

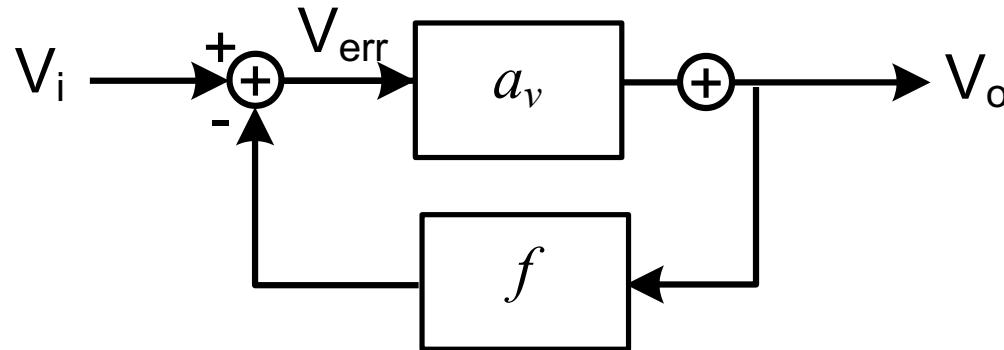
EE 240B – Spring 2019

Advanced Analog Integrated Circuits
Lecture 9: Feedback



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Generic Feedback System



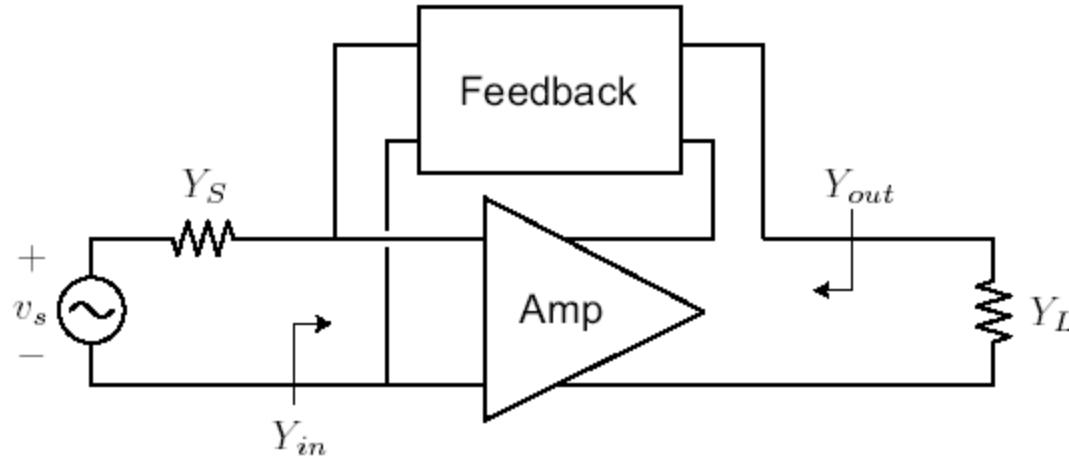
- **Open-loop gain:** a_v
- **Feedback factor:** f
- **Loop gain:** $T = a_v f$
- **Closed-loop gain:**

$$A = \frac{V_o}{V_i} = \frac{a_v}{1+T} = \frac{1}{f} \frac{1}{1+\frac{1}{T}} \approx \frac{1}{f}$$

Feedback

- Benefits
 - Reduced sensitivity to
 - Gain variations
 - Nonlinearity
 - Increased bandwidth
- Caveat: potential instability
- Stability test
 - Bounded input, bounded output: no general test available
 - Linear system:
 - Poles in LHP (“left half-plane”)
 - Bode criterion
 - Nyquist criterion
 - Hand-analysis
 - SPICE

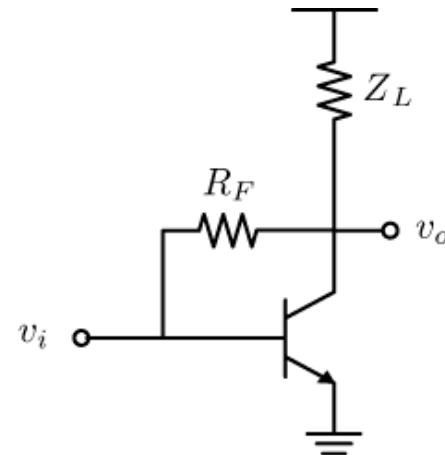
Two-Port Analysis (Review)



- Amplifiers can often be decomposed into a *unilateral* forward gain and a feedback section.
- Based on the type of feedback (series versus shunt at each port), we should use the simplest two-port equations.

Examples: Y-Parameters

- If the feedback is shunt at both ports, then the currents at the input and output are summing so Y parameters are natural.
- Since the output is connected in shunt, we sample the output voltage. Since the input is in shunt too, we add a feedback current into the input.
- Thus shunt feedback is appropriate for a trans-resistance amplifier (current \rightarrow voltage)



$$\begin{pmatrix} i_1 \\ i_2 \end{pmatrix} = \begin{pmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix}$$

Admittance Parameters

- Notice that y_{11} (y_{22}) is the short-circuit input (output) admittance:

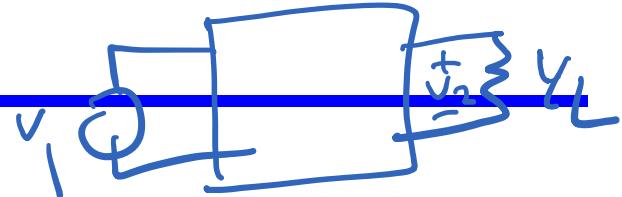
$$y_{11} = \left. \frac{i_1}{v_1} \right|_{v_2=0}$$

- The forward trans-conductance is described by y_{21} :

$$y_{21} = \left. \frac{i_2}{v_1} \right|_{v_2=0}$$

- The reverse trans-conductance is given by y_{12} . For a *unilateral* amplifier $y_{12} = 0$

Voltage Gain



- Since $i_2 = -v_2 Y_L$, we can write

$$(y_{22} + Y_L)v_2 = -y_{21}v_1$$

- The “internal” voltage gain is thus given by

$$A_v = \frac{v_2}{v_1} = \frac{-y_{21}}{y_{22} + Y_L}$$

- The input admittance is now easily given by

$$Y_{in} = \frac{i_1}{v_1} = y_{11} + y_{12} \frac{v_2}{v_1}$$

$$Y_{in} = y_{11} - \frac{y_{12}y_{21}}{y_{22} + Y_L}$$

Output Admittance

- By symmetry we can write down the output admittance by inspection

$$Y_{out} = y_{22} - \frac{y_{12}y_{21}}{y_{11} + Y_S}$$

- Note that for a unilateral amplifier $y_{12} = 0$ implies that

$$Y_{in} = y_{11}$$

$$Y_{out} = y_{22}$$

- The input and output impedance are de-coupled!

External Voltage Gain

- The gain from the voltage source to the output can be derived by a simple voltage divider equation

$$A'_v = \frac{v_2}{v_s} = \frac{v_2}{v_1} \frac{v_1}{v_s} = A_v \frac{Y_S}{Y_{in} + Y_S} = \frac{-Y_S y_{21}}{(y_{22} + Y_L)(Y_S + Y_{in})}$$

- If we substitute and simplify the above equation we have

$$Y_{in} = Y_{11} - \frac{Y_{12} Y_{21}}{(Y_{22} + Y_L)}$$

$$A'_v = \frac{-Y_S y_{21}}{(Y_S + y_{11})(Y_L + y_{22}) - \underline{y_{12} y_{21}}}$$

Feedback Interpretation

- Note that in an ideal feedback system, the amplifier is unilateral and $\frac{y}{x} = \frac{A}{1+Af}$
- We know that the voltage gain of a general two-port driven with source admittance Y_S is given by

$$A'_v = \frac{\left(-Y_S y_{21} \right) \left(Y_S + y_{11} \right) \left(Y_L + y_{22} \right)}{\underbrace{\left(Y_S + y_{11} \right) \left(Y_L + y_{22} \right)}_1 - y_{12} y_{21}} \left(Y_S + y_{11} \right) \left(Y_L + y_{22} \right) = A_{vu}$$

- If we unilateralize the two-port by arbitrarily setting $y_{12} = 0$, we have an “open” loop forward gain of

$$A_{vu} = A'_v \Big|_{y_{12}=0} = \frac{-Y_S y_{21}}{\left(Y_S + y_{11} \right) \left(Y_L + y_{22} \right)}$$

Identification of Loop Gain

- Re-writing the gain A'_v by dividing numerator and denominator by the factor $(Y_S + y_{11})(Y_L + y_{22})$ we have

$$A'_v = \frac{\frac{-Y_S y_{21}}{(Y_S + y_{11})(Y_L + y_{22})}}{1 - \frac{y_{12} y_{21}}{(Y_S + y_{11})(Y_L + y_{22})}}$$

- We can now see that the “closed” loop gain with y_{12} is given by
- where T is identified as the loop gain

$$T = A_{vu}f = \frac{-y_{12} y_{21}}{(Y_S + y_{11})(Y_L + y_{22})}$$

Feedback Factor

- Using the last equation also allows us to identify the feedback factor
- If we include the loading by the source Y_S , the input admittance of the amplifier is given by

$$Y_{in} = Y_S + y_{11} - \frac{y_{12}y_{21}}{Y_L + y_{22}}$$

- Note that this can be re-written as

$$Y_{in} = (Y_S + y_{11}) \left(1 - \frac{y_{12}y_{21}}{(Y_S + y_{11})(Y_L + y_{22})} \right)$$

