

White Dwarfs as Dark Matter Detectors

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White dwarfs can serve as detectors for ultra-heavy dark matter states which interact to trigger type Ia supernovae. This was originally proposed in [1] and used to place bounds on primordial black holes. In this paper we extend the capability of white dwarf detectors to candidates with non-gravitational couplings, focusing on dark matter transits and collisions within the white dwarf. In particular, we provide a detailed analysis of the explosiveness for any heating mechanism in the white dwarf which releases high-energy standard model particles. We apply this mechanism to constrain Q-ball dark matter and model of dark nuclei in regions of parameter space fundamentally inaccessible to terrestrial-based experiments.

PACS numbers:

I. INTRODUCTION

The detection of ultra-heavy dark matter (DM) is an open problem which will ultimately require a confluence of astrophysical probes. For instance, DM masses above $\sim 10^{22}$ GeV will register fewer than 1 event per year in a typical terrestrial detector of size $\sim (100 \text{ m})^2$. Furthermore, the lack of conclusive signatures on a variety of experimental fronts has led many to seriously consider DM candidates far above the weak scale and their potential signatures [cite people](#). One possibility proposed by [1] is that ultra-heavy DM can trigger supernovae in sub-Chandrasekhar white dwarf (WD) stars by inducing runaway fusion. In this regard, white dwarfs can serve as detectors for ultra-heavy DM states.

White dwarfs are particularly suited to this task, as they are more susceptible to runaway fusion than are main-sequence stars. Runaway fusion requires that two criteria be met: a region within the star must be hot enough to support exothermic fusion reactions, and the rate at which energy is released by these reactions must dominate any cooling mechanisms that drain energy from the fusing region. The stellar medium of a WD has fewer cooling mechanisms available than does a non-degenerate star - WD cooling relies on thermal diffusion whereas main-sequence stars can also cool via thermal expansion. This is suppressed in a WD since its pressure is determined by electron degeneracy and is thus independent of temperature. The remaining primary cooling mechanism, diffusion, becomes less important over longer length scales and can be overcome by sufficiently heating a large enough region of the WD.

The necessary trigger for runaway fusion was initially computed in [2] and subsequently implemented in [1] to constrain primordial black holes, which can ignite WD stars via gravitational dynamical friction. In addition, the authors of [1] identify several other heating mechanisms involving DM which may be constrained in a similar manner. [Some of these have been explored in follow-up works...citations, citations.](#) In this work, we extend their analysis to DM candidates with generic non-gravitational couplings, focusing on DM transits through

the WD and DM-DM collisions within the WD which release energy in the form of standard model (SM) particles. More generally, we provide a detailed analysis of the explosive power and resulting constraints on any DM with interactions of this sort.

Concrete examples of DM candidates with interactions of this type include baryonic Q-balls found in supersymmetric extensions of the SM and [dark nuclei with high-order couplings to the SM](#). We are able to constrain these models in regions of parameter space fundamentally inaccessible to terrestrial experiments. However, it is important to note that any such DM constraints are by nature complimentary to terrestrial ones - it is more massive DM that is likely to trigger supernovae, and also more massive DM that have sufficiently low flux on Earth. What allows the WD to be effective in this regime is its enhanced surface area $\sim (4000 \text{ km})^2$ and exceptionally long lifetime $\sim \text{Gyr}$. In this sense, the WD is a large “space-time volume” detector. [We also have a “flux is too low” limit...should we include here?](#)

[Other ignition sources exist \(i.e., detector backgrounds\). How does this limit our constraints? Discuss the specific tests we apply \(WD lifetime, SN rate\) to derive our constraints. Possible long term addition: improve constraints by using non-type IA sn rate instead of total rate. Should talk with SN people first.](#)

[Add the traditional table-of-contents paragraph](#)

