

(CURRENT) ELECTRICITY

(1)

(CHAPTER-3)

ELECTRIC CURRENT (I)

It is defined as rate of flow of electric charge through any cross section of a conductor.

$$\boxed{I = \frac{\text{total charge}}{\text{time taken}}}$$
$$I = \frac{q}{t} = \frac{ne}{t}$$
$$I = \lim_{\Delta t \rightarrow 0} \frac{\Delta q}{\Delta t} = \frac{dq}{dt}$$

→ Scalar quantity

SI unit → A

CGS unit → st A

CURRENT DENSITY (J):-

It is the ratio of the current at that point in the conductor to the area of the cross section of the conductor at that point.

$$J = \frac{I}{A}$$

$$I = JA$$

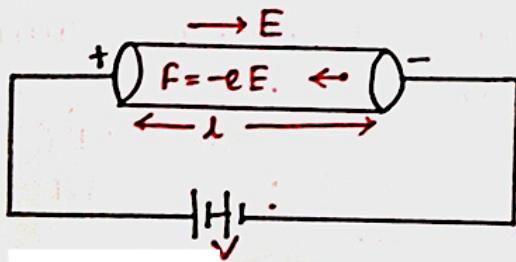
$$\rightarrow \boxed{I = \vec{J} \cdot \vec{A}}$$

→ Vector quantity.

DRIFT VELOCITY (v_d)

It is defined as avg. velocity gained by the free e⁻s of a conductor in the opposite direction of the externally applied electric field.

DRIFT OF ELECTRONS:-



If $\vec{v}_1, \vec{v}_2, \dots, \vec{v}_N$ be the velocities of N no of free electrons,

Then, avg velocities of electrons = $\frac{\vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_N}{N} = 0$

Thus, there is no net flow of charge in any direction. In the presence of electric field, each e^- experiences a force, $\vec{F} = -e\vec{E}$

The negative sign indicate e^- are moving in the opp. direction of \vec{E} .

$$\begin{aligned}\vec{F} &= -e\vec{E} \\ \Rightarrow m\vec{a} &= -e\vec{E} \\ \Rightarrow \vec{a} &= \frac{-e\vec{E}}{m}, \quad m = \text{mass of the electron.}\end{aligned}$$

If n , no. of e^- gain velocity component

$$\vec{v}_1, \vec{v}_2, \dots, \vec{v}_n$$

$$\vec{v}_1 = \vec{v}_1 + \vec{a}t_1$$

$$\vec{v}_2 = \vec{v}_2 + \vec{a}t_2$$

$$\vdots$$

$$\vec{v}_n = \vec{v}_n + \vec{a}t_n$$

$$\vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_n = \vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_n + \vec{a}(t_1 + t_2 + \dots + t_n)$$

$$\Rightarrow \frac{\vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_n}{n} = \cancel{\frac{\vec{v}_1 + \vec{v}_2 + \dots + \vec{v}_n}{n}}^0 + \frac{\vec{a}(t_1 + t_2 + \dots + t_n)}{n}$$

$$\Rightarrow \vec{v}_d = \vec{a}\tau, \quad v_d = \text{drift velocity}$$

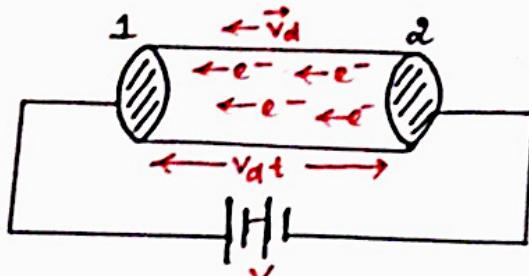
$\tau = \text{relaxation time.}$

τ is the avg. time elapsed between 2 successive collision of the electron.

$$\boxed{\vec{v}_d = \frac{-e\vec{E}\tau}{m}}$$

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RELATION BETWEEN ELECTRIC CURRENT AND DRIFT VELOCITY:-



A = area of the cross-section
 n = free electron density
 t = time taken by electron to move from cross-section 1 to 2.