Feedback and Terminal Impedance

- The last equation can be re-written as

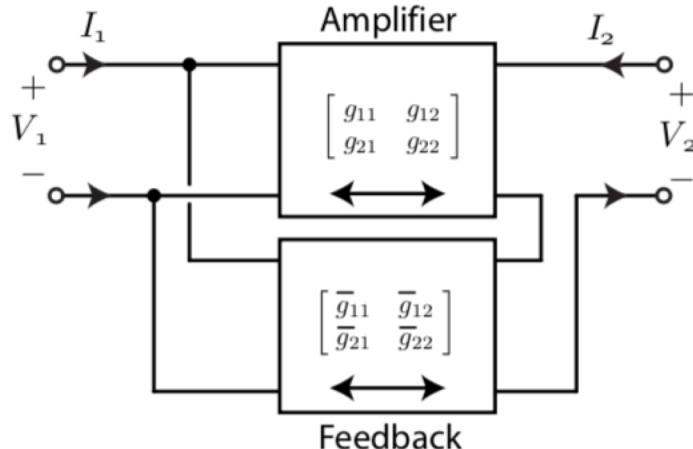
$$Y_{in} = (Y_S + y_{11})(1 + T)$$

- Since $Y_S + y_{11}$ is the input admittance of a unilateral amplifier, we can interpret the action of the feedback as raising the input admittance by a factor of $1 + T$.
- Likewise, the same analysis yields

$$Y_{out} = (Y_L + y_{22})(1 + T)$$

- It's interesting to note that the same equations are valid for series feedback using Z parameters, in which case the action of the feedback is to boost the input and output impedance. This same is true for hybrid feedback.

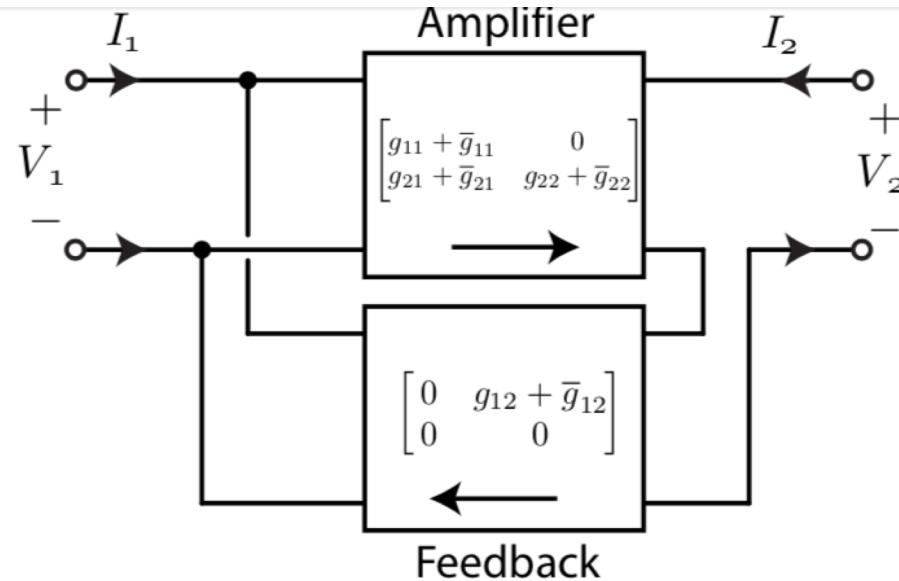
Non-Ideal Feedback



$$\begin{aligned} I_1 &= i_1 + j_1 \\ I_2 &= i_2 = j_2 \\ V_1 &= v_1 = u_1 \\ V_2 &= v_2 + u_2 \end{aligned}$$

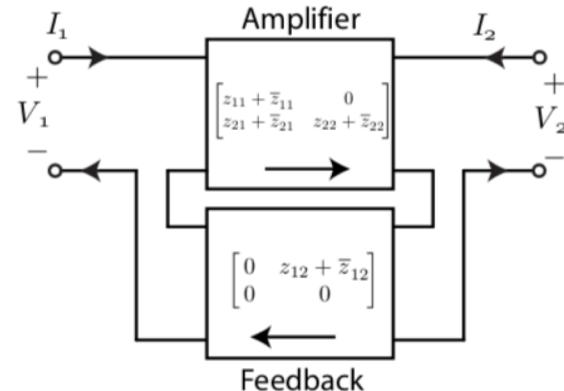
- Any real feedback amplifier is non-ideal due to intrinsic feedback in the amplifier itself (bilateral nature) and the feedforward through the feedback network.
- The feedback network also loads the primary amplifier.
- It's hard to apply ideal signal flow analysis to the real circuit unless...

Non-Ideal FB → Ideal FB

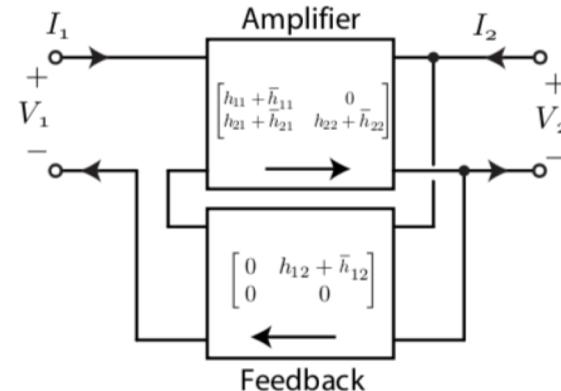


- Since the overall two-port parameters of the amplifier in closed loop is simply the *sum* of the amplifier and feedback network two-port parameters, we can simply move the non-idealities of the feedback network (loading and feedforward) into the main amplifier and likewise move the intrinsic feedback of the amplifier to the feedback network.
- Now we can use ideal feedback analysis.

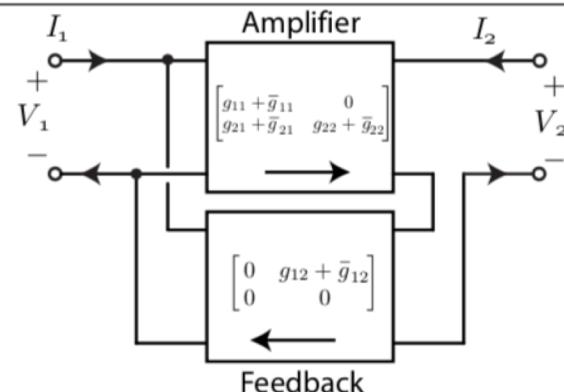
Series or Shunt ?



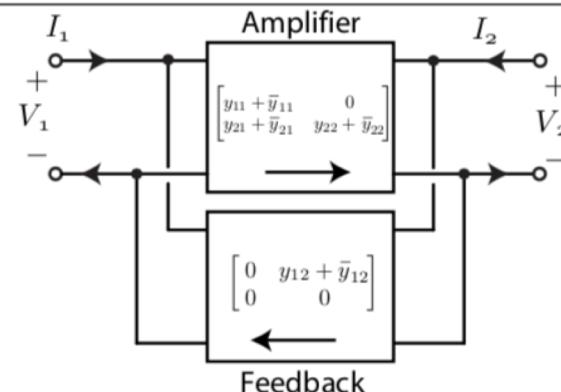
(a) Series-Series



(b) Series-Shunt

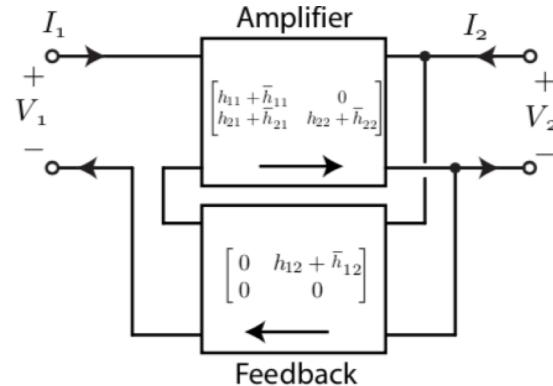


(c) Shunt-Series



(d) Shunt-Shunt

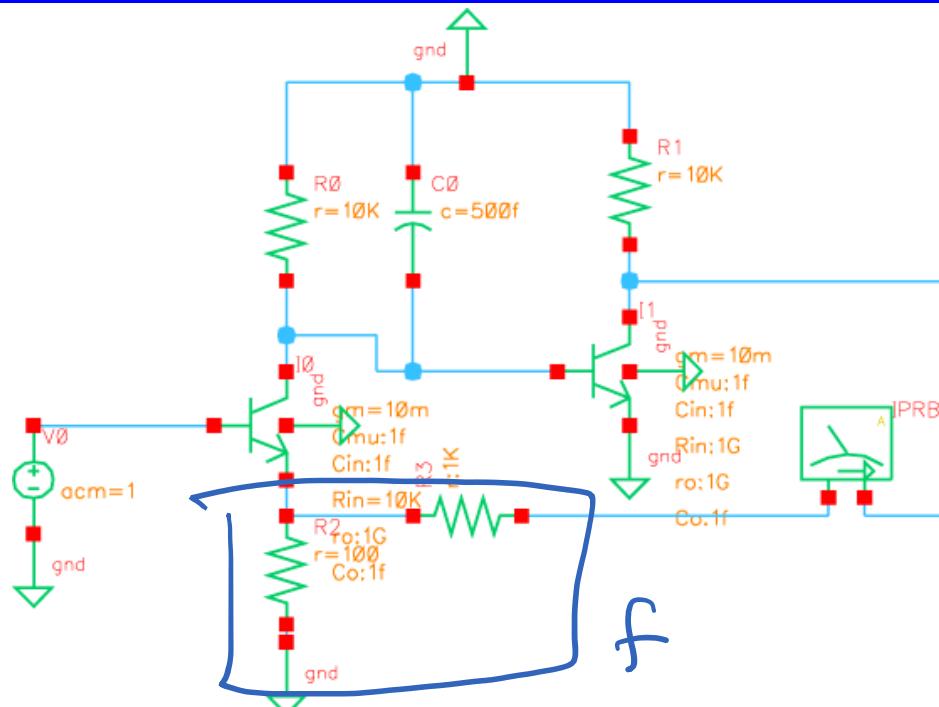
How to Decide



- Which two variables (v or i) are the same for both two-ports: $i_1 = i_1^A = i_1^B$ and $v_2 = v_2^A = V_2^B$ Make these the independent variables.
- Which two variables (v or i) sum to form the two-port variables: $v_1 = v_1^A + v_1^B$ and $i_2 = i_2^A + i_2^B$. Make these the dependent variables.
- Order variables with the first row port 1, and the second row port 2.

