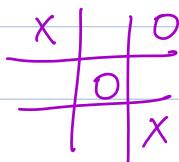


Applications

- 1) Image Processing
- 2) Chess $\rightarrow 8 \times 8$
- 3) Sudoku
- 4) Ludo
- 5) Tic Tac Toe



Suppose we want to

store 5 subjects marks for a single student

$A[1] = [5 | 1 | 2 | 5 | 4]$

Scoring 5 subjects marks for 10 students

— Having 10 different 1D arrays doesn't make sense

Rather let's have array of arrays \rightarrow 2D arrays

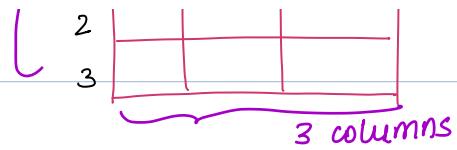
```
int mat[10][5] = { { {5, 1, 2, 4, 5}, {4, 19, 10, 25, 17} },  
                   {4, 1, 11, 12, 15}, ... . . . }
```

2D arrays are better to visualize in form of matrix
having rows & columns.

```
int mat[4][3];
```

4 rows

0	1	2
0		
1		
2		



`int mat [N][M];`

↑ no. of rows ↑ no. of columns.

$N \rightarrow$ rows
 $M \rightarrow$ columns

0,0	0	1	2	3	$\dots M-1$	$(0, M-1)$
0	0	1	2	3	$\dots M-1$	$(0, M-1)$
1	0	1	2	3	$\dots M-1$	$(0, M-1)$
2	(2,0)	(2,1)	(2,2)	(2,3)	.	.	.	$\dots (2, M-1)$	$(2, M-1)$
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
$N-1$	$(N-1, 0)$	$(N-1, 1)$	$(N-1, 2)$	$(N-1, 3)$	$\dots (N-1, M-1)$	$(N-1, M-1)$

Ques: Given a row no., find the sum of the elements of that row.

Eg \Rightarrow row no. $\Rightarrow 2$

	i	j	0	1	2	3
0	4	1	5	2		
1	9	6	1	7		
2	10	14	1	17		

$\rightarrow 10 + 14 + 1 + 17 = 32$

Along a row

constant - row no.

unstarru \rightarrow unu nu,

change \rightarrow col NO.

$[0 \quad M-1]$

$i = 2$

$sum = 0$

$\text{for}(j=0; j < M; j++)\{$

$sum += A[i][j]$

$\}$

Dry Run

i	j	$sum = 0$
2	0	$A[2][0] = 10$
2	1	$A[2][1] = 14$
2	2	$A[2][2] = 1$
2	3	$A[2][3] = 17$

Q. Print sum of all the rows one by one



$\text{for}(i = 0; i < N; i++)\{$

$sum = 0$

$\text{for}(j=0; j < M; j++)\{$

$sum += A[i][j]$

$\}$

$\text{print}(sum)$

$\}$

TC $\rightarrow O(N \times M)$

SC $\rightarrow O(1)$

$i = 0$	$j = 0$	$A[0][0]$	+
	1	$A[0][1]$	+
	2	$A[0][2]$	+
	3	$A[0][3]$	

$$i = 1 \quad j = 0 \quad -$$

$$\begin{array}{c} 1 \\ 2 \\ 3 \end{array} \quad \underline{\underline{=}}$$

$$i = 2 \quad j = 0 \quad -$$

$$\begin{array}{r} \\ \begin{array}{r} 1 \\ 2 \\ \hline 3 \end{array} \end{array}$$

Ques Print sum of ele of a given column no.

	0	1	2	3	4	.	.	.	M-1
0				(0,3)					
1				(1,3)					
2				(2,3)					
3				(3,3)					
.				.					
.				.					
N-1				(N-1,3)					

Along column

row no \Rightarrow changing [0 N-1]

col no. \rightarrow constant

j
sum = 0

for (i = 0 ; i < N ; i++) {

sum + = A[i][j]

Dry Run

say j = 1

i = 0

A[0][1]

i = 1

A[1][1]

i = 2

A[2][1]

Ques.

