

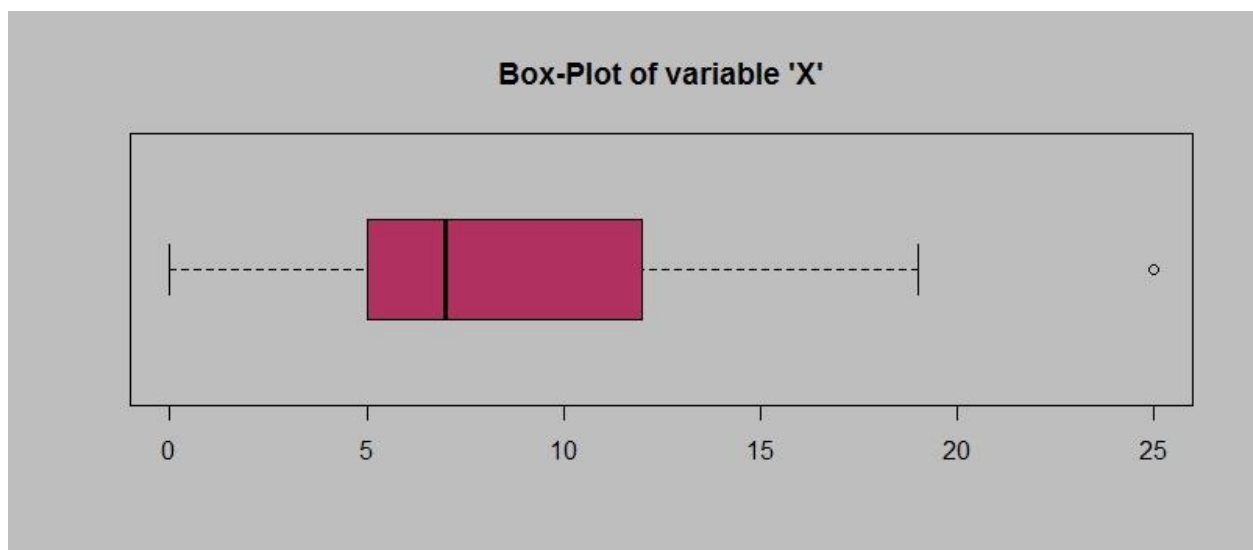
## Descriptive Statistics and Probability

1. Look at the data given below. Plot the data, find the outliers and find out  $\mu, \sigma, \sigma^2$

Name of company	Measure X
Allied Signal	24.23%
Bankers Trust	25.53%
General Mills	25.41%
ITT Industries	24.14%
J.P.Morgan & Co.	29.62%
Lehman Brothers	28.25%
Marriott	25.81%
MCI	24.39%
Merrill Lynch	40.26%
Microsoft	32.95%
Morgan Stanley	91.36%
Sun Microsystems	25.99%
Travelers	39.42%
US Airways	26.71%
Warner-Lambert	35.00%

Ans : From Boxplot----> Morgan Stanley = 91.36% is outlier  
Mean = 33.27  
Std = 16.94  
Var = 287.14

2.



Answer the following three questions based on the box-plot above.

- (i) What is inter-quartile range of this dataset? (please approximate the numbers) In one line, explain what this value implies.

