

A. Transits

a. Ignition Condition. Runaway fusion only occurs in the degenerate WD interior where thermal expansion is suppressed as a cooling mechanism. The outer layers of the WD, however, are composed of a non-degenerate gas and it is therefore essential that a DM candidate penetrate this layer in order to ignite a SN. We parameterize this by a DM stopping power $(dE/dx)_{\text{SP}}$, the kinetic energy lost by the DM per distance traveled in the non-degenerate layer, and demand that

$$\left(\frac{dE}{dx}\right)_{\text{SP}} \ll \frac{m_\chi v_{\text{esc}}^2}{R_{\text{env}}}, \quad (1)$$

where $R_{\text{env}} \approx 50$ km is the width of a WD envelope [?].

The energy deposited during a continuous heating event such as a DM transit is best described in terms of a linear energy transfer $(dE/dx)_{\text{LET}}$, the kinetic energy of SM particles produced per distance traveled by the DM. If these products have a heating length L_0 then the relevant energy deposit must at minimum be taken as the energy transferred over the transit distance L_0 . Of course, we can always choose to consider energy deposits over a longer segment of the DM trajectory. Importantly, as per the general condition (??) such a deposition is *less* explosive unless L_0 is smaller than the trigger size λ_T . Thus, we consider the energy deposited in a transit over the larger of these two length scales. Assuming the energy of the DM is roughly constant over this heating event, the ignition condition for transit heating is:

$$\left(\frac{dE}{dx}\right)_{\text{LET}} \gtrsim \frac{\mathcal{E}_{\text{boom}}}{\lambda_T} \cdot \max\left\{\frac{L_0}{\lambda_T}, 1\right\}^2. \quad (2)$$

Note that the DM stopping power in the non-degenerate layer $(dE/dx)_{\text{SP}}$ and the linear energy transfer in the degenerate interior $(dE/dx)_{\text{LET}}$ are possibly controlled by different physics and may have very different numerical values. In addition, a transit heating event satisfying condition (1) will have negligible energy loss over the parametrically smaller trigger size or heating length L_0 , validating (2).

The above argument sums the individual energy deposits along the DM trajectory as though they are all deposited simultaneously. This is possible if the DM moves sufficiently quickly so that this energy does not diffuse out of the region of interest before the DM has traversed the region. We therefore require that the diffusion time $\tau_{\text{diff}} \approx 10^{-12}$ s across a heated region at temperature T_f be larger than the DM crossing-time:

$$\tau_{\text{diff}} \sim \frac{L^2}{\alpha(T_f)} \gg \frac{L}{v_{\text{esc}}}, \quad (3)$$

where $\alpha(T)$ is the temperature-dependent diffusivity, and the DM transits at the stellar escape velocity $v_{\text{esc}} \sim 10^{-2}$. This condition is more stringent for smaller regions, so we focus on the smallest region of interest, $L = \lambda_T$. (3) is then equivalent to demanding that the escape speed is greater than the conductive speed of the fusion wave front, $v_{\text{cond}} \sim \alpha(T_f)/\lambda_T$. Numerical calculations of v_{cond} are tabulated in [?], and indeed condition (3) is satisfied for all WD densities.

b. Event Rate: Wind Scenario. The rate of transit events is given by the flux of DM passing through a WD

$$\Gamma_{\text{trans}} \sim \frac{\rho_\chi}{m_\chi} R_{\text{WD}}^2 \left(\frac{v_{\text{esc}}}{v_{\text{halo}}}\right)^2 v_{\text{halo}}, \quad (4)$$

where m_χ is the DM mass, ρ_χ is the DM density in the region of the WD, and R_{WD} is the WD radius. Here $v_{\text{halo}} \sim 10^{-3}$ is the virial velocity of our galactic halo, and the transit rate contains an $(v_{\text{esc}}/v_{\text{halo}})^2 \sim 100$ enhancement due to gravitational focusing.

B. Collisions and Decays

a. Ignition Condition. For a point-like DM-DM collision or DM decay event releasing particles of heating length L_0 , ignition will occur if the total energy in SM products satisfies condition (??). Such an event will likely result in both SM and dark sector products, so we parameterize the resulting energy in SM particles as a fraction f_{SM} of the DM mass. For non-relativistic DM, the DM mass is the dominant source of energy and therefore $f_{\text{SM}} \lesssim 1$ regardless of the interaction details. With this parameterization, a single DM-DM collision or DM decay has an ignition condition:

$$m_\chi f_{\text{SM}} \gtrsim \mathcal{E}_{\text{boom}} \cdot \max\left\{\frac{L_0}{\lambda_T}, 1\right\}^3. \quad (5)$$

We are thus sensitive to DM masses $m_\chi \gtrsim 10^{16}$ GeV.