distance b/w two cross-section = v_{dt}

volume bounded by two cross-section = $A \cdot l = A v_{dt}$

no. of electrons in that volume = $n A v_{dt}$

no. of electron passes through the cross-section 1 in time t = $n A v_{dt} t$

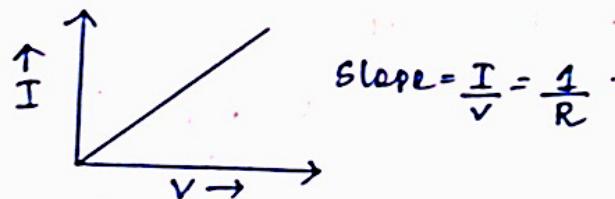
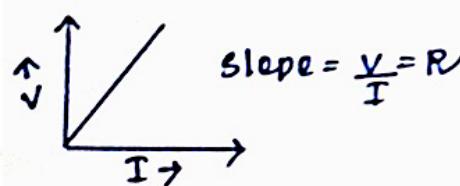
$$I = \frac{dv}{t} = \frac{n A v_{dt} \cdot e}{t} = n e A v_d$$

$$\boxed{I = n e A v_d}$$

OHM'S LAW:- The potential difference between two ends of a conductor is directly proportional to current passing through it at constant temperature.

$$V \propto I$$

$$\Rightarrow V = IR$$



DEDUCTION OF OHM'S LAW:-

$$I = n e A v_d$$

$$= n e A \left(\frac{e V Z}{m_e} \right) = \left(\frac{n e^2 A Z}{m_e} \right) V$$

$$V = \left(\frac{m_e}{n A e^2 Z} \right) I$$

$$\Rightarrow V = RI \quad , \quad R = \frac{m_e}{n A e^2 Z} \text{, constant for a particular conductor at constant temp.}$$

$$\Rightarrow V \propto I$$

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LIMITATIONS OF OHM'S LAW:-

- ① only valid at constant temp.
- ② some substances do not obey ohm's law.

VECTOR FORM OF OHM'S LAW:-

$$\begin{aligned} J &= \frac{I}{A} \\ &= \frac{n e A v d}{A} \\ &= n \cdot \frac{e E Z}{m} \cdot e \\ &= \left(\frac{n e^2 Z}{m} \right) E \end{aligned}$$

$$J = G E$$

In vector form.

$$\vec{J} = G \vec{E}$$

RESISTANCE (R):- It is defined as the opposition offered to the flow of current

SI unit $\rightarrow \Omega$

CGS unit \rightarrow st Ω / ab Ω

$$R = \frac{m l}{n A e^2 Z}$$

Resistance depends on:-

- ① Geometry of conductor
- ② Nature of material
- ③ Temperature.

CONDUCTANCE (G):- It is defined as the reciprocal of resistance.

$$G = \frac{1}{R} = \frac{n A e^2 Z}{m l}$$

SI unit. $\rightarrow \Omega^{-1}$

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RESISTIVITY (ρ):-

$$R = \frac{m l}{n A e^2 \tau}$$

$$= \left(\frac{m}{n e^2 \tau} \right) \frac{l}{A}$$

$$\Rightarrow R = \rho \frac{l}{A} \quad \text{where } \boxed{\rho = \frac{m}{n e^2 \tau}}, \text{ which is constant for a particular material at constant temp.}$$

DEFINITION OF ρ : - $\rho = \frac{RA}{l}$, $A = 1\text{m}^2$, $l = 1\text{m}$, $\rho = R$

It is defined as resistance of a rod of that material of length 1m and area of cross section 1m^2 .

SI unit $\rightarrow \Omega\text{m}$

$$R = \frac{\rho L}{A}, R \propto L \quad (\text{A is constant})$$

$$R \propto \frac{L}{A} \quad (\text{L is constant})$$

SPECIAL CASE:-

CASE-I

When A is not constant

$$R = \rho \frac{L}{A} \times \frac{A}{L}$$

$$= \frac{\rho L^2}{V_{\text{rod}}}$$

$$\Rightarrow \boxed{R \propto L^2}$$

CASE-II

when L is not constant

$$R = \rho \frac{L}{A} \times \frac{A}{A} = \frac{\rho L A}{A^2}$$

$$= \frac{\rho \times V_{\text{rod}}}{A^2}$$

$$\Rightarrow \boxed{R \propto \frac{1}{A^2}}$$

CONDUCTIVITY (σ):-

It is defined as reciprocal of resistivity

$$\boxed{\sigma = \frac{1}{\rho} = \frac{n e^2 \tau}{m}}$$

SI unit :- $\Omega^{-1}\text{m}^{-1}$

MOBILITY (μ)

Mobility of a charge is defined as drift velocity per unit electric field.

