

## Homework 2 Report

### The Question:

On Aug 3, 2015 you buy a note for \$98 that will pay, on Dec 31, 2020, the arithmetic average of an underlying bond's prices observed on Jan 1 of each year 2016–2020.

The underlying is a 10-year bond issued Jan 1, 2010, 5% coupon, semiannual payments, face \$100.

Using Bond\_Ex3.csv, was buying this note a good investment?

### Results:

Underlying bond prices on observation dates

Observation Date	TTM (years)	Price
Jan 1, 2016	5	118.359
Jan 1, 2017	4	113.114
Jan 1, 2018	3	107.355
Jan 1, 2019	2	103.492
Jan 1, 2020	1	102.5

Arithmetic average (2016–2020): 108.964

Discounting the average back to Aug 3, 2015

- Year fraction (ACT/365) from 2015-08-03 to 2020-12-31: 5.41644
- Nearest-neighbor zero rate at  $T = 5.41644$ : 0.004419
- Discount factor  $e^{(-rT)}$ : 0.976349
- Present value at purchase =  $108.964 \times 0.976349 = 106.387$
- NPV versus purchase price \$98: +8.3868

### Conclusion:

The present value of the note's expected payoff at the purchase date is \$106.387, which exceeds the \$98 purchase price. The NPV is positive (+8.39). Therefore, buying the security on Aug 3, 2015 was a good investment under the given curve and assumptions.

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→ HW2_6767_Vidit_Pokharna git:(main) ✗ g++ -Wall -pedantic -std=c++11 bond.cpp main.cpp -o main
→ HW2_6767_Vidit_Pokharna git:(main) ✗ ./main

--- Demo ---
Bond (0, 0, 0)
Bond (11/19/2035, 0.5, 0.07)

--- Bond Pricing Unit Tests ---
[PASS] ToString exact
[PASS] Default ctor zeroes
[PASS] Flat-rate monotone
[PASS] Curve equals flat TS
[PASS] First coupon proration

All tests passed

--- Investment Analysis Using Pricing Data ---
Jan 1, 2016 TTM=4 Price=118.359
Jan 1, 2017 TTM=3 Price=113.114
Jan 1, 2018 TTM=2 Price=107.355
Jan 1, 2019 TTM=1 Price=103.492
Jan 1, 2020 TTM=0 Price=102.5
Average price (2016-2020): 108.964
Year fraction 2015-08-03 -> 2020-12-31 (ACT/365): 5.41644
Discount rate (nearest-neighbor at T=5.41644): 0.004419
Discount factor: 0.976349
PV at purchase: 106.387
NPV vs $98: 8.3868 => Good investment
```