However, there is the possibility if DM is captured in the WD that allows collisions or decays of lower mass DM to ignite the star. Multiple DM-DM collisions or decays in a sufficiently small region can occur rapidly enough to be counted as a single heating event. This is similar in nature to a transit heating event, where multiple scatters across a transit length λ_T can release an energy $\mathcal{E}_{\text{boom}}$ and satisfy (2) even if any individual scatter is not explosive by itself. If a single DM-DM collision is unable to ignite the star, the sum total of the energy released in many collisions can still result in a SN if

$$m_\chi f_{\text{SM}} \gtrsim \frac{\mathcal{E}_{\text{boom}}}{N_{\text{mult}}} \cdot \max\left\{\frac{L_0}{\lambda_T}, 1\right\}^3, \quad N_{\text{mult}} \gtrsim 1, \quad (6)$$

We define N_{mult} as the number of collisions within a region of size $\max\{\lambda_T, L_0\}^3$ (or smaller) during a diffusion time τ_{diff} . This necessarily depends on additional DM parameters and the evolution of the captured DM in the star. These are discussed in detail below.

b. Event Rate: DM Wind. For the remainder of this section, all numerical quantities are evaluated assuming a WD lifetime $\tau_{\text{WD}} \sim 5$ Gyr and central WD density $n_{\text{ion}} \sim 10^{31} \text{ cm}^{-3}$. At this density, the relevant WD parameters are approximately:

$$M_{\text{WD}} \approx 1.25 M_\odot, \quad R_{\text{WD}} \approx 4000 \text{ km}, \quad v_{\text{esc}} \approx 2 \times 10^{-2}. \quad (7)$$

We also assume a typical WD temperature $T \sim \text{keV}$. DM that is not captured traverses the WD in $R_{\text{WD}}/v_{\text{esc}} \approx 0.1$ s, and the rate of DM-DM collisions within the WD parameterized by cross-section $\sigma_{\chi\chi}$ is:

$$\Gamma_{\text{ann}} \sim \left(\frac{\rho_\chi}{m_\chi}\right)^2 \sigma_{\chi\chi} \left(\frac{v_{\text{esc}}}{v_{\text{halo}}}\right)^3 v_{\text{halo}} R_{\text{WD}}^3. \quad (8)$$

Similarly the net DM decay rate inside the WD parameterized by a lifetime τ_χ is:

$$\Gamma_{\text{decay}} \sim \frac{1}{\tau_\chi} \frac{\rho_\chi}{m_\chi} \left(\frac{v_{\text{esc}}}{v_{\text{halo}}}\right) R_{\text{WD}}^3. \quad (9)$$

c. Event Rate: DM Capture. For the DM to be captured in a WD, it must lose energy $\sim m_\chi v^2$, where v is the relative DM velocity (in the rest frame of the WD) asymptotically far away. Properly, this DM velocity is described by a (boosted) Maxwell distribution peaked at the galactic virial velocity $v_{\text{halo}} \sim 10^{-3}$. Since typically $v \ll v_{\text{esc}}$, the DM has initial velocity v_{esc} in the star and must lose a fraction $(v/v_{\text{esc}})^2$ of its energy to become captured.

The physics of DM capture can be made more precise for a specific interaction. Consider a spin-independent, elastic scattering off ions with cross section $\sigma_{\chi A}$. Assuming $m_{\text{ion}} \ll m_\chi$, the typical momentum transfer in an elastic scatter is $q \sim \mu_A v_{\text{esc}} \approx 200 \text{ MeV}$, where $\mu_A \sim m_{\text{ion}}$ is the reduced mass of the DM-nuclei system. This corresponds to an energy transfer $q^2/m_{\text{ion}} \sim m_{\text{ion}} v_{\text{esc}}^2 \approx 10 \text{ MeV}$. The average number of DM scatters during a full transit of the WD is simply a ratio of the mean free path to the size of the WD

$$\bar{N}_{\text{scat}} \sim n_{\text{ion}} \sigma_{\chi A} R_{\text{WD}}. \quad (10)$$