$$\begin{pmatrix} v_1 \\ i_2 \end{pmatrix} = \begin{pmatrix} v_1 \\ i_2 \end{pmatrix}^A + \begin{pmatrix} v_1 \\ i_2 \end{pmatrix}^B = (H^A + H^B) \begin{pmatrix} i_1 \\ v_2 \end{pmatrix}$$

Example:



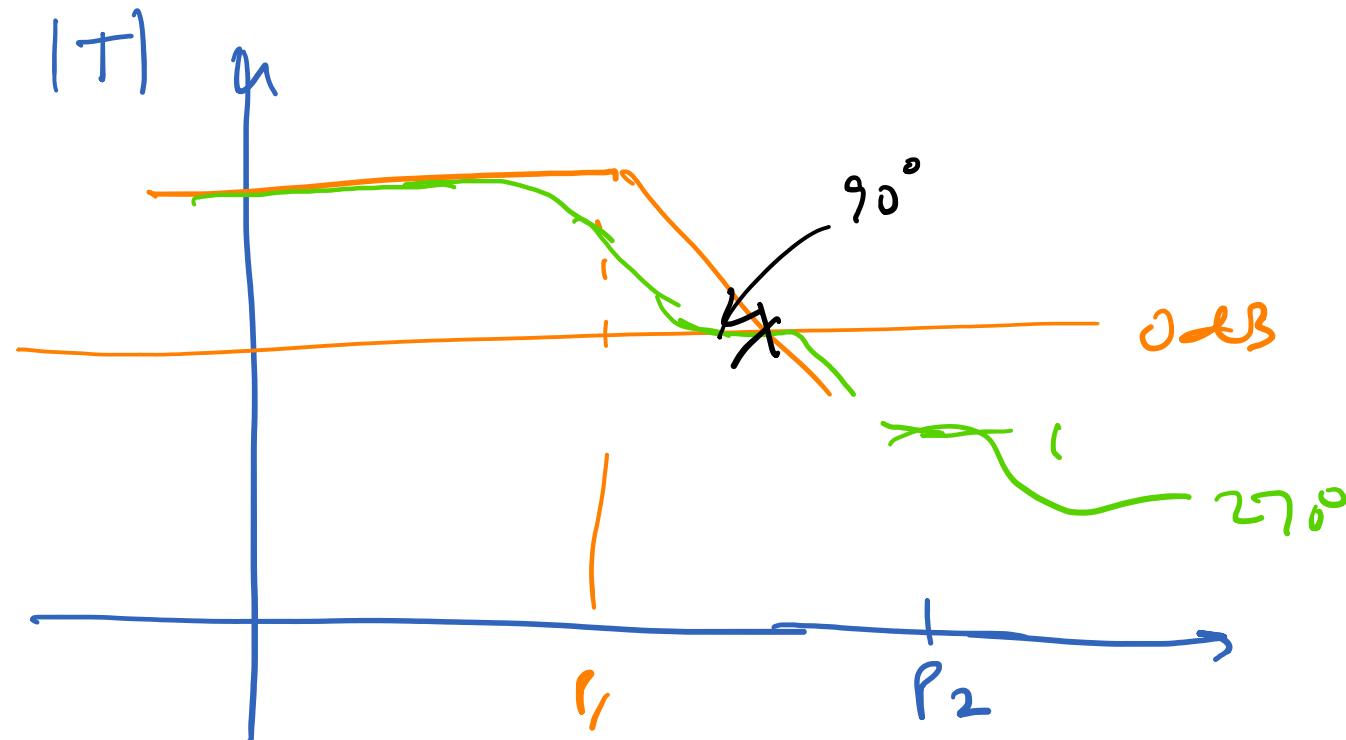
- We'd like to partition our system into an ideal feedback system. Real feedback circuits load the amplifier.
- What parameters should we use for the above amplifier?

Real Feedback Two-Port

- Pick the appropriate two-port representation and include loading in calculations ... review 142/242A notes
- I invite you to analyze the previous circuit ...
- Interesting question: Loop gain should be independent of two-port representation, right?

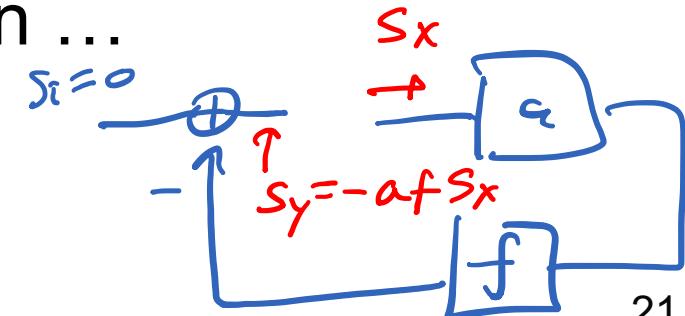
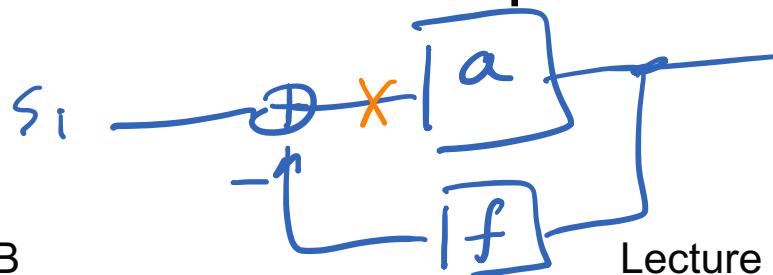
Bode Plot -- Stability

- Plot loop gain and make sure that the phase at unity gain is as far from 180 degrees as possible
- PM is defined as the difference between the phase and 180 degrees ... usually good to have 60 degrees for a robust design



Return Ratio Analysis

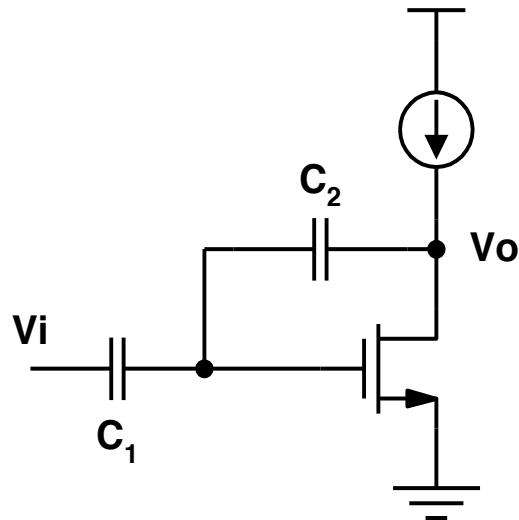
- Two-port analysis is great for understanding feedback and proving some theorems but...
- We really only care about loop gain $T!!!$
- The loop gain can be calculated directly by breaking the feedback loop and injecting a test signal and observing the “return ratio”. The return signal should have negative phase for negative feedback.
- Problem: Loading effects must be taken into account when loop is broken ...



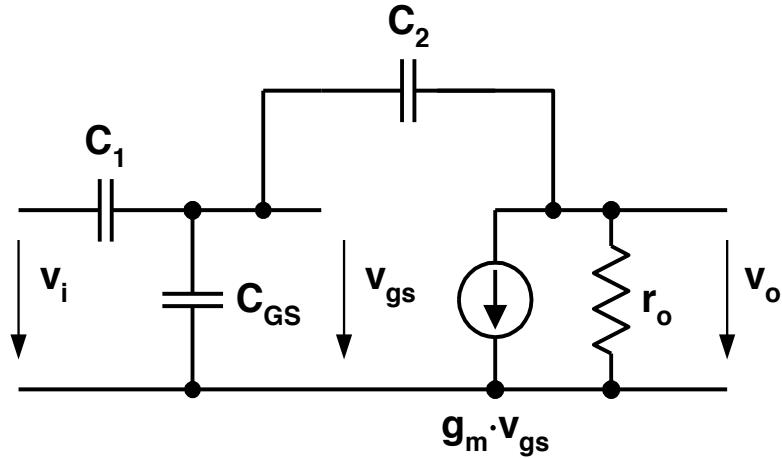
Stability Analysis

- Depends on $T(s)$
 - NOT $a(s)$
- Finding $T(s)$:
 - Hand analysis:
 - Break loop at controlled source (e.g. g_m)
 - $T = -s_r / s_t$
 - SPICE:
 - Controlled sources not accessible
 - a) Break loop, model load (approximation), or
 - b) Determine T from T_v and T_i (exact)

Simple Circuit Example



Feedback Amplifier
(Biasing for V_{gs} not shown)

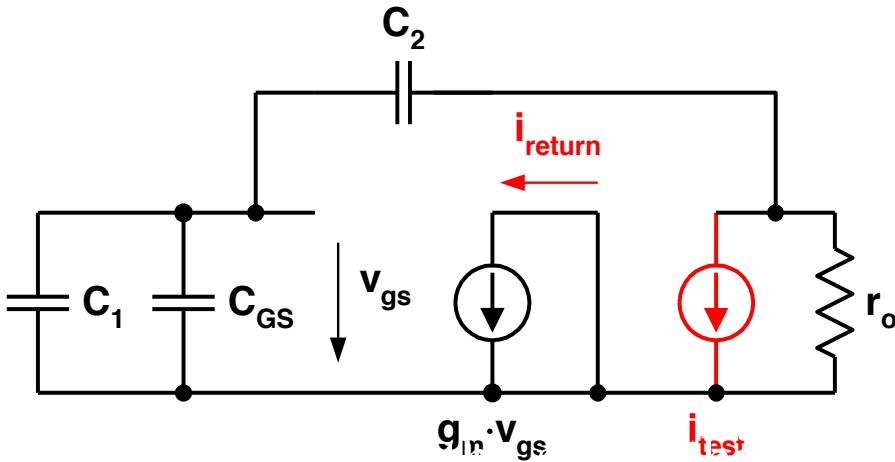


Small Signal Equivalent

Loop Gain = ?

