

# 2008 Physics

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AI24BTECH11003 - Badde Vijaya Sreyas

- 18) An  $O^{16}$  nucleus is spherical and has a charge radius  $R$  and a volume  $V \equiv \frac{4}{3}\pi R^3$ . According to the empirical observations of the charge radii, the volume of the  ${}_{54}Xe^{128}$  nucleus, assumed to be spherical, is
- a)  $8V$                       b)  $2V$                       c)  $6.75V$                       d)  $1.89V$
- 19) A common emitter transistor amplifier circuit is operated under a fixed bias. In this circuit, the operating point
- a) remains fixed with an increase in temperature.  
b) moves towards cut-off region with an increase in temperature.  
c) moves towards saturation region with a decrease in temperature.  
d) moves towards saturation region with an increase in temperature
- 20) Under normal operating conditions, the gate terminal of an  $n$ -channel junction field effect transistor (JFET) and an  $n$ -channel metal oxide semiconductor field effect transistor (MOSFET) are
- a) both biased with positive potentials  
b) both biased with negative potentials  
c) biased with positive and negative potentials, respectively  
d) biased with negative and positive potentials, respectively
- 21) The eigenvalues of the matrix  $\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$
- a)  $\frac{1}{2}(\sqrt{3} \pm i)$  when  $\theta = 45^\circ$                       c)  $\pm 1$  since the matrix is unitary  
b)  $\frac{1}{2}(\sqrt{3} \pm i)$  when  $\theta = 30^\circ$                       d)  $\frac{1}{\sqrt{2}}(1 \pm i)$  when  $\theta = 30^\circ$
- 22) If the Fourier transform  $F[\delta(x - \alpha)] = \exp(-i2\pi\nu\alpha)$ , then  $F^{-1}(\cos 2\pi\nu\alpha)$  will correspond to
- a)  $\delta(x - \alpha) - \delta(x + \alpha)$                       c)  $\frac{1}{2}[\delta(x - \alpha) + i\delta(x + \alpha)]$   
b) a constant                      d)  $\frac{1}{2}[\delta(x - \alpha) + \delta(x + \alpha)]$
- 23) If  $I = \oint_C dz \ln(z)$ , where  $C$  is the unit circle taken anticlockwise and  $\ln(z)$  is the principal branch of the Logarithmic function, which of the following is correct?
- a)  $I = 0$  by residue theorem                      c)  $I \neq 0$   
b)  $I$  is not defined since  $\ln(z)$  has a branch cut                      d)  $\oint_C dz \ln(z^2) = 2I$
- 24) The value of  $\int_{-i}^i \pi(z + 1) dz$  is

a) 0

b)  $2\pi i$

c)  $-2\pi i$

d)  $(-1 + 2i)\pi$

25) Consider the Bessel equation  $\nu = 0$ ,  $\frac{d^2 y}{dz^2} + \frac{1}{z} \frac{dy}{dz} + y = 0$ . Which one of the following statements is correct?

a) Equation has regular singular points at  $z = 0$  and  $z = \infty$

b) Equation has 2 linearly independent solutions that are entire

c) Equation has an entire solution and a second linearly independent solution singular at  $z = 0$ .

d) Limit  $z \rightarrow \infty$ , taken along  $x$  axis, exists for both the linearly independent solutions.

26) Under a certain rotation of coordinate axes, a rank-1 tensor  $v_a$  ( $a = 1, 2, 3$ ) transforms according to the orthogonal transformation defined by the relations  $v'_1 = \frac{1}{\sqrt{2}}(v_1 + v_2)$ ;  $v'_2 = \frac{1}{\sqrt{2}}(-v_1 + v_2)$ ;  $v'_3 = v_3$ . Under the same rotation, a rank-2 tensor  $T_{a,b}$  would transform such that

a)  $T'_{1,1} = T_{1,1}T_{1,2}$

c)  $T'_{1,1} = T_{1,1} + 2T_{2,2} - T_{2,1}$

b)  $T'_{1,3} = T_{1,3}$

d)  $T'_{1,1} = \frac{1}{2}(T_{1,1} + T_{2,2} + T_{1,2} + T_{2,1})$

27) The Lagrangian of a system is given by  $L = \frac{1}{2}\dot{q}^2 + q\dot{q} - \frac{1}{2}q^2$ . It describes the motion of

a) a harmonic oscillator

c) an anharmonic oscillator

b) a damped harmonic oscillator

d) a system with unbounded motion

28) The moment of inertia tensor of a rigid body is given by  $I = \begin{pmatrix} 8 & 0 & -4 \\ 0 & 4 & 0 \\ -4 & 0 & 8 \end{pmatrix}$ . The magnitude of the moment of inertia about an axis  $\hat{n} = \left(\frac{1}{2}, \frac{\sqrt{3}}{2}, 0\right)$  is

a) 6

b) 5

c) 2

d)  $\frac{8}{3}$

29) A hoop of radius  $R$  is pivoted at a point on the circumference. The period of small oscillations in the plane of the hoop is

