

From lecture slide.

$$F_{in} \partial L = k_1 \phi_1 \partial \theta_2 + k_2 \phi_2 (\partial \theta_2 - \partial \theta_3) + k_3 \phi_3 \partial \theta_3$$

$$F_{in} = k_1 (\theta_2 - \theta_{20}) \frac{\partial \theta_2}{\partial L_1} + k_2 ((\theta_2 - \theta_{20}) - (\theta_3 - \theta_{30})) \left(\frac{\partial \theta_2}{\partial L_1} - \frac{\partial \theta_3}{\partial L_1} \right) + k_3 (\theta_3 - \theta_{30}) \frac{\partial \theta_3}{\partial L_1}$$

Unknowns.

$$\frac{\partial \theta_2}{\partial L_1} = \frac{\omega_2}{v_1} \quad \frac{\partial \theta_3}{\partial L_1} = \frac{\omega_3}{v_1} \quad \theta_2 = \theta_3.$$

Displacement analysis

$$L_2 \cos \theta_2 + L_3 \cos \theta_3 = L_1 \Rightarrow \theta_3 = \sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right)$$

$$L_2 \sin \theta_2 + L_3 \sin \theta_3 = 0.$$

Velocity analysis

$$-L_2 \omega_2 \sin \theta_2 - L_3 \omega_3 \sin \theta_3 = -v_1$$

$$L_2 \omega_2 \cos \theta_2 + L_3 \omega_3 \cos \theta_3 = 0.$$

$$\omega_2 = -\frac{L_3 \cos \theta_3}{L_2 \cos \theta_2} \omega_3.$$

$$\Rightarrow \left(\frac{L_3 \cos \theta_3 \sin \theta_2}{\cos \theta_2} - \frac{L_3 \cos \theta_2 \sin \theta_3}{\cos \theta_2} \right) \omega_3 = v_1$$

$$\frac{L_3 \sin(\theta_3 - \theta_2)}{\cos \theta_2} \omega_3 = v_1$$

$$\frac{\omega_3}{v_1} = \frac{-\cos \theta_2}{L_3 \sin(\theta_3 - \theta_2)}$$

$$\theta_3 = \sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right)$$

$$\frac{\omega_3}{v_1} = -\frac{\cos \theta_2}{L_3 \sin \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_2 \right)}$$

$$\omega_3 = -\frac{L_2 \cos \theta_2}{L_3 \cos \theta_3} \omega_2$$

$$-L_2 \omega_2 \sin \theta_2 + \frac{L_2 \cos \theta_2 \sin \theta_3}{\cos \theta_3} \omega_2 = -v_1$$

$$\frac{L_2 \sin(\theta_3 - \theta_2)}{\cos \theta_3} \omega_2 = v_1$$

$$\frac{\omega_2}{v_1} = \frac{-\cos \theta_3}{L_2 \sin(\theta_3 - \theta_2)}$$

$$\theta_3 = \sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right)$$

$$\frac{\omega_2}{v_1} = -\frac{\cos \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) \right)}{L_2 \sin \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_2 \right)}$$

$$F_{in} = k_1 (\theta_2 - \theta_{20}) \frac{-\cos \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) \right)}{L_2 \sin \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_2 \right)} + k_2 ((\theta_2 - \theta_{20}) - (\theta_3 = \sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_{30})) \left(-\frac{\cos \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) \right)}{L_2 \sin \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_2 \right)} + \frac{\cos \theta_2}{L_3 \sin \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_2 \right)} \right) + k_3 (\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_{30}) \frac{-\cos \theta_2}{L_3 \sin \left(\sin^{-1} \left(\frac{L_2}{L_3} \sin \theta_2 \right) - \theta_2 \right)}$$

$$\theta_{20} = \frac{1}{10} \pi \quad \theta_{30} = 2\pi - \frac{1}{10} \pi.$$

Initial conditions. $\theta_{20}, \theta_{30} \neq 0$
Singularity.

$$k_1 = k_2 = k_3 = \frac{EI}{l} = \frac{E}{l} \cdot \frac{wt^3}{12}$$

Given values.

$$l = 0.05m \quad w = 0.05m \quad t = 0.005 \quad E = 8GPa. \approx 8 \cdot 10^9 Pa.$$

$$L_2 = 0.2m \quad L_3 = 0.25m$$

