



Tutorial T08

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Das

Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

Programming in Modern C++

Tutorial T08: How to design a UDT like built-in types?: Part 2: Int and Poly UDT

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All url's in this module have been accessed in September, 2021 and found to be functional



Tutorial Recap

Tutorial T08

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Das

Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- Analysed the difference between Built-in & UDT
- Discussed the meaning of Building a data type
- Understood the necessity of Building a data type
- Built a Fraction data type by iterative refinement



Tutorial Objectives

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Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- To build more UDTs: `Int<N>` and `Poly<T>`
- To test mix of UDTs



Tutorial Outline

Tutorial T08

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Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- 1 Tutorial Recap
- 2 Int<N> UDT
 - Design
 - Operations
 - Class Design
 - Implementation
 - Test
- 3 Polynomial UDT
 - Design
 - Implementation
 - Test
- 4 Practice UDTs
- 5 Tutorial Summary



Int<N> UDT

Tutorial T08

Partha Pratim
Das

Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

Int<N> UDT



Understanding int

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Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- The datatype we are most familiar with is `int` which is a signed integer
 - Represented in a given number of bits, typically, 8, 16, 32, 64, or 128
 - Hence, `int` can represent numbers from `INT_MAX` to `INT_MIN`
 - For example, for 32 bits, $INT_MAX = 2^{31} - 1 = 2147483647$ and $INT_MIN = -2^{31} = -2147483648$
 - Beyond the `INT_MAX` .. `INT_MIN` range we get integer overflow and numbers wraparound

```
#include <bits/stdc++.h>
using namespace std;
int main() {
    cout << INT_MAX    << endl; // 2147483647
    cout << INT_MIN    << endl; // -2147483648
    cout << INT_MAX+1  << endl; // -2147483648 integer overflow in expression of type 'int'
    cout << INT_MIN-1  << endl; // 2147483647 integer overflow in expression of type 'int'
    cout << -INT_MIN   << endl; // -2147483648 integer overflow in expression of type 'int'
}
```



Design of Int UDT

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- To understand `int` better, we intend to design a UDT `Int<N>` which can behave like `int` albeit for a of size $N > 0$ bits that can be specified
- The range of values will be:
 - $\text{MinInt} = -2^{N-1} \dots \text{MaxInt} = 2^{N-1} - 1$
- The broad tasks involved include:
 - Make a clear statement of the concept of `Int`
 - Identify a representation for a `Int` object
 - Identify the properties and assertions applicable to all objects
 - Identify the operations for `Int` objects
 - ▷ Choose appropriate operators to overload for the operations
 - ▷ For example `operator+` to add two `Int` objects, or `operator<<` to stream a `Int` to `cout`
 - ▷ *Do not break the natural semantics for the operators*



Notion of Int

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Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- Intuitively $\text{Int}\langle N \rangle$ is a notation for whole numbers of the form of N bits signed integers
- $\text{MinInt} = -2^{N-1} \dots \text{MaxInt} = 2^{N-1} - 1$
- Numbers in $\text{Int}\langle N \rangle$ bits within a range of values $\text{MinInt} .. \text{MaxInt}$. Beyond this range the numbers wrap around:
 - $\text{MaxInt} + 1 = \text{MinInt}$
 - $\text{MinInt} - 1 = \text{MaxInt}$
- For example:
 - $N = 4 \Rightarrow \text{Range: } -8 .. 7$
 - $\text{MinInt} = -2^3 = -8$ and $\text{MaxInt} = 2^3 - 1 = 7$
 - Except for *overflow*¹ as follows, all operations of $\text{Int}\langle N \rangle$ is same as `int`
 - ▷ $7 + 1 = -8$
 - ▷ $-8 - 1 = 7$
 - ▷ $-8 = -8$

¹Some authors distinguish between *overflow* (being more than MaxInt) and *underflow* (being less than MinInt). However, we prefer to use the term *overflow* in both cases because actually representation *overflows* the bits in both cases



Operations of $\text{Int}\langle N \rangle$

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

$\text{Int}\langle N \rangle$ UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

Definition

Limits:

$$\text{MaxInt} = 2^{N-1} - 1$$

$$\text{MinInt} = -2^{N-1}$$

Negation:

$$\begin{aligned} -a &= a, \text{ if } a == \text{MinInt} \\ &= -a, \text{ otherwise} \end{aligned}$$

