

1) (10 pts) ALG (Algorithm Analysis)

Consider the following function:

```
int* makeArray(int n) {  
    int* array = calloc(n, sizeof(int));  
    int i, j;  
    for (i=0; i<n; i++)  
        for (j=i; j<n; j = j+i+1)  
            array[j]++;  
    return array;  
}
```

(a) (1 pt) Assuming that the function is called with a value of $n = 12$ or greater, what will `array[11]` store when the array is returned from the function?

(b) (3 pts) In general, what will `array[k]` store when the function completes, assuming the function was called with an input value of $k+1$ or greater?

(c) (2 pts) Write a summation that provides a tight upper bound on the number of times the line of code `array[j]++` runs when the function is called with the input value n .

(d) (4 pts) Utilizing the fact that $\sum_{i=1}^n \frac{1}{i} = O(\lg n)$, determine the run time of the function `makeArray` for an input of size n . (Note: This run time is equal to the summation from part c.)