= Given a matrix, print sum of column by column

Eg

	0	1	2	
0	4	1	5	N=3 M=3
1	6	7	9	
2	2	5	9	

```

for(j=0; j < M; j++) {
    sum = 0
    for(i=0; i < N; i++) {
        sum += A[i][j]
    }
    print(sum)
}
  
```

TC : O(N * M)

SC : O(1)

j=0	i=0	A[0][0]
	1	A[1][0]
	2	A[2][0]
<hr/>		
j=1	i=0	A[0][1]
	1	A[1][1]
	2	A[2][1]
<hr/>		
j=2	i=0	A[0][2]
	1	A[1][2]
	2	A[2][2]

Ques. Given a square matrix [no. of rows = no. of cols]

int mat[N][N]

Eg

5x5

	0	1	2	3	4	5
0	3	2	14	15	19	
1	7	13	15	26	22	
2	22	20	5	28	22	
3	30	10	16	11	21	
4	32	29	8	28	7	

Right to left

$$\rightarrow 19 + 26 + 5 + 10 + 32$$

Left to Right

$$\rightarrow 3 + 13 + 5 + 11 + 7$$

	0	1	2	3	4	
0	3	2	14	15	19	0, 0
1	7	13	15	26	27	1, 1
2	22	20	5	28	22	2, 2
3	30	10	6	11	21	3, 3
4	32	29	8	29	7	4, 4

let's consider left to right diagonal first.

```

sum = 0
for (i=0; i < N; i++) {
    for (j=0; j < N; j++) {
        if (i == j) {
            sum += A[i][j]
        }
    }
}
print(sum)
    
```

$$\begin{aligned} TC &= O(N^2) \\ SC &= O(1) \end{aligned}$$

II

Optimized Code

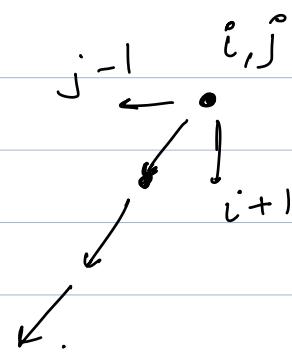
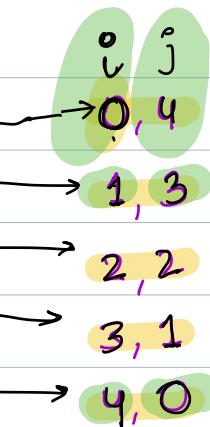
```

sum = 0
for (i=0; i < N; i++) {
    sum += A[i][i]
}
print(sum)
    
```

$$\begin{aligned} TC &\rightarrow O(N) \\ SC &\rightarrow O(1) \end{aligned}$$

Right
to
left

	0	1	2	3	4
0	3	2	14	15	19
1	7	13	15	26	27
2	22	20	5	28	22
3	30	10	6	11	21
4	32	29	8	29	7



$$\boxed{\begin{array}{l} i < N \\ j \geq 0 \end{array}}$$

1

$$\text{sum} = 0$$

$$i = 0, j = N - 1$$

while ($i < N \&& j \geq 0$) {

| sum += A[i][j]
| i++
| j--

}

A single condition will do

TC $\rightarrow O(N)$

SC $\rightarrow O(1)$

0 1 2 ... N-1

	0	1	2	3	4	i	j	
0	0	3	2	14	15	19	0, N-1	$= 0 + (N-1) = N-1$
1	1	7	13	15	26	27	1, N-2	$= 1 + (N-2) = N-1$
2	2	22	20	5	28	22	2, N-3	$= 2 + (N-3) = N-1$
:	3	30	10	6	11	21		
N-1	4	32	29	8	29	7	N-1, 0	$= N-1 + 0 = N-1$

$$\boxed{i + j = N-1}$$

$$\boxed{j = N-1 - i}$$

II

sum = 0

for($i = 0$; $i < N$; $i++$) {

| $j = N - 1 - i$

| sum += A[i][j]

