

In general, a recurrence of the form  $T(n) = T(n-1) + f(n)$  with a constant value for a small input value of  $T$  will have the solution  $T(n) = \sum_{i=1}^n f(i) + c$ , for some constant  $c$ . (This can be shown by iterating down to a base case.)

Alternatively, one can note that if we "unroll" the recursion, the code effectively runs a nested set of loops where the first loop runs  $n$  times, the second loop runs  $n-1$  times, etc., last loop runs once. From that observation, we obtain the same summation as the one shown above.

**Grading: 2 pts for recognizing that the initial recursive call does  $O(n)$  work.**

**2 pts for recognizing that the effective input size to the recursive call is  $n-1$ , if the input size of the previous input was  $n$ .**

**2 pts for either setting up the recurrence relation or summation**

**4 pts for solving the recurrence relation or summation**

**If an answer of  $O(n^2)$  is given without any justification, award 1 pt as stated.)**