II. REVIEW: WHITE DWARF RUNAWAY FUSION

In a WD, the *fusion temperature* T_B is a constant set by the energy required for ions to overcome their mutual Coulomb barriers $T_B \sim \text{MeV}$. WD cooling is set by the thermal diffusivity of photons and degenerate electrons. The two species dominate the cooling at different stellar densities, as determined precisely in [2]. Note that for a heated region of size R , this cooling rate scales as R^{-2} while the fusion rate scales as R^{-3} . Thus there is a critical *trigger size* λ_T below which diffusive cooling dominates the thermal evolution of a temperature

peak, and above which the liberated fusion energy dominates [2]. Therefore, a region with temperature greater than T_B and size greater than λ_T in a given WD will launch a runaway fusion chain-reaction and result in a type Ia supernova. The numerical value of λ_T is highly sensitive to the WD density and has been analytically scaled for varying WD masses in [1]. These results are reproduced in Figure 1. As in [1], we restrict our attention to carbon-oxygen WDs in the upper mass range $0.7 - 1.4 M_\odot$ which correspond to a number density of nuclei $n \sim 10^{29} - 10^{32} \text{ cm}^{-3}$. Over this range, the trigger size is approximately $\lambda_T \sim 10^{-5} - 10^{-2} \text{ cm}$.

A general energy deposition event in the WD can be roughly characterized by two parameters: a temperature T and heating length L . This energy deposit will eventually take the form of a local peak in the WD temperature profile. We define T to be the characteristic temperature and L the characteristic length scale of this local peak as it initially appears. L is determined by the efficiency with which a given energy deposition mechanism interacts with the stellar medium. To demonstrate the significance of L , suppose that kinetic energy were transferred directly to neighboring ions via short-range elastic scatterers. These ions would thermalize over their collisional time scale resulting in a heating length L of order the ion mean free path. In fact, this is the minimal L possible for any process which couples to WD constituents (ions or electrons). In the other extreme, suppose that a process produces a large number of electrons with energy just above the Fermi energy. These electrons have Pauli-suppressed interactions with the medium and will travel a long distance before their energy is scattered and thermalized, resulting in a large L - possibly of order the stellar radius.

We find that a heating event will destroy a given WD as long as the energy density *and* energy deposited are sufficiently large:

$$T \gtrsim T_B, \quad L \gtrsim \lambda_T. \quad (1)$$

Note that this condition determines if a region of size L and temperature T *immediately* initiates runaway fusion. Instead, it is more useful to determine whether a given energy deposit will *eventually* initiate runaway fusion. In particular, a heating event that results in $T \gg T_B$ and $L < \lambda_T$ is perhaps initially dominated by diffusive cooling but can potentially evolve into an “explosive” temperature profile capable of igniting the star. When diffusion dominates, the thermal evolution will approximately be given by the dilution of the fixed total energy of the initial region over the final volume. Taking this into account, we can express the explosion condition (1) in terms of an excess energy within the temperature peak (rather than the temperature itself):

$$E \gtrsim n T_B \max\{L, \lambda_T\}^3. \quad (2)$$

In fact, there is an absolute minimum explosion energy given by

$$E_{\text{boom}} \sim n T_B \lambda_T^3 \sim 10^{14} - 10^{22} \text{ GeV}, \quad (3)$$

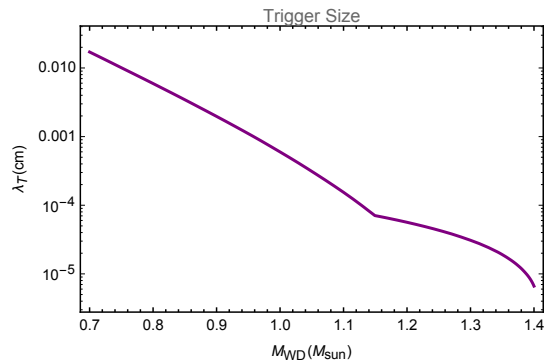


FIG. 1: Approximate trigger sizes for carbon-oxygen white dwarfs, based on numerical results in [2] and analytically scaled in [1]. [extend to 0.4 solar mass](#)

