# Assignment - 1

# AI24BTECH11003 - B. Vijaya Sreyas

### 17.Indefinite Integrals - Section B

- 5. The value of  $\sqrt{2} \int \frac{\sin x dx}{\sin(x \frac{\pi}{4})}$ (2008)
  - $(a)x + log|\cos(x \frac{\pi}{4})| + c$
  - (b) $x log |\sin(x \frac{\pi}{4})| + c$
  - $(c)x + log |\sin(x \frac{\pi}{4})| + c$
  - $(d)x log|\cos\left(x \frac{\pi}{4}\right)| + c$
- 6. If the  $\int \frac{5 \tan x}{\tan x 2} dx = x + a \ln \mod \sin x 2 \cos x + k$ , then a is equal to
  - (a) -1
- (b) 2
- (c) 1
- (d) 2
- 7. If  $\int f(x) dx = \psi(x)$ , then  $\int x^5 f(x^3) dx$  is equal to: (JEE M 2013)
  - (a)  $\frac{1}{3}[x^3\psi(x^3) \int x^2\psi(x^3)dx] + C$
  - (b)  $\frac{1}{2}x^3\psi(x^3) 3\int x^3\psi(x^3)dx + C$
  - (c)  $\frac{1}{2}x^3\psi(x^3) \int x^2\psi(x^3)dx + C$
  - (d)  $\frac{1}{3}[x^3\psi(x^3) \int x^3\psi(x^3)dx] + C$
- 8. The integral  $\int (1+x-\frac{1}{x})e^{x+\frac{1}{x}}dx$  is equal to (JEE M 2014)
  - (a)  $(x+1)e^{x+\frac{1}{x}} + c$  (b)  $-xe^{x+\frac{1}{x}} + c$  (c)  $(x-1)e^{x+\frac{1}{x}} + c$  (d)  $xe^{x+\frac{1}{x}} + c$
- 9. The integral  $\int \frac{dx}{x^2(x^4+1)^{3/4}}$  equals: (JEE M 2015)
  - (a)  $-\left(x^4+1\right)^{\frac{1}{4}}+c$  (c)  $\left(\frac{x^4+1}{x^4}\right)^{\frac{1}{4}}+c$  (b)  $-\left(\frac{x^4+1}{x^4}\right)+c$  (d)  $\left(x^4+1\right)^{\frac{1}{4}}+c$
- 10. The integral  $\int \frac{2x^{12}+5x^9}{(x^5+x^3+1)^3} dx$  is equal to (JEE M 2016)
  - (a)  $\frac{x^5}{2(x^5-x^3+1)^2} + C$  (b)  $\frac{-x^{10}}{2(x^5+x^3+1)^2} + C$  (c)  $\frac{-x^5}{(x^5+x^3+1)^2} + C$  (d)  $\frac{x^{10}}{2(x^5+x^3+1)} + C$

where C is an arbitrary constant

- 11. Let  $I_n = \int \tan^x dx$ , (n > 1).  $I_4 + I_6 = a \tan^5 x + bx^5 + C$ , where C is constant of integration, then the ordered pair (JEE M 2017) (a,b) is equal to:

- (a)  $\left(-\frac{1}{5},0\right)$  (b)  $\left(-\frac{1}{5},1\right)$  (c)  $\left(\frac{1}{5},0\right)$  (d)  $\left(\frac{1}{5},-1\right)$
- 12. The integral  $\int \frac{\sin^2 x \cos^2 x}{\left(\sin^5 x + \cos^3 x \sin^2 x + \sin^3 x \cos^2 x + \cos^5 x\right)^2} dx$  is equal (JEE M 2018)

- (a)  $\frac{-1}{3(1+\tan^3 x)} + C$  (b)  $\frac{1}{1+\cos^3 x} + C$  (c)  $\frac{-1}{1+\cot^3 x} + C$  (d)  $\frac{1}{3(1+\tan^3 x)} + C$
- 13. For  $x^2 \neq n\pi + 1$ ,  $n \in \mathbb{N}$  (the set of natural numbers), the integral  $\int x \sqrt{\frac{2\sin(x^2-1)-\sin 2(x^2-1)}{2\sin(x^2-1)+\sin 2(x^2-1)}} dx$  is equal to: EE M 2019 - 9 Jan(M))

  - (a)  $\log_e |\frac{1}{2} \sec^2 (x^2 1)| + c$  (c)  $\frac{1}{2} \log_e |\sec^2 (\frac{x^2 1}{2})| + c$  (b)  $\frac{1}{2} \log_e |\sec^2 (\frac{x^2 1}{2})| + c$  (d)  $\log_2 |\sec (\frac{x^2 1}{2})| + c$

(where c is a constant of integration)

- 14. The integral  $\int \sec^{2/3} x \csc^{4/3} x dx$  is equal to (JEE M 2019 - 9 April (M))
- (c)  $-3\cot^{-1/3}x + C$ (d)  $3\tan^{-1/3} + C$
- (a)  $-3\tan^{-1/3}x + C$ (b)  $-\frac{3}{4}\tan^{-4/3}x + C$