If $\bar{N}_{\text{scat}} < 1$, then \bar{N}_{scat} is the probability for a *single* scatter to occur during the transit. Thus, DM with initial velocities less than

$$v_{\text{cap}}^2 \sim v_{\text{esc}}^2 \left(\frac{m_{\text{ion}}}{m_\chi}\right) \max\{\bar{N}_{\text{scat}}, 1\}. \quad (11)$$

will be captured in the WD. A detailed calculation of the rate of DM capture [?] yields

$$\Gamma_{\text{cap}} \sim \Gamma_{\text{trans}} \cdot \min\{1, \min\{\bar{N}_{\text{scat}}, 1\}\left(\frac{v_{\text{cap}}}{v_{\text{halo}}}\right)^2\}. \quad (12)$$

Since the momentum transfer q is roughly of order the inverse nuclear size, it is reasonable to expect the DM coherently scatters off all nucleons in the nucleus. The average per-nucleon cross section (spin-independent) is given by

$$\sigma_{\chi A} = A^2 \left(\frac{\mu_A}{\mu_n}\right)^2 F^2(q) \sigma_{\chi n} \sim A^4 F^2(q) \sigma_{\chi n}, \quad (13)$$

where

$$F_{\text{SI}}^2(q) = \exp(-q^2 s^2) \left(\frac{3j_1(qR_n)}{qR_n} \right)^2 \quad (14)$$

is the Helm form factor [?], with $s \sim \text{fm}$, $R_n \approx \sqrt{(A^{1/3})^2 - 5s}$. For momentum transfers corresponding to a DM velocity $v_{\text{esc}} \sim 2 \times 10^{-2}$, we find that $F^2 \approx 0.1$. In general, the form factor should range from $F^2 \sim 10^{-2} - 1$, where at sufficiently large momentum transfers the DM is scattering off individual nucleons. As a result we will conservatively take $F^2 \approx 0.1$ for all momentum transfers, and this does not affect the results significantly. Currently, the bound on spin-independent DM nuclear elastic scatters from XENON 1T is

$$\sigma_{\chi n} < 10^{-45} \text{ cm}^2 \left(\frac{m_\chi}{10^3 \text{ GeV}} \right). \quad (15)$$

Interestingly, any DM candidate whose scattering cross section satisfies the direct detection constraint is necessarily capturing only a fraction $\sim 10^{-2}$ of those DM which transit the star.

If the DM is captured, it eventually thermalizes to an average velocity

$$v_{\text{th}} \sim \sqrt{\frac{T}{m_\chi}} \approx 10^{-12} \left(\frac{m_\chi}{10^{16} \text{ GeV}} \right)^{-1/2} \quad (16)$$

and settles at the thermal radius

$$R_{\text{th}} \sim \left(\frac{T}{Gm_\chi \rho_{\text{WD}}} \right)^{1/2} \approx 0.1 \text{ cm} \left(\frac{m_\chi}{10^{16} \text{ GeV}} \right)^{-1/2}, \quad (17)$$

where its kinetic energy balances against the gravitational potential energy of the (enclosed) WD mass. For simplicity we take a constant WD density $\rho_{\text{WD}} \sim n_{\text{ion}} m_{\text{ion}}$ within R_{th} . Of course, the timescale to reach thermalization depends on the nature of the DM-SM interaction. This has been explicitly calculated in the case that the DM loses energy via elastic nuclear scatters, see [?]. First, the DM passes through the WD many times before the size of its orbit becomes fully contained within the star. This occurs after a time

$$t_1 \sim \left(\frac{m_\chi}{m_{\text{ion}}} \right)^{3/2} \frac{R_{\text{WD}}}{v_{\text{esc}}} \frac{1}{\bar{N}_{\text{scat}}} \frac{1}{\max\{\bar{N}_{\text{scat}}, 1\}^{1/2}} \approx 2 \times 10^3 \text{ yr} \left(\frac{m_\chi}{10^{10} \text{ GeV}} \right)^{3/2} \left(\frac{\sigma_{\chi A}}{10^{-38} \text{ cm}^2} \right)^{-3/2}. \quad (18)$$

Note that the time to complete a single orbit is simply the free-fall timescale:

$$t_{\text{ff}} \sim \sqrt{\frac{1}{G\rho_{\text{WD}}}} \approx 0.1 \text{ s}. \quad (19)$$

This stage is relevant only if the energy loss after a single transit is does not exceed $\sim m_\chi v_{\text{esc}}^2$:

$$\left(\frac{m_{\text{ion}}}{m_\chi} \right) \max\{\bar{N}_{\text{scat}}, 1\} < 1. \quad (20)$$