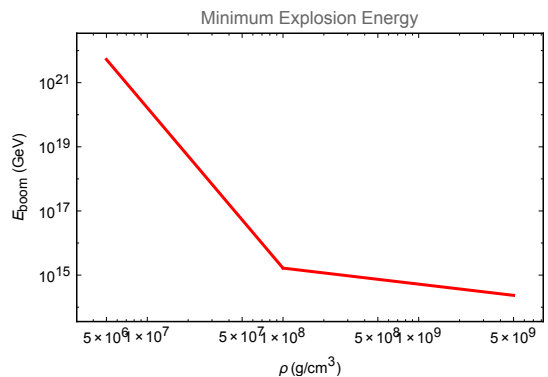


FIG. 2: Minimum energy required to trigger explosion in a WD of density ρ .

where λ_T varies over a range of WD densities as shown in Figure 1. E_{boom} is plotted for different WD densities in Figure 2. However, this energy is sufficient only if it thermalizes within the trigger size. If an energy is deposited on a length scale larger than λ_T , the explosion energy required is given by (2) and may be parametrically larger. Since we are concerned with processes that have a fixed deliverable energy (the energy of the incoming DM), the most explosive processes will be those that result in the most localized heating. As a result, understanding the heating length L for various processes is critical to assessing their explosive potential. This is done in Section IV.

III. DARK MATTER EXPLOSIVENESS

In this section, we parameterize the explosive power of a generic (ultra-heavy) DM interaction in the WD which releases n_i SM particles of species i each with kinetic energy ϵ .



FIG. 3: General interaction between ultra-heavy DM and WD constituents, producing n_i additional particles of species i .

A. DM Transit

Consider a DM transit through the WD, interacting with stellar constituents in a general manner as shown in Figure III A. The cross section for this interaction is denoted as $\sigma_{i,\epsilon}$. Setting the total energy released during a transit of length $\max\{\lambda_T, L\}$ to be greater than the explosive energy (2), we find a lower bound on the interaction cross section sufficient to trigger runaway fusion:

$$n_i \sigma_{\epsilon,i} \gtrsim \begin{cases} \lambda_T^2 \left(\frac{T_B}{\epsilon} \right) & L < \lambda_T \\ \lambda_T^2 \left(\frac{L}{\lambda_T} \right)^2 \left(\frac{T_B}{\epsilon} \right) & L > \lambda_T \end{cases}. \quad (4)$$

Note that in deriving (4), we require that the DM transit time is less than the diffusion time corresponding to the explosive temperature profile. This results in the condition

$$\tau_d \gtrsim \frac{\max\{\lambda_T, L\}}{v_{\text{esc}}}, \quad (5)$$

where τ_d is the characteristic time for a region of size $\max\{\lambda_T, L\}$ and temperature T_B to diffuse $\mathcal{O}(1)$ of its heat, and v_{esc} is the DM transit velocity (set by the escape velocity of the WD). An estimate from the heat equation yields $\tau_d \sim \frac{\lambda_T^2}{\alpha}$, where α is the (temperature-dependent) diffusivity. **Show condition is true for all densities.** Similarly, we also require that the time to transfer energy ϵ out to the initial temperature profile of length L is less than the diffusion time scale τ_d . Both of these conditions are necessary to ensure that energy depositions from individual collisions add coherently into a temperature profile during the full transit length. While a heating event can still be explosive if either of these conditions are violated, the formalism of (4) no longer holds in this case.

In addition, we require that a DM with this interaction makes it through the crust of the WD of size of density n_c and size R_c :

$$n_i \sigma_{\epsilon,i} \lesssim \left(\frac{m_{\text{DM}} v_{\text{esc}}^2}{n_c R_c} \right) \frac{1}{\epsilon}. \quad (6)$$

Imposing (4), we find lower bound on m_{DM} such that the DM is able to both penetrate the crust *and* trigger an explosion:

$$m_{\text{DM}} \gtrsim T_B \max\{\lambda_T, L\}^2 \left(\frac{n_c R_c}{v_{\text{esc}}^2} \right) \quad (7)$$