Return Ratio Analysis [HLGM 01]

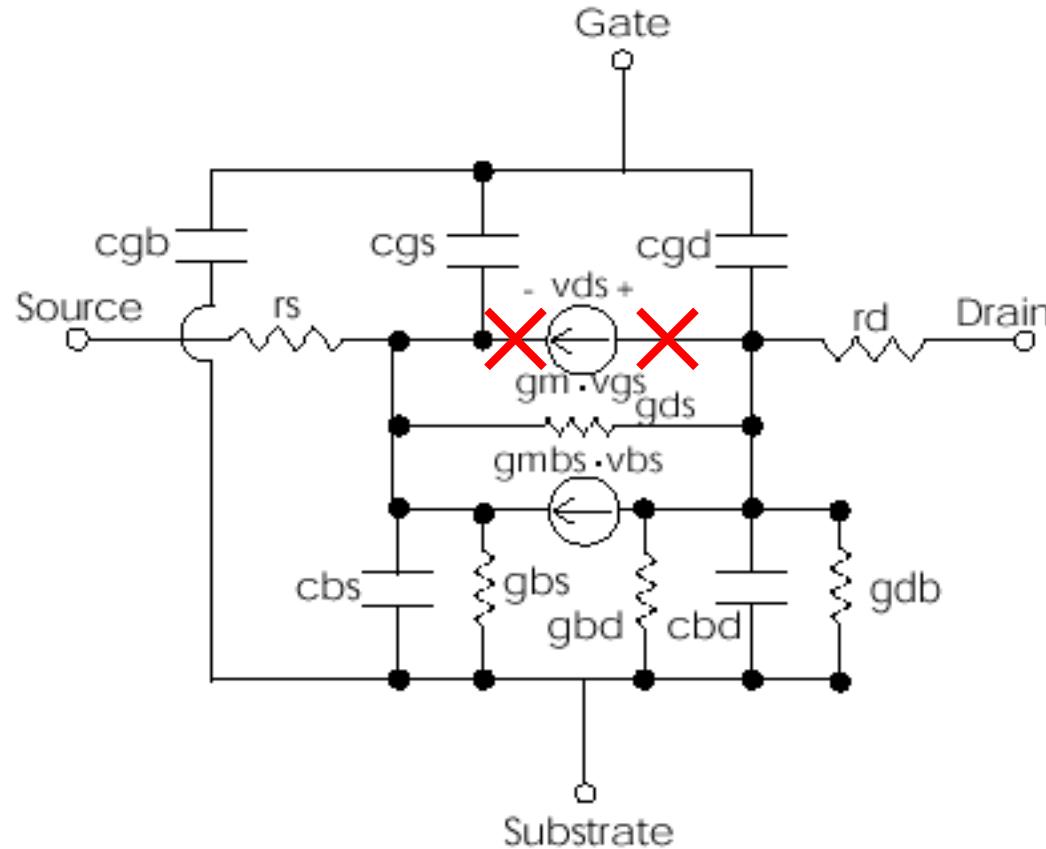
1. Set all independent sources to zero ($v_i=0$)
2. Disconnect (ideal) controlled source from circuit
3. Replace with test source
4. Find ratio return signal/test signal = Return Ratio => Loop Gain



$$T(s) = F \cdot g_m \cdot r_o \cdot \frac{1}{1 + \frac{s}{p_1}}$$

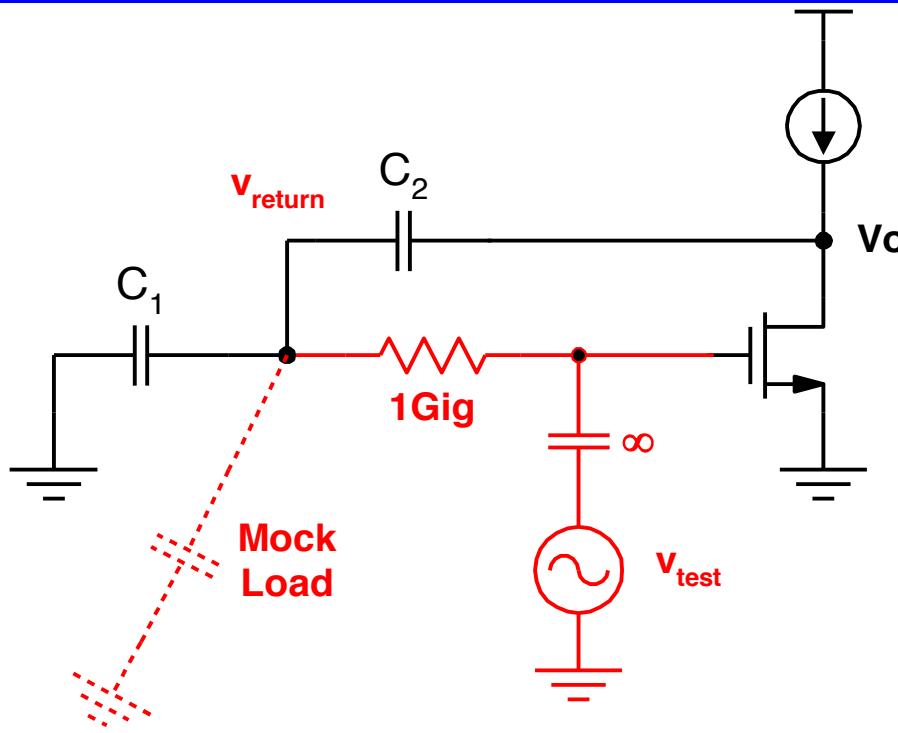
$$F = \frac{C_2}{C_1 + C_2 + C_{GS}}$$
$$p_1 = -\frac{1}{r_o \cdot \frac{C_2(C_1 + C_{GS})}{C_2 + C_1 + C_{GS}}}$$

MOSFET AC Simulation Model



Small-signal model not accessible in SPICE!

Popular Simulation Approach



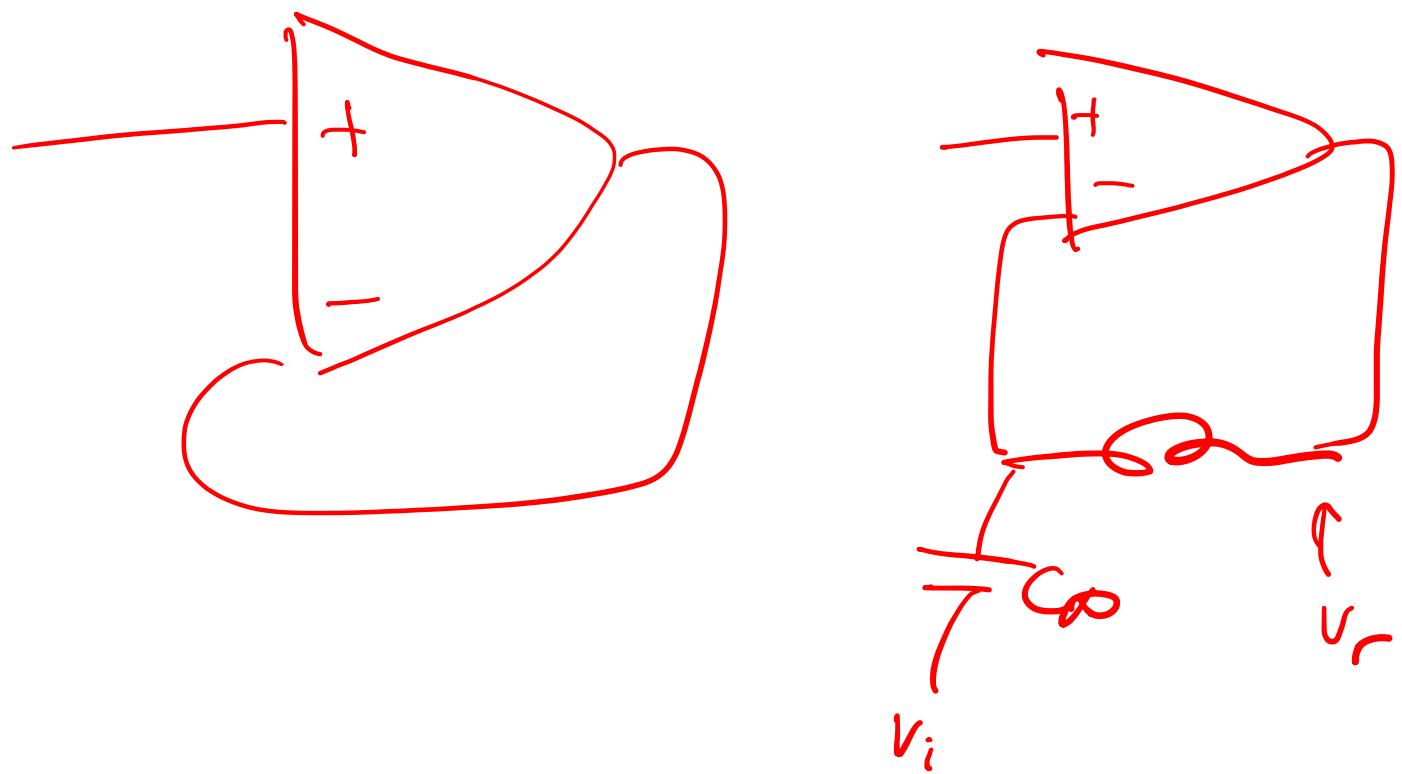
$$T(s) \cong \frac{v_{return}}{v_{test}}$$

