

## 1) (10pts) ANL (Algorithm Analysis)

Consider the recursive function `diminish` shown below:

```
double diminish(int m, int n){
    if (n == 0)
        return m;
    return 1.0/2*diminish(m,n-1)
}
```

(a) (3 pts) Let  $T(n)$  represent the run time of the function `diminish`. Write a recurrence relation that  $T(n)$  satisfies.

$$T(n) = T(n - 1) + O(1)$$

**Grading: 1 pt for each component. Note that the last component may be any positive integer constant and still receive full credit.**

(b) (6 pts) Using the iteration method, determine a closed-form solution (Big-Oh bound) for  $T(n)$ .

$$\begin{aligned} T(n) &= T(n - 1) + O(1) \\ T(n) &= T(n - 2) + O(1) + O(1) \\ T(n) &= T(n - 3) + O(1) + O(1) + O(1) \\ T(n) &= T(n - k) + kO(1) \end{aligned}$$

Plugging in  $k = (n-1)$ , we find:

$$\begin{aligned} T(n) &= T(n - (n - 1)) + (n - 1)O(1) \\ T(n) &= T(1) + (n - 1)O(1) \\ T(n) &= 1 + (n - 1)O(1) \\ T(n) &= O(n) \end{aligned}$$

**Grading: 3 pts for couple iterations and generalization, 3 pts for rest - allow with or without Big-Oh notation. Give full credit to any function that is  $O(n)$ , most likely ones are  $n$ ,  $2n$ ,  $3n$ , with a plus or minus 1, potentially.**

(c) (1 pt) In terms of the values of  $m$  and  $n$ , respectively, what does the function call `diminish(m, n)` return? (You may assume that  $m$  and  $n$  are both positive.)

$$\text{diminish}(m, n) = \frac{m}{2^n}$$

**Grading: 1 pt for correct answer, 0 otherwise**