

# Capacitor

**Capacitance of a Conductor**  $C = q/V$

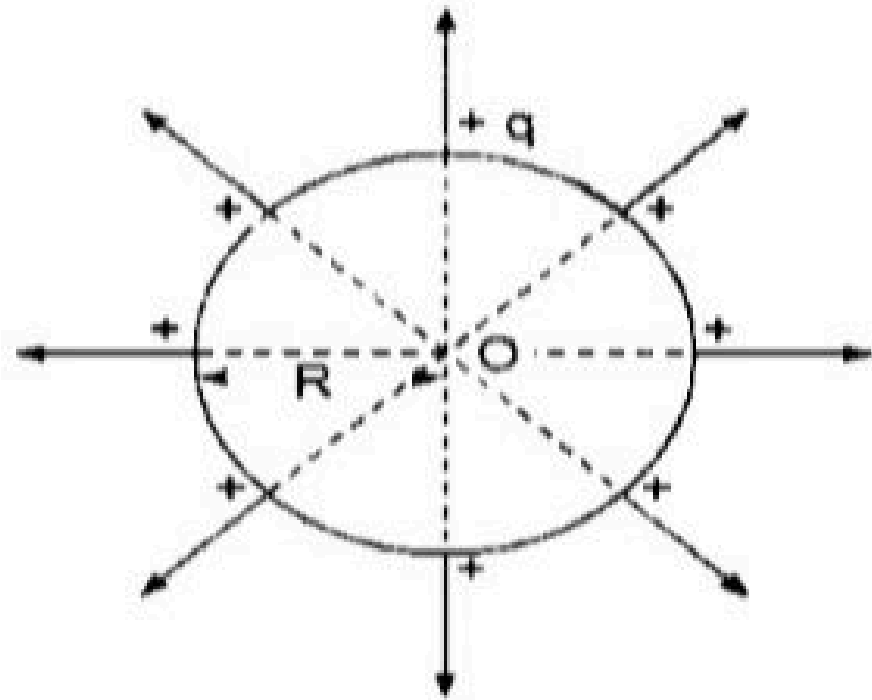
**Unit of Capacitance is 'coulomb/volt' or 'Farad'**

(Capacity of an Isolated Spherical Conductor)

$$C = \frac{q}{V} = \frac{q}{(q/4 \pi \epsilon_0 K R)}$$

$$\therefore C = 4 \pi \epsilon_0 K R$$

$$\text{if } K = 1 \quad \boxed{C_0 = 4 \pi \epsilon_0 R}$$



(Potential Energy of a charged Conductor)

$$U = \frac{1}{2} qV = \frac{1}{2} CV^2 = \frac{1}{2} \frac{q^2}{C} \quad \text{Joule}$$

(Energy Density)

$$u = \frac{U}{V_{\text{volume}}} = \frac{1}{2} \epsilon_0 E^2 \quad \text{Joule/meter}^3$$

Capacitance of a Parallel plate Capacitor  $C_0 = \frac{K\epsilon_0 A}{d}$

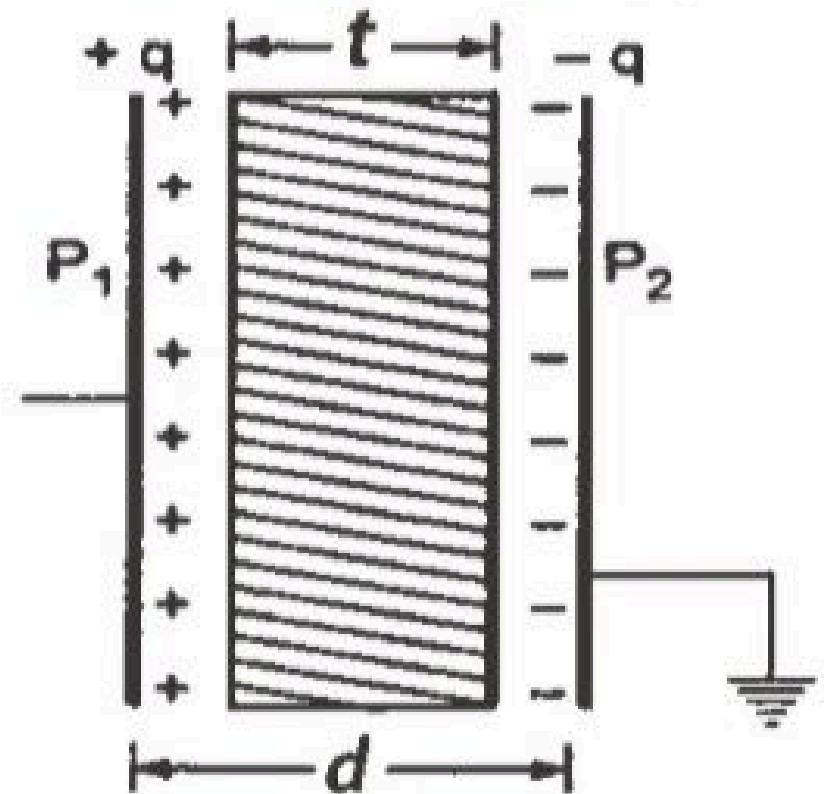
*Capacitance of a Parallel-Plate Capacitor depends on :-*

