TCS-505 Assignment 1

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Asymptotic Notations are mathematical tooks to supresent tere time a space complexities of algorithms for asymptotic analysis.

The different asymptotic notations:

 $\begin{array}{ccc}
\hline
\mathbf{O} & \underline{\mathbf{Big}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} \\
\Rightarrow & \underline{\mathbf{fcn}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} & \underline{\mathbf{O}} \\
\hline
\end{array}$

forex:

T(u) = 3n + 2

⇒ 0(n)

(2) Big anega (-2):-

⇒ fen1 = -12 Cgcm)

> gins is the "tight" lower bound of fins.

forex:

fen1= 4n+3

g(n) = n

7 fen = -2 (g(n))

lets see if fin1 ≥ cg(n)

=> 4m+3 \(\geq \) eno for some (>0 & no \(\geq 1)

when c=1 Anoch for amy M>!

4n+3 zue 13 true

Thus of 4n+3= 2(n)

(3) Thata(θ):-⇒ 9 gives "tight" opper & lower bound of function. Freni finie 3nr2 & ten = ocging of ginn=n 3n+2= O(n) 3m2 2 3n 3 3n+2 x4n, for notare stranger to the + Ky= 3 K224 & no 22 => Complexity of f(n) can be representated as O(n). Q2.) Time complexity > O(logn) I'm - 8mt 2 $T(y) = \int_{1}^{3} T(y-1)$ M > 0 Ten) = 3T(n-1) - O'B went at a me $\frac{3}{3} \text{ T(n+1)} = 3\text{T(n-2)} - \Phi$ Using value of T(n-1) in D ⇒ T(n)= 32 T(n-2) - 1 => T(n-2) = 3T(n-3) _B Using value of T(n-2) In(1) → T(n) = 3³T(n-3) — (1)
→ Gen form:

From: $T(u) = 3^{1/2} T(u-K) - (v)$ T(0) = 1 = u-K = 0

Fru) =
$$3^{h} T(n-n)$$

Tru) = 3^{h}
 $0(3^{h})$

Ref.

Tru) = $5^{h} T(n-1) - 1$
 1×0
 1×0

Q4.)

25.) Time Complexity: O(Vm) Q6.) Time Complexity: O(vin) Q7.) Time Complexity: O(n log2n) Q8) Time Complexity: O(12) Qq.) Time Complexity: O (nlogn) fin N>=1 (SM)TE = (IN)TE gen = an ca> (ca) c = (m) Stree, exponential funce, grow faster toon polynamial functions O(4k) < O(an) K>=x1 = Solving for X2y Assuming K= 2 fq=2 f(u) = n2 g(u)= 2" Take log on both sides 17 (g(m))= n1 of 2 log (fen) = 2/g2n -> Octog2n) 2. Condition satts fice for all K > = 2 8 9, = 2.

QIII)
$$O(\sqrt{n})$$
 as I Joes as follows:

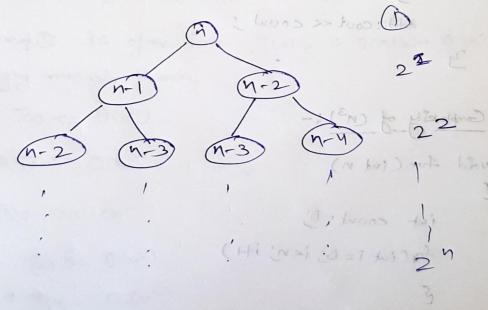
1,3,2,10,18,21

1,3,6 ... will Stop when an becomes equal to en Jreater than n.