If (7) is violated, then the DM interaction is either not strong enough to ignite the WD or it is too strong that it has no chance to transit the interior as it gets stopped in the crust. In the case of $\lambda_T > L$, this translates to a model-independent lower-bound on the DM mass $\sim 10^{27} - 10^{34}$ GeV. **used 1 km crust and same number density as interior.**

We now calculate the maximum possible DM mass that may transit a single WD within its lifetime \sim Gyr. The expected transit rate for an ultra-heavy DM state is given by

$$\Gamma_{\text{DM}} = n_{\text{DM}} \sigma_g v \sim \frac{\rho_{\text{DM}}}{m_{\text{DM}}} \pi R_s^2 \left(\frac{v_{\text{esc}}}{v} \right)^2 v, \quad (8)$$

where $v \sim 10^{-3}$ is the virial velocity of DM and ρ_{DM} is the energy density of DM in the region of interest. σ_g denotes the capture cross section including a gravitational Sommerfeld enhancement. Considering a $1.25 M_\odot$ WD in the local dark matter halo $\rho_{\text{DM}} \sim 0.3$ GeV/cm³, we find that $m_{\text{DM}} \lesssim 10^{44}$ GeV $\sim 10^{20}$ g will transit the WD at least once in a Gyr. If we instead consider (recently discovered) heavy white dwarfs in the galactic center $\rho_{\text{DM}} \sim 10^3$ GeV/cm³, this upper bound improves to $m_{\text{DM}} \lesssim 10^{48}$ GeV $\sim 10^{24}$ g. **Hard to put this into “scaling” notation.**

B. DM-DM Collisions

IV. WHITE DWARF - PARTICLE DETECTOR

In the DM interactions under consideration, the released energy must be transferred to the stellar medium in order for the WD to be heated. For a given particle type, each value of ϵ is characterized by a distance $R_{i,\epsilon}$ from the point of release over which it is deposited. In particular, we define $R_{i,\epsilon}$ as the distance over which a particle i and any secondaries transfer $\mathcal{O}(1)$ of the initial energy ϵ to electrons or ions in the WD. In this section we describe the dominant mechanism of energy loss for various SM particles in a WD. We then use this to compute the deposition length $R_{i,\epsilon}$, which can be related to the heating length in a straightforward manner. For the purpose of depositing sufficient energy to trigger supernovae, we focus on high-energy particles $\epsilon \gg$ MeV which interact via the strong and electromagnetic forces (i.e. electrons, muons, photons, pions, and neutral hadrons). In this way, the WD may be thought of as a “particle detector” with electromagnetic and hadronic “calorimeter” components.

A. Electromagnetic Calorimeter

The interior of a WD is a complex environment (unless otherwise noted, we will assume a carbon-oxygen WD). Famously, the star is supported against collapse by electron degeneracy pressure with a characteristic Fermi energy $E_F \sim n_e^{1/3}$, where n_e is the number density of electrons. In addition, the nuclei are at an ambient temperature $T \sim \text{keV}$ and form a strongly-coupled plasma $\frac{Ze^2}{n^{1/3}T} \gg 1$.

For charged particles, Coulomb scattering is a useful mechanism for energy transfer. Generically, an incident (spin-0) particle of mass m_i , charge e , and velocity β scattering off a target M_t of charge Ze is described by the “Rutherford” differential cross section [Originally derived by Bhabha?](#)

$$\frac{d\sigma}{dE'} = \frac{2\pi\alpha^2 Z^2}{M_t\beta^2} \frac{1}{E'^2} \left(1 - \frac{\beta^2 E'}{E_{\text{kin}}}\right), \quad (9)$$

where we have assumed a sufficiently fast incident particle so that interactions are governed by single collisions with energy transfer E' [3]. E_{kin} denotes the maximum energy transfer possible satisfying kinematic constraints [target at rest and zero relative angle between incoming incident and outgoing target momenta](#):

$$E_{\text{kin}} = \frac{2M_t\beta^2\gamma^2}{1 + 2\gamma(M_t/m_i) + (M_t/m_i)^2}, \quad (10)$$

where $\gamma = (1 - \beta^2)^{-1/2}$.