1. Area of plates '**A**'  $C \propto A$
2. Distance between the plates '**d**'  $C \propto 1/d$
3. Medium between the plates  $C \propto K$

When medium is air  $K=1$ ,  $C_0 = \frac{\epsilon_0 A}{d}$

## Capacity of Parallel Plate Capacitor Partially filled with Dielectric Substance

$$C = \frac{\epsilon_0 A}{\left[ (d - t) + \frac{t}{K} \right]}$$



## Special Conditions :-

1. If Capacitor is completely filled with dielectric, or ( $t = d$ )

then Capacitance 
$$C = \frac{\epsilon_0 A}{\left[ (d - d) + \frac{d}{K} \right]} = \frac{K\epsilon_0 A}{d} \text{ Farad}$$

2. If Capacitor is containing air only, or ( $t = 0$ )

then Capacitance 
$$C = \frac{\epsilon_0 A}{\left[ (d - 0) + \frac{0}{K} \right]} = \frac{\epsilon_0 A}{d} \text{ Farad}$$

3. If metal plate of thickness ' $t$ ' is placed between plates ( $K = \infty$ )

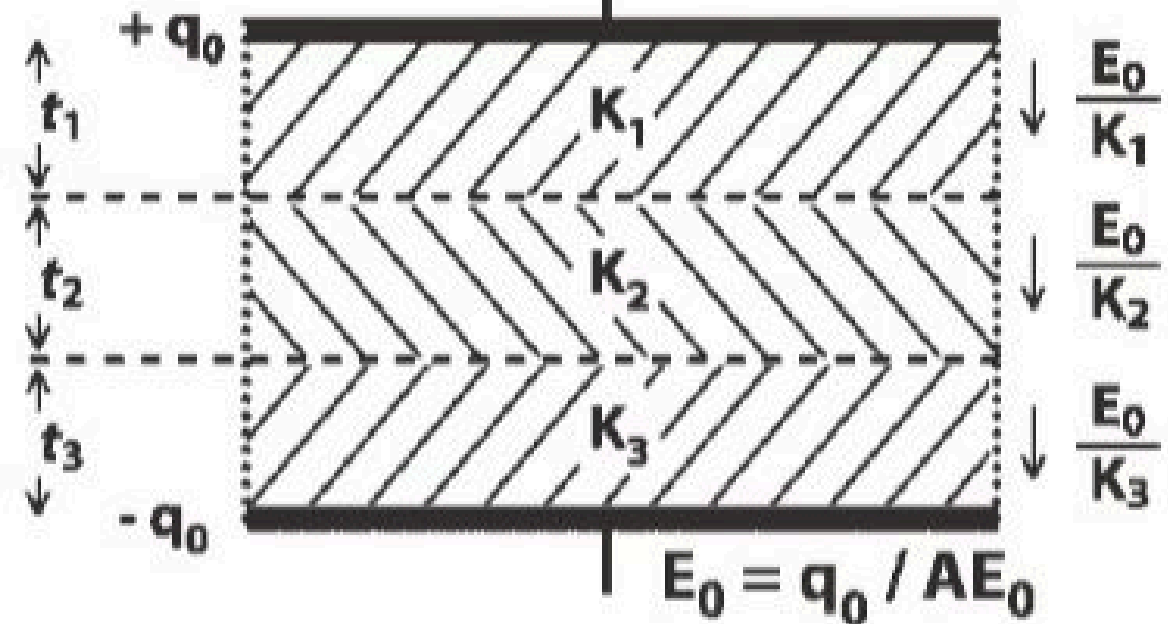
then Capacitance 
$$C = \frac{\epsilon_0 A}{\left[ (d - t) + \frac{t}{\infty} \right]} = \frac{\epsilon_0 A}{(d - t)} \text{ Farad}$$