This is the case for any cross sections which satisfy the XENON bound (15). Subsequently, the DM completes many orbits within the star until dissipation from elastic scatters reduces the orbital size to the thermal radius. This occurs after a time

$$t_2 \sim \left(\frac{m_\chi}{m_{\text{ion}}} \right) \frac{1}{n_{\text{ion}} \sigma_{\chi A}} \frac{1}{v_{\text{ion}}} \left(1 + \log \left(\frac{m_\chi}{m_{\text{ion}}} \right) \right) \approx 10^2 \text{ yr} \left(\frac{m_\chi}{10^{10} \text{ GeV}} \right) \left(\frac{\sigma_{\chi A}}{10^{-38} \text{ cm}^2} \right)^{-1}. \quad (21)$$

where $v_{\text{ion}} \sim \sqrt{\frac{T}{m_{\text{ion}}}}$. Thus, DM will only settle at the thermal radius if the total thermalization time is shorter than the age of the WD:

$$t_1 + t_2 < \tau_{\text{WD}}. \quad (22)$$

We now turn towards the rate of DM-DM collisions for captured DM. Ultimately, the most interesting constraint in the capture scenario will be from the focusing of annihilations during self-gravitational collapse of a DM sphere at the thermal radius. However, we first carefully examine the effect of annihilations on the evolution of captured DM.

To begin, the settling DM constitutes a number density of DM throughout the WD volume as well as outside the star. [discuss annihilations of infall?](#) After a settling time has passed, DM will begin steadily accumulating at R_{th} . If (??) is satisfied, the accumulation rate is roughly the same as the capture rate. However, this density of accumulating DM is also depleting due to annihilations. Eventually, these two rates become comparable and there is an equilibrium number of DM particles

$$N_{\text{eq}} \sim \left(\frac{\Gamma_{\text{cap}} R_{\text{th}}^3}{\sigma_{\chi\chi} v_{\text{th}}} \right)^{1/2} \approx 5 \times 10^{27} \left(\frac{m_\chi}{10^{10} \text{ GeV}} \right)^{-3/2} \left(\frac{\sigma_{\chi\chi}}{10^{-40} \text{ cm}^2} \right)^{-1/2} \left(\frac{\sigma_{\chi A}}{10^{-38} \text{ cm}^2} \right)^{1/2} \left(\frac{\rho_\chi}{0.4 \text{ GeV/cm}^3} \right)^{1/2}. \quad (23)$$

Of course, there is no guarantee that this equilibrium is achieved within the age of the WD. In that case, annihilations can be ignored and the total number of DM particles accumulated is simply

$$N_{\text{life}} \sim \Gamma_{\text{cap}} \tau_{\text{WD}} \approx 10^{30} \left(\frac{m_\chi}{10^{10} \text{ GeV}} \right)^{-2} \left(\frac{\sigma_{\chi A}}{10^{-38} \text{ cm}^2} \right) \left(\frac{\rho_\chi}{0.4 \text{ GeV/cm}^3} \right) \quad (24)$$

However, if the collected mass of DM at the thermal radius ever exceeds the WD mass within this volume, then there is the possibility of self-gravitational collapse of the DM. The critical number of DM for self-gravitation is given by

$$N_{\text{sg}} \sim \frac{\rho_{\text{WD}} R_{\text{th}}^3}{m_\chi} \approx 10^{27} \left(\frac{m_\chi}{10^{10} \text{ GeV}} \right)^{-5/2}. \quad (25)$$

This can only be achieved if the time to collect a critical mass of DM is shorter than the time for annihilations to deplete this mass sufficiently *and* shorter than the WD lifetime. Thus the condition for collapse is:

$$N_{\text{sg}} < N_{\text{eq}}, \quad N_{\text{sg}} < N_{\text{life}}. \quad (26)$$

DM masses less than $\sim 10^6 \text{ GeV}$ do not have enough time within the age of the WD to collect a number N_{sg} and begin a collapse.