(Here, C is a constant of integration)

## 18. Definite Integrals - Section B

- 31. The area of the region bounded by the parabola  $(y-2)^2 = x-1$ , the tangent of the parabola at the point (2,3) and the x-axis is:
  - (a) 6
- (b) 9
- (c) 12
- (d) 3
- 32.  $\int_0^{\pi} [\cot x] dx$ , where [.] denotes the greatest integer function, is equal to (2009)
  - (a) 1
- (b) -1
- (c)  $-\frac{\pi}{2}$
- (d)  $\frac{\pi}{2}$
- 33. The area bounded between the curves  $y = \cos x$  and  $y = \sin x$  between the ordinates x = 0 and  $x = \frac{3\pi}{2}$  is (2010)
  - (a)  $4\sqrt{2} + 2$ (b)  $4\sqrt{2} 1$

- (c)  $4\sqrt{2} + 1$ (d)  $4\sqrt{2} 2$
- 34. Let p(x) be a function defined on **R** such that p'(x) =p'(1-x), for all  $x \in [0,1]$ , p(0) = 1 and p(1) = 41. Then  $\int_0^1 p(x) dx$  equals (2010)
  - (a) 21
- (b) 41
- (c) 42
- (d)  $\sqrt{41}$

(2011)

35. The value of  $\int_0^1 \frac{8log(1+x)}{1+x^2} dx$  is

(c)  $\pi - \frac{4}{3}$ (d)  $\pi - \frac{8}{3}$ 

(a)  $\pi - \frac{4\sqrt{2}}{3}$ (b)  $\frac{\pi}{2} - \frac{2\sqrt{2}}{3}$ 

36. The area of the region enclosed by the $e, y = \frac{1}{x}$ and the positive x axis is	the curves $y = x, x = (2011)$
(a) 1 square unit (b) $\frac{3}{2}$ square units (c) $\frac{5}{2}$ square (d) $\frac{1}{2}$ square	uare units uare unit
37. The area between the parabolas: $x^2 = \frac{y}{4}$ and $x^2 = 9y$ and the straight line $y = 2$ is: (2012)	
(a) $20\sqrt{2}$ (b) $\frac{10\sqrt{2}}{3}$ (c) $\frac{20\sqrt{2}}{3}$	(d) $10\sqrt{2}$
38. If $g(x) = \int_0^x \cos 4t dt$ , then $g(x + \pi)$ equals (2012)	
(a) $\frac{g(x)}{g(\pi)}$ (c) $g(x)$ (b) $g(x) + g(\pi)$ (d) $g(x)$ .	<u> </u>
39. <b>Statement-1</b> : The value of the integer equal to $\pi/6$ <b>Statement-2</b> : $\int_a^b f(x) dx = \int_a^b f(a+b) dx$	
<ul> <li>(a) Statement-1 is true; Statement-2 i is a correct explanation for Statemen (b) Statement-1 is true; Statement-2 i is not a correct explanation fo Statem (c) Statement-1 is true; Statement-2 (d) Statement-1 is false; Statement-2</li> <li>40. The area (in square units) bounded √x, 2y-x+3 = 0, x-axis, and lying i is:</li> </ul>	s true; Statement-2 t-1 s true; Statement-2 nent-1 is false is true by the curves $y =$
(a) 9 (b) 36 (c) 18	(d) $\frac{27}{4}$
41. The integral $\int_0^{\pi} \sqrt{1 + 4 \sin^2 \frac{x}{2} - 4 \sin^2 \frac{x}{2}}$	$\frac{x}{2}dx$ equals: (JEE M 2014)
(a) $4\sqrt{3} - 4$ (c) $\pi - 4$ (b) $4\sqrt{3} - 4 - \frac{\pi}{3}$ (d) $\frac{2\pi}{3}$	$4 - 4\sqrt{3}$
42. The area of the region described by <i>A</i> 1 and $y^2 \le 1 - x$ } is:	$= \{(x, y) : x^2 + y^2 \le (\text{JEE M 2014})$
(a) $\frac{\pi}{2} - \frac{2}{3}$ (b) $\frac{\pi}{2} + \frac{2}{3}$ (c) $\frac{\pi}{2} + \frac{2}{3}$	$\frac{4}{3}$ (d) $\frac{\pi}{2} - \frac{4}{3}$
43. The area (in sq. units) of the region do $y^2 \le 2x$ and $y \ge 4x - 1$ } is	escribed by {( <i>x</i> , <i>y</i> ) : (JEE M 2015)
. 15	
(a) $\frac{15}{64}$ (b) $\frac{9}{32}$ (c) $\frac{7}{32}$	(d) $\frac{5}{64}$
(a) $\frac{63}{64}$ (b) $\frac{2}{32}$ (c) $\frac{2}{32}$ 44. The integral $\int_{2}^{4} \frac{\log x^{2}}{\log x^{2} + \log(36 - 12x + x^{2})} dx$ is	04
52 52	is equal to:

(c) log 2(d) π log2

(a)  $\frac{\pi}{8} \log 2$  (b)  $\frac{\pi}{2} \log 2$