Project Euler #207: Integer partition equations



This problem is a programming version of Problem 207 from projecteuler.net

For some positive integers k, there exists an integer partition of the form $4^t = 2^t + k$, where 4^t , 2^t and k are all positive integers and t is a real number.

The first two such partitions are $\mathbf{4^1} = \mathbf{2^1} + \mathbf{2}$ and $\mathbf{4^{1.5849625...}} = \mathbf{2^{1.5849625...}} + \mathbf{6}$.

Partitions where t is also an integer are called perfect.

For any m>1 let P(m) be the proportion of such partitions that are perfect with $k\leq m$. Thus P(6)=1/2.

In the following table are listed some values of $\mathit{P}(\mathit{m})$

$$P(5) = 1/1$$

$$P(10) = 1/2$$

$$P(15) = 2/3$$

$$P(20) = 1/2$$

$$P(25) = 1/2$$

$$P(30) = 2/5$$

...

$$P(180) = 1/4$$

$$P(185) = 3/13$$

Find the smallest m for which P(m) < a/b.

Input Format

First line of each test file contains a single integer q that is the number of queries per test file. q lines follow, with two integers a and b separated by a single space on each.

Constraints

- $1 \le q \le 3 \times 10^5$
- $1 \le a < b \le 10^{18}$

Output Format

Print exactly q lines with an answer for the corresponding query on each.

Sample Input 0

2 2 3 9 20

Sample Output 0

6 30

Explanation 0

P(2)=P(3)=P(4)=P(5)=1/1>2/3 , but P(6)=1/2<2/3 , therefore, an answer for the first query is 6.

P(30) = 2/5, which is the first value less than 9/20 among all P(m) where $1 < m \le 30$.