Once the DM sphere becomes self-gravitating, it will start to collapse. Although the evolution of the collapsing DM is initially set by the dynamical free-fall time, it is ultimately slowed by the need to release gravitational potential energy and happens on a timescale set by DM cooling. In this sense the nature of the collapsing DM sphere shares similarities with the formation of DM halos, with an essential difference being dissipation. If the dominant source of dissipation is elastic nuclear scatters, the timescale for cooling is initially independent of DM velocity but decreases once the DM velocity exceeds the velocity of ions v_{ion} :

$$t_{\text{cool}}(r) \sim \frac{m_\chi}{\rho_{\text{WD}} \sigma_{\chi A}} \frac{1}{\max\{v_{\text{ion}}, v_\chi\}}, \quad (27)$$

where the velocity of DM is simply set by the virial relation

$$v_\chi \sim \sqrt{\frac{G N_{\text{sg}} m_\chi}{r}}. \quad (28)$$

It is straightforward to see that the dynamical free-fall time $\propto r^{3/2}$ is always smaller the collapse time, so that the DM requires many orbits before dissipation affects its trajectory. The timescale for $\mathcal{O}(1)$ of the collapsing DM at a radius r and number N_{sg} to deplete by annihilations is simply:

$$t_{\text{ann}}(r) \sim \frac{r^3}{N_{\text{sg}} \sigma_{\chi\chi} v_\chi}. \quad (29)$$

The collapse of the full DM sphere proceeds the timescale for annihilations becomes of order the timescale for cooling. This occurs at a characteristic radius:

$$R_{\chi\chi} \sim R_{\text{th}} \min \left\{ \left(\frac{\sigma_{\chi\chi}}{\sigma_{\chi A}} \right)^{1/3}, \left(\frac{\sigma_{\chi\chi}}{\sigma_{\chi A}} \right)^{2/7} \left(\frac{m_{\text{ion}}}{m_\chi} \right)^{1/7} \right\}. \quad (30)$$

Essentially, the number of collapsing DM particles is depleting by an $\mathcal{O}(1)$ fraction once the DM sphere has focused to within $R_{\chi\chi}$. Of course, such a collapse of the accumulated DM in the WD is only sensible if

$$R_{\chi\chi} < R_{\text{th}}. \quad (31)$$

It turns out this condition is ultimately satisfied for any DM mass and annihilation cross section which satisfy the ignition condition (6) during a collapse.

We also briefly mention the possibility that the number of DM particles initially collapsing can be much larger than N_{sg} . [elaborate](#). Once the accumulated DM becomes self-gravitating, evolution of the DM sphere can either be collapse (by cooling) or further collection. The later occurs if the timescale for collapse is greater than the timescale of collection:

$$\frac{N_{\text{sg}}}{\Gamma_{\text{cap}}} < \frac{m_{\chi}}{\rho_{\text{WD}} \sigma_{\chi A} v_{\text{ion}}}, \quad (32)$$

which occurs for DM masses above $\sim 10^{14}$ GeV, independent of $\sigma_{\chi A}$. In this case, the number of collapsing DM particles saturates to $\Gamma_{\text{cap}} t_{\text{cool}}$, with the cooling time set to match the collection time. If in addition the collection time is also initially shorter than the dynamical free-fall time, then the DM sphere at R_{th} will simply continue to collect more DM until a saturation number $\sim N_{\text{sg}}^{1/3} (\Gamma_{\text{cap}} t_{\text{ff}})^{2/3}$ greater than N_{sg} is reached.

There are two potential evolutions of the captured DM: either the DM collapses or it does not. In the later case, the DM has reached its equilibrium number at the thermal radius or is still continuing to accumulate, not yet having the critical mass necessary for collapse within its lifetime. We have checked that this scenario does not yield any constraints on DM parameters which ignite the star. Thus we turn our attention to collapsing DM, characterized by (26). The number of collisions N_{mult} that are counted as a single heating event is given by an integral of the annihilation rate over a diffusion time τ_{diff} . This depends on the radius of the collapsing DM sphere, but there exists an optimum radius R_* at which the annihilation rate is maximized. Assuming the diffusion time is the shortest timescale during the collapse and the number of particles collapsing is N_{sg} , this number is of order:

$$N_{\text{mult}} \sim \left(\frac{N_{\text{sg}}}{R_*^3} \right)^2 \sigma_{\chi\chi} v_{\chi} \min\{\lambda_T, R_*\}^3 \tau_{\text{diff}}, \quad (33)$$

Naively, we would suspect that the optimum radius is just $R_* \sim R_{\chi\chi}$. Of course, the process of cooling via elastic nuclear scatters becomes slightly complicated if the DM sphere collapses to within a radius $n_{\text{ion}}^{-1/3} \approx 10^{-10}$ cm. However, there may be some stabilizing pressure which prevents the DM from ever collapsing or annihilating below a certain radius. This is to be expected for heavy, composite DM, although such a stable radius would depend on unknown physics. Famously, gravity itself provides such a “pressure”, arresting collapses below the Schwarzschild radius by the formation of a black hole:

$$R_{\text{BH}} \sim G N_{\text{sg}} m_{\chi} \approx 5 \times 10^{-15} \text{ cm} \left(\frac{m_{\chi}}{10^{10} \text{ GeV}} \right)^{-3/2}. \quad (34)$$

