## AI24BTECH11003 - Badde Vijaya Sreyas

1) For the natural numbers m, n, if  $(1 - y)^m (1 + y)^n = 1 + a_1 y + a_2 y^2 + \dots + a_{m+n} y^{m+n}$  and  $a_1 = a_2 = 10$ ,

3) Let  $r_1$  and  $r_2$  be the radii of the largest and smallest circles, respectively, which pass through the point (-4, 1) and having their centres on the circumference of the circle  $x^2 + y^2 + 2x + 4y - 4 = 0$ .

c) 100

c)  $\frac{-291}{76}$ d)  $\frac{151}{63}$ 

c) 5

d) 80

d) 7

then the value of (m + n) is equal to

If  $\frac{r_1}{r_2} = a + b\sqrt{2}$ , then a + b is equal to:

4) Consider the following three statements: (A): If 2 + 4 = 7, then 3 + 4 = 8(B): If 3 + 5 = 8, then the earth is flat

a) 88

a)  $\frac{-181}{69}$  b)  $\frac{220}{21}$ 

a) 3

b) 664

2) The value of  $\tan \left(2 \arctan \left(\frac{3}{5}\right) + \arcsin \left(\frac{5}{13}\right)\right)$  is equal to

b) 11

		(C): If (A) and (B) are true, then $5 + 6 = 17$ Then which of the following statements is correct?						
	<ul><li>a) (A) is false but (B) and (C) are true</li><li>b) (A) and (C) are true while (B) is false</li></ul>		c) (A) is true while (B) and (C) are false d) (A) and (B) are false while (C) is true					
	5) The lines $x = ay - 1 =$	The lines $x = ay - 1 = z - 2$ and $x = 3y - 2 = bz - 2$ , $(ab \ne 0)$ are coplanar, if:						
a) $b = 1, a \in R - \{0\}$ b) $a = 1, b \in R - \{0\}$		c) $a = 2, b = 2$ d) $a = 2, b = 3$						
6) If $[x]$ denotes the greatest integer less than or equal to $x$ , then the value of the integral $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} [x] - \sin x dx$ is equal to:								
	a) <i>-π</i>	b) π	c) –	d) 1				
7) If the real part of the complex number $(1 - \cos \theta + 2i \sin \theta)^{-1}$ is $\frac{1}{5}$ for $\theta \in (0, \pi)$ , then the value of the integral $\int_0^{\theta} \sin x  dx$ is equal to:								
	a) 1	b) 2	c) -1	d) 0				
	8) Let $f: R - \left\{\frac{\alpha}{6}\right\} \to R$ be defined by $f(x) = \frac{5x+3}{6x-\alpha}$ . Then the value of $\alpha$ for which $(f \circ f)(x) = x$ , for all $x \in R - \{\{\alpha\}6\}$ , is:							

d)  $\frac{7}{2}$ 

	one of C and A occurs is $(1 - k)$ and the probability of all A, B and C occur simultaneously is $k^2$ , where $0 < k < 1$ . Then the probability that at least one of A, B and C occur is:					
	a) greater than $\frac{1}{8}$ but less than $\frac{1}{4}$ b) greater than $\frac{1}{2}$		c) greater than $\frac{1}{4}$ but less than $\frac{1}{2}$ d) exactly equal to $\frac{1}{2}$			
11)	The sum of all the local minimum values of the twice differentiable function $f: R \to R$ defined by $f(x) = x^3 - 3x^2 - \frac{3f''(x)}{2} + f''(1)$ is:					
	a) -22	b) 5	c) -27	d) 0		
12)	Let in a right angled triangle, the smallest angle be $\theta$ . If a triangle formed by taking the reciprocal of it's sides is also a right angled triangle, then $\sin \theta$ is equal to:					
	a) $\frac{\sqrt{5}+1}{4}$	b) $\frac{\sqrt{5}-1}{2}$	c) $\frac{\sqrt{2}-1}{2}$	d) $\frac{\sqrt{5}-1}{4}$		
13)	Let $y = y(x)$ satisfies $y(\pi) = \pi + 2$ , then the	the equation $\frac{dy}{dx} -  A  =$	0, for all $x > 0$ , where	$A = \begin{pmatrix} y & \sin x & 1 \\ 0 & -1 & 1 \\ 2 & 0 & \frac{1}{x} \end{pmatrix}. \text{ If }$		
			2- 1			
	a) $\frac{\pi}{2} + \frac{4}{\pi}$	b) $\frac{\pi}{2} - \frac{1}{\pi}$	c) $\frac{3\pi}{2} - \frac{1}{\pi}$	d) $\frac{\pi}{2} - \frac{\pi}{\pi}$		
14)	4) Consider the line L given by the equation $\frac{x-3}{2} = \frac{y-1}{1} = \frac{z-2}{1}$ . Let Q be the mirror the image of the point $(2, 3, -1)$ with respect to L. Let a plane P be such that it passes through Q, and the line I is perpendicular to P. Then which of the following points is on the plane P?					
	a) (-1,1,2) b) (1,1,1)		c) (1, 1, 2) d) (1, 2, 2)			
15)	5) If the mean and variance of six observations 7, 10, 11, 15, $a$ , $b$ are 10 and $\frac{20}{3}$ , respectively, then the value of $ a - b $ is equal to:					
	a) 9	b) 11	c) 7	d) 1		

c) 8

d) 6

c)  $\frac{1}{2}$ 

10) Let A, B and C be three events such that the probability that exactly one of A and B occurs is (1-k), the probability that exactly one of B and C occurs is (1-2k), the probability that exactly

a) No such  $\alpha$  exists

9) If  $f: R \to R$  is given by f(x) = x + 1, then the value of  $\lim_{\substack{x \to \infty \\ \text{is:}}} \frac{1}{n} \left[ f(0) + f\left(\frac{5}{n}\right) + f\left(\frac{0}{n}\right) + \dots + f\left(\frac{5(n-1)}{n}\right) \right]$ 

b)  $\frac{5}{2}$ 

b) 5

a)  $\frac{3}{2}$