- Inaccurate
- Cumbersome
- Different results for different breakpoints

An ideal loop gain test circuit would:

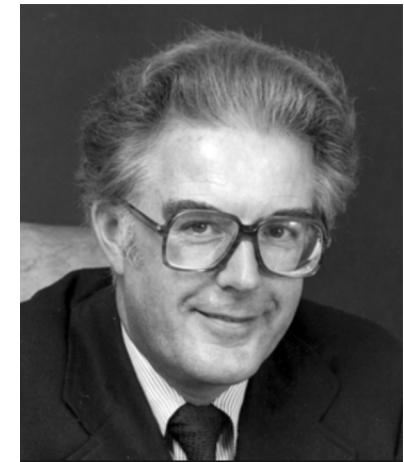
- not alter node impedances
- not affect the DC bias point

Another Hack....



Middlebrook Genius

INT. J. ELECTRONICS, 1975, VOL. 38, NO. 4, 485-512



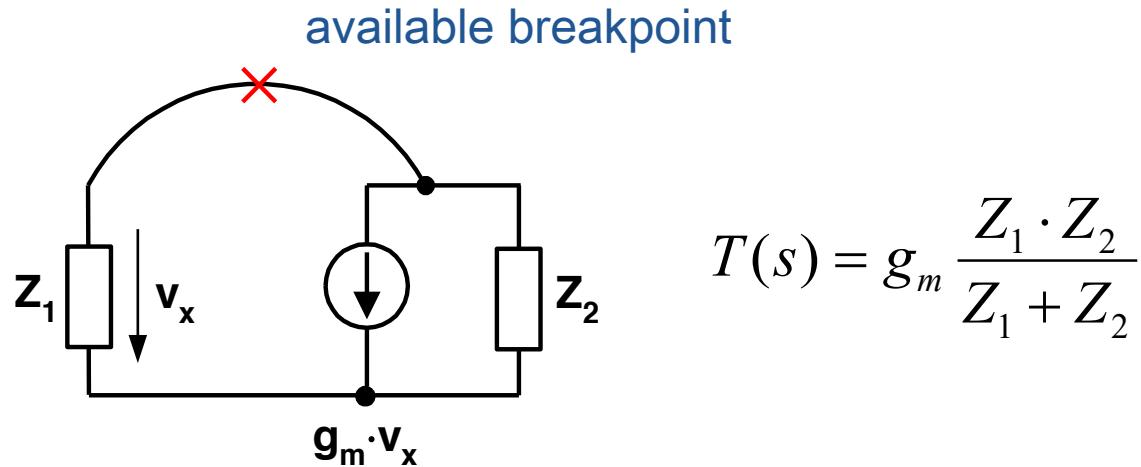
Measurement of loop gain in feedback systems†

R. D. MIDDLEBROOK‡

In the design of a feedback system it is desirable to make experimental measurements of the loop gain as a function of frequency to ensure that the physical system operates as analytically predicted or, if not, to supply information upon which a design correction can be based. In high loop-gain systems it is desirable that the loop-gain measurement be made without opening the loop. This paper discusses practical methods of measuring and interpreting the results for loop gain of the closed-loop system by a voltage injection or a current-injection technique; extension to the case in which the measurement can be made even though the system is unstable; and extension to the case in which neither the voltage nor current-injection technique alone is adequate, but in which a combination of both permits the true loop gain to be derived. These techniques have been found useful not only in linear feedback systems but also in describing-function analysis of switching-mode converters and regulators.

Problem Generalization

Any “single loop“ feedback circuit can be represented as:



Breakpoint at ideal source is not available.
But there is a breakpoint “between finite impedances“

An interesting observation...

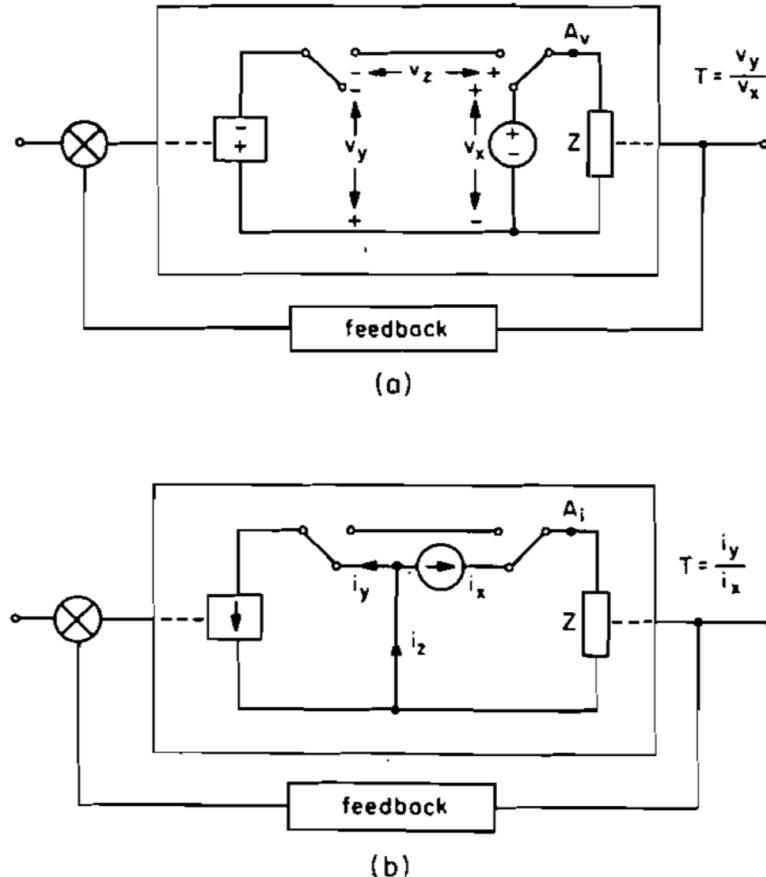
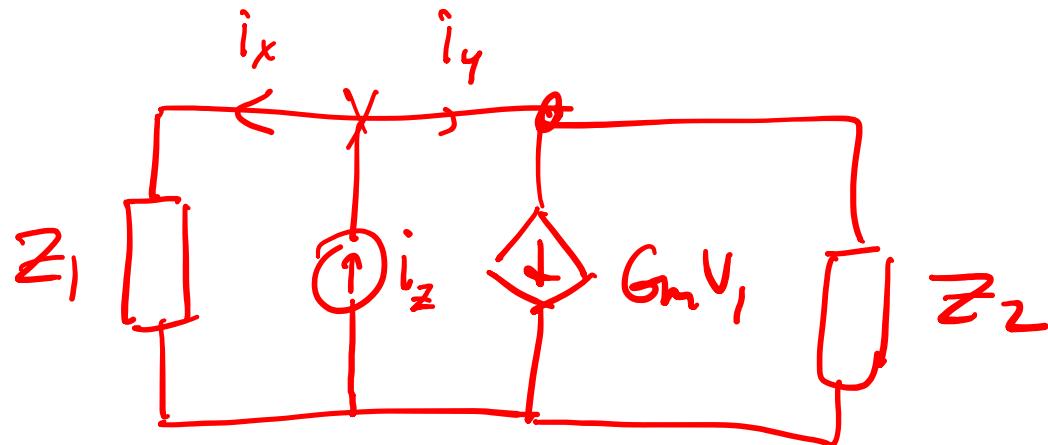


Figure 1. Measurement of loop gain T by opening the loop, (a) by voltage ratio, (b) by current ratio.

