Descriptive statistics, I

Throughout the course, we will review and talk about descriptive statistics. This is the first bit of it.

Reviewed / discussed here are max, min, mean, median, percentile, and quartile

The R code chunks involved in this part are NOT IMPORTANT for now, and they will be explained later when the need comes up

- > The point is to review the descriptive statistics
- ➤ So you can treat every code block in this part as a blackbox, and don't worry too much about them

Set up 20 integers

```
# The following code puts the 20 integers into the variable `sample`
## use "?c" in console to read the help messages
# The name `sample` now represents the 20 integers
sample <- c(29, 35, 33, 32, 34, 30, 28, 33, 34, 35, 10, 14, 14, 12, 12, 12, 10, 14,
16, 10)
```

max, min, median, percentile, and quartile

Only for data that allows reasonable comparison in some way

The first two are more straightforward

- ✓ max: the largest entry in the data
- \checkmark for the 20 integers in sample, the max is 35
- ✓ min: the smallest entry in the data
- \checkmark for the 20 integers in sample, the min is 10

The others generally take some work, and will use R code to help. With the 20 integers here, can still be done manually to see if things indeed work out right.

- ✓ median: a value for which at most half of the data are larger than it, AND at most half are smaller than it
- ✓ for the 20 integers in sample, we can sort them and count from either end
- ✓ ... any number in between 16 and 28 could be a median
- ✓ ... In this case, convention is to take the average of 16 and 28,
- ✓ ... thus "the" median for the sample data is 22

```
# this sorts the entries contained in sample
## use "?sort" to read the help messages
sort(sample)
#> [1] 10 10 10 12 12 12 14 14 14 16 28 29 30 32 33 33 34 34 35 35
```

In fact, R has functions that directly output these statistics

```
# the names of the functions are very intuitive
max(sample)
#> [1] 35
min(sample)
#> [1] 10
median(sample)
#> [1] 22
```

percentile

- Basic ideas:
 - ✓ 30 th percentile is a value so that 30% of the data are below it
 - ✓ median is basically 50 th percentile
 - ✓ 90 th percentile is a value so that 90% of the data are below it

quartile: three of these, Q1, Q2, Q3

- ✓ Q1: the 25th percentile, also called first quartile
- ✓ Q2: the 50th percentile, i.e. the median, also called second quartile
- ✓ Q3: the 75th percentile, also called the third quartile
- ✓ Q1 and Q3 may be thought of as the medians of the lower and upper half of the data respectively

The R function quantile finds percentile and quartiles

```
# print out the sorted sample, for manual verification
sort(sample)
#> [1] 10 10 10 12 12 12 14 14 14 16 28 29 30 32 33 33 34 34 35 35
# The code below finds the 20th percentile for the entris contained in sample
# Changing ".20" below by ".25", ".50", ".75" to see the quartiles
quantile(sample, .20)
#> 20%
#> 12
# without giving the numeric percentage, it produces all the quartiles, with max,
and min
quantile(sample)
#> 0% 25% 50% 75% 100%
#> 10 12 22 33 35
```

mean

Only for data that allows reasonable arithmetic operations

- The data must be numerical
- ... but not any numerical looking data
 - ✓ your student IDs look numerical, but taking mean really makes no sense

mean: the average of the values in the data

- computed by adding all the values up and divide by the number of entries
- for sample, there are 20 entries, so add everything up in sample, and divide the result by 20

```
# directly computing the mean (29+35+33+32+34+30+28+33+34+35+10+14+12+12+12+10+14+16+10)/20 #> [1] 22.35
```

Even better, the mean function in R directly computes the mean for sample

```
mean(sample) #> [1] 22.35
```

<u>Comment</u>: There are always more than one ways of doing things, as long as we understand what is going on.

summary function

The function summary in R produces six of the statistics described here:

```
# try "?summary" in console to see the help information summary(sample)
#> Min. 1st Qu. Median Mean 3rd Qu. Max.
#> 10.00 12.00 22.00 22.35 33.00 35.00
```

