

# Project Euler #231: The prime factorisation of binomial coefficients

This problem is a programming version of [Problem 231](#) from [projecteuler.net](#)

For a positive integer  $n = \prod_{i=1}^r p_i^{\alpha_i}$  where  $p_i$  are distinct primes, define  $\omega(n) = \sum_{i=1}^r \alpha_i$ .

For example,  $\omega(1) = 0$ ,  $\omega(9) = 2$  and  $\omega(12) = 3$ .

Let

$$f(N, M, k) = \sum_{\substack{d | \binom{N}{M} \\ \omega(d) = k}} d$$

That is,  $f(N, M, k)$  is the sum of all positive divisors  $d$  of the binomial coefficient  $\binom{N}{M}$  satisfying  $\omega(d) = k$ . Given  $N$ ,  $M$  and  $K$ , find  $f(N, M, k)$  modulo 1004535809, for all  $1 \leq k \leq K$ .

## Input Format

The only line of each test file contains three space-separated integers:  $N$ ,  $M$  and  $K$ .

## Constraints

- $1 \leq M \leq N \leq 10^9$ .
- $1 \leq K \leq 15$ .

## Output Format

Print exactly  $K$  lines, the  $i$ -th line must contain the answer when  $k = i$ .

## Sample Input 0

```
15 9 3
```

## Sample Output 0

```
36
466
2556
```

## Explanation 0

$$\binom{15}{9} = 5 \cdot 7 \cdot 11 \cdot 13 = 5005.$$

- $k = 1$ :  $5 + 7 + 11 + 13 = 36$ .
- $k = 2$ :  $35 + 55 + 65 + 77 + 91 + 143 = 466$ .
- $k = 3$ :  $385 + 455 + 715 + 1001 = 2556$ .

#### Sample Input 1

```
16 3 1
```

#### Sample Output 1

```
14
```

#### Explanation 1

$$\binom{16}{3} = 2^4 \cdot 5 \cdot 7 = 560.$$

- $k = 1$ : the answer is  $2 + 5 + 7 = 14$ .

#### Sample Input 2

```
22 6 4
```

#### Sample Output 2

```
57
1210
11730
50629
```

#### Explanation 2

$$\binom{22}{6} = 3 \cdot 7 \cdot 11 \cdot 17 \cdot 19 = 74613.$$

- $k = 1$ :  $3 + 7 + 11 + 17 + 19 = 57$ .
- $k = 2$ :  $21 + 33 + 51 + 57 + 77 + 119 + 133 + 187 + 209 + 323 = 1210$ .
- $k = 3$ :  $231 + 357 + 399 + 561 + 627 + 969 + 1309 + 1463 + 2261 + 3553 = 11730$ .
- $k = 4$ :  $3927 + 4389 + 6783 + 10659 + 24871 = 50629$ .