Addition:

$$\begin{aligned} a + b &= a + b - 2^N, \text{ if } a + b > \text{MaxInt} \\ &= a + b + 2^N, \text{ if } a + b < \text{MinInt} \\ &= a + b, \text{ otherwise} \end{aligned}$$

Subtraction:

$$a - b = a + (-b)$$

Let $N = 4$

Example 1: $2 + 3 = 5$. $4 + 7 = -5$. $(-5) + 6 = 1$. $(-3) + (-2) = -5$. $(-6) + -7 = 3$

Example 2: $2 - 3 = -1$. $4 - 7 = -3$. $(-5) - 6 = 5$. $(-3) - (-2) = -1$. $(-6) - (-7) = 1$

Multiplication, Division, and Modulus: Left as exercise



Design of `Int<N>` Class

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

`Int<N>` UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- Clearly, the representation of a `Int<N>` needs to be a template with an `unsigned int` param `N`
- For the implementation, the `Int<N>` needs to use an underlying type `T` where basic arithmetic operations are available. So `T` is a type parameter for `Int<N>`. By default this can be `int`
- It is important to note that `N <= sizeof(T) * 8`. Otherwise, our basic operations may overflow

- Hence, the `Int<N>` class would look like:

```
template<typename T = int, unsigned int N = 4>
class Int_ { // an N-bits integer class with underlying type T
    T v_;    // actual value in underlying type T
    // ... Rest of the class
}
```

- Note that we name the type as `Int_` so that we can conveniently alias it in the user program as:

```
template<typename T, unsigned int N> class Int_;
typedef Int_<int, 4> Int; // T = int and N = 4
// Use as Int
```

- `Int<N>` should support the operation of `int`:
- `Int<N>` should also support conversion the underlying type `T`
- `Int<N>` may support the following constants for convenience of implementation:

```
static const Int_<T, N> MaxInt; // 2^(N-1)-1
static const Int_<T, N> MinInt; // -2^(N-1)
```



Design of Int<N> Interface and Implementation

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
template<typename T = int, unsigned int N = 4>
class Int_ { public:
    static const Int_<T, N> MaxInt; // 2^(N-1)-1
    static const Int_<T, N> MinInt; // -2^(N-1)

    explicit Int_<T, N>(int v = 1) : v_(v) { // Two overloads of Constructor
        assert(v_ <= static_cast<int>(MaxInt)); // assert will fire if the value is out of limits
        assert(v_ >= static_cast<int>(MinInt));
    }
    Int_<T, N>(const Int_<T, N>& i) : v_(i.v_) { } // Copy Constructor
    ~Int_<T, N>() { } // No virtual destructor needed
    Int_<T, N>& operator=(const Int_<T, N>& i) { v_ = i.v_; return *this; } // Assignment
    // Streaming operators for IO
    friend ostream& operator<<(ostream& os, const Int_<T, N>& i) { os << i.v_; return os; }
    friend istream& operator>>(istream& is, Int_<T, N>& i) {
        T v; is >> v; i = Int_<T, N>(v); // We deliberately construct to test that v is within limits
        return is;
    }
    // Unary arithmetic operators
    Int_<T, N> operator-() const { return Int_<T, N>(v_ == MinInt_T? v_: -v_); }
    Int_<T, N> operator+() const { return *this; }
    Int_<T, N>& operator++() { *this = *this + Int_<T, N>(1); return *this; }
    Int_<T, N>& operator--() { *this = *this - Int_<T, N>(1); return *this; }
    Int_<T, N> operator++(int) { Int_<T, N> i = *this; ++*this; return i; }
    Int_<T, N> operator--(int) { Int_<T, N> i = *this; --*this; return i; }
```



Design of Int<N> Interface and Implementation

Tutorial T08

Partha Pratim
Das

Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
// Binary arithmetic operators
```

```
friend Int_<T, N> operator+(const Int_<T, N>& i1, const Int_<T, N>& i2) {  
    T v = i1.v_ + i2.v_; // add values in underlying type T  
    if (v > MaxInt_T) // MaxInt_T is MaxInt in type T  
        return Int_<T, N>(v - TwoPowerN_T); // wrap around if the value is more than MaxInt  
    else if (v < MinInt_T) // MinInt_T is MinInt in type T  
        return Int_<T, N>(v + TwoPowerN_T); // wrap around if the value is less than MinInt  
    else  
        return Int_<T, N>(v); // value within limits - no action  
}  
friend Int_<T, N> operator-(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1 + (-i2); }
```

```
// NOT IMPLEMENTED - left as exercises
```

```
friend Int_<T, N> operator*(const Int_<T, N>& i1, const Int_<T, N>& i2);  
friend Int_<T, N> operator/(const Int_<T, N>& i1, const Int_<T, N>& i2);  
friend Int_<T, N> operator%(const Int_<T, N>& i1, const Int_<T, N>& i2);
```

```
// Logical comparison operators
```

```
friend bool operator==(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1.v_ == i2.v_; }  
friend bool operator!=(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1.v_ != i2.v_; }  
friend bool operator<(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1.v_ < i2.v_; }  
friend bool operator<=(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1.v_ <= i2.v_; }  
friend bool operator>(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1.v_ > i2.v_; }  
friend bool operator>=(const Int_<T, N>& i1, const Int_<T, N>& i2) { return i1.v_ >= i2.v_; }
```