T_i derivation

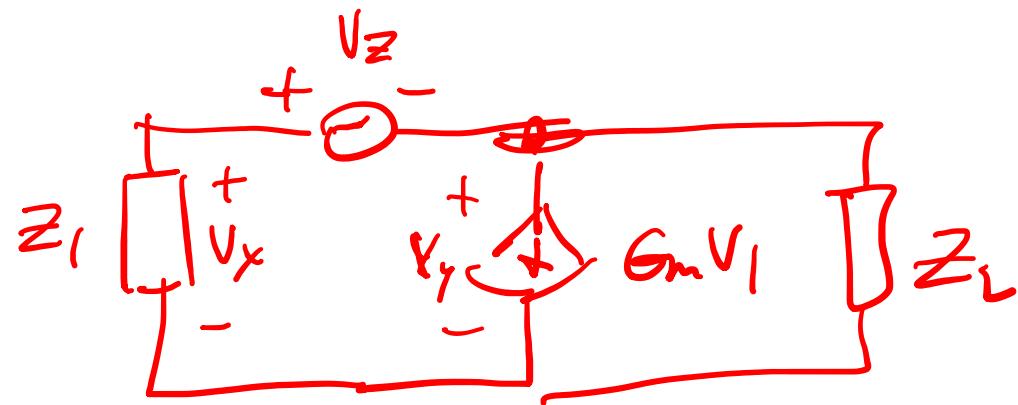


$$T_i \triangleq \frac{i_y}{i_x} \quad i_y = G_m V_1 + \frac{V_1}{Z_2}$$

$$V_1 = i_x Z_1$$

$$T_i = \frac{i_y}{i_x} = G_m Z_1 + \frac{Z_1}{Z_2} \neq T$$

T_v derivation



$$T_v \triangleq -\frac{V_y}{V_x}$$

$$V_y = V_x - V_z$$

$$= G_m Z_2 + \frac{Z_2}{Z_1}$$

$$\frac{V_x}{Z_1} + \frac{V_y}{Z_2} + G_m V_x = 0$$

$$V_x (1 + G_m Z_1) + \frac{Z_1}{Z_2} V_y = 0$$

Derivation of T

$$T_i = G_m Z_1 + \frac{Z_1}{Z_2}$$

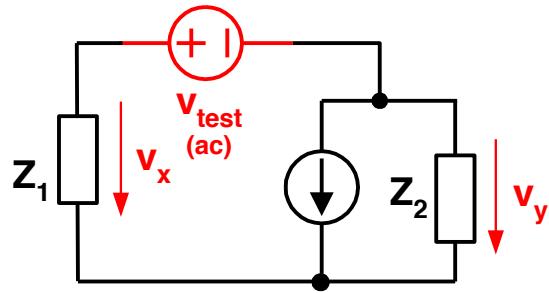
$$T = \frac{G_m Z_1 Z_2}{Z_1 + Z_2}$$

$$\left(T_i - \frac{Z_1}{Z_2}\right) \frac{Z_2}{Z_1 + Z_2} = T$$

$$T_v = G_m Z_2 + \frac{Z_2}{Z_1}$$

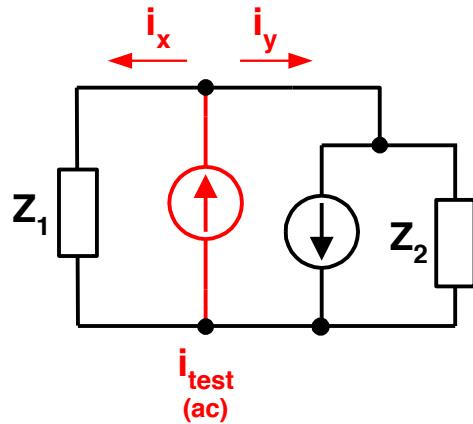
$$\left(T_v - \frac{Z_2}{Z_1}\right) \frac{Z_1}{Z_1 + Z_2} = T$$

Middlebrook Double Injection



$$\frac{v_y}{v_x} \equiv T_v = g_m \cdot Z_2 + \frac{Z_2}{Z_1}$$

Solving yields:



True Loop
Gain:

$$T = g_m \cdot \frac{Z_1 Z_2}{Z_1 + Z_2}$$

$$T = \frac{T_v T_i - 1}{T_v + T_i + 2}$$

$$\frac{i_y}{i_x} \equiv T_i = g_m \cdot Z_1 + \frac{Z_1}{Z_2}$$

- No “DC“ break in the loop, all loading effects covered.
- Measure T_v and T_i , then calculate actual T

Potential Accuracy Problem of Middlebrook Method

$$T = \frac{T_v T_i - 1}{T_v + T_i + 2}$$

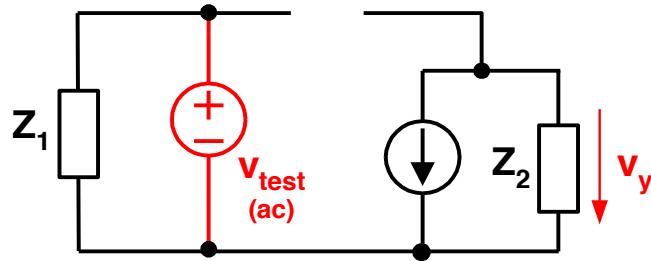
- For small $|T|$, evaluation of the above expression becomes sensitive to errors in the individual T_i and T_v measurements

- Sensitivity analysis: $S_x^y = \frac{\text{fractional change in } y}{\text{fractional change in } x}$

- For small $|T|$, it can be shown that: $S_{T_v, T_i}^T \cong \frac{1}{|T|}$

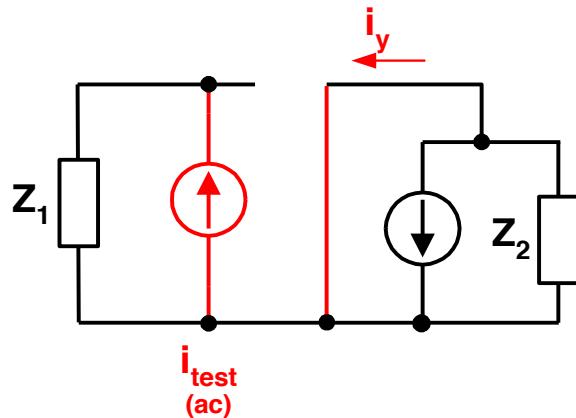
- E.g. at $|T| = 0.01$ simulation accuracy decreases by a factor of 100
- Not a problem in a typical circuit simulation/application
- Alternative approach for the *purist*: Rosenstark method [Rosenstark 84, Hurst 94]

Same Idea: Double Injection



$$\frac{v_y}{v_{test}} \equiv T_v = g_m \cdot Z_2$$

Solving yields:



True Loop
Gain:

$$T = g_m \cdot \frac{Z_1 Z_2}{Z_1 + Z_2}$$

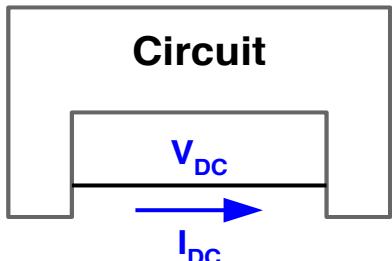
$$T = \frac{T_v T_i}{T_v + T_i}$$

$$\frac{i_y}{i_{test}} \equiv T_i = g_m \cdot Z_1$$

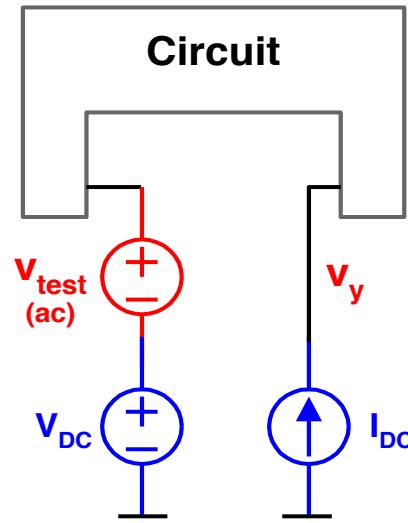
- Final loop gain calculation has no accuracy problems!
- Problem: Broken loop, no DC path to establish bias point

Solution to DC problem

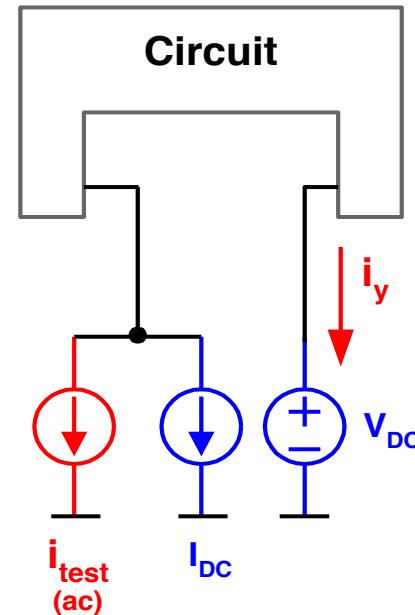
Closed loop DC replica



T_v measurement



T_i measurement



- Replicate DC conditions using a closed loop dummy circuit
- Looks complicated, but all sources can be conveniently combined in a subcircuit.

Spectre Simulation

- You can use a “iprobe” to break the loop without affecting the DC operating point
- Use the TF analysis to find loop gain and even plot the Nyquist Diagram
- For fully differential circuits (more later), you can use the CM/DM probe

Multiple Loops ?

- All practical feedback circuits have multiple loops:
 - Fully differential circuits have two feedback loops
 - Intrinsic device feedback through C_{gd} , R_{source}
 - Compensation capacitors
 - ...
- Solutions:
 - Decompose fully differential circuit into common/diff. mode loops
 - If a local feedback loop can be modeled as a combination of a stable controlled source and passive impedances, the multi-loop circuit reduces to a single loop [Hurst 94].
 - If there is a common breakpoint that breaks all feedback loops simultaneously, stability can be checked by finding the return ratio at the single breakpoint [Hurst 94].