1 n (m+t) = no

1 n \(\text{The} \)

012) Recurrance relation:



T(n)= 1+2+4. ... 2 n

$$(= 1) (2^{1} + 1)$$

$$0 (2^{1} + 1)$$

```
It we consider function call stak Size It will have
   space complexity: O(n), else O(1).
@130
  (1) Emplexity of (nlagn):-
      void fun ( lut n)
          Int Count = 0)
          for ( IW 1 = 0 ; Kn; It+)
            for(intj=1'jx=n' j=j*2)
           std:: cout << count;
  (11) Complexity of (113):-
                          (P. 2) (P. 3) (M. 3)
    vad fun ( lut n)
          int count = 0'
        facint 1= 0: ix n: i++)
             for(14)=1;j<=1;j++)
                 for Club K= 1' K+1/2 <= 1' K++)

Count ++;
```

State College Comprisoners on Wines. 110 Complexity of (lay (lay (n))! void func (ut n) for (lut i= 2; k=n; i*=i) std:: cout << i << " " Q14) Ten = Ten/4) + Ten/2) + cn2 - D => Assuming T(n/2) >= T(n/4) => T(n) 7= 2T(n/2) + cn2 - 1 Now = 20 is of the form: Time a Timb + ofin) > Applying moster's theorem, ⇒ T(n) <= O(n²)
</p> => TCM = O(42) and th) >= ch2 => Tu) >= O(u2) 7 TCm = - 12(m2) since Tens - nens of Tens = O(MY) => T(M) = O(N2)

QIED OUTER loop rous: ntimes

juner roux: 1/i+hund

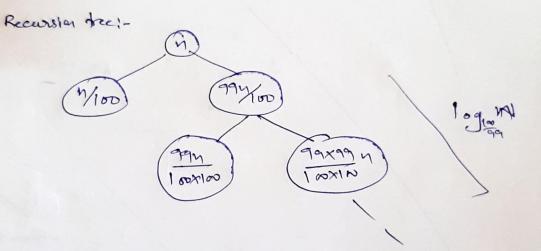
- 1+1+13 +14: 1-11

= ln(4)

> Time carplexity: O(nlagn)

Que The loop Trows exponentially time complexity: O(lagelogn))

Q17) T(n) = T(n/100) + T(99N/100) + N



at each kirch, we have to goterrough N values terrefore amplexity is: NX laylow

- neglecting 1 2/2/99

7 Time Complexity: Wigh

The analysis showskat, queksat an avergetakes o(NIGN) companish three to sort in Plems.

- 6) I < n < 2 n < log(| g(n) < log(| n) <
- c) 96 = 17801 < 1920 < MIJEN < MIJEN < MIJEN < 19101) <

- Stateled

201) Herative 1

void in scrttan Sort Cint arr () int n) {

the n =

for Cint 1=0; i<nj)++)

E int j=j;

while G>0 28 arr (j) < arr (j-17)

E wap Carr (j), arr (j-17);

j'--;

Charles - told in

Recursives void inserting Sort (vectorally dam, lut i) 17 CHREDI refurn inscrim Sout (aw, 1-1); i wiz ij White Giro ar arreis ranci-13) & Swop(ar []) arg-171:5-3

It is called online sorting also because it doesn't have the constraint of horry entire input available at the beginning like sorthy algoe like bubble or selectionsort. Can handle datapiece by piece.

O (nlgn) Q21) Quicksort O Culyn) Merse 11! O(42) Bulblole: 0(42) selection! 0(42)

INSCHE!

Bubble, Selectry, Quick, lyserthy luplace! Q22) Bushe, Inserten, Merje Stable! Inserten Online!

Steak

(1) DAM COMED OF THE 2237 Herotive! 10 W= 0 high= n-1 while lower high : mid= (lowt high)//2 if key == a [mid]: PHU+ (md)

```
ellf key > a cmid):
              low=mld+1
       else:
             highe mid-1
Recursive:
    Let BS (am, low, high, key):
         if Clow > high):
             return -1
         mid= (low+ High) 1/2
         If archid) = 2 key!
            return mid
        elif archid) > key!
            retorn BS (any low, mid-1, key)
        else:
           return BE Carr, midtl, high, key)
TIME Employed of BS!
                                     Time Complexity of LS
  Herative ! OCLOGN)
                                     Herative; O(n)
 Reconstre! O (1911)
                                     Recursive! O(n)
  Space!
                                     Space !
  Heradire! O(1)
                                      Iterative: O(1)
  Reausive: O(1-gn)
                                       Recursive: 0 (N)
```

824.

Recurrence relation for Bln, Search!

T(n)= T(n/2) +1