

# Exam1PraacticeSolutions

## Question #1

```
library(car)
```

```
## Loading required package: carData
```

```
bodyfat <- read.csv("~/Dropbox/STAT512/Assigns/Assign4/BodyFat.csv")
```

```
#A
```

```
Model1 <- lm(BodyFat ~ ., data = bodyfat)
```

```
vif(Model1)
```

```
## Triceps Thigh Midarm
```

```
## 708.8429 564.3434 104.6060
```

```
Model2 <- lm(Triceps ~ Thigh + Midarm, data = bodyfat)
```

```
1/(1-summary(Model2)$r.squared)
```

```
## [1] 708.8429
```

```
#B
```

```
Model3 <- lm(BodyFat ~ Triceps + Midarm, data = bodyfat)
```

```
vif(Model3)
```

```
## Triceps Midarm
```

```
## 1.265118 1.265118
```

```
#The above VIF's are the same because,
```

```
1/(1-cor(bodyfat$Triceps,bodyfat$Midarm)^2)
```

```
## [1] 1.265118
```

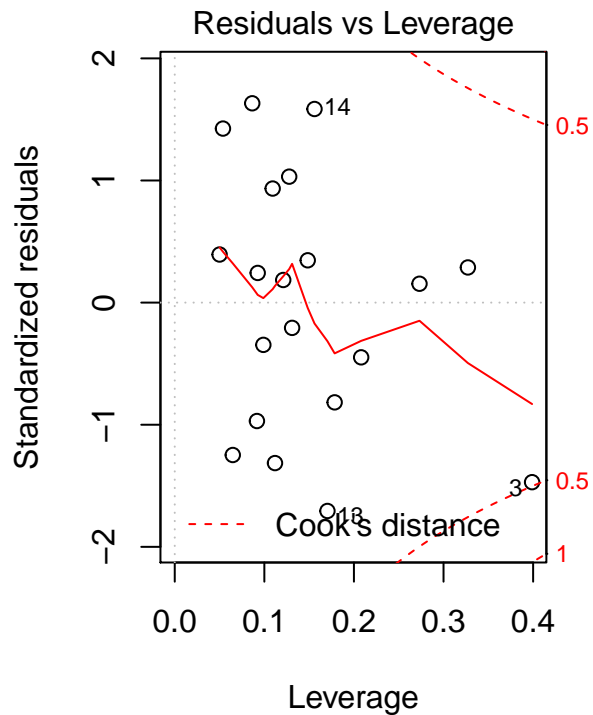
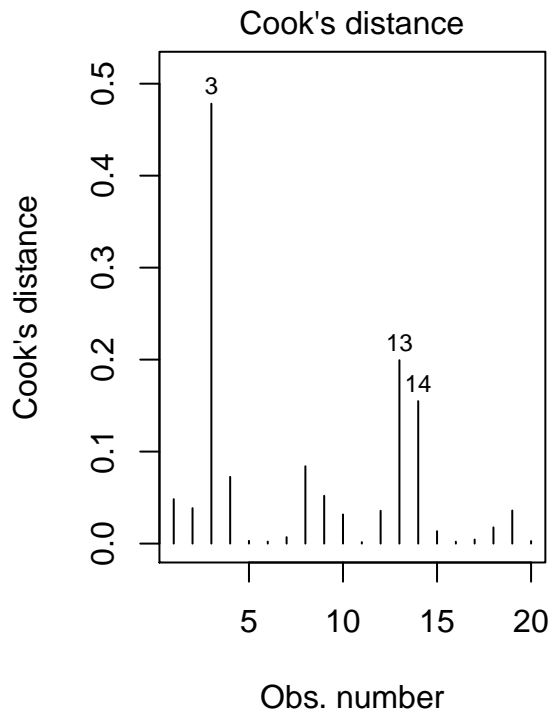
```
#is the same as due to commutative property of only have 2 predictors
```

```
1/(1- summary(lm(Midarm ~ Triceps, data = bodyfat))$r.squared)
```

```
## [1] 1.265118
```

```
par(mfrow = c(1,2))
```

```
plot(Model3, which = c(4,5))
```



```
influence.measures(Model3)
```

```
## Influence measures of
## lm(formula = BodyFat ~ Triceps + Midarm, data = bodyfat) :
##
##      dfb.1_  dfb.Trctp dfb.Mdrn  dffit cov.r  cook.d   hat inf
## 1  -0.01417  0.308728 -0.21515 -0.3768 1.295 0.04831 0.1785
## 2   0.00575 -0.075532  0.08371  0.3514 0.865 0.03851 0.0538
## 3   1.05631  0.052521 -1.05722 -1.2439 1.327 0.47826 0.3988  *
## 4   0.30021 -0.168675 -0.20053 -0.4774 0.979 0.07251 0.1119
## 5  -0.01333 -0.074759  0.06649  0.0919 1.643 0.00299 0.2732  *
## 6  -0.05045 -0.030637  0.06128 -0.0780 1.370 0.00215 0.1310
## 7  -0.01524  0.114639 -0.05289  0.1408 1.379 0.00697 0.1484
## 8  -0.29157  0.066364  0.27028  0.5306 0.787 0.08408 0.0865
## 9   0.33347 -0.023774 -0.26269  0.3956 1.133 0.05195 0.1278
## 10 -0.17910 -0.102926  0.20727 -0.3076 1.113 0.03165 0.0917
## 11 -0.03196  0.042322  0.00616  0.0668 1.356 0.00158 0.1211
## 12 -0.06659  0.236274 -0.07068  0.3259 1.150 0.03568 0.1093
## 13 -0.70148  0.378629  0.34248 -0.8242 0.823 0.19936 0.1704
## 14  0.07310 -0.579789  0.36482  0.7163 0.879 0.15486 0.1560
## 15  0.16720 -0.117851 -0.06671  0.1953 1.757 0.01344 0.3272  *
## 16 -0.03801  0.033493  0.01903  0.0754 1.308 0.00201 0.0926
## 17 -0.03646 -0.065715  0.06818 -0.1116 1.303 0.00438 0.0989
## 18 -0.06520 -0.171702  0.16163 -0.2242 1.462 0.01760 0.2081
## 19 -0.11269  0.153656 -0.03214 -0.3343 0.961 0.03595 0.0648
## 20  0.01396 -0.000594 -0.00237  0.0881 1.228 0.00273 0.0501
```

