

assign function:

- This function calculates the number of different assignments of  $n$  different topics to  $n$  students such that each student gets exactly one topic they like.
- It uses dynamic programming to solve the problem.
- The function takes two parameters:  $n$  (the number of students) and preference (a 2D array of size  $n \times n$ , where  $\text{preference}[i][j]$  is 1 if student  $i$  likes topic  $j$ , and 0 otherwise).
- The function initializes a dynamic programming table  $dp$  of size  $2^n$ , where  $dp[i]$  represents the number of ways to assign topics to students  $s$  to  $n$  given the state  $i$ .
- The function fills up the  $dp$  table in a bottom-up manner. For each state  $mask$ , it calculates the number of ways to assign topics to students  $s$  to  $n$  by considering each topic that the current student likes and has not been assigned yet.
- The function returns  $dp[0]$ , which represents the number of ways to assign topics to all students.

main function:

- The program reads the number of students  $n$  from the user.
- It initializes a 2D array preference of size  $n \times n$  to store the preferences of each student.
- The program then reads the preferences of each student from the user and stores them in the preference array.
- The program calls the assign function to calculate the number of different assignments.
- Finally, the program prints the total number of assignments that can be prepared. Dynamic Programming:

- The dynamic programming table  $dp$  is used to store the number of ways to assign topics to students  $s$  to  $n$  given the state  $i$ .
- The state  $i$  is represented as a bitmask, where the  $j$ -th bit of  $i$  is set if topic  $j$  is already assigned to a student.
- The function fills up the  $dp$  table in a bottom-up manner, starting from the state where all topics are assigned (i.e.,  $\text{mask} = 2^n - 1$ ).
- For each state  $mask$ , the function calculates the number of ways to assign topics to students  $s$  to  $n$  by considering each topic that the current student likes and has not been assigned yet.
- The function uses the previously calculated values in the  $dp$  table to calculate the new values. Time and Space Complexity:
- The time complexity of this program is  $O(n \cdot 2^n)$  because it iterates over all possible states of the assignments.
- The space complexity is  $O(2^n)$  because it uses a dynamic programming table of size  $2^n$ .