

Started on	Thursday, 1 July 2021, 7:01 AM
State	Finished
Completed on	Thursday, 1 July 2021, 7:01 AM
Time taken	15 secs
Marks	0.00/50.00
Grade	0.00 out of 10.00 (0%)

Question 1

Not answered

Marked out of 1.00

Evaluate the expression: $(1111 \wedge 1101) \vee 1000$

Select one:

- ☐ a. 0000
- ☐ b. 0100
- ☐ c. 0101
- ☐ d. 1101

Question 2

Not answered

Marked out of 1.00

Suppose G and W_4 are isomorphic. Select correct statement(s).

Select one:

- ☐ a. G has an Euler circuit
- ☐ b. G has a Hamilton circuit
- ☐ c. G has 10 edges
- ☐ d. G has an Euler path

Question **3**

Not answered

Marked out of 1.00

Given the adjacency matrix of an undirected graph with vertices {m, n, p}

	m	n	p
m	2	1	3
n	1	1	1
p	3	1	0

How many **paths of length 3** are there from the vertex n to the vertex m in this graph?

Select one:

- ☐ a. 21
- ☐ b. 6
- ☐ c. 13
- ☐ d. 27

Question **4**

Not answered

Marked out of 1.00

If a complete graph with 45 edges has n vertices, then n is ...

Select one:

- ☐ a. 9
- ☐ b. 11
- ☐ c. 8
- ☐ d. 10

Question **5**

Not answered

Marked out of 1.00

Study a simple graph having the degree sequence $\{6, 5, 4, 4, 3, 3, 2, 2, 2, 2, 1\}$.
If the graph has n edges, then $n = \dots$

Select one:

- ☐ a. 34
- ☐ b. 17
- ☐ c. 38
- ☐ d. 19

Question **6**

Not answered

Marked out of 1.00

Let $U = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$. Given the subsets $A = \{0, 2, 3, 4, 8\}$, $B = \{0, 5, 6, 7, 8\}$.

The bit string representing the subset $A \oplus B$ is ...

Select one:

- ☐ a. 00 1111 1100
- ☐ b. 10 1011 0010
- ☐ c. 00 1111 1110
- ☐ d. 01 1110 0110

Question **7**

Not answered

Marked out of 1.00

Given $A = \{0, \emptyset, 0\}$. Find the cardinality of $P(A)$.

Select one:

- ☐ a. 8
- ☐ b. 2
- ☐ c. 4
- ☐ d. 3

Question **8**

Not answered

Marked out of 1.00

What is the value of the postfix expressions?

5 2 1 - - 3 1 4 ++ *

Select one:

- ☐ a. 32
- ☐ b. None of the others
- ☐ c. 2
- ☐ d. 1/2

Question **9**

Not answered

Marked out of 1.00

Determine whether the following statements are true or false:

- (i) Every graph has only one minimum spanning tree.
- (ii) If all the weights of the graph are positive, then the minimum spanning tree of the graph is a minimum cost subgraph.

Select one:

- ☐ a. true, true
- ☐ b. false, true
- ☐ c. true, false
- ☐ d. false, false

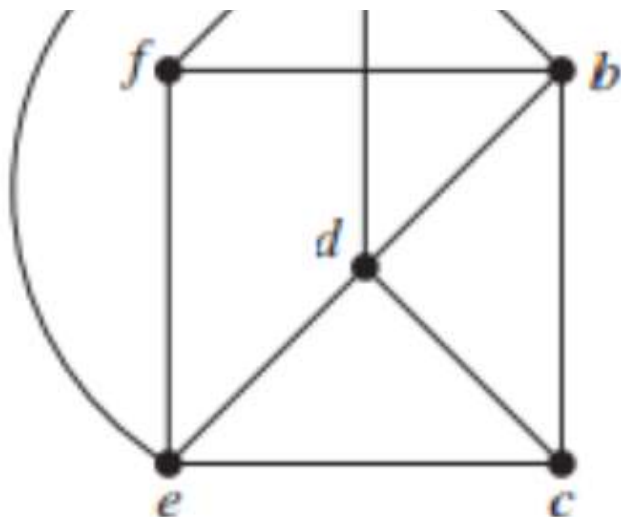
Question **10**

Not answered

Marked out of 1.00

Consider the following graph:





Select one:

- ☐ a. The graph does not have an Euler circuit, and does not have an Euler path.
- ☐ b. None of the others
- ☐ c. The graph does not have an Euler circuit, but has an Euler path.
- ☐ d. The graph has an Euler circuit, but does not have an Euler path.
- ☐ e.

Question **11**

Not answered

Marked out of 1.00

Which the following propositions is FALSE:

Select one:

- ☐ a. $1+1 = 2$ if and only if $2 + 2 = 2$
- ☐ b. If $1 < 0$, then $1 = 0$
- ☐ c. If $2 + 1 = 3$ or $3 - 2 = 2$, then $2 = 3 - 1$
- ☐ d. If $1 + 1 = 3$ and $1 + 1 = 2$, then $2 + 2 = 4$ and $2 + 2 = 1$

Question **12**

Not answered

Marked out of 1.00

Let $A = \{a,b,c,d\}$ and $B = \{1,2,3,4,5\}$

If $f: A \rightarrow B$ is a function such that $f(a) = 1$, $f(b) = 3$, $f(c) = 4$, $f(d) = 2$.
Which of the following statements is true?

- (i) f is one-to-one
- (ii) f is onto

Select one:

- ☐ a. (i)
- ☐ b. Both

☐ c. None of the others

☐ d. (ii)

Question 13

Not answered

Marked out of 1.00

Consider the algorithm:

Procedure T(m: integer, n: positive integer)

 If $n=1$ then $T(m, n) := m$

 else $T(m, n) := m + T(m, n-1)$

Find $T(2,3)$

Select one:

☐ a. 6

☐ b. 8

- ☐ c. 9
- ☐ d. 5

Question 14

Not answered

Marked out of 1.00

Let P is the statement "Mr. Bean has an invention"

Let Q is the statement "Mr. Bean gets a prize"

Which of the following English statements can be used for " $Q \rightarrow P$ "?

- (i) He will get a prize whenever he has an invention
- (ii) A prize is necessary for having an invention

Select one:

- ☐ a. Both
- ☐ b. None of the others
- ☐ c. (ii)

☐ d. (I)

Question 15

Not answered

Marked out of 1.00

Let B be the set $\{a, \{b\}\}$. How many functions are there from B to B^3 ?

Select one:

- ☐ a. 16
- ☐ b. 256
- ☐ c. 64
- ☐ d. 56

Question 16

Not answered

Marked out of 1.00

How many edges do the graph Q_5 have?

Select one:

- ☐ a. 32
- ☐ b. 80
- ☐ c. 160
- ☐ d. 10

Question **17**

Not answered

Marked out of 1.00

Use **Huffman coding algorithm** to encode the word "corona".

What is the **average number** of bits required to encode a character?

Select one:

- ☐ a. $13/6$
- ☐ b. $8/3$
- ☐ c. $14/6$
- ☐ d. $15/6$

Question **18**

Not answered

Marked out of 1.00

Consider the algorithm:
procedure fun($a_1, a_2, a_3, \dots, a_n$: integer)

k:=0

for i=1 to n:

 if ($a_i = 0$) then k:=k+1

return n - k

Find fun(-1,0,1,2)

Select one:

- ☐ a. 2
- ☐ b. 1
- ☐ c. None of the others
- ☐ d. 3

Question **19**

Not answered

Marked out of 1.00

Study the statements:

(i) $K_{2,3}$ does not have no a Hamilton circuit, but has a Hamilton path.

(ii) $K_{2,3}$ has a Hamilton circuit.

Which statement is true?

Select one:

- ☐ a. None of the others
- ☐ b. (i) only
- ☐ c. Both (i) and (ii)
- ☐ d. (ii) only

Question **20**

Not answered

Marked out of 1.00

How many vertices does a full 5-ary with 45 leaves have?

