Weight Loss Example

In this designed experiment (from Ott & Longnecker), we the relationship between weight loss (response) versus time and humidity (predictors). Because this is a designed experiment, the predictors (time and humidity) are uncorrelated.

```
WtLoss <- read.csv("~/Dropbox/STAT512/Lectures/MultReg1/MR1_WtLoss.csv")
WtLoss</pre>
```

```
##
      wt_loss time humid
## 1
           4.3
                       0.2
                   4
## 2
           5.5
                   5
                       0.2
## 3
           6.8
                   6
                       0.2
## 4
           8.0
                       0.2
## 5
           4.0
                       0.3
           5.2
## 6
                       0.3
## 7
           6.6
                       0.3
           7.5
                       0.3
## 8
                   7
## 9
           2.0
                       0.4
## 10
           4.0
                   5
                       0.4
                   6
## 11
           5.7
                       0.4
## 12
           6.5
                       0.4
```

cor(WtLoss)

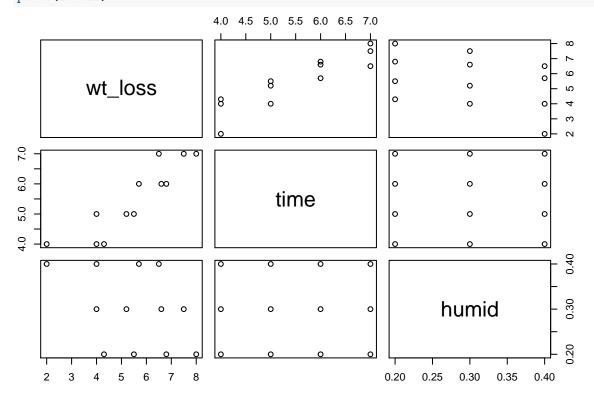
```
## wt_loss time humid

## wt_loss 1.0000000 0.8949235 -0.3970996

## time 0.8949235 1.0000000 0.0000000

## humid -0.3970996 0.0000000 1.0000000
```

pairs(WtLoss)



```
Model1 <- lm(wt_loss ~ time, data = WtLoss)</pre>
summary(Model1)
##
## lm(formula = wt_loss ~ time, data = WtLoss)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -1.5333 -0.5625 0.3917 0.5458 0.7667
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -1.7333
                          1.1652 -1.488
                                             0.168
                           0.2076 6.342 8.44e-05 ***
## time
                1.3167
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8041 on 10 degrees of freedom
## Multiple R-squared: 0.8009, Adjusted R-squared: 0.781
## F-statistic: 40.22 on 1 and 10 DF, p-value: 8.437e-05
Model2 <- lm(wt_loss ~ humid, data = WtLoss)</pre>
summary(Model2)
##
## Call:
## lm(formula = wt_loss ~ humid, data = WtLoss)
##
## Residuals:
##
                 1Q Median
       Min
                                   3Q
                                           Max
## -2.70833 -0.98333 0.09167 1.24167 1.99167
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 7.908
                            1.818 4.350 0.00144 **
                            5.847 -1.368 0.20119
                -8.000
## humid
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.654 on 10 degrees of freedom
## Multiple R-squared: 0.1577, Adjusted R-squared: 0.07346
## F-statistic: 1.872 on 1 and 10 DF, p-value: 0.2012
Model3 <- lm(wt_loss ~ time + humid, data = WtLoss)</pre>
summary(Model3)
## Call:
## lm(formula = wt_loss ~ time + humid, data = WtLoss)
## Residuals:
##
       Min
                 1Q Median
## -0.73333 -0.17083 -0.04167 0.33750 0.46667
##
```

```
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
   (Intercept)
                  0.66667
                               0.69423
                                           0.960 0.361994
##
## time
                  1.31667
                               0.09981
                                          13.191 3.43e-07 ***
                 -8.00000
                               1.36677
                                          -5.853 0.000243 ***
## humid
##
                      0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.3866 on 9 degrees of freedom
## Multiple R-squared: 0.9586, Adjusted R-squared: 0.9494
## F-statistic: 104.1 on 2 and 9 DF, p-value: 5.993e-07
par(mfrow = c(2, 2))
plot(Model3)
                                                     Standardized residuals
                                                                         Normal Q-Q
                 Residuals vs Fitted
                O5
                                                                                     0.0.70
                                                                                                50
                               70
                        0
Residuals
                           0
      -0.8 0.0
                                                                        00000
                                                          0
                                   00
                                                          7
             3
                         5
                               6
                                     7
                                           8
                                                                -1.5
                                                                          -0.5
                                                                                    0.5
                                                                                              1.5
                   4
                      Fitted values
                                                                       Theoretical Quantiles
(Standardized residuals)
                                                     Standardized residuals
                   Scale-Location
                                                                    Residuals vs Leverage
                                                                                                    0.5
                                                                                     O<sup>5</sup>
                                                                         8
                        0 0
                                            0
                                                          0
                   00
                                                                                                    0.5
                                                          7
                                                                       Cook's distance
      0.0
                                        0
             3
                         5
                               6
                                           8
                                                              0.00
                                                                       0.10
                                                                                 0.20
                                                                                          0.30
                   4
```

Fitted values

Leverage