}

}

TC $\rightarrow O(N)$

SC $\rightarrow O(1)$

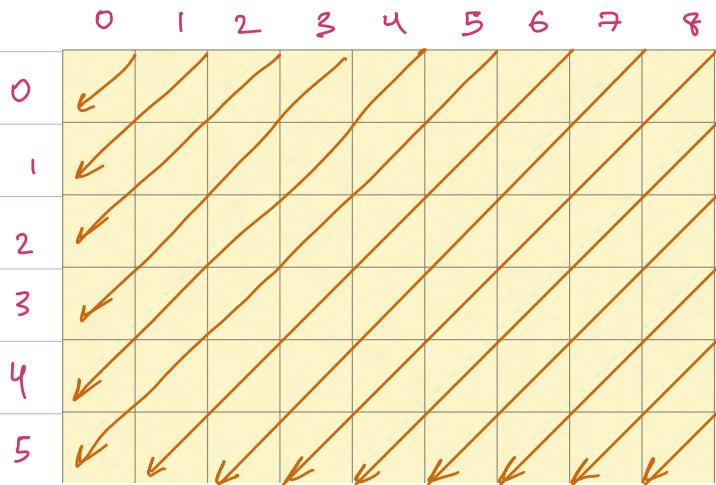
Break! $\rightarrow 8 \text{ min.}$

9:30

Ques'

Given rectangular matrix, print elements diagonal by diagonal in the given direction.

Ques.



6×5

	0	1	2	3	4
0	11	9	3	5	10
1	18	13	100	9	-1
2	6	2	5	10	7
3	14	13	26	8	18

11

9 18

3 13 6

5 100 2 14

10 9 5 13

-1 10 26

7 8

18

From each cell of first row, a diagonal is originating.

No. of cells in first row $\rightarrow M$

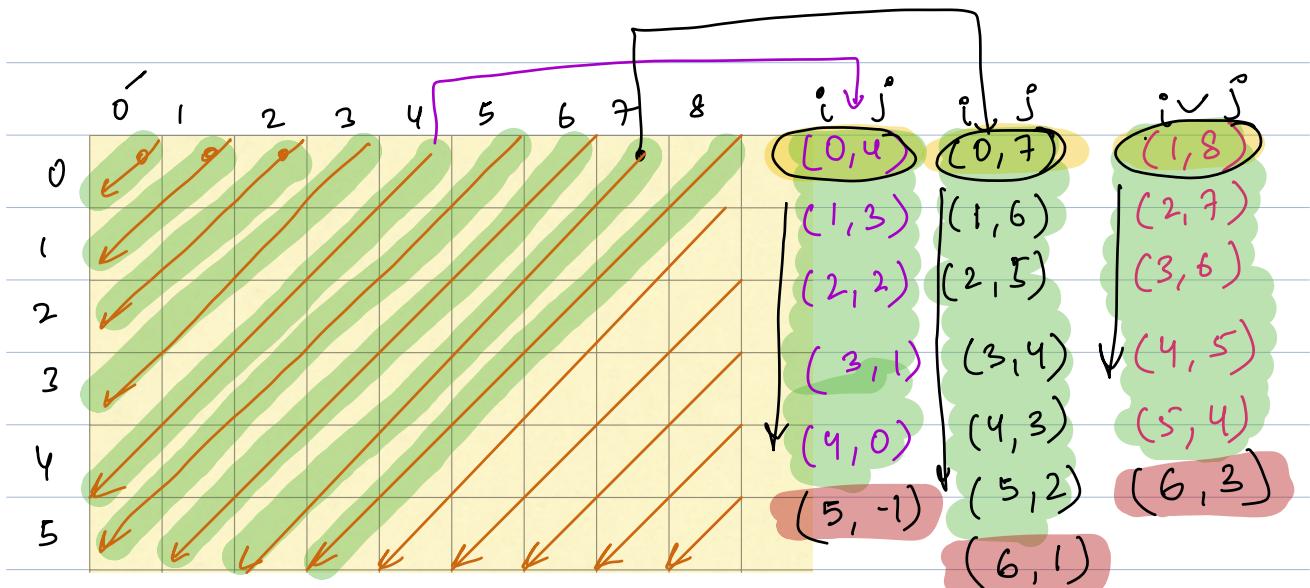
From each cell of last col, a diag. is originating.

No. of cells in last col $\rightarrow N$

$M + N ?$

$N + M - 1$

[since we are calculating top right diagonal twice]



Observations

$$(\underbrace{i < N}_{=} \& \underbrace{j \geq 0}_{=})$$

① Along a diagonal, $i \uparrow, j \downarrow$

② If a starting coordinates of an diagonal are known, we can iterate over ele of that diagonal.