For sufficiently heavy incident particles, the differential cross section depends only on the velocity of the incident particle. Note that higher-spin particles receive additional corrections to the cross section, but for small energy transfers these corrections are negligible. It is straightforward to understand the parametric dependences of (9): there is increased likelihood to scatter for slowly moving incident particles undergoing “soft-scatters” against lighter targets. Therefore, one would expect that soft scattering dominates the energy loss and that collisions with nuclei of mass M are suppressed by a factor $\mathcal{O}\left(\frac{Zm_e}{M}\right)$ as compared to collisions with electrons. This is certainly true for incident charged particles in non-degenerate matter. However, both of these naive expectations turn out to be false when considering scattering off a degenerate species.

To understand the effect of degeneracy, we first consider the energy loss from scattering a high-energy charged particles off non-degenerate targets in the WD, for instance, the carbon nuclei. In this case, the stopping power due to collisions with a number density n is given by:

$$\frac{dE}{dx} = - \int dE' \left(\frac{d\sigma}{dE'} \right) nE' \quad (11)$$

$$\sim - \frac{2\pi n Z^2 \alpha^2}{M_t \beta^2} \log \left(\frac{E_{\text{max}}}{E_{\text{min}}} \right). \quad (12)$$

This integration must be performed over all E' within the regime of validity for (9), fixing the lower and upper bounds of the “Coulomb Logarithm”. Quantum mechanical uncertainty sets a limit to the accuracy that can be achieved in “aiming” an incident particle at a target. In terms of impact parameter b for the collision, this translates to a bound $b \gtrsim (\min\{m_i, M_t\}\beta\gamma)^{-1}$ corresponding to the larger de Broglie wavelength. In terms of energy transfer, this becomes

$$E' \lesssim E_q = \frac{2 \min\{m_i, M_t\}^2 Z^2 \alpha^2 \gamma^2}{M_t}. \quad (13)$$

In addition, the expression for the differential cross section (9) no longer holds when E' becomes larger than the mass of the target [4]. For our calculations, we take the maximum energy that an incident particle is able to transfer to be

$$E_{\text{max}} = \min\{E_q, E_{\text{kin}}, M_t\}. \quad (14)$$

On the other hand, the maximum impact parameter is determined by charge screening. In a WD, this is simply the screening due to a degenerate electron gas [similar to a solid](#) and is given by the Thomas-Fermi length [5]

$$l_{\text{sc}} = \left(\frac{6\pi Z e^2 n_e}{E_F} \right)^{-1/2} \sim \frac{1}{m_e}. \quad (15)$$

[This is the equivalent of the Debye screening length for a degenerate gas at Fermi energy \$E_F\$.](#) This corresponds to a lower bound

$$E_{\text{sc}} = \frac{2m_e^2 Z^2 \alpha^2}{M_t \beta^2}. \quad (16)$$

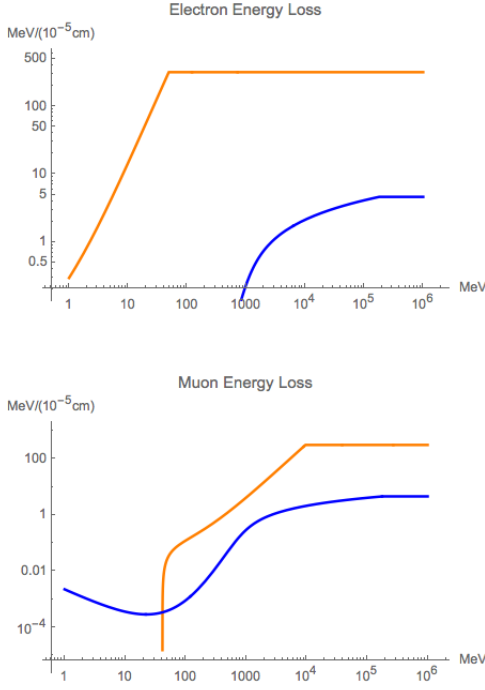
Note that when the incident particle reaches velocity $\beta\gamma \approx \frac{m_e}{\min\{m_i, M_t\}}$, the minimum possible energy transfer due to Thomas-Fermi screening will in fact exceed the maximum. At this point, the form of equation (11) becomes modified to avoid unphysical non-negative values of dE/dx and there is negligible stopping power due to collisions. However, the lattice structure of ions in the WD introduces further complications [5]. The typical lattice binding energy between ions is given by the electric potential