Rules of Thumb:  $|DFBETA| > 2/\sqrt{n} = 0.447$   $|DFFITS| = 2*\sqrt{(k+1)/n} = 0.774$  Cooks  $D > 1$  Obs#3 is influential for DFBETAS and DFFITS, but not Cook's distance

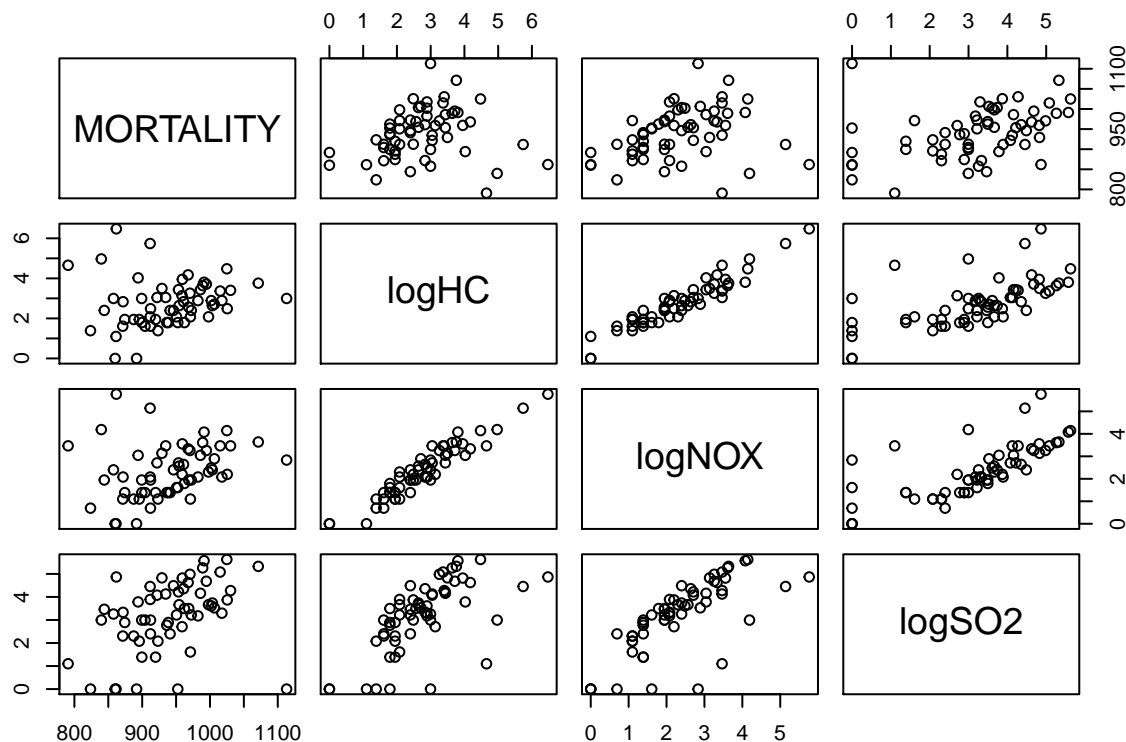
## Question #2

```
library(MuMin)
library(car)
Mortality <- read.csv("~/Dropbox/STAT512/ExamMaterial/Exam1/Mortality.csv", row.names=1)
Mortality$logHC <- log(Mortality$HC)
Mortality$logNOX <- log(Mortality$NOX)
Mortality$logSO2 <- log(Mortality$SO2)
colnames(Mortality)
```

```
## [1] "MORTALITY" "PRECIP" "HUMIDITY" "JANTEMP" "JULYTEMP"
## [6] "OVER65" "HOUSE" "EDUC" "SOUND" "DENSITY"
## [11] "NONWHITE" "WHITECOL" "POOR" "HC" "NOX"
## [16] "SO2" "logHC" "logNOX" "logSO2"
```