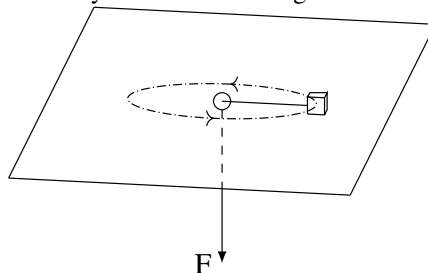
a)  $2\pi\sqrt{\frac{2R}{g}}$

b)  $2\pi\sqrt{\frac{R}{4g}}$

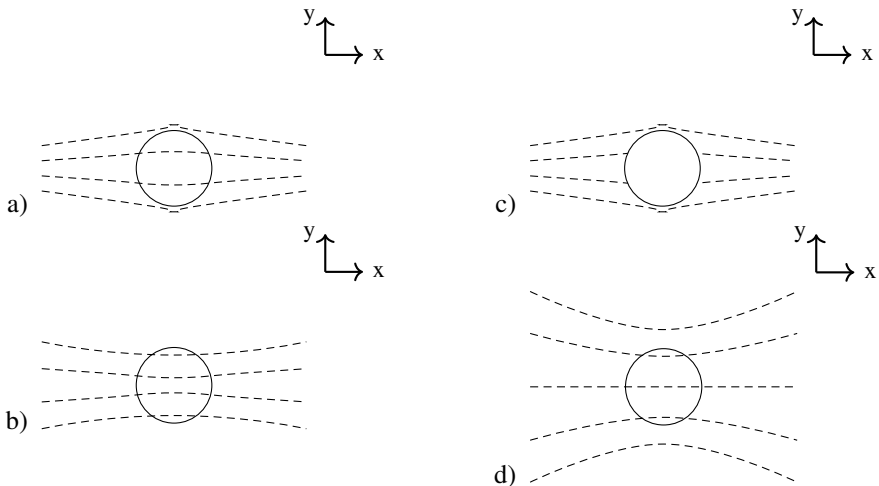
c)  $2\pi\sqrt{\frac{R}{g}}$

d)  $2\pi\sqrt{\frac{9R}{7g}}$

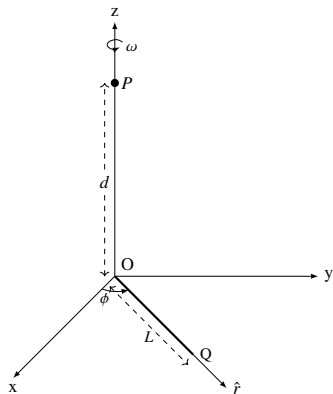
30) A mass  $m$  is constrained to move on a horizontal frictionless surface. It is set in circular motion with radius  $r_0$  and angular speed  $\omega_0$  by an applied force  $\vec{F}$  communicated through an inextensible thread that passes through a hole on the surface as shown in the figure. This force is suddenly doubled. The magnitude of radial velocity of the mass



- a) increases till the mass falls into the hole  
 b) decreases till the mass falls into the hole  
 c) remains constant  
 d) becomes zero at a radius  $r_1$  where  $0 < r_1 < r_0$
- 31) For a simple harmonic oscillator the Lagrangian is given by  $L = \frac{1}{2}\dot{q}^2 - \frac{1}{2}q^2$ . If  $A(p, q) = \frac{p+iq}{\sqrt{2}}$  and  $H(p, q)$  is the Hamiltonian of the system, the Poisson bracket  $\{A(p, q), H(p, q)\}$  is given by
- a)  $iA(p, q)$                       b)  $A^*(p, q)$                       c)  $-iA^*(p, q)$                       d)  $-iA(p, q)$
- 32) A plane electromagnetic wave is given by  $E_0(\hat{x} + e^{i\delta}\hat{y})\exp\{i(kz - \omega t)\}$ . At a given location, the number of times  $\hat{E}$  vanishes in one second is
- a) An integer near  $\frac{\omega}{\pi}$  when  $\delta = n\pi$  and zero when  $\delta \neq n\pi$ ,  $n$  is integer  
 b) An integer near  $\frac{\omega}{2\pi}$  and is independent of  $\delta$   
 c) An integer near  $\frac{\omega}{2\pi}$  when  $\delta = n\pi$  and zero when  $\delta \neq n\pi$ ,  $n$  is integer  
 d) An integer near  $\frac{\omega}{2\pi}$  and is independent of  $\delta$
- 33) A dielectric sphere is placed in a uniform electrical field directed along the positive  $y$ -axis. Which of the following represents correct equipotential surfaces?



- 34) A rod of length  $L$  with uniform charge density  $\lambda$  per unit length is in the  $xy$ -plane and rotating about  $z$ -axis passing through one of its edge with an angular velocity  $\vec{\omega}$  as shown in the figure below.  $(\hat{r}, \hat{\phi}, \hat{z})$  refer to the unit vectors at  $Q$ ,  $\vec{A}$  is the vector potential at a distance  $d$  from the origin  $O$  along  $z$ -axis for  $d \gg L$  and  $\vec{J}$  is the current density due to the motion of the rod. Which of the following statements is correct?



a)  $\vec{J}$  along  $\hat{r}$ ;  $\vec{A}$  along  $\hat{z}$ ;  $|\vec{A}| \propto \frac{1}{d}$   
 b)  $\vec{J}$  along  $\hat{\phi}$ ;  $\vec{A}$  along  $\hat{\phi}$ ;  $|\vec{A}| \propto \frac{1}{d^2}$

c)  $\vec{J}$  along  $\hat{r}$ ;  $\vec{A}$  along  $\hat{z}$ ;  $|\vec{A}| \propto \frac{1}{d^2}$   
 d)  $\vec{J}$  along  $\hat{\phi}$ ;  $\vec{A}$  along  $\hat{\phi}$ ;  $|\vec{A}| \propto \frac{1}{d}$