Fall 2019 Algorithms and Analysis Tools Exam, Part B

1) (10 pts) DSN (Recursive Coding)

The longest increasing subsequence problem is as follows: given a sequence of integers, find the largest subset of those integers such that within the sequence, those integers are in increasing order. For example, for the sequence $\underline{2}$, 9, 4, $\underline{3}$, 7, $\underline{5}$, $\underline{6}$, $\underline{8}$, has some increasing subsequences of length 5 (one of these is highlighted) but none of length 6, so the length of the longest increasing subsequence of this sequence is 5.

In order to solve this problem recursively, we have to reformulate the problem a little bit. Namely, our input will be:

- 1. An array, values, storing the original sequence
- 2. An integer, k, representing that we want to only consider the values in the array upto index k, including it.
- 3. An integer, *max*, representing the maximum value allowed in the increasing sequence.

Our recursive function will return the length of the longest increasing subsequence of values[0..k] such that no value in the increasing subsequence exceeds max.

Complete the implementation of this *recursive* function below:

```
int lis(int* values, int k, int max) {
```

}