#A

```
pairs(Mortality[,c(1, 17:19)])
```



```
cor(Mortality[,c(1, 17:19)])
```

```
##           MORTALITY      logHC      logNOX      logSO2
## MORTALITY 1.0000000 0.1507561 0.2919995 0.4031280
## logHC      0.1507561 1.0000000 0.9474952 0.6408135
## logNOX     0.2919995 0.9474952 1.0000000 0.7328074
## logSO2     0.4031280 0.6408135 0.7328074 1.0000000
```

#B

```
FullModel1 <- lm(MORTALITY ~ PRECIP + HUMIDITY + JANTEMP +
                  JULYTEMP + OVER65 + HOUSE + EDUC + SOUND +
                  DENSITY + NONWHITE + WHITECOL + POOR, data = Mortality)
options(na.action = "na.fail")
```

```
AllSubsets1 <- dredge(FullModel1, rank="AIC")
```

```
## Fixed term is "(Intercept)"
```

The Final model has these seven predictors: DENSITY EDUC HOUSE JANTEMP JULYTEMP NONWHITE PRECIP

## C

```
FullModel2 <- lm(MORTALITY ~ DENSITY + EDUC + HOUSE + JANTEMP
+ JULYTEMP + NONWHITE + PRECIP + logHC + logNOX + logSO2, data = Mortality)
AllSubsets2 <- dredge(FullModel2,
fixed = c("DENSITY", "EDUC", "HOUSE", "JANTEMP",
"JULYTEMP", "NONWHITE", "PRECIP"), rank="AIC")
```

```
## Fixed terms are "DENSITY", "EDUC", "HOUSE", "JANTEMP", "JULYTEMP", "NONWHITE", "PRECIP" and "(Intercept)"
```

```
AllSubsets2
```

```
## Global model call: lm(formula = MORTALITY ~ DENSITY + EDUC + HOUSE + JANTEMP + JULYTEMP +
## NONWHITE + PRECIP + logHC + logNOX + logSO2, data = Mortality)
```

```
## ---
```

```
## Model selection table
```

##	(Intrc)	DENSI	EDUC	HOUSE	JANTE	JULYT	logHC	lgNOX	lgSO2	NONWH
## 4	1353	0.003128	-13.76	-55.03	-1.980	-2.1730	-28.480	37.65		5.032
## 8	1460	0.003873	-16.16	-69.76	-2.548	-2.3700	-29.190	45.53	-7.793	5.254
## 3	1229	0.002266	-16.04	-51.90	-2.265	-0.5672		15.66		4.500
## 7	1325	0.002939	-18.32	-65.54	-2.801	-0.7131		22.49	-7.252	4.694
## 2	1322	0.003490	-18.78	-59.26	-2.306	-0.9799	10.730			4.955
## 1	1525	0.005555	-20.03	-70.03	-2.123	-2.7280				5.892
## 5	1339	0.003809	-16.70	-52.19	-1.731	-1.8270			6.007	5.228
## 6	1295	0.003266	-17.84	-55.00	-2.132	-0.9944	8.683		2.126	4.899

```
## PRECI df logLik AIC delta weight
```

## 4	1.766	11	-287.984	598.0	0.00	0.411
## 8	1.903	12	-287.140	598.3	0.31	0.352
## 3	2.067	10	-290.177	600.4	2.39	0.125
## 7	2.201	11	-289.499	601.0	3.03	0.090
## 2	1.807	10	-292.917	605.8	7.87	0.008
## 1	1.276	9	-294.284	606.6	8.60	0.006
## 5	1.450	10	-293.368	606.7	8.77	0.005
## 6	1.768	11	-292.850	607.7	9.73	0.003

```
## Models ranked by AIC(x)
```

## D

2 of the 3 new natural logged pollution variables are added

```
PolluteModel <- lm(MORTALITY ~ DENSITY + EDUC + HOUSE + JANTEMP +
JULYTEMP + NONWHITE + PRECIP + logHC + logNOX, data = Mortality)
vif(PolluteModel)
```

##	DENSITY	EDUC	HOUSE	JANTEMP	JULYTEMP	NONWHITE	PRECIP
##	1.480251	1.871509	2.112059	1.980619	3.420447	3.929744	2.350081

```
##      logHC      logNOX
## 16.835589 12.660836
```

## E

One unit increase in logHC is associated with a 28.48 unit DECREASE in predicted Mortality, holding all other variables in the model constant. One unit increase in logNOX is associated with a 37.65 unit INCREASE in predicted Mortality, holding all otehr variable in the model constant.

\*\*Also, note that the estimated partial regression coefficients associated with logHC in different ‘runner up’ models has the sign changes when logNOX is in the mode which indicate sensitivity to including both variables in a model.