Example and Practice

```
>x <- c(2, 3, 5, 2, 7, 1) # x then holds values 2, 3, 5, 2, 7, 1
>x
[1] 2 3 5 2 7 1
>y <- c(10, 15, 12)
>y
[1] 10 15 12
>z <- c(x, y)
>z
[1] 2 3 5 2 7 1 10 15 12
```

Example and Practice

```
>x <- c(3, 11, 8, 15, 12)

>x > 8

[1] FALSE TRUE FALSE TRUE TRUE

>x != 8

[1] TRUE TRUE FALSE TRUE TRUE
```

Patterned data

Use, for example, 5:15 to generate all integers in a range, here between 5 and 15 inclusive:

>5:15 [1] 5 6 7 8 9 10 11 12 13 14 15

Conversely, 15:5 will generate the sequence in the reverse order.

Example and Practice

```
class(c(1, 2, 3))
## [1] "numeric"
class(c(TRUE, TRUE, FALSE))
## [1] "logical"
class(c("Hello", "World"))
## [1] "character"
is.numeric(c(1, 2, 3))
## [1] TRUE
is.numeric(c(TRUE, TRUE, FALSE))
## [1] FALSE
is.numeric(c("Hello", "World"))
## [1] FALSE
```

Example and Practice

Strings cannot be directly used for numerical operations

```
strings <- c("1", "2", "3")
class(strings)
## [1] "character"

strings + 10
```

Error in strings + 10

We can use as.numeric() to convert a character vector into a numeric vector:

```
numbers <- as.numeric(strings)
numbers
## [1] 1 2 3
class(numbers)
## [1] "numeric"

numbers + 10
## [1] 11 12 13</pre>
```

```
as.numeric(c("1", "2", "3", "a"))
## Warning:
## [1] 1 2 3 NA

as.character(c(1, 2, 3))
## [1] "1" "2" "3"
as.character(c(TRUE, FALSE))
## [1] "TRUE" "FALSE"
```

```
> library(datasets)
> head(BJsales)
[1] 200.1 199.5 199.4 198.9 199.0 200.2
> class(BJsales)
[1] "ts"
> mode(BJsales)
[1] "numeric"
> length(BJsales)
[1] 150
```

- > the second line of code displays the first 6 elements of BJsales
- The third line of code examines the attributes of BJsales, which returns "ts," indicating that BJsales contains a time series vector, meaning the data in BJsales is arranged in chronological order.
- > Typing "?ts" in the console provides more information about the ts data type.

- The result of the mode() function indicates that the data in BJsales is numeric, making it meaningful to calculate the mean, median, and quantiles of BJsales.
- ➤ The length() function reveals that BJsales contains a total of 150 elements.

> mean(BJsales)
[1] 229.978
> mean(BJsales,trim=0.1)
[1] 229.715
> median(BJsales)
[1] 220.65

- > The first line calculates the mean of all elements in BJsales,
- The second line's trim parameter specifies that the largest 10% and smallest 10% of values should be excluded when calculating the mean.
- > This trimming function helps mitigate the impact of outliers.

Note: The results of these two calculation methods are very close, indicating that there are no outliers in BJsales that significantly deviate from the majority of the data.

Set up tidyverse packages and load them

- ✓ First time installation may take some time, because some packages will need to be compiled and installed from scratch
- ✓ Packages need to be installed **only once**, so later files will not contain the following code block

```
install.packages('tidyverse', repos = "https://utstat.toronto.edu/cran/")
install.packages('ggthemes', 'ggridges')
```

If you have problem using install.packages,running one of the following in the Console might help

• where PACKAGE_NAME is replaced by the name of the package you wish to install

```
install.packages(PACKAGE_NAME, repos="https://utstat.toronto.edu/cran/") install.packages(PACKAGE_NAME, repos="https://muug.ca/mirror/cran/")
```

A package must be loaded before we can use it. Thus each new session must load all the packages that will be used in it

• In particular, library(tidyverse) should **appear in the beginning of every .qmd (or .rmd) file** we have from now on

library(tidyverse)
library(ggthemes)

Datasets

Later files will not have to contain the following line.

```
install.packages(c('nycflights13', 'gapminder', 'Lahman'), repos =
"http://cran.utstat.utoronto.ca/")
```

```
install.packages(c('nycflights13', 'gapminder', 'Lahman'), repos="https://muug.ca/mirror/cran/")
```

✓ Running the following command in the Console or clicking the run arrow of the code block below will show a list of available datasets in a separate tab

data()

✓ You can also use? in the Console to get more details on a specific dataset. The Help panel in the lower right of the RStudio window should contain further information.