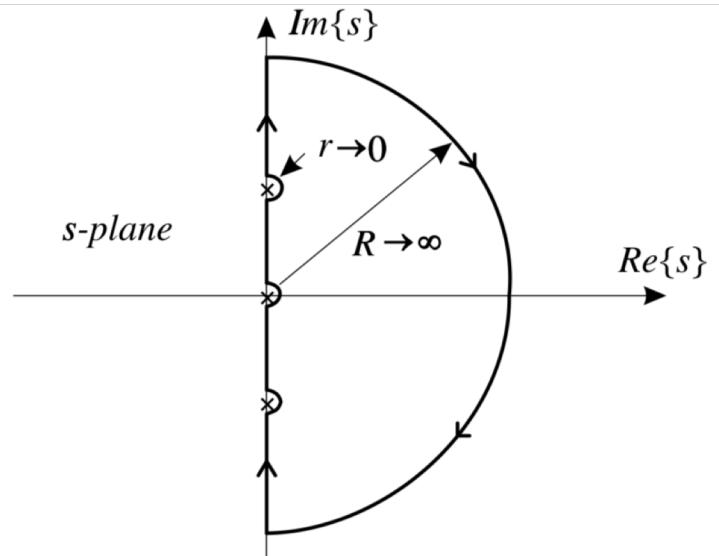
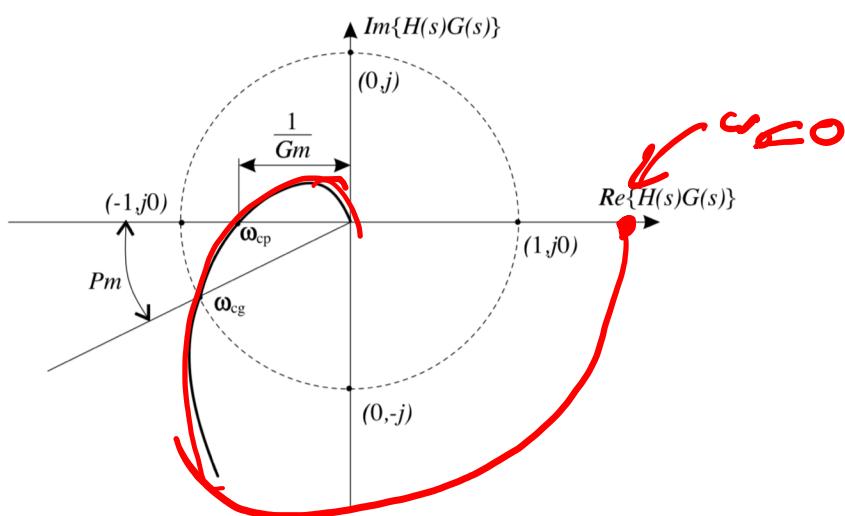
Nyquist Stability Criterion

- Can be applied without explicitly computing the poles and zeros.
- Applicable to systems defined by non-rational functions, such as systems with delays.
- In contrast to Bode plots, it can handle transfer functions with right half-plane singularities.
- In addition, there is a natural generalization to more complex systems with multiple inputs and multiple outputs, such as control systems for airplanes.

https://en.wikipedia.org/wiki/Nyquist_stability_criterion#Summary

The Criterion

Given a Nyquist contour Γ_s , let P be the number of poles of $G(s)$ encircled by Γ_s , and Z be the number of zeros of $1 + G(s)$ encircled by Γ_s . Alternatively, and more importantly, if Z is the number of poles of the closed loop system in the right half plane, and P is the number of poles of the open-loop transfer function $G(s)$ in the right half plane, the resultant contour in the $G(s)$ -plane, $\Gamma_{G(s)}$ shall encircle (clock-wise) the point $(-1 + j0)$ N times such that $N = Z - P$.



General Nyquist Criterion

[Bode 45]:

“If a circuit is stable when all its tubes have their nominal gains, the total number of clockwise and counterclockwise encirclements of the critical point must be equal to each other in the series of Nyquist diagrams for the individual tubes obtained by beginning with all tubes dead and restoring the tubes successively in any order to their nominal gains“



Comments and Observations

- Problem: Simulating the “Nyquist diagrams for the individual tubes” (return ratios) in principle requires access to the ideal breakpoints of controlled sources
- Single loop case is special in that the return ratio for the active device(s) can be found by breaking the loop *anywhere* in the circuit
- It is not clear how to apply the general Nyquist criterion without having ideal source breakpoints available. Best bet: Break all loops at “near ideal” breakpoints (voltage/current drive)? Time for a good publication on this topic!
- If there is a “single tube” that breaks all feedback, this “tube” can be put back last in the Nyquist plot sequence and therefore establishes stability

Always run a transient analysis for a true stability check!

[Bode 45]:

“... thus the circuit may sing when the tubes begin to lose their gain because of age, and it may also sing, instead of behaving as it should, when the gain increases from zero as power is supplied to the circuit

...“



Conclusion

- Presented two methods for loop gain simulation in single loop amplifiers
- Most circuits with (parasitic) multi-loops can be reduced to a single loop problem
- Assessment of stability in a general multi-loop circuit requires Nyquist stability check
- Loop gain simulations would greatly simplify if AC transistor models had a built-in ideal *break and inject* capability
- Stability analysis (as discussed here) assumes a linear system

References

- [Bode 45] H.W. Bode, *Network Analysis and Feedback Amplifier Design*, Van Nostrand, New York, 1945.
- [Middlebrook 75] R.D. Middlebrook, “Measurement of Loop Gain in Feedback Systems,” Int. J. Electronics, Vol. 38, No.4, .pp. 485-512, 1975.
- [Rosenstark 84] S. Rosenstark, “Loop Gain Measurement in Feedback Amplifiers,” Int. J. Electronics, Vol. 57, No.3., pp. 415-421, 1984.
- [Hurst 91] P.J. Hurst, “Exact Simulation of Feedback Circuit Parameters,” Trans. on Circuits and Systems, pp.1382-1389, Nov. 1991.
- [Hurst 94] P.J. Hurst, S.H. Lewis, “Simulation of Return Ratio in Fully Differential Feedback Circuits,” Proc. CICC 1994, pp.29-32.
- [HLGM 01] P.Gray, P.Hurst, S.Lewis, R. Meyer, *Analysis and Design of Analog Integrated Circuits*, 4th ed., Wiley & Sons, 2001.

Example

Loop-Gain Analysis

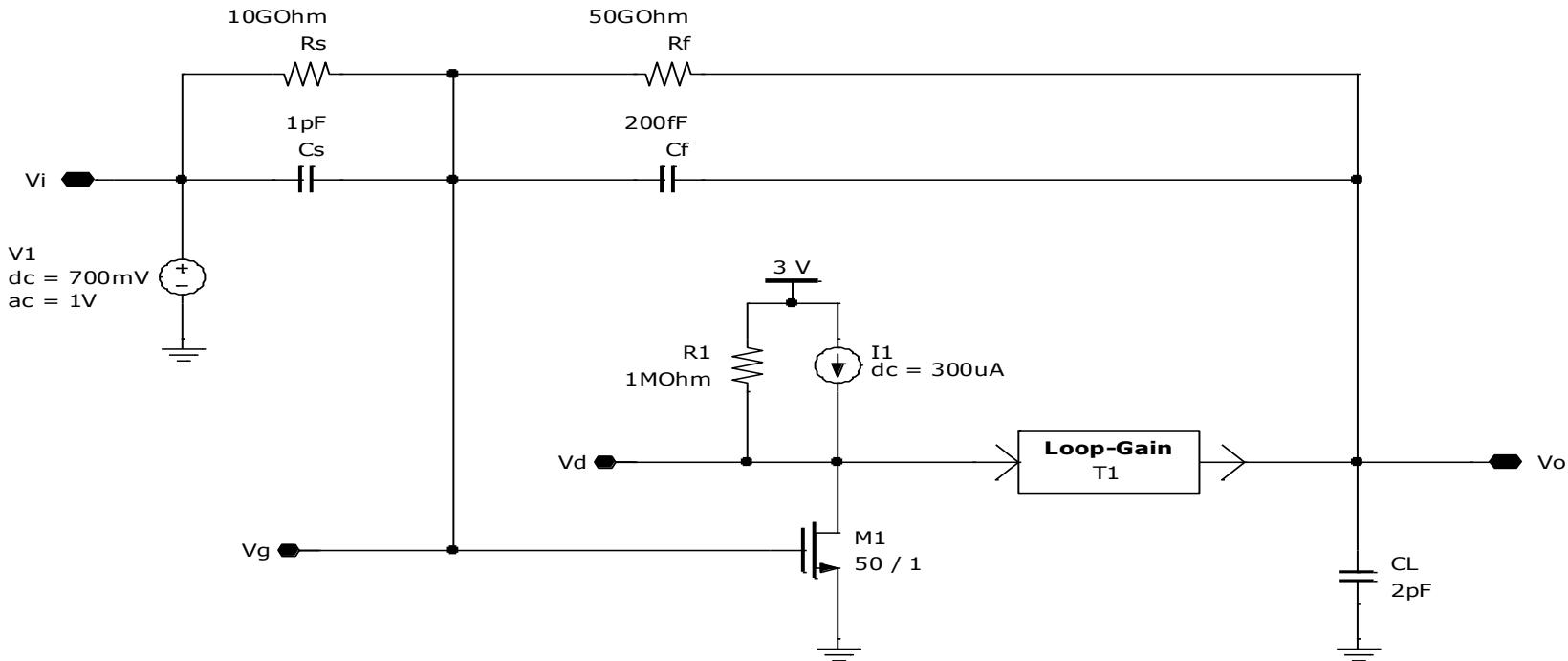
DC Analysis DC1

Device V1

sweep from 0 to 3 (51 steps)

AC Analysis AC1

log sweep from 1k to 10G (101 steps)



Loop-Gain from SPICE

```
loopgain_example
simulator lang=spectre
output_options options save=all

CL ( Vo 0 ) capacitor c=2p
Cs ( Vi Vg ) capacitor c=1p
Cf ( Vg Vo ) capacitor c=200f
I1 ( p Vd ) isource type=dc dc=300u
VDD ( p 0 ) vsource type=dc dc=3
V1 ( Vi 0 ) vsource type=dc dc=700m mag=1 xfmag=1 pacmag=1
Rs ( Vi Vg ) resistor r=10G
Rf ( Vg Vo ) resistor r=50G
R1 ( p Vd ) resistor r=1M
T1 ( Vd Vo ) tech_misc_loopgain_log start=10k stop=100G points=101
M1 ( Vd Vg 0 0 ) tech_cmos35_nmos w=50u l=1u ad=37.5p pd=51u

DC1 dc start=0 stop=3 lin=51 dev=V1
AC1 ac start=1k stop=10G log=101
```

SPICE (cont.)

```
subckt tech_misc_loopgain_log (vx vy)
    parameters start=1k stop=10G points=100
    VX (v vx) vsource
    VY (v vy) vsource
    I (0 v) isource
    start_ti alter dev=I param=mag value=1
        loopgain_ix xf probe=VX start=start stop=stop log=points
        loopgain_iy xf probe=VY start=start stop=stop log=points
    end_ti alter dev=I param=mag value=0
    start_tv alter dev=VX param=mag value=1
        loopgain_vx (vx 0) xf start=start stop=stop log=points
        loopgain_vy (vy 0) xf start=start stop=stop log=points
    end_tv alter dev=VX param=mag value=0
ends tech_misc_loopgain_log

model tech_cmos35_nmos bsim3v3 type=n ...
```

SPICE (cont.)