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$$\mu = \frac{v_d}{E}$$

$$\mu = \frac{eEZ}{m} \times \frac{1}{E}$$

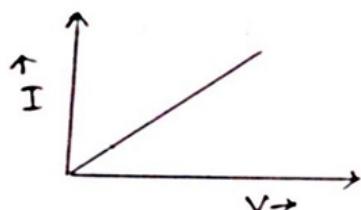
$$\boxed{\mu = \frac{eZ}{m}} \text{ (for electron)}$$

$$\boxed{\mu = \frac{az}{m}} \text{ (general)}$$

* For a particular charge, $\mu \propto Z \propto \frac{1}{\text{temp.}}$

* At constant temperature, $\mu \propto \frac{a}{m}$.

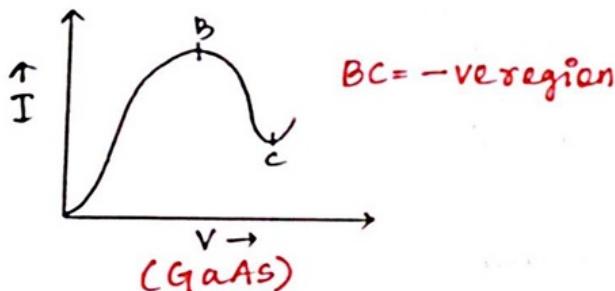
OHMIC SUBSTANCE:- Substance which obeys ohm's law.



e.g.: - all metals carrying low current.

NON-OHMIC SUBSTANCE:- Substance which doesn't obey ohm's law.

e.g.: - dil H_2SO_4 , water voltameter, vacuum diode, GaAs



TEMPERATURE DEPENDANCE OF RESISTIVITY:-

$\beta_0 \rightarrow$ initial velocity at temp T_0

$\beta \rightarrow$ final velocity at temp T

$\beta - \beta_0 \rightarrow$ change in resistivity.

$$\Rightarrow \rho - \rho_0 \propto (T - T_0)$$

$$\Rightarrow \rho - \rho_0 \propto \rho_0$$

$$\Rightarrow \rho - \rho_0 \propto \rho_0 (T - T_0)$$

$$\Rightarrow \rho - \rho_0 = \alpha \rho_0 (T - T_0) , \quad \alpha = \text{temp. coefficient of resistivity.}$$

$$\Rightarrow \boxed{\alpha = \frac{\rho - \rho_0}{\rho_0 (T - T_0)}}$$

It is defined as the ratio between change in resistivity per original resistivity for degree rise of temp.

SI unit $\rightarrow \text{K}^{-1}$

CONDUCTOR:- few conductors, $\alpha = +ve$ i.e. ρ increases with \uparrow in temp.

Cause:- When temp \uparrow , N.E. of free $e^- \uparrow$ so no of collision per sec \uparrow .
Hence, resistivity \uparrow .

