexB) {
    return false;
} else if(indexA == indexB) {
    return true;
} else {
    while(indexA >= indexB) {
        indexA /= 2;
        if(indexA == indexB) {
            return true;
        }
    }
    return false;
}

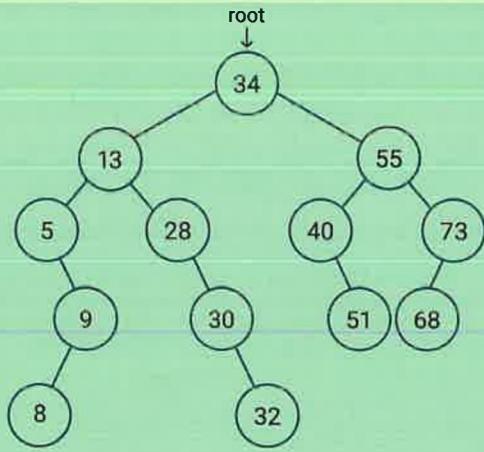
} // END OF METHOD

} //END OF CLASS
```

## 9) BST - Coding [15 points]

**Goal:** Given a binary search tree with integers, write a method which returns a list of all of the even integers that are ancestors of the passed in data. **Even integers refer to data in the node being even, not the level.** An ancestor node is **either the parent of the node or the parent of some ancestor of the node**. Data contained in the list should be in the order of **increasing depth**. The data being searched for should not be included, even if it is even.

**Requirements:** Your implementation should be **recursive**. Do not modify the tree or the method header provided. Feel free to write any helper methods you consider to be necessary. Since **Node** is an inner class, access its fields directly (e.g. `node.left`). **Assume the List, ArrayList, LinkedList, and NoSuchElementException classes are imported.** Your code should be as efficient as possible.



**Examples:** (on the tree above):

- `listEvenAncestors(32)` returns [34, 28, 30]
- `listEvenAncestors(51)` returns [34,40]

```
public class BST {  
  
    private static class Node {  
        int data;  
        Node right, left;  
    }  
    private Node root;  
  
    /**  
     * Records the even ancestors of input data in order of increasing depth.  
     * This should be implemented recursively.  
     * @param data - data to be searched for  
     * @return a list containing all even ancestors  
     * @throws NoSuchElementException if data is not present in BST  
     */  
    public List<Integer> listEvenAncestors(int data) {  
        List<Integer> list = new ArrayList<>();  
        return listEAHelper(root, data, list);  
    }  
}
```

```
private List<Integer> listEAHelper(Node node, int data, List<Integer> list) {  
    if (node == null) {  
        throw new NoSuchElementException("Data is not in tree!");  
    }  
    if (node.data > data) {  
        if (node.data % 2 == 0) {  
            list.add(node.data);  
        }  
        return listEAHelper(node.left, data, list);  
    } else if (node.data < data) {  
        if (node.data % 2 == 0) {  
            list.add(node.data);  
        }  
        return listEAHelper(node.right, data, list);  
    }  
    return list;  
}
```

```
} // END OF METHOD  
} // END OF CLASS
```

## 10) Bonus - Fill in the Blank [1 point]

For 1 extra point, please describe ONE city in the world  you would like to visit 😊 and why (inappropriate content will not receive credit):

Iceland. Some students visited my school from there and I've always wanted to go visit them since they came.