## Descriptive Statistics and Probability

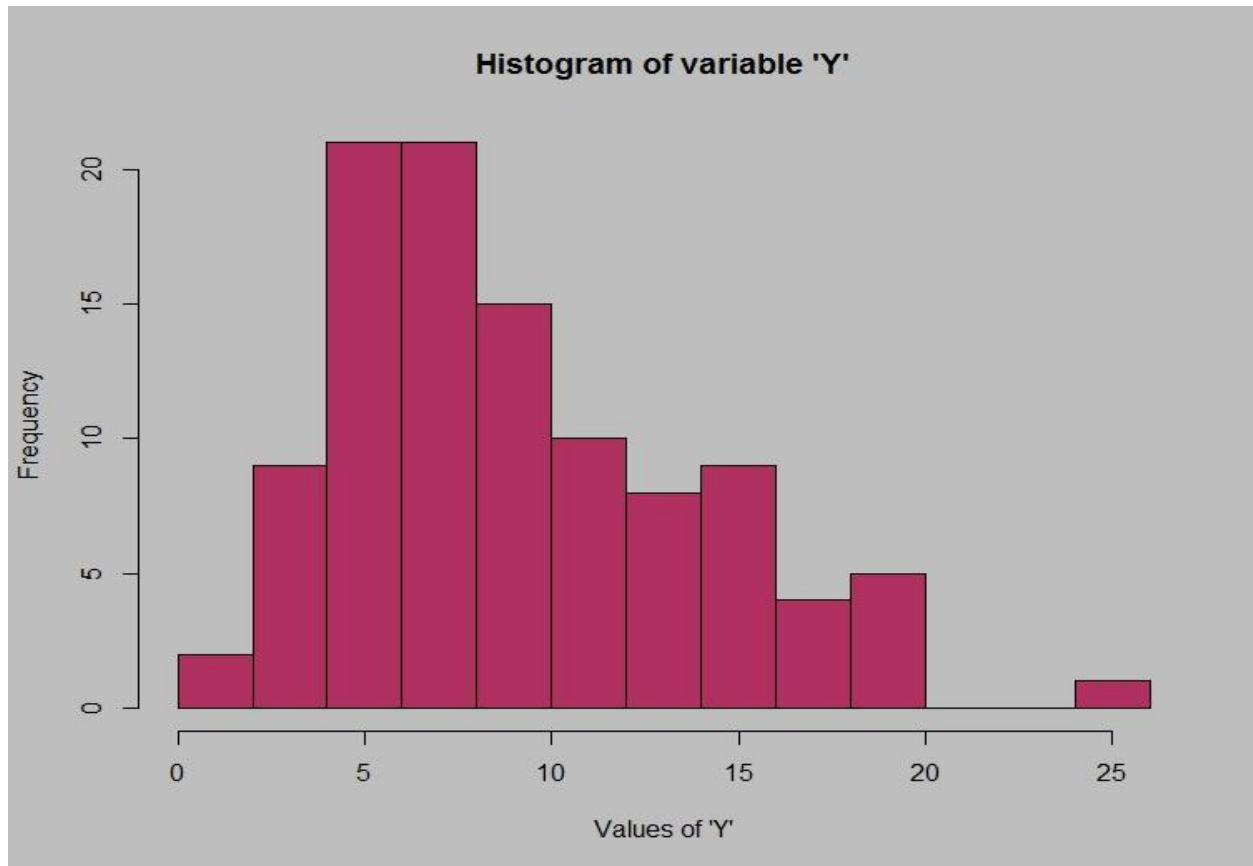
- (ii) What can we say about the skewness of this dataset?
- (iii) If it was found that the data point with the value 25 is actually 2.5, how would the new box-plot be affected?

Ans : (1)  $IQR = Q3 - Q1 = 12 - 5 = 7$  , From IQR we can infer that 50% lies in b/n 5 to 12

(2) Right skewed

(3) 2.5 will not be considered as outlier and mean will change

3.



Answer the following three questions based on the histogram above.

- (i) Where would the mode of this dataset lie?
- (ii) Comment on the skewness of the dataset.
- (iii) Suppose that the above histogram and the box-plot in question 2 are plotted for the same dataset. Explain how these graphs complement each other in providing information about any dataset.

Ans: (1) It would range from 4-8

(2) Right skewed

(3) Boxplot : will identify the outliers in the data which effect the accuracy

Histogram : will identify how data is spread

## Descriptive Statistics and Probability

4. AT&T was running commercials in 1990 aimed at luring back customers who had switched to one of the other long-distance phone service providers. One such commercial shows a businessman trying to reach Phoenix and mistakenly getting Fiji, where a half-naked native on a beach responds incomprehensibly in Polynesian. When asked about this advertisement, AT&T admitted that the portrayed incident did not actually take place but added that this was an enactment of something that “could happen.” Suppose that one in 200 long-distance telephone calls is misdirected. What is the probability that at least one in five attempted telephone calls reaches the wrong number? (Assume independence of attempts.)

Soln: Probability of misdirected =  $1/200=0.005$

Probability of not misdirected =  $1-1/200=0.995$

Probability of atleast one out of 5 number

=  $1 - \text{Probability of all 5 numbers are not misdirected}$

=  $1 - [(1-.005)^5]$

=  $1 - [(1-.005) (1-.005) (1-.005) (1-.005) (1-.005)]$

=  $1-0.9752$

=  $.02475$

=  $2.475=2.5\%$

5. Returns on a certain business venture, to the nearest \$1,000, are known to follow the following probability distribution

x	P(x)
-2,000	0.1
-1,000	0.1
0	0.2
1000	0.2
2000	0.3
3000	0.1

- (i) What is the most likely monetary outcome of the business venture?
- (ii) Is the venture likely to be successful? Explain
- (iii) What is the long-term average earning of business ventures of this kind? Explain
- (iv) What is the good measure of the risk involved in a venture of this kind? Compute this measure

Ans: (1)  $x=2000$  with  $P(x)=0.3$  will be monetary outcome

(2) Yes , Because probability of profit is higher than the loss

(3) Long term avg =  $x * P(x)$

$$= (-2000*.1) + (-1000*.1) + (0*.2) + (1000*.2) + (2000*.3) + (3000*.1) \\ = 800$$

(4) Probability of loss is less =  $(-2000*.1) + (-1000*.1) = 0.2 = 20\%$  loss