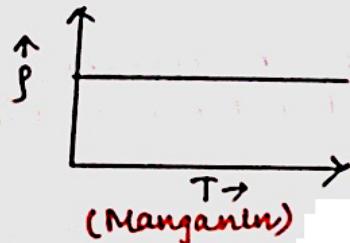
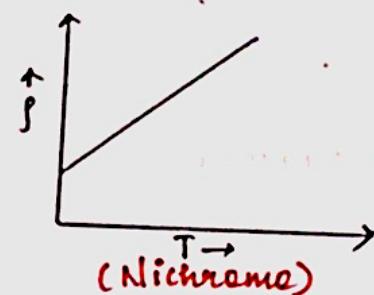
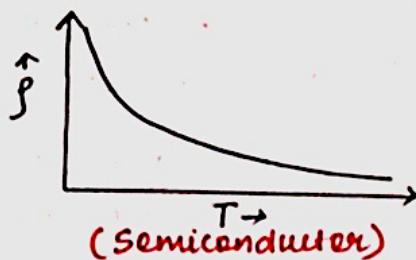
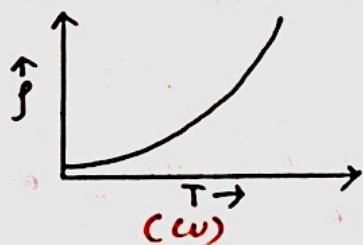
SEMICONDUCTOR:- $\alpha = -ve$, with \uparrow in temp, $\rho \downarrow$

Cause:- When temp \uparrow , charge carrier density \uparrow res which dominate the effect of τ .

$$\text{As } \rho = \frac{m}{ne^2\tau}, \text{ so } \rho \text{ decreases.}$$

INSULATOR:- $\alpha = -ve$, $\rho \downarrow$ res with temperature.

$\rho \sim T$ GRAPHS:-



USE OF ALLOY IN MANUFACTURING RESISTOR:-

- ① ρ of alloy is very high
- ② They have very small temp. of coefficient.
- ③ least affected by atmospheric conditions such as air, moisture, pressure.

COLOUR CODE OF CARBON RESISTOR:-

• B	→ Black	→ 0
• B	→ Brown	→ 1
• R	→ Red	→ 2
• O	→ Orange	→ 3
• Y	→ Yellow	→ 4
• G	→ Green	→ 5
• B	→ Blue	→ 6
• V	→ Violet	→ 7
G	→ Grey	→ 8
W	→ White	→ 9
G	→ Gold	→ 5%
S	→ Silver	→ 10%
N	→ No colour	→ 20%

} Tolerance

TRICK TO REMEMBER:- B.B ROY of Great Britain had a Very Good Wife Wearing Gold & Silver Necklace.

INTERNAL RESISTANCE (δ):- The opposition offered by electrolyte due to flow of electric current is called internal resistance.

CAUSE:- Due to collision of ions.

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- It depends on
- (1) nature of electrolyte and electrode
 - (2) area of electrode dipped in electrolyte
(more is the area, less is the internal resistance)
 - (3) distance between the two electrodes
(more is the separation, more is the internal resistance)
 - (4) temperature
(when temp rises, internal resistance \downarrow because viscosity decreases)

RELATION BETWEEN EMF AND POTENTIAL DIFFERENCE:-

(A) DISCHARGING CONDITION

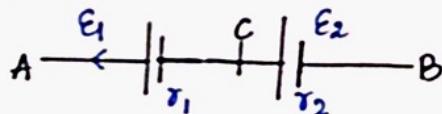
$$E = V + I\gamma$$

(B) CHARGING CONDITION

$$V = E + I\gamma$$

COMBINATION OF CELL:-

(A) SERIES



for cell 1, $V_{AC} = E_1 - I\gamma_1$

$$\Rightarrow V_A - V_C = E_1 - I\gamma_1 \quad \text{--- (1)}$$

for cell 2, $V_{CB} = E_2 - I\gamma_2$

$$\Rightarrow V_C - V_B = E_2 - I\gamma_2 \quad \text{--- (2)}$$

Adding (1) & (2),

$$V_A - V_B = E_1 + E_2 - I(\gamma_1 + \gamma_2) \quad \text{--- (3)}$$

for the combination,

$$V_{AB} = E - I\gamma$$

$$\Rightarrow V_A - V_B = E - I\gamma \quad \text{--- (4)}$$

From eqn (3) & (4),

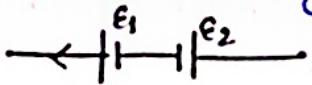
$$E_1 + E_2 - I(\gamma_1 + \gamma_2) = E - I\gamma$$