$$E_B \sim \frac{Z^2 e^2}{n^{-1/3}}. \quad (17)$$

For energy transfers greater than E_B , any lattice effects can be safely ignored. On the other hand, momentum transfers from collisions below this threshold may lead to suppressed energy loss due to collective effects. For simplicity we set the lower bound on nuclei scattering (not applicable for electron targets) to be

$$E_{\text{min}} = \max\{E_B, E_{\text{sc}}\} \quad (18)$$

so that we only account for energy transfers greater than the ionic lattice binding energy.

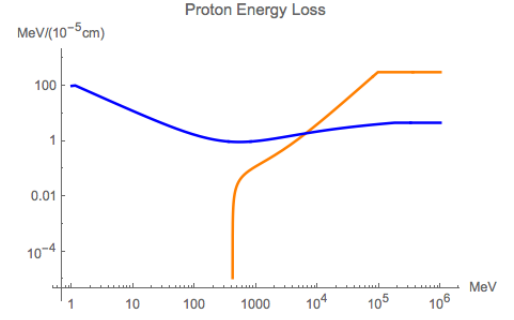


When considering collisions with the degenerate electrons, an incident particle transferring energy E' can only scatter those electrons within E' of the Fermi surface. We define a modified density of electrons $n_e(E')$ as:

$$n_e(E') = \begin{cases} \int_{E_F - E'}^{E_F} dE g(E) & E' \leq E_F \\ n_e & E_F \leq E' \end{cases}, \quad (19)$$

where $g(E)$ is the density of states per unit volume for a three-dimensional free electron gas. This can also be expressed as a suppression of the differential cross section of order $\mathcal{O}(E'/E_F)$ whenever energy less than E_F is transferred. Therefore, unlike in the non-degenerate case, the energy loss due to soft-scatters are in fact subdominant to the contributions from rare hard-scatters. The stopping power is also highly sensitive to E_{\max} and E_{\min} , governed by a power-law dependence rather than the logarithmic sensitivity in the case of a non-degenerate target.

We have calculated the stopping power of high-energy particles solely due to Coulomb collisions, differentiating between nuclei and degenerate electron targets. This is shown in Figure [Figure](#) for an electron density $n_e \sim 10^{33} \text{ cm}^{-3}$. It is found that for heavy incident particles, the stopping power is dominated by collisions with nuclei at low-energies although it is dominated by collisions with degenerate electrons at high-energies. In addition, scattering off degenerate electrons becomes completely screened at a comparatively higher energies.