Select one:

- ☐ a. 50
- ☐ b. 61
- ☐ c. 65
- ☐ d. 56

Question **21**

Not answered

Marked out of 1.00

How many comparisons are required to locate number 2 in the binary search tree for the sequence 5, 1, 9, 0, 4, 6, 8, 2 ?

Select one:

- ☐ a. 2

- ☐ b. 5
- ☐ c. 3
- ☐ d. 4

Question **22**

Not answered

Marked out of 1.00

How many integers in $\{1, 2, 3, \dots, 100\}$ are divisible by 3 but not by 5 ?

Select one:

- ☐ a. 27
- ☐ b. 40
- ☐ c. 13
- ☐ d. 30

Question **23**

Not answered

Marked out of 1.00

The function $f(x) = 10x + x^2 \log x + 2 \log x$ is ...

Select one:

- ☐ a. $O(x)$
- ☐ b. $\Theta(2^x)$
- ☐ c. $\Theta(x^3)$
- ☐ d. $\Theta(x^3)$

☐ d. $O(x)$

Question 24

Not answered

Marked out of 1.00

Determine whether each of the following arguments is valid or not valid

(1) All parrots like fruit. My pet bird is not a parrot. Therefore, my pet bird does not like fruit.

(2) Everyone who eats granola every day is healthy. Linda is not healthy. Therefore, Linda does not eat granola every day.

Select one:

- ☐ a. Both the arguments are not valid.
- ☐ b. (1) is not valid and (2) is valid.
- ☐ c. (1) is valid and (2) is not valid.
- ☐ d. Both the arguments are valid.

Question 25

Not answered

Marked out of 1.00

If the adjacency matrix of the graph $K_{2,3}$ has n 0s, then $n = \dots$

Select one:

- ☐ a. 12
- ☐ b. 24
- ☐ c. 13

☐ d. 5×6

Question 26

Not answered

Marked out of 1.00

Suppose that $f\left(\frac{n}{3}\right) = f(n/3) + 1$ when n is a positive integer divisible by 3, and $f(1) = 1$.

Find $f(81)$

Select one:

- ☐ a. 5
- ☐ b. 8
- ☐ c. 4
- ☐ d. None of the others

Question **27**

Not answered

Marked out of 1.00

Give a recursive definition of the set $A = \{2, 4, 6, 8, \dots\}$

Select one:

- ☐ a. $0 \in A$, and if $x \in A$ then $x+2 \in A$
- ☐ b. $0 \in A$, and if $x \in A$ then $x-2 \in A$
- ☐ c. if $x \in A$ then $x+2 \in A$
- ☐ d. $2 \in A$, and if $x \in A$ then $x+2 \in A$

Question **28**

Not answered

Marked out of 1.00

How many bit strings of length 8 begin with 11 and end with 00?

Select one:

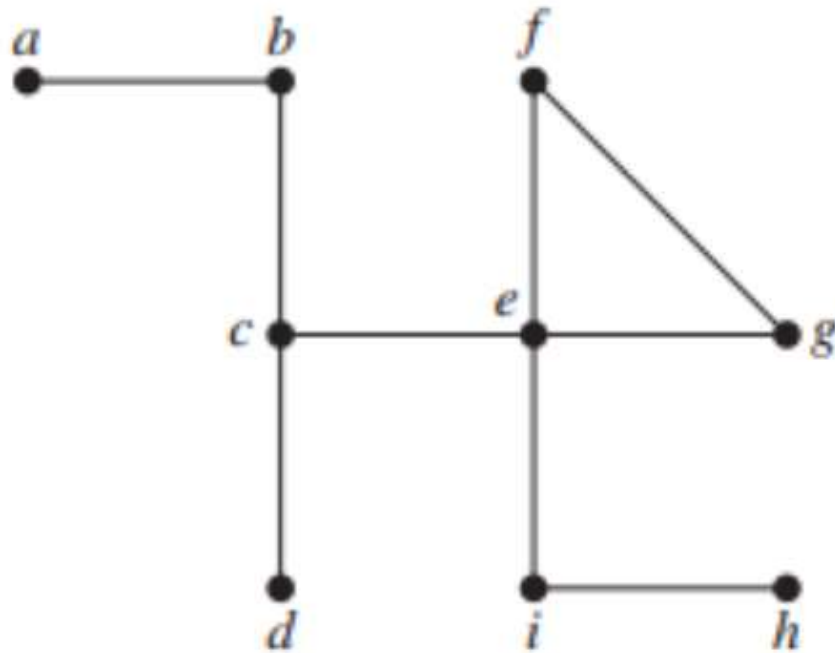
- ☐ a. $2^6 - 2^4$
- ☐ b. 2^4
- ☐ c. $2 \cdot 2^4$
- ☐ d. $2 \cdot 2^6 - 2^4$