Design of Int<N> Interface and Implementation

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
// Advanced assignment operators: NOT IMPLEMENTED - left as exercises
Int_<T, N>& operator+=(const Int_<T, N>& i);
Int_<T, N>& operator-=(const Int_<T, N>& i);
Int_<T, N>& operator*=(const Int_<T, N>& i);
Int_<T, N>& operator/=(const Int_<T, N>& i);
Int_<T, N>& operator%=(const Int_<T, N>& i);

operator T() const { return v_; } // conversion to underlying type T

private: // data members
    T v_; // Value in underlying type T
    static const T MaxInt_T; // MaxInt = 2^(N-1)-1 in underlying type T
    static const T MinInt_T; // MinInt = -2^(N-1) in underlying type T
    static const T TwoPowerN_T; // 2^N in underlying type T

public: static int Int_<T, N>::pow() { return Int_<T, N - 1>::pow() * 2; }
};
template<typename T> class Int_<T, 1> { public: static int Int_<T, 1>::pow() { return 1; } };

// Instantiations of static const members
const Int Int::MaxInt = Int(Int::pow() - 1);
const Int Int::MinInt = Int(-Int::pow());
const int Int::MaxInt_T = static_cast<int>(Int::MaxInt); // 2^(N-1)-1
const int Int::MinInt_T = static_cast<int>(Int::MinInt); // -2^(N-1)
const int Int::TwoPowerN_T = (Int::MaxInt_T+1) << 1; // 2^N
```

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Testing Int<N>

Tutorial T08

Partha Pratim
Das

Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
#include <iostream>
using namespace std;
```

```
template<typename T, unsigned int N> class Int_;
typedef Int_<int, 4> Int; // N = 4
```

```
#include "Int.h"
```

```
void main() {
    cout << "Int::MaxInt = " << Int::MaxInt << endl; // Int::MaxInt = 7
    cout << "Int::MinInt = " << Int::MinInt << endl; // Int::MinInt = -8
```

```
    // Constructor, Copy Operations and Write Test
```

```
    Int f1(5);    cout << "Int f1(5) = " << f1 << endl;    // Int f1(5) = 5
    Int f2(0);    cout << "Int f2(0) = " << f2 << endl;    // Int f2(0) = 0
    Int f3;       cout << "Int f3 = " << f3 << endl;       // Int f3 = 1
    Int f4(f1);   cout << "Int f4(f1) = " << f4 << endl;   // Int f4(f1) = 5
    cout << "Assignment: f2 = f1: f2 = " << (f2 = f1) << endl; // Assignment: f2 = f1: f2 = 5
```

```
    // Read Test
```

```
    cin >> f1;    // 3
    cout << "Read f1 = " << f1 << endl; // Read f1 = 3
```



Testing Int<N>

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

// Unary Operations Test

```
cout << "-Int(2) = " << -Int(2) << endl;      // -Int(2) = -2
cout << "-Int(-2) = " << -Int(-2) << endl;     // -Int(-2) = 2
cout << "-Int(-8) = " << -Int(-8) << endl;     // -Int(-8) = -8
cout << "-Int(7) = " << -Int(7) << endl;       // -Int(7) = -7
cout << "++Int(2) = " << ++Int(2) << endl;     // ++Int(2) = 3
cout << "++Int(7) = " << ++Int(7) << endl;     // ++Int(7) = -8
cout << "++Int(-8) = " << ++Int(-8) << endl;  // ++Int(-8) = -7
cout << "--Int(0) = " << --Int(0) << endl;     // --Int(0) = -1
cout << "--Int(-7) = " << --Int(-7) << endl;  // --Int(-7) = -8
cout << "--Int(-8) = " << --Int(-8) << endl;  // --Int(-8) = 7
```