4. if  $K_1, K_2, K_3, \dots, K_n$

Dielectrics is placed between plates whose thickness are

$t_1, t_2, t_3, \dots, t_n$

then :-

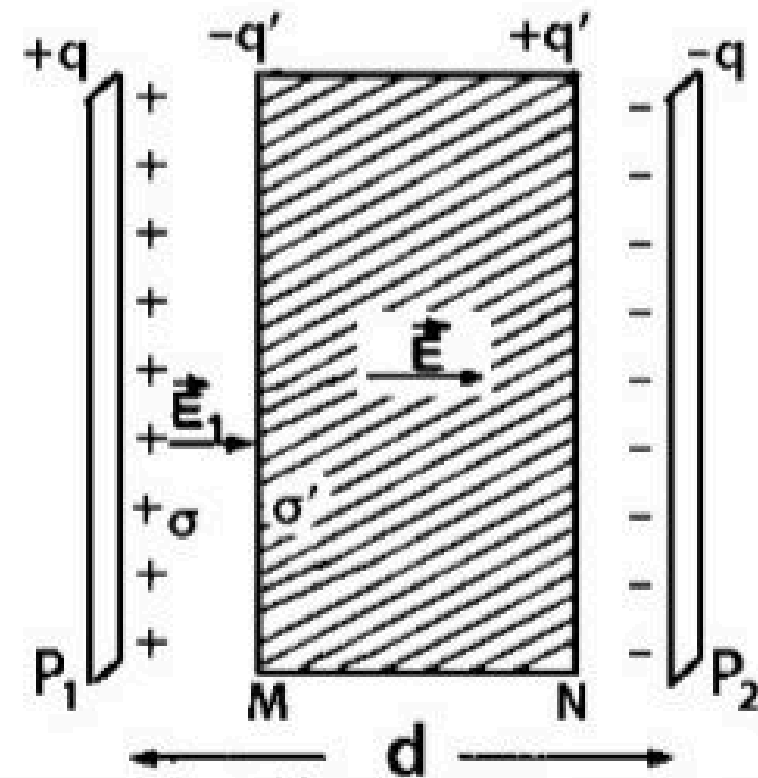


$$C = \frac{\epsilon_0 A}{\left[ d - (t_1 + t_2 + t_3 + \dots + t_n) + \frac{t_1}{K_1} + \frac{t_2}{K_2} + \frac{t_3}{K_3} + \dots + \frac{t_n}{K_n} \right]}$$

**Magnitude of induced charge on Dielectric :-**

$$q' = q \left( 1 - \frac{1}{K} \right)$$

$$\sigma' = \sigma \left( 1 - \frac{1}{K} \right)$$



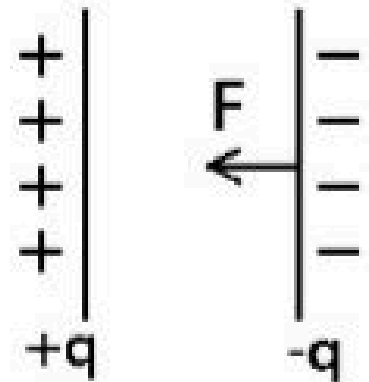
**Parallel plate capacitor attract with force :-**

$$F = \frac{q^2}{2A \epsilon_0}$$

or

$$\frac{F}{A} = \frac{\sigma^2}{2 \epsilon_0}$$

(Electrostatic stress)



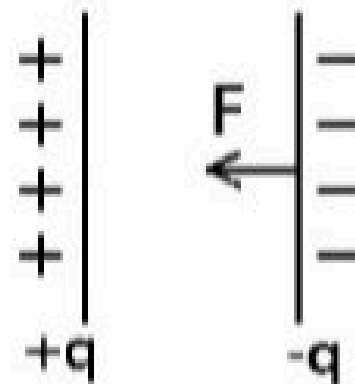
**Parallel plate capacitor attract with force :-**

$$F = \frac{q^2}{2A \epsilon_0}$$

or

$$\frac{F}{A} = \frac{\sigma^2}{2 \epsilon_0}$$

(Electrostatic stress)