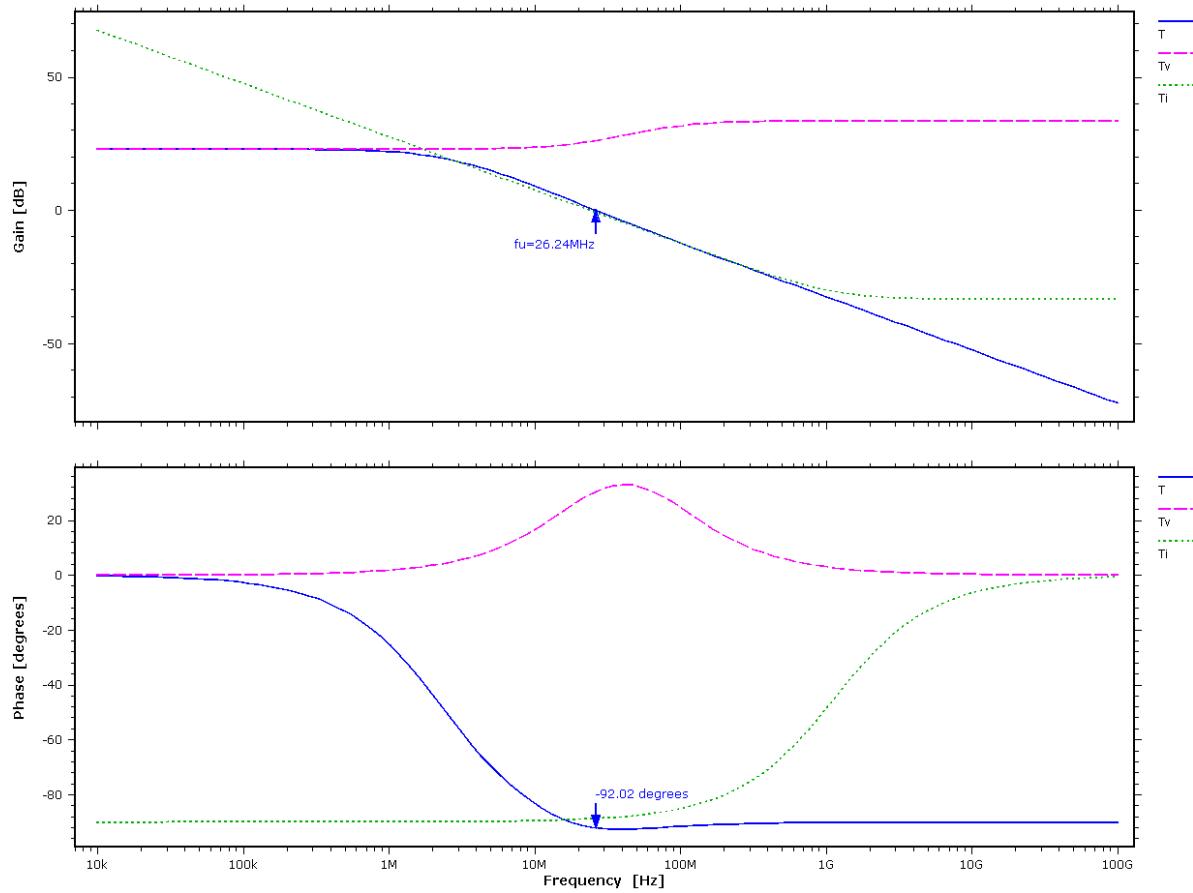
```
Vy = T1.loopgain_vy/T1.VX;           // analysis / trace
Vx = T1.loopgain_vx/T1.VX;
Iy = T1.loopgain_iy/T1.I;
Ix = T1.loopgain_ix/T1.I;
freq = T1.loopgain_ix/freq;

Tv = Vx / Vy;                      // compute result
Ti = -Ix / Iy;

T = (Tv * Ti - 1) / (Tv + Ti + 2);

plot(freq, -T, "T");
plot(freq, -Tv, "Tv");
plot(freq, -Ti, "Ti");
```

SPICE Result



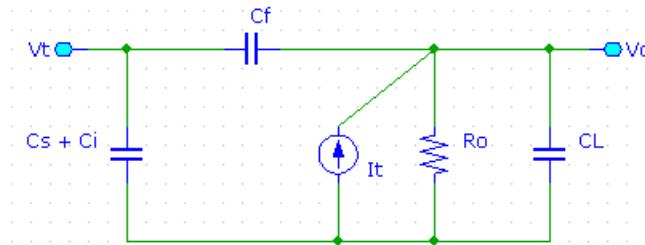
Loop-Gain by Hand

$$F = \frac{C_f}{C_f + C_s + C_i}$$

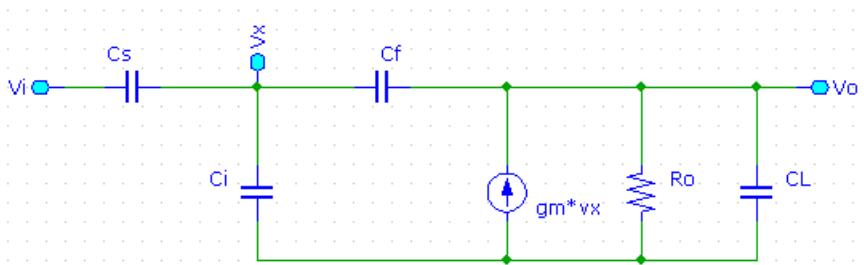
$$\approx \frac{200}{200+1000+170} = \frac{1}{6.85}$$

$$T = \frac{1}{s} \frac{g_m F}{C_L + C_f(1-F)} = \frac{1}{s} \frac{g_m F}{C_{L_{eff}}}$$

$$f_u = \frac{1}{2\pi} \frac{g_m F}{C_L + C_f(1-F)}$$
$$\approx \frac{1}{2\pi} \frac{2.2\text{mS}}{2\text{pF} \times 6.85} = \underline{\underline{26\text{MHz}}}$$



Closed-Loop Gain



$$v_x C_T - v_i C_s - v_o C_f = 0$$

$$v_o s (C_L + C_f) - v_x s C_f + v_x g_m = 0 \quad (R_o \rightarrow \infty)$$

$$A = \frac{v_o}{v_i}$$

$$= -\frac{C_s}{C_f} \frac{1 - s \frac{C_f}{g_m}}{1 + s \frac{C_L + C_f(1-F)}{F g_m}}$$

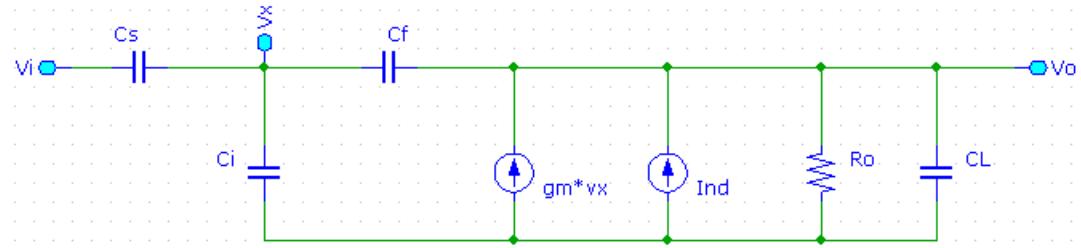
$$A_{vo} = -c = -\frac{C_s}{C_f}$$

$$\omega_z = +\frac{g_m}{C_f}$$

$$\omega_p = -F \frac{g_m}{C_L + C_f(1-F)}$$

$$\approx -F \omega_u \quad \text{for } 1-F \ll 1$$

Noise



$$v_o = \frac{i_{nd}}{1 + s \frac{C_L + C_f(1-F)}{Fg_m}}$$

$$\overline{i_{nd}^2} = 4k_B T g_m \Delta f$$

$$v_x C_T - v_o C_f = 0$$

$$v_o s(C_L + C_f) - v_x s C_f + v_x g_m = i_{nd} \quad (R_o \rightarrow \infty)$$

$$\overline{v_{oT}^2} = \frac{k_B T}{C_L + C_f(1-F)} \frac{1}{F}$$

- Noise gain: $1/F$
- Signal gain: $c < 1/F = 1 + c + C_i/C_f$
- C_i has no effect on c but increases $1/F \rightarrow$ increases noise gain
- Choose $C_i/C_f \ll 1+c$ to minimize noise enhancement
- C_f increases load \rightarrow lowers noise (depends also on switch resistance)