Question 29

Not answered

Marked out of 1.00

Find all the cut vertices of the given graph



Select one:

- ☐ a. *b,c,e,i*
- ☐ b. *a,d,h*
- ☐ c. *a,b,c,i,h*
- ☐ d. *b,c,i*

Question 30

Not answered

Marked out of 1.00

Suppose a_n is defined recursively by: $a_0=1$, $a_{n+1}=3.a_n$, $n>0$.
What is a_n ?

Select one:

- ☐ a. $a_n=3n+1$
- ☐ b. $a_n=3^n$
- ☐ c. $a_n=3n - 2$
- ☐ d. $a_n=3^{n+1}$

Question **31**

Not answered

Marked out of 1.00

Study the following prefix expression:

- * 2 4 / 6 * 2 3

It will be evaluated to

Select one:

- ☐ a. 6
- ☐ b. 5
- ☐ c. -2
- ☐ d. 2

Question **32**

Not answered

Marked out of 1.00

Which codes are prefix codes?

(i) a: 0101, b: 010, c: 1101, d: 100

(ii) a: 10, b: 0101, c: 1110, d: 1001

Select one:

- ☐ a. Both (i) and (ii)
- ☐ b. (i) only
- ☐ c. None of the others
- ☐ d. (ii) only

Question **33**

Not answered

Marked out of 1.00

What are $-124 \div 15$ and $-107 \bmod 15$?

Select one:

- ☐ a. -4 and 7
- ☐ b. -9 and 13
- ☐ c. -8 and -2
- ☐ d. 11 and -8

Question **34**

Not answered

Marked out of 1.00

How many rows appear in a truth table for the following proposition?

$(p \vee \neg t) \wedge (p \vee \neg c) \wedge \dots$

א (כִּי־וְאֵלֶּה הַמִּשְׁפָּטִים)

Select one:

- ☐ a. 8
- ☐ b. 5
- ☐ c. 32
- ☐ d. 16

Question **35**

Not answered

Marked out of 1.00

How many edges must be removed from a connected graph with 8 vertices and 10 edges to produce a spanning tree?

Select one:

- ☐ a. 0
- ☐ b. 2
- ☐ c. 1
- ☐ d. 3

Question **36**

Not answered

Marked out of 1.00

Find $f(0)$ if $f(2) = 5$, $f(3) = 21$ and $f(n) = f(n-1) \times f(n-2) + 1$ for $n > 1$

Select one:

- ☐ a. 2
- ☐ b. 1
- ☐ c. 0
- ☐ d. -1

Question **37**

Not answered

Marked out of 1.00

How many leaves does a full 3-ary tree with 100 vertices have?