// Binary Operations Test

```
cout << "Int(2) + Int(3) = " << (Int(2) + Int(3)) << endl;    // Int(2) + Int(3) = 5
cout << "Int(4) + Int(7) = " << (Int(4) + Int(7)) << endl;    // Int(4) + Int(7) = -5
cout << "Int(-5) + Int(6) = " << (Int(-5) + Int(6)) << endl;  // Int(-5) + Int(6) = 1
cout << "Int(-3) + Int(-2) = " << (Int(-3) + Int(-2)) << endl; // Int(-3) + Int(-2) = -5
cout << "Int(-6) + Int(-7) = " << (Int(-6) + Int(-7)) << endl; // Int(-6) + Int(-7) = 3
```



Testing Int<N>

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

// Binary Operations Test

```
cout << "Int(2) - Int(3) = " << (Int(2) - Int(3)) << endl;    // Int(2) - Int(3) = -1
cout << "Int(4) - Int(7) = " << (Int(4) - Int(7)) << endl;    // Int(4) - Int(7) = -3
cout << "Int(-5) - Int(6) = " << (Int(-5) - Int(6)) << endl;   // Int(-5) - Int(6) = 5
cout << "Int(-3) - Int(-2) = " << (Int(-3) - Int(-2)) << endl; // Int(-3) - Int(-2) = -1
cout << "Int(-6) - Int(-7) = " << (Int(-6) - Int(-7)) << endl; // Int(-6) - Int(-7) = 1
```

// Logical Operations Test

```
cout << "Int(-6) == Int(-6): " << ((Int(-6) == Int(-6)) ? "T" : "F") << endl; // Int(-6) == Int(-6): T
cout << "Int(4) != Int(3): " << ((Int(4) != Int(3)) ? "T" : "F") << endl;    // Int(4) != Int(3): T
cout << "Int(-7) < Int(2): " << ((Int(-7) < Int(2)) ? "T" : "F") << endl;    // Int(-7) < Int(2): T
cout << "Int(-7) <= Int(2): " << ((Int(-7) <= Int(2)) ? "T" : "F") << endl;  // Int(-7) <= Int(2): T
cout << "Int(-5) > Int(-6): " << ((Int(-5) > Int(-6)) ? "T" : "F") << endl; // Int(-5) > Int(-6): T
cout << "Int(4) >= Int(4): " << ((Int(4) >= Int(4)) ? "T" : "F") << endl;    // Int(4) >= Int(4) = T
```

}



Polynomial UDT

Tutorial T08

Partha Pratim
Das

Tutorial Recap

Objective &
Outline

Int\mathbb{N} UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

Polynomial UDT



Design of Polynomial UDT

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- Polynomials $A(x)$ of x having degree $\text{degree}(A) = n$ and $n + 1$ coefficients $a_0, a_1, a_2, \dots, a_n$:

$$A(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n = \sum_{i=0}^n a_ix^i$$

- The representation of a polynomial UDT `Poly` would need
 - a vector to keep the coefficients, and
 - a simple member to the degree (for null polynomials without coefficients)
- The types of coefficient and variable should be appropriate so that they can be multiplied and added. For simplicity, let us assume that they have the same type:

```
template<typename T = int> // Type of Coefficients and value
class Poly {               // a polynomial of type T
    vector<T> coeff_;      // coefficients
    size_t deg_;          // deg_ = coeff_.size()-1
    // ... Rest of the class
}
```



Design of Polynomial UDT

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- A polynomial $A(x)$ of degrees n may be negated to generate polynomial $R(x)$ of degrees n by flipping the sign of every coefficient. That is:

$$R(x) = -A(x) = -\sum_{i=0}^n a_i x^i = \sum_{i=0}^n (-a_i) x^i$$

Hence,

$$r_i = -a_i, \quad 0 \leq i \leq n$$

- Two polynomials $A(x)$ and $B(x)$ of degrees n and m respectively may be added to generate polynomial $R(x)$ of degree $\max(n, m)$ by pairwise adding the coefficients of the same power. That is, for $n \geq m$

$$R(x) = A(x) + B(x) = \sum_{i=0}^n a_i x^i + \sum_{i=0}^m b_i x^i = \sum_{i=0}^m (a_i + b_i) x^i + \sum_{i=m+1}^n a_i x^i$$