?mpg

- The software is constantly being updated and tidyverse installed may not be the latest version.
- To keep the tidyverse installation up-to-date, run the command in the code block below once in a while.

tidyverse_update()

ggplot2 basics

ggplot2 is a part of tidyverse. Main tool for data visualization used throughout the course.

mpg data

US EPA data on 38 models of cars: run the following in console, and look at the details in the Help panel on the lower right part of RStudio.

mpg

View(mpg)

Terminology

- ✓ Columns are variables
- ✓ Rows are observations
- ✓ The whole thing is a dataframe

Intuitively, a **dataframe** is a *rectangular shaped collection of data*, with **column** headers indicating the properties that we are interested in, and the **rows** correspond to individual instances that have those properties.

Variable types

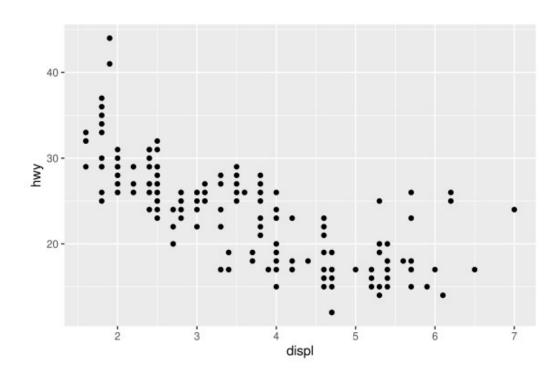
Each column is supposed to contain a certain type of data. The types are defined by the R language and the packages you load.

There are many, and we list some below:

- **character**: <chr>, strings, formed by characters
- numeric: <dbl>,doubles, real numbers
- integer: <int>,integers,
- boolean: <lgl>,can only be TRUE or FALSE
- datetime: <dttm>,date-times, a date + a time
- others ... will talk about them as they show up

First plots

```
ggplot(data = mpg) +
geom_point(mapping = aes(x= displ, y= hwy))
```



Comment:

In the above, the parameters for the functions are passed by **name**. For instance

• ggplot(data = mpg) indicates that the function ggplot accepts a parameter named data

for this particular call of ggplot, it is to be mpg

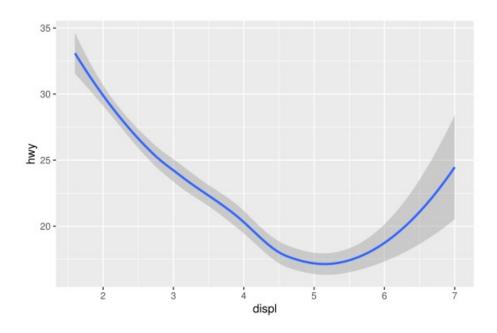
• Similarly, aes(x = displ, y = hwy) indicates that the function aes accepts two parameters named x and y

for this particular situation, the x is to be displ and y is to be hwy

• Then, geom_point(mapping = aes(x = displ, y = hwy)) indicates that the function geom_point accepts a parameter named mapping

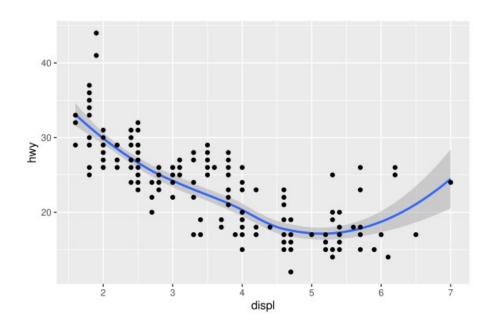
Smooth curve

```
ggplot(data = mpg) +
geom_smooth(mapping = aes(x = displ, y = hwy))
```



Can overlay on top of each other

```
ggplot(data = mpg) +
geom_smooth(mapping = aes(x = displ, y = hwy)) +
geom_point(mapping = aes(x = displ, y = hwy))
```