Select one:

- ☐ a. 51

- ☐ b. 67
- ☐ c. 52
- ☐ d. 33

Question **38**

Not answered

Marked out of 1.00

Given the coding scheme: a: 00, b: 01, c: 10, d: 110, e: 111.
Find the word represented by: 1100001

Select one:

- ☐ a. abc
- ☐ b. daa
- ☐ c. dab
- ☐ d. acb

Question **39**

Not answered

Marked out of 1.00

Let $a_n = -a_{n-2}$ for all $n > 1$. If $a_0 = 3$ and $a_1 = 5$, find a_{2021}

Select one:

- ☐ a. 3
- ☐ b. -3
- ☐ c. 5

☐ d. -5

Question 40

Not answered

Marked out of 1.00

Encrypt the message "ID" by translating the letters into numbers (the character A is translated to 0), applying the encryption function $f(p) = (p + 3) \bmod 26$, and then translating the numbers back into letters. Encrypted form:

Select one:

- ☐ a. HZ
- ☐ b. LG
- ☐ c. HA
- ☐ d. AH

Question 41

Not answered

Marked out of 1.00

Study the following computer code segment:

x:= 5

y:= 6

If (1+1=0) AND (2+2=1) then x:=x+1

If (1+1=2) OR (1+1=0) then y:=y+1

What are values of x and y after the codes execute?

Select one:

Select one.

- ☐ a. 5; 6
- ☐ b. 6; 6
- ☐ c. 6; 8
- ☐ d. 5; 7

Question **42**

Not answered

Marked out of 1.00

How many one-to-one functions are there from the set $\{00, 01, 11\}$ to the set $\{a, b, c, d, e, f\}$?

Select one:

- ☐ a. 120
- ☐ b. 729
- ☐ c. 0
- ☐ d. 216

Question **43**

Not answered

Marked out of 1.00

Which memory locations are assigned by the hashing function $h(k) = k \bmod 101$ to the records of insurance company customers with the Social Security Number 104578690?

Select one:

- ☐ a. 18
- ☐ b. 58
- ☐ c. 62
- ☐ d. 100

Question **44**

Not answered

Marked out of 1.00

How many **edges** does a full binary tree with 20 internal vertices have?

Select one:

- ☐ a. 40
- ☐ b. 41
- ☐ c. 39
- ☐ d. 42

Question **45**

Not answered

Marked out of 1.00

Consider the following algorithm:

```
procedure FUN(a: real number; n: positive integer)
if n = 1 return a
else return a*FUN(a, n-1).
```

What is the output if inputs are: $n = 3$, $a = 5$

Select one:

- ☐ a. 8
- ☐ b. 125
- ☐ c. 243
- ☐ d. 15

Question **46**

Not answered

Marked out of 1.00

Suppose $a \bmod 3 = 2$ and $b \bmod 6 = 4$, find $ab \bmod 3$

Select one:

- ☐ a. 0
- ☐ b. 2
- ☐ c. 1
- ☐ d. 8

Question **47**

Not answered

Marked out of 1.00

How many vertices and how many edges do the graph K_7 have?

Select one:

- ☐ a. 7 and 21
- ☐ b. 7 and 42
- ☐ c. 8 and 14
- ☐ d. 8 and 14

Question **48**

Not answered

Marked out of 1.00

Which of the following functions is big-oh of n ?

Select one:

- ☐ a. $g(n) = 2021n + 1$
- ☐ b. $g(n) = n^2 - 2n$
- ☐ c. $g(n) = 2^n - 5n^3$
- ☐ d. $g(n) = n \log n + 2021$

Question **49**

Not answered

Marked out of 1.00

Let f be floor function and g be ceiling function.

Which of the following is true ?

Select one:

- ☐ a. $f(5.001) = 6$
- ☐ b. $g(5.4) = 6$
- ☐ c. $g(5) = 6$
- ☐ d. $f(3.8) = 4$

Question **50**

Not answered

Marked out of 1.00

Let S be the set defined recursively by: 10 is in S , and if x is an element of S then $x+10$ is an element of S . What is S ?

Select one:

- ☐ a. S is **the set** of all **natural numbers**
- ☐ b. S is the set of all **positive** multiples of 10.
- ☐ c. S is the set of all **positive** multiples of 5.
- ☐ d. S is the set of all **nonnegative** multiples of 10.