$$\Rightarrow E = E_1 + E_2$$

$$\gamma = \gamma_1 + \gamma_2$$

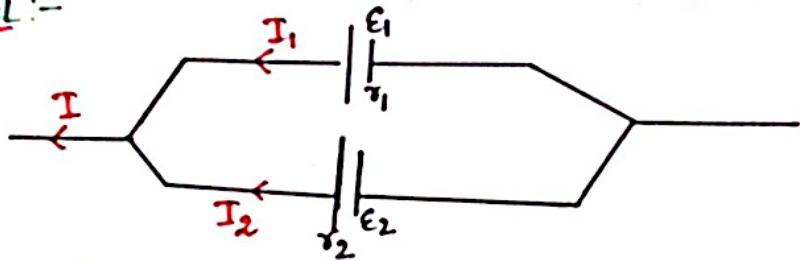
SPECIAL CASE :-

If the connection is wrong



$$E = E_1 - E_2 \quad (\text{If } E_1 > E_2)$$

$$\gamma = \gamma_1 + \gamma_2$$

(B) PARALLEL :-

$$\text{for cell 1, } V = E_1 - I\gamma_1 \Rightarrow I_1 = \frac{E_1 - V}{\gamma_1} \quad \text{--- ①}$$

$$\text{for cell 2, } I_2 = \frac{E_2 - V}{\gamma_2} \quad \text{--- ②}$$

Similarly for the combination,

$$I = \frac{E - V}{\gamma} \quad \text{--- ③}$$

$$I = I_1 + I_2$$

$$\rightarrow \frac{E - V}{\gamma} = \frac{E_1 - V}{\gamma_1} + \frac{E_2 - V}{\gamma_2}$$

$$\rightarrow \frac{E}{\gamma} - \frac{V}{\gamma} = \frac{E_1}{\gamma_1} - \frac{V}{\gamma_1} + \frac{E_2}{\gamma_2} - \frac{V}{\gamma_2} \Rightarrow \frac{E}{\gamma} - \frac{V}{\gamma} = \left(\frac{E_1}{\gamma_1} + \frac{E_2}{\gamma_2} \right) - V \left(\frac{1}{\gamma_1} + \frac{1}{\gamma_2} \right)$$

Comparing both sides,

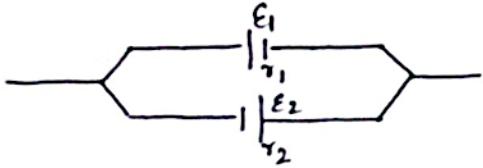
$$\frac{E}{\gamma} = \frac{E_1}{\gamma_1} + \frac{E_2}{\gamma_2} \quad \& \quad \frac{1}{\gamma} = \frac{1}{\gamma_1} + \frac{1}{\gamma_2} = \frac{\gamma_1 + \gamma_2}{\gamma_1 \gamma_2} \Rightarrow \gamma = \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2}$$

$$= \frac{E_1 \gamma_2 + E_2 \gamma_1}{\gamma_1 \gamma_2} \cdot \gamma = \frac{E_1 \gamma_2 + E_2 \gamma_1}{\gamma_1 \gamma_2} \cdot \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2}$$

$$E = \frac{E_1 \gamma_2 + E_2 \gamma_1}{\gamma_1 + \gamma_2}$$

SPECIAL CASE:-CASE-I

If connection is wrong

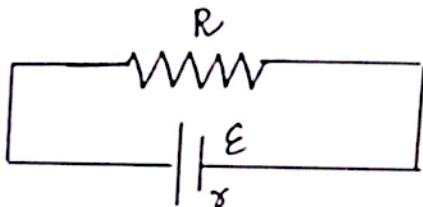


$$E = \frac{E_1 r_2 - E_2 r_1}{r_1 + r_2}$$

CASE-II :-If $E_1 = E_2 = E$

$$r_1 = r_2 = r$$

$$E_{\text{net}} = E$$

EXPRESSION OF CURRENT:-

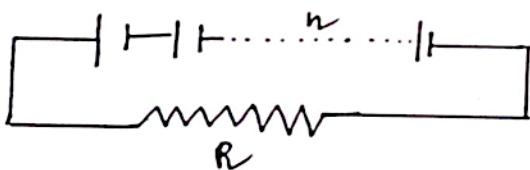
$$E = V + I_r$$

$$\Rightarrow E = IR + I_r$$

$$\Rightarrow E = I(R + r)$$

$$\Rightarrow I = \frac{E}{R+r}$$

$$I = \frac{\text{net emf}}{\text{net resistance}}$$

COMBINATION OF IDENTICAL CELL:-(A) SERIES COMBINATION:- $n = \text{no. of cells connected in series}$