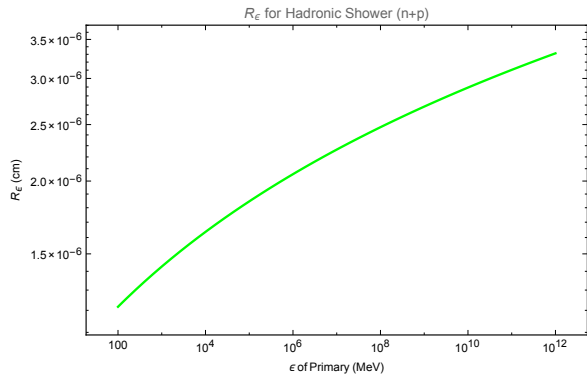


B. Strong Interactions

Strong interactions are a significant channel for energy transfer in the WD. For sufficiently energetic particles greater than the nuclear binding energy $E_{nuc} \sim \mathcal{O}(10 \text{ MeV})$, nuclear interactions (absorption) result in an $\mathcal{O}(1)$ number of energetic secondary hadrons (protons, neutrons, pions, etc.) emitted roughly in the direction of the primary particle. These secondary particles approximately split the initial total energy of the absorbed primary particle and can collide with other nuclei in the WD. In addition, the nucleus will generally be left in an excited state and relax through the emission of low-energy $\mathcal{O}(10 \text{ MeV})$ nucleons (“nuclear evaporation”) and photons [4]. The cross section for any such process is approximately set by the nuclear length scale $\sim \text{fm}$. A hadronic shower is a result of all such reactions caused by primary and secondary particles.

To estimate the typical shower length, we assume a primary particle of energy ϵ interacting with nuclei to produce N secondary particles each of energy ϵ/N . The shower will end once final-state particles reach energies of order E_{nuc} . We ignore the effects of the evaporative stage in each reaction as this will only introduce minor corrections at sufficiently large ϵ . We find a hadronic shower length $L = l_{nuc} \left(\frac{\log(\epsilon/E_{nuc})}{\log N} \right)$, where l_{nuc} is the mean free path for nuclear collisions. For a number density $n \sim 10^{32} \text{ cm}^{-3}$ and hadronic cross section $\sim 0.1 \text{ barn}$ [match nuclear data for carbon nonelastic scattering](#) this results in a shower length $L \approx 10 l_{nuc} \approx 10^{-6} \text{ cm}$. Note that this only has a mild, logarithmic sensitivity to the initial energy $\epsilon \gg 10 \text{ MeV}$ and number of secondaries $N \sim \mathcal{O}(1)$.

The end products of a hadronic shower will generally be hadrons of kinetic energy $1 - 10 \text{ MeV}$ which are incapable of inducing further nuclear disintegration. Charged hadrons have appreciable electromagnetic interactions with nuclei, while collisions with degenerate electrons are completely screened at these energies. Integrating (11), we find that in a density of $n \sim 10^{32} \text{ cm}^{-3}$ protons traverse $\approx 10^{-6} \text{ cm}$ slowing down from 5 MeV to 1 MeV . [The corresponding distance is significantly larger for charged pions \$\sim 10^{-2} \text{ cm}\$](#) On the other hand, electromagnetic couplings are highly suppressed for final-state neutral hadrons. The dominant source of energy loss for



neutrons in this range is elastic scattering off nuclei [neutron capture cross section in C+O is negligible](#). Each scatter transfers a fraction $\left(1 - \left(\frac{m}{m+M}\right)^2\right) \approx 0.1$ of the neutron energy to nuclei (averaging over scattering angles), where m and M are the masses of the neutron and nuclei, respectively. At kinetic energies below \sim MeV, the typical energy transfer in an elastic collision is of order the binding energy in the Coulomb lattice E_B . We find that $\mathcal{O}(10)$ elastic scatters are needed to slow neutrons from 5 MeV to 1 MeV. For a number density $n \sim 10^{32} \text{ cm}^{-3}$ and elastic cross section \sim barn [set to match nuclear data for carbon nonelastic scattering](#), we find that neutrons traverse a total distance (in the form of a random-walk) $\sim 10^{-8} \text{ cm}$ during this energy deposition.

V. Q-BALLS

In various supersymmetric extensions of the standard model (SM), non-topological solitons called Q-balls can be produced in the early universe [6, 7]. If these Q-balls were stable, they would comprise a component of the dark matter today. Q-balls can be classified into two groups: supersymmetric electrically charged solitons (SECS) and supersymmetric electrically neutral solitons (SENS). When a neutral baryonic Q-ball interacts with a nucleon, it absorbs its baryonic charge as a minimum-energy configuration and induces the dissociation of the nucleon into free quarks. In this process (known as the “KKST” process), \sim GeV of energy is released through the emission of 2-3 pions [8]. The KKST process provides a useful way to detect such Q-balls. The cross section for interaction is approximately the geometric cross section

$$\sigma_Q \simeq \pi R_Q^2. \quad (20)$$

In gauge-mediated models with flat scalar potentials, the Q-ball mass and radius are given by

$$M_Q \sim m_F Q^{3/4}, \quad R_Q \sim m_F^{-1} Q^{1/4}, \quad (21)$$

where m_F is related to the scale of supersymmetry breaking (messenger scale). The condition $M_Q/Q < m_p$ ensures that the Q-ball is stable against decay to nucleons [8].