Structure of ggplot() calls

The general form of plotting using ggplot is the following:

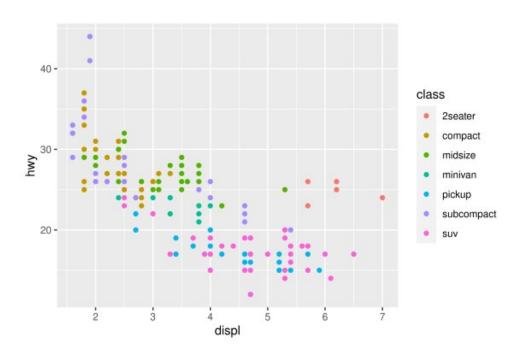
ggplot(data = DATA) + GEOM_FUNCTION(mapping = aes(MAPPINGS))

- DATA: the actual dataframe
- **GEOM_FUNCTION**: e.g. geom_point, geom_smooth, geom_bar, geom_polygon, etc.
- Names of the function are generally self-explanatory. Use ?FUNCTION NAME in console if not sure.
- ... generally it gives the most up to date information, if your RStudio is up-to-date

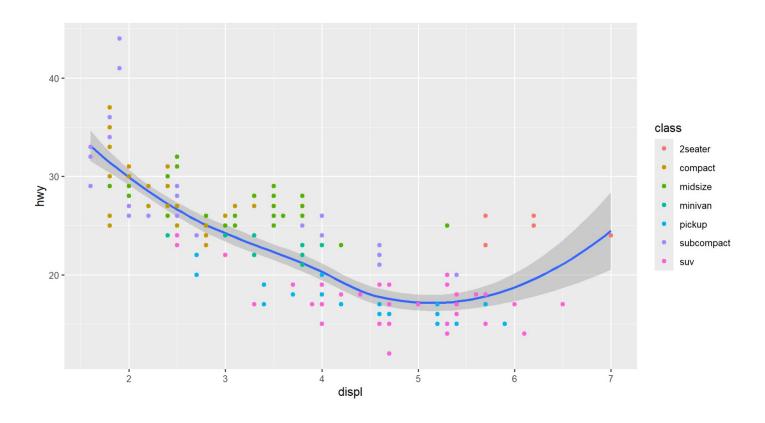
- To highlight details, there are more parameters that one can put in these functions
- MAPPINGS component provides ways of adding details to the plot, such as *shades*, *size*, *shape*, etc, to represent other variables / properties
- GEOM_FUNCTIONs can be combined by + them together, as above, and can also combine with other functions

Add color to represent other variables

```
ggplot(data = mpg) +
geom_point(mapping = aes(x = displ, y = hwy, color = class))
```



```
ggplot(data = mpg) +
geom_smooth(mapping = aes(x = displ, y = hwy)) +
geom_point(mapping = aes(x = displ, y = hwy, color = class))
```



Aesthetics matching variable type

Besides color, there are also

- alpha: the shades of the points
- size: the sizes of the points
- shape: the shapes of the points

Two classes of variable types:

- continuous: values may be continuously distributed, as on the real line
 - alpha and size
- categorical: values are discretely distributed, generally finitely many
 - shape
 - only 25 building shapes in R
- color can be used on both types

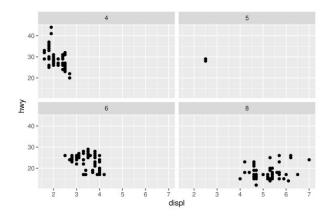
For categorical variables – also called factors, can also use the facet_ functions

• Plot data with different values on the variable separately

facet_wrap with respect to one variable

This generates a list of plots, each plotting a subset of the data, and the plots are titled by the value of the faceting variable

```
ggplot(data = mpg) +
geom_point(mapping = aes(x = displ, y = hwy)) +
#facet_wrap(~ class, nrow = 2) # test what would happen with ncol=2?
facet_wrap(~cyl)
```



facet_grid with respect to two variables

This generates a grid of plots, labelled across columns and rows by the values in the respective variable

```
ggplot(data = mpg) +
geom_point(mapping = aes(x = displ, y = hwy, color = class))+ facet_grid(drv ~
cyl)
```