$$\text{net emf} = nE$$

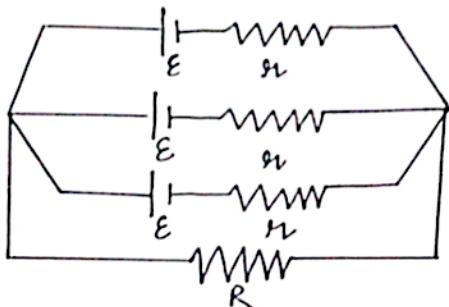
$$I = \frac{nE}{nr+R} = \frac{nE}{nr+r} = \frac{nE}{n(r+\frac{R}{n})}$$

CASE-IIf $R \ggg n\gamma$

$$I = \frac{nE}{R}$$

Current depends on
no. of cells.CASE-IIIf $R \lll n\gamma$

$$I = \frac{E}{\gamma}$$

Series connection is useful when external
resistance is very large.(B) PARALLEL COMBINATION:-

$$\text{Total emf} = E$$

$$\text{Net internal resistance} = \gamma/n$$

$$\text{Net resistance of entire network} = R + \frac{\gamma}{n}$$

$$I = \frac{E}{R + \frac{\gamma}{n}} = \frac{nE}{nR + \gamma}$$

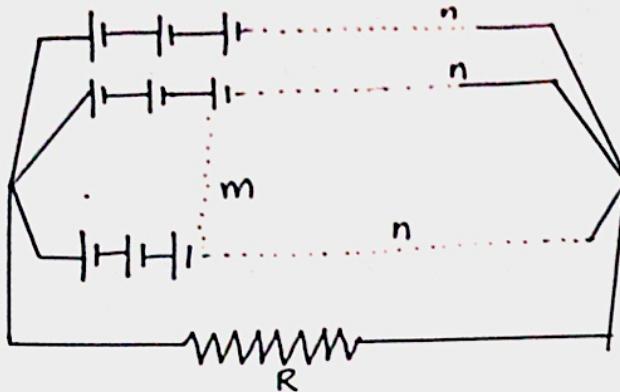
CASE-IIf $R \ggg \gamma$, γ can be
neglected

$$I = \frac{nE}{nR} = \frac{E}{R}$$

CASE-IIIf $R \lll \gamma$, R can be neglected

$$I = \frac{nE}{\gamma} = \frac{n(E)}{R}$$

MIXED CONNECTION :-



n = no. of cells in each row
 m = no. of such rows

$$\text{Net emf} = nE$$

$$\text{Net internal resistance} = \frac{1}{R'} = \frac{1}{nr} + \frac{1}{nr} + \dots + \frac{1}{nr} = \frac{m}{nr}$$

$$R' = \frac{nr}{m}$$

$$I = \frac{nE}{R+nr} = \frac{mnE}{Rm+nr}$$

$$mR + nr = (\sqrt{mR})^2 + (\sqrt{nr})^2 = (\sqrt{mR} - \sqrt{nr})^2 + 2\sqrt{mnRr}$$

Current will be max. when $\sqrt{mR} = \sqrt{nr}$

$$\Rightarrow mR = nr$$

$$\Rightarrow R = \frac{nr}{m}$$

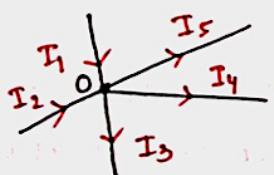
\Rightarrow Total external resistance - Total internal resistance.

KIRCHHOFF'S LAWS:-

(a) KIRCHHOFF CURRENT LAW / JUNCTION LAW:

It states that algebraic sum of currents meeting at a junction is zero.

$$\sum I = 0$$



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The current coming towards the junction is taken as +ve.
 The current going away from the junction is taken as -ve.

$$\rightarrow I_1 + I_2 - I_3 - I_4 - I_5 = 0$$

$$\Rightarrow \boxed{I_1 + I_2 = I_3 + I_4 + I_5}$$

So, net current coming towards the junction = net current going out of the junction.

