

5) (10 pts) ALG (Sorting)

a) (3 pts) The following diagram shows an initial array, followed by what the array looks like after a single pass of some sorting algorithm. Indicate what sorting algorithm is being applied, and give that algorithm's worst-case runtime (using big-oh notation).

22	49	36	22	17	18	4
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4	49	36	22	17	18	22
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Sorting algorithm being applied: **Selection Sort** Grading: 2 pt, all or nothing

Worst-case runtime for algorithm: **$O(n^2)$** Grading: 1 pt, all or nothing

b) (3 pts) For the following arrays, follow the same instructions from part (a):

84	19	23	66	91	44	42
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19	23	66	84	44	42	91
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Sorting algorithm being applied: **Bubble Sort** Grading: 2 pt, all or nothing

Worst-case runtime for algorithm: **$O(n^2)$** Grading: 1 pt, all or nothing

c) (4 pts) Give a recurrence relation that represents the runtime for Merge Sort of n items. Let $T(n)$ represent the runtime of Merge Sort of n items in setting up your recurrence relation.

$$T(0) = T(1) = c_1$$

$$T(n) = 2T(n/2) + c_2 \cdot n + c_3 \quad (\text{for } n > 1)$$

$$\text{Alternatively: } T(n) = 2T(n/2) + O(n) \quad (\text{for } n > 1)$$

Grading: 2 pts for $2T(n/2)$
 2 pts for $+ O(n)$ or similar