

# EE142 Problem Set 5

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## Problem 1

Find  $y$  for the following normalized impedance on Smith Chart.

The straightforward procedure is to plot  $z_L$  on the impedance Smith Chart, and then look at what constant admittance and constant susceptance curves cross over the point in the admittance smith chart.

But, we can also plot  $z_L$  on the impedance smith chart, then rotate the point by  $\pi$  degrees along the constant SWR circle, and then read off the admittance by looking at the constant resistance and reactance curves.

I'm going to use the second technique; annotated charts aren't included in this document, but I'll compare the chart result I get to the exact calculation.

(a)  $z_L = 1.4 + 2j$

$$y_L = \frac{1}{z_L} = \frac{1}{\alpha + \beta j} = \frac{\alpha - \beta j}{\alpha^2 + \beta^2} = 0.234899 - 0.33557j$$
$$y_{L,chart} = 0.22 - 0.32j$$

(b)  $z_L = 0.5 + 0.9j$

$$y_L = 0.471698 - 0.849j$$
$$y_{L,chart} = 0.45 - 0.85j$$

(c)  $z_L = 1.6 - 0.3j$

$$y_L = 0.60377 + 0.1132j$$
$$y_{L,chart} = 0.6 + 0.12j$$

## Problem 2

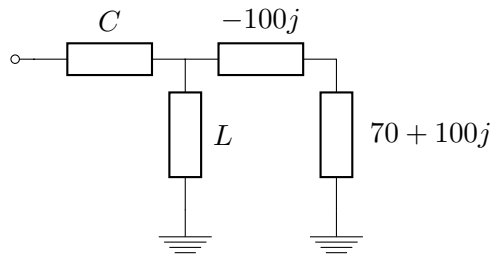
Use the Smith Chart. Also use equations for lumped component matching to check.

(a) Match  $Z_L = 70 + 100j\Omega$  to 50 Ohm with lumped components.

Let's clear up some things:

$$\begin{aligned} Z_C &= \frac{1}{j\omega C} & X_C &= \Im Z_C = -\frac{1}{\omega C} \\ Z_L &= j\omega L & X_L &= \Im Z_L = \omega L \end{aligned}$$

The load is complex, so we have to resonant out the load's complex impedance so only a real part is seen before solving using the L network method.



Now, the L-network will see a purely real  $70\Omega$  impedance with which we can use the regular matching equations.

$$\begin{aligned} R_S &= 50 \\ R_L &= 70 \\ R_{hi} &= \max(R_S, R_L) = 70 \\ R_{lo} &= \min(R_S, R_L) = 50 \\ \text{Boosting factor: } m &= \frac{R_{hi}}{R_{lo}} = 1.4 \\ Q &= \sqrt{m^2 - 1} = 0.632 \\ \text{Dropping resistance so, } X_p &= \frac{R_L}{Q} = 110.76 \\ X'_p &= \frac{X_p}{1 + Q^2} = 31.613 \\ X_s &= -X'_p = -31.613 \end{aligned}$$

We arrive at the capacitor reactance of  $-79.15j$  and the inductor reactance of  $110.76j$ . The circuit is simulated in ADS to match at 1 GHz with component values  $C = 5.0344$  pF,  $L = 17.6$  nH, and  $C_{res} = 1.59$  pF. S-parameter simulation verifies that the source and load are perfectly matched at 1 GHz with  $S_{21} = 0dB$ .

The same calculation can be performed using the smith chart.

$$\begin{aligned} Z_{L,norm} &= 1.4 + 2j \\ Z_{L,real} &= 1.4 \\ X_p &= (1/0.45)j \cdot 50 = 111.1j \\ X_s &= -0.62 \cdot 50 = -31j \end{aligned}$$

The values calculated using the Smith Chart are very close to the values from the equations.

(b) Match  $Z_L = 70 + 100j\Omega$  to 50 Ohm using transmission lines.

(c) Match  $Z_L = 160 - 30j\Omega$  to 100 Ohm using lumped circuits.

Assume a resonating inductor with reactance  $30j$  to make the load purely real.

$$R_S = 100$$

$$R_L = 160$$

$$R_{hi} = \max(R_S, R_L) = 160$$

$$R_{lo} = \min(R_S, R_L) = 100$$

$$\text{Boosting factor: } m = \frac{R_{hi}}{R_{lo}} = 1.6$$

$$Q = \sqrt{m - 1} = 0.775$$

$$\text{Dropping resistance so, } X_p = \frac{R_L}{Q} = 206.452$$

$$X'_p = \frac{X_p}{1 + Q^{-2}} = 77.47$$

$$X_s = -X'_p = -77.47$$

We simulate in ADS with  $L_{res} = 4.77$  nH,  $L = 32.858$  nH,  $C = 2.05$  pF. The simulation shows that these values give a perfect match at 1 Ghz. This match appears more broadband than the one in part a).

(d) Match  $Z_L = 160 - 30j\Omega$  to 100 Ohm using transmission lines.

(e) Match  $Z_L = 25 + 90j\Omega$  to 50 Ohm using lumped circuits.

(f) Match  $Z_L = 25 + 90j\Omega$  to 50 Ohm using transmission lines.