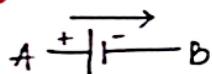
(b) KVL / loop law :-

It states that the algebraic sum of potential differences across cells and resistors in a close loop is 0.

$$\boxed{\sum \Delta V = 0}$$

SIGN CONVENTION:-

① If one moves from +ve to -ve of a cell, then emf is -ve



$$\Delta V = V_B - V_A$$

$$\boxed{E = -ve}$$

② If one moves opposite to direction of current then the product of current and resistance (IR) is taken as +ve.

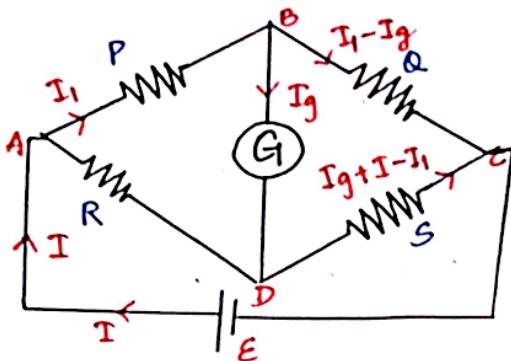


$$\Delta V = V_B - V_A$$

$$\Rightarrow \boxed{IR = +ve}$$

WHEATSTONE BRIDGE:-

P, Q, R, S are the 4 resistors connected in wheatstone bridge.
 $G \rightarrow$ resistance of galvanometer.



Using KVL,

ABDA

$$-PI_1 - GIg + R(I - I_1) = 0$$

$$-I_1 P - Ig G + (I - I_1) R = 0 \quad \text{--- (1)}$$

BCDB

$$-Q(I_1 - Ig) + S(I - I_1 + Ig) + GIg = 0 \quad \text{--- (2)}$$

The bridge is said to be balanced when no current passes through galvanometer
i.e. $Ig = 0$

on (1) & (2) becomes,

$$-I_1 P + (I - I_1) R = 0$$

$$(I - I_1) R = I_1 P \quad \text{--- (3)}$$

$$-QI_1 + SI - SI_1 = 0$$

$$I_1 Q = (I - I_1) S \quad \text{--- (4)}$$

Dividing (3) & (4),

$$\frac{P}{Q} = \frac{R}{S}$$

It is the balanced condition of wheatstone bridge.

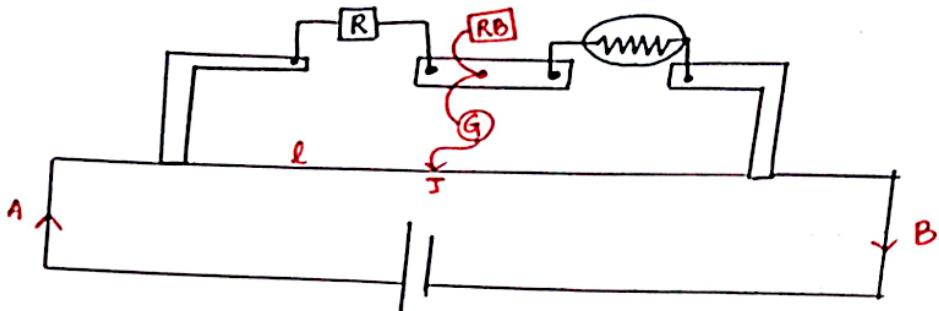
(Q):- What happens to the balanced condition if cell & galvanometer are interchanged?

No change.

METER BRIDGE :-

It is an electrical device used to measure unknown resistance.

PRINCIPLE:- It works on the balanced condition of wheatstone bridge.



R = known resistance from resistance box

S = unknown resistance

J = null point such that AJ = l

According to balanced condition of wheatstone bridge.

$$\frac{R}{S} = \frac{RAJ}{SBJ}$$

$$\Rightarrow \frac{R}{S} = \frac{l}{100-l}$$

$$\Rightarrow S = \frac{R(100-l)}{l}$$

(Q) :- When is metre bridge most sensitive?