Note that a sufficiently massive Q-ball will become a black hole if the Q-ball radius is less than the Schwarzschild radius $R_Q \lesssim R_s \sim GM_Q$. In the model described above, this translates into the condition

$$m_F \left(\frac{M_{\text{pl}}}{m_F}\right)^3 \lesssim m_Q, \quad \left(\frac{M_{\text{pl}}}{m_F}\right)^4 \lesssim Q. \quad (22)$$

For Q-ball masses of this order, gravitational interactions become relevant while the KKST interaction ceases to exist.

A. Q-ball Constraints

We assume that for each Q-ball collision, there is equal probability to produce π^0, π^+ and π^- under the constraint of charge conservation. In the notation of Section [overview](#), $n_\pi \sim \mathcal{O}(10)$ pions are released with $\epsilon_\pi \sim \text{GeV}$. [The mean distance travelled by a relativistic particle before decaying is \$d = \gamma v \tau\$. \$\gamma \approx 5\$, so for neutral pions \$d_{\pi^0} \sim 10^{-5} \text{ cm}\$ while for charged pions, \$d_{\pi^\pm} \sim 10 \text{ m}\$.](#)

Numerous experiments have studied the effects of 50 – 500 MeV pions incident upon complex nuclei targets such as carbon. It is found that there is roughly equal cross section of order ~ 0.1 barn for a (neutral or charged) pion to either scatter elastically, scatter inelastically, or become absorbed with no final state pion [9]. Of these possibilities, pion absorption is the most relevant for energy loss as this will induce a hadronic shower. During this process, ~ 2 -3 hadrons (i.e. protons, neutrons, alpha particles) are emitted. [Point of this paragraph: argue that KKST range lies within trigger size](#)

Therefore, Q-balls with sufficiently large cross section $\sigma_Q \gtrsim 10^{-4} \lambda_T^2$ will result in explosions. This is plotted in Figure [Figure](#). For the model described in Section [previous Section](#), the Q-ball cross section is related to its mass $m_Q = \sigma_Q^{3/2} m_F^4$ and $Q = \sigma_Q^2 m_F^4$. Therefore, find that

$$m_Q \gtrsim 10^8 \text{ g} \left(\frac{m_F}{\text{TeV}}\right)^4, \quad Q \gtrsim 10^{38} \left(\frac{m_F}{\text{TeV}}\right)^4 \quad (23)$$

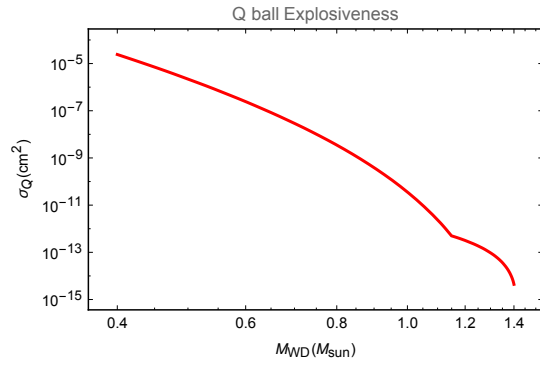
is capable of triggering runaway fusion in a heavy $\sim 1.25 M_\odot$ WD for which $\lambda_T \sim 10^5 \text{ cm}$.

VI. DISCUSSION

Appendix A: Detail Study of Heating Lengths

Appendix B: Acknowledgements

We are grateful to S. Rajendran for suggestions and collaboration during the early stages of this work, as well as his “benign negligence”. We would also like to thank D. Grabowska, K. Harigaya, R. McGehee, and J. Wurtele for stimulating discussions.



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