If the DM is a fermion, degeneracy pressure may also affect the collapse. Even more famously, this is never an issue if the collapsing DM mass $N_{\text{sg}} m_{\chi}$ than the Chandrasekhar mass

$$M_{\text{ch}} \sim \frac{1}{G^{3/2} m_{\chi}^2}, \quad (35)$$

which is the case for $m_{\chi} \gtrsim 10^9$ GeV. Otherwise, the DM will collapse until it reaches a radius

$$R_{\text{deg}} \sim \frac{1}{G m_{\chi}^3 N_{\text{sg}}^{1/3}} \approx 3 \times 10^{-11} \text{ cm} \left(\frac{m_{\chi}}{10^8 \text{ GeV}} \right)^{-13/6}, \quad (36)$$

where the DM sphere can will either continue collecting until it reaches the Chandrasekhar mass, or annihilate beforehand. If the timescale for annihilations is less than the time to collect $\sim N_{\text{sg}}$ DM particles, than $\mathcal{O}(1)$ of the DM sphere annihilates while still supported by degeneracy pressure at the initial radius R_{deg} . If the timescale for annihilations matches the collection time for a number great than N_{sg} but less than the Chandrasekhar number M_{ch}/m_{χ} , we have checked that the energy released is not sufficient to satisfy (6). To summarize, for fermions we take

$$R_* \sim \max\{R_{\chi\chi}, \max\{R_{\text{BH}}, R_{\text{deg}}\}\}. \quad (37)$$

[add boson story](#).

Finally, we examine the decay rate of captured DM in the WD. Of course, this rate is proportional to the number of DM particles within the WD at any given instance. In the wind scenario (9), this number is given by $\sim (\Gamma_{\text{trans}} \times t_{\text{ff}})$. In the capture scenario, the number of DM particles available for decay is instead determined by the settling time

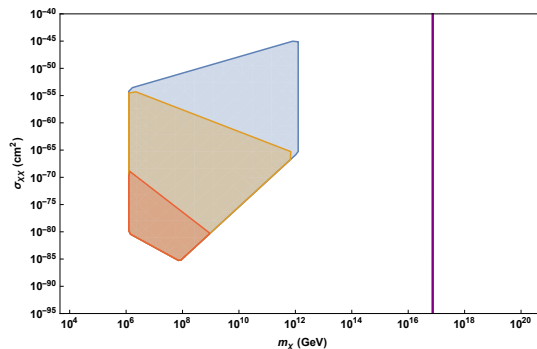


FIG. 1: Constraints on DM-DM annihilation cross-section into SM particles which deposit their energy compactly within a trigger size λ_T during self-gravitational collapse in a WD. Bounds come from observation of a single $1.25 M_\odot$ WD. Here we assume a value of $\sigma_{\chi A}$ saturated at the direct detection bounds.

inside the WD. Note that for DM masses above $\mathcal{E}_{\text{boom}}$, it is the case that gravitational collapse will occur within the age of the WD, i.e. $N_{\text{sg}} < N_{\text{life}}$. If the DM is captured via elastic scatters, the rate of decays is given by

$$\Gamma_{\text{decay}} \sim \frac{1}{\tau_\chi} \Gamma_{\text{cap}} t_2 \quad (38)$$

Since, (38) is independent of $\sigma_{\chi A}$ and scales inversely with m_χ , the rate of captured DM decays in the WD is simply enhanced by a factor $\approx 10^5$ compared to the rate of transiting “wind” decays (9). Lastly, we have checked that the enhancement of the DM number in the star is not sufficient to yield novel bounds on the DM lifetime if multiple decays are examined.

C. Constraints

We now turn towards constraints on DM-DM collisions in the capture scenario. We do not show the bounds that can be placed if $m_\chi > \mathcal{E}_{\text{boom}}$ and a single collision is capable of blowing up the star. These are obviously much more stringent than the wind scenario. In Figure 1, we derive the constraints on $\sigma_{\chi\chi}$ from the focusing of multiple collisions during gravitational collapse due of DM in the star. Bounds are from the observation of a single $1.25 M_\odot$ in our local DM density. The results of Figure 1 are valid for any SM annihilation products which deposit their energy compactly upon release within the trigger size λ_T .