Hence,

$$\begin{aligned} r_i &= a_i + b_i, \quad 0 \leq i \leq m \\ &= a_i, \quad m+1 \leq i \leq n \end{aligned}$$

Note: $A(x) - B(x) = A(x) + (-B(x))$



Design of Poly<T> Interface and Implementation

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
template<typename T = int>          // Type of Coefficients and Value
class Poly { public:
    Poly(vector<T>& c = vector<T>( 1 )) : coeff_(c), deg_(c.size() - 1) { }
    Poly(size_t n) : coeff_(vector<T>(n+1)), deg_(n) { } // null polynomial
    Poly(const Poly& p) : coeff_(p.coeff_), deg_(p.deg_) { }
    ~Poly() { } // No virtual destructor needed
    Poly& operator=(const Poly& p) { deg_ = p.deg_; coeff_ = p.coeff_; return *this; }

    Poly operator+() const { return *this; }
    Poly operator-() const { Poly r(deg_);
        for (unsigned int i = 0; i <= deg_; i++) r.coeff_[i] = -coeff_[i];
        return r;
    }
    Poly operator+(const Poly& p) const { Poly r(max(p.deg_, deg_)); // result
        vector<T> v;
        if (deg_ > p.deg_) { v = p.coeff_; r.coeff_ = coeff_; } // copy the longer (shorter) vector
        else { v = coeff_; r.coeff_ = p.coeff_; } // of coefficients to r.coeff_ (v)
        for (unsigned int i = 0; i <= min(p.deg_, deg_); i++) { // add the common coefficients
            r.coeff_[i] = t.coeff_[i] + v[i];
        }
        return r;
    }
    Poly operator-(const Poly& p) const { return *this + (-p); }
```



Design of Poly<T> Interface and Implementation

Tutorial T08

Partha Pratim
Das

Tutorial Recap

Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
Poly& operator+=(const Poly& p) { *this = *this + p; return *this; }
Poly& operator-=(const Poly&p) { *this = *this - p; return *this; }

friend ostream& operator<<(ostream& os, const Poly& p) { int j;
    for (j = p.deg_; j >= 0; --j)
        { if (static_cast<T>(0) != p.coeff_[j]) break; } // first non-zero coeff.
    if (0 > j)
        os << 0;
    else
        if (0 == j) os << p.coeff_[j];
        else os << p.coeff_[j] << "x^" << j;
    for (int i = j-1; i >= 0; --i) {
        if (static_cast<T>(0) != p.coeff_[i]) {
            if (0 != i)
                if (static_cast<T>(1) != p.coeff_[i])
                    os << " + " << p.coeff_[i] << "x^" << i;
                else
                    os << " + " << "x^" << i;
            else
                os << " + " << p.coeff_[i];
        }
    }
    os << ".";
    return os;
}
```

Programming in Modern C++



Design of Poly<T> Interface and Implementation

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

```
friend istream& operator >>(istream& is, Poly& p) {
    cout << "Enter degree of the polynomial ";
    is >> p.deg_;
    p.coeff_.resize(p.deg_ + 1);
    cout << "Enter all the coefficients like a0+a1*x+a2*x^2+....an*x^n" << endl;
    for (unsigned int i = 0; i <= p.deg_; i++)
        is >> p.coeff_[i];
    return is;
}

// Evaluates the polynomial - use Horner's Rule
T operator()(const T& x) {
    T val = 0;
    for (int i = deg_; i >= 0; i--)
        val = val * x + coeff_[i];
    return val;
}

private:
    vector<T>    coeff_;
    size_t      deg_;
    template<typename T> inline static T max(T a, T b) { return a > b ? a : b; }
    template<typename T> inline static T min(T a, T b) { return a < b ? a : b; }
};
```



Testing Poly<T>

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Design

Implementation

Test

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Tutorial Summary

```

#include <iostream>
using namespace std;
#include "fraction.h"
#include "polynomial.h"

void main() { vector<int> v = { 1, 2, 1 };
    Poly<int> p(v); cout << "p(x): " << p << " p(2) = " << p(2); // p(x): 1x^2 + 2x^1 + 1. p(2) = 9
    Poly<int> q(p); cout << "q(p): " << q << " q(2) = " << q(2); // q(p): 1x^2 + 2x^1 + 1. q(2) = 9
    Poly<int> s(vector<int>({ 0, 0, 1, 2, 1, 0, 2, 7, 0 }));
    cout << "s(x): " << s << " s(1) = " << s(1); // s(x): 7x^7 + 2x^6 + x^4 + 2x^3 + x^2. s(1) = 13
    Poly<int> r; cout << "r: " << r << " r(2) = " << r(2); // r: 1. r(2) = 1

    cin >> r; // 2 1 2 1
    cout << "r: " << r << " r(2) = " << r(2); // r: 1x^2 + 2x^1 + 1. r(2) = 9

    Poly<int> t(2); cout << "t(x): " << t << " t(2) = " << t(2); // t(x): 0. t(2) = 0

    r = p; cout << "r = p: " << r << " r(2) = " << r(2); // r = p: 1x^2 + 2x^1 + 1. r(2) = 9
    r = -p; cout << "r = -p: " << r << " r(2) = " << r(2); // r = -p: -1x^2 + -2x^1 + -1. r(2) = -9

    p = vector<int>({ 1, 5, 6 });
    cout << "p(x): " << p << " p(2) = " << p(2); // p(x): 6x^2 + 5x^1 + 1. p(2) = 35

    q = vector<int>({ 1, -2, 1 });
    cout << "q(x): " << q << " q(2) = " << q(2); // q(x): 1x^2 + -2x^1 + 1. q(2) = 1

```



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Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

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```

r = p + q; cout << "r = p + q: " << r << " r(2) = " << r(2); // r = p + q: 7x^2 + 3x^1 + 2. r(2) = 36
r = p - q; cout << "r = p - q: " << r << " r(2) = " << r(2); // r = p - q: 5x^2 + 7x^1. r(2) = 34
r = p; p += q; cout << "p += : " << p << " p(2) = " << p(2); // p += : 7x^2 + 3x^1 + 2. p(2) = 36
p = r; p -= q; cout << "p -= : " << p << " p(2) = " << p(2); // p -= : 5x^2 + 7x^1. p(2) = 34

```

```

vector<Fraction> vf = { Fraction(1, 2), Fraction(-3, 5), Fraction(2, 3) };
Poly<Fraction> pf1(vf); cout << "pf1(x): " << pf1 << " pf1(2) = " << pf1(2) << endl;
// pf1(x): 2/3x^2 + -3/5x^1 + 1/2. pf1(2) = 59/30

```

```

Poly<Fraction> pf2; cout << "pf2(x): " << pf2 << " pf2(2) = " << pf2(2) << endl;
// pf2(x): 1. pf2(2) = 1

```

```

cin >> pf2; // 1 2 3 1 2
cout << "pf2: " << pf2 << " pf2(2) = " << pf2(2) << endl;
// pf2(x): 1/2x^1 + 2/3. pf2(2) = 5/3

```

```

Poly<Fraction> pf3 = pf1 + pf2;
cout << "pf3(x): " << pf3 << " pf3(2) = " << pf3(2) << endl;
// pf3(x): 2/3x^2 + -1/10x^1 + 7/6. pf3(2) = 109/30

```

```

Poly<Fraction> pf4 = pf1 - pf2;
cout << "pf4(x): " << pf4 << " pf4(2) = " << pf4(2) << endl;
// pf4(x): 2/3x^2 + -11/10x^1 + -1/6. pf4(2) = 3/10

```

}



Practice UDTs

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Objective &
Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

Practice UDTs



Practice UDTs

Tutorial T08

Partha Pratim Das

Tutorial Recap

Objective & Outline

Int<N> UDT

Design

Operations

Class Design

Implementation

Test

Polynomial UDT

Design

Implementation

Test

Practice UDTs

Tutorial Summary

- **Fraction**
 - Change binary arithmetic and comparison operators to **friend** functions from methods
 - Parameterize **Fraction** with type **T = int**
 - Provide mixed mode support
- **Int<N>**
 - Implement **operator*()**
 - Implement **operator/()**
 - Implement **operator%()**
- **Poly<T>**
 - Test **Poly<double>**
 - Use member function template for **operator()()** with another type parameter **U** for **x**
 - Analyze the compatibility issues between types **T** and **U**
- **Mixed UDTs**
 - Test **Fraction<Int<N> >**
 - Test **Poly<Int<N> >**
 - Test **Poly<Fraction<Int<N> > >**



Tutorial Summary

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Implementation

Test

Polynomial UDT

Design

Implementation

Test

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Tutorial Summary

- Presented the design, implementation and test for `Int<N>` and `Poly<T>` types
- Showed how `Poly<int>` as well as `Poly<Fraction>` works
- Outlined several practice UDTs for homework