If It is obtained at the middle of the wire

(Q) :- Why thick copper strips are used?

Because of negligible resistance

(Q) :- What happens to balancing length if resistance R increases?
Increases.

POTENTIOMETER

It is an electrical device which is used to measure emf of a cell.

PRINCIPLE OF POTENTIOMETER:-

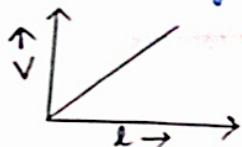
$$V = IR$$

$$\Rightarrow V = I \cdot l / A$$

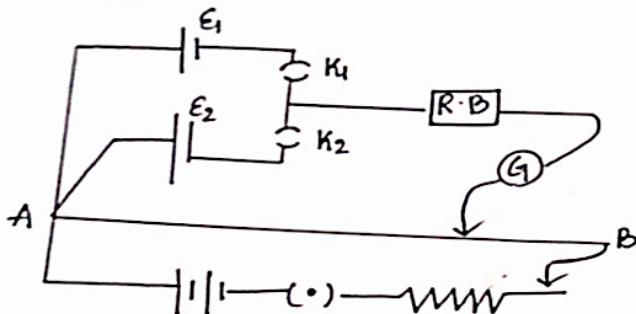
$$\Rightarrow V = \frac{(I l)}{A} l$$

$$\Rightarrow V = k l , \quad k = SI/A$$

The principle is that when a constant current flows through a wire of uniform cross-section and composition, the potential drop across any length of the wire is directly proportional to that length.



① Comparison of emf:-



E_1 & E_2 \rightarrow are two primary cells

K_1 & K_2 \rightarrow Two way key

RB \rightarrow Resistance box

E \rightarrow Driving cell

K \rightarrow Key of Auxillary/primary circuit

R \rightarrow Rheostat

AB \rightarrow Potentiometer wire

Close K_1 , K_2 is open

$$E_1 \propto l_1$$

$$\Rightarrow E_1 = k l_1 \quad \text{--- (I)}$$

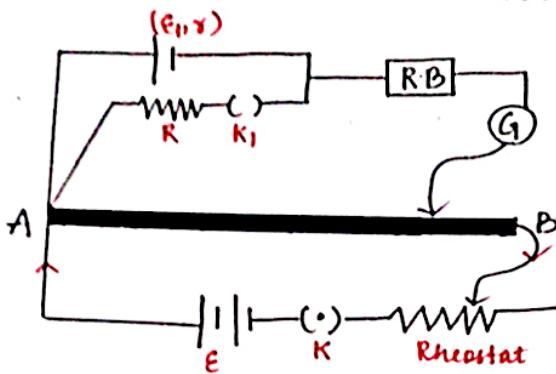
Close K_2 , K_1 is open. $E_2 \propto l_2$

$$\Rightarrow E_2 = k l_2 \quad \text{--- (II)}$$

Eqn (I) by Eqn (II),

$$\frac{E_1}{E_2} = \frac{l_1}{l_2}$$

② DETERMINATION OF INTERNAL RESISTANCE OF GIVEN PRIMARY CELL:



CASE-I

K_1 is open

$$E_1 \propto l_1 \Rightarrow [E_1 = K l_1] \quad \text{--- (I)}$$

CASE-II

V_1 is closed.

$$V \propto l_2 \Rightarrow [V = K l_2] \quad \text{--- (II)}$$

$$\frac{\text{Eqn (I)}}{\text{Eqn (II)}} = \frac{E_1}{V} = \frac{l_1}{l_2}$$

$$\Rightarrow \frac{I(R+r)}{IK} = \frac{l_1}{l_2}$$

$$\Rightarrow 1 + \frac{r}{R} = \frac{l_1}{l_2}$$

$$\Rightarrow \frac{r}{R} = \frac{l_1}{l_2} - 1$$

$$\Rightarrow [r = \left(\frac{l_1 - l_2}{l_2} \right) R]$$

l_1 = balancing length when only E_1 is connected

l_2 = balancing length when R is connected