# Project Euler #228: Minkowski Sums



This problem is a programming version of Problem 228 from projecteuler.net

Let  $S_n$  be the regular n-sided polygon – or shape – whose vertices  $v_k$  ( $k=1,2,\ldots,n$ ) have coordinates:

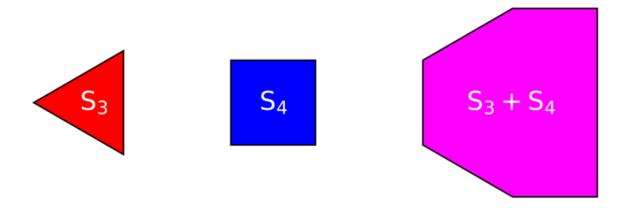
$$x_k = \cos\left(rac{(2k-1)\pi}{n}
ight)$$

$$y_k = \sin\left(rac{(2k-1)\pi}{n}
ight)$$

Each  $S_n$  is to be interpreted as a filled shape consisting of all points on the perimeter and in the interior.

The Minkowski sum, S+T, of two shapes S and T is the result of adding every point in S to every point in T, where point addition is performed coordinate-wise: (u, v) + (x, y) = (u + x, v + y).

For example, the sum of  $S_3$  and  $S_4$  is the six-sided shape shown in pink below:



Given two integers L and R, how many sides does the Minkowski sum  $\sum_{i=L}^R S_i$  have?

#### **Input Format**

The first line of each test file contains a single integer q which is the number of queries. Each of the next q lines contains two space-separated integers, L and R.

#### **Constraints**

- $1 < q < 10^4$
- 3 < L < R.
- The sum of R over all queries  $\leq 4 imes 10^{10}$  .

#### **Output Format**

Print the answer to each query in a new line.

# Sample Input 0

```
1
3 4
```

## Sample Output 0

6

## **Explanation 0**

The figure in the problem description shows  $S_3 + S_4$ . We can see that the number of sides of that shape is  $\bf 6$ .

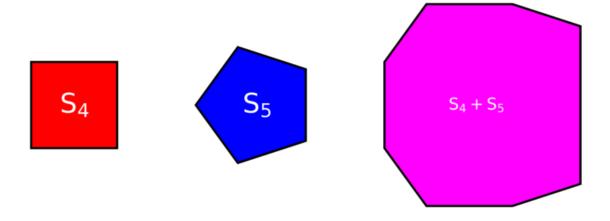
#### Sample Input 1

```
1
4 5
```

## Sample Output 1

8

#### **Explanation 1**



## Sample Input 2

```
1
3 5
```

## Sample Output 2