$i \uparrow$
 $j \downarrow$

given
starting
coordinates
of only
diagonal,
we can
iterate over
ele of mat
diagonal

```
while(i < N && j >= 0){  
    print(A[i][j])  
    i++  
    j--  
}
```

starting indices of all the diagonals

$\Rightarrow 0,0 \ 0,1 \ 0,2 \ 0,3 \ 0,4 \ 0,5 \ 0,6 \ 0,7 \ 0,8$

$i=0$

for ($j = 0 ; j < M ; j++$) { //M
 $I=i \ J=j$

while ($I < N \ \&\ J >= 0$) {
 |
 print ($A[I][J]$)
 $I++$
 $J--$
 }
 point ("\n")
 }
 $i=[1 \ N-1] \ j \text{ const}$

$N+M-1$

0	4	5	1	7	8
1	1	9	7	5	10
2	2	5	11	10	9
3	6	4	5	3	11

$j = M-1$

for ($i = 1 ; i < N ; i++$) {
 $I=i \ J=j$

while ($I < N \ \&\ J >= 0$) {
 |
 print ($A[I][J]$)
 $I++$
 $J--$
 }
 }
 $i=0 \ j=0$

$I=0 \ J=0 \ 4$
 $I=0 \ J=1 \ 1 \ -1$
 $I=0 \ J=1 \ 5 \ 1$
 $I=0 \ J=0 \ 1 \ 0$
 $I=0 \ J=2 \ 1 \ 9 \ 2$
 $I=0 \ J=2 \ 1 \ 1$
 $I=0 \ J=0 \ 2 \ 0$
 $I=0 \ J=3 \ 3 \ -1$
 $i=0 \ j=3$

point ("m")

2

TL

$O(N * M)$

Due: Transpose

Square matrix

int mat [N] [N]

[INPLACE - means
no extra
space]

(0,1)	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16

0	1	2	3
0	1	5	9
1	2	6	10
2	3	7	11
3	4	8	12

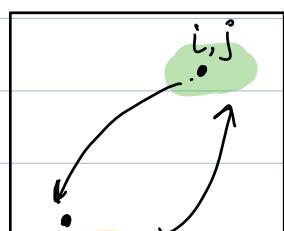
Observation

The big diagonal from left to right is same.

```
for(i=0; i<N; i++) {
```

```
    for(j=0; j<N; j++) {
```

```
        cout << arr[i][j];
```



swap(A[i][j], A[j][i])

(j, i)

}

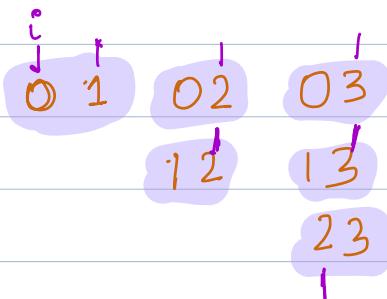
}

swap(a, b) {

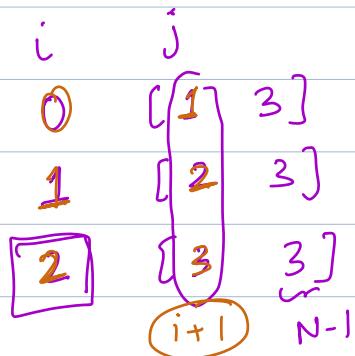
$$\begin{cases} c = a \\ a = b \\ b = c \end{cases}$$

}

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16



N=4



for (i=0; i<N-1; i++) {

 for (j=i+1; j<N; j++) {

 swap (A[i][j], A[j][i])

}

}

$$\text{Iterations} = \frac{N^2}{2}$$

TC $\Rightarrow O(N^2)$

SC $\Rightarrow O(1)$

$N=4$

	0	1	2	3
0	1	5	9	13
1	2	6	10	14
2	3	7	11	15
3	4	8	12	16

$$i=0 \quad j=1$$

swap($A[0][1]$, $A[1][0]$)

$$i=0 \quad j=2$$

$A[0][2]$, $A[2][0]$

$$i=0 \quad j=3$$

$A[0][3]$, $A[3][0]$

transposed

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16

1	5	9	13
2	6	10	14
3	7	11	15
4	8	12	16

$$i=1 \quad j=2$$

$A[1][2]$, $A[2][1]$

$$i=1 \quad j=3$$

$A[1][3]$, $A[3][1]$

$$\underline{i=2} \quad \underline{j=3}$$

$A[2][3]$, $A[3][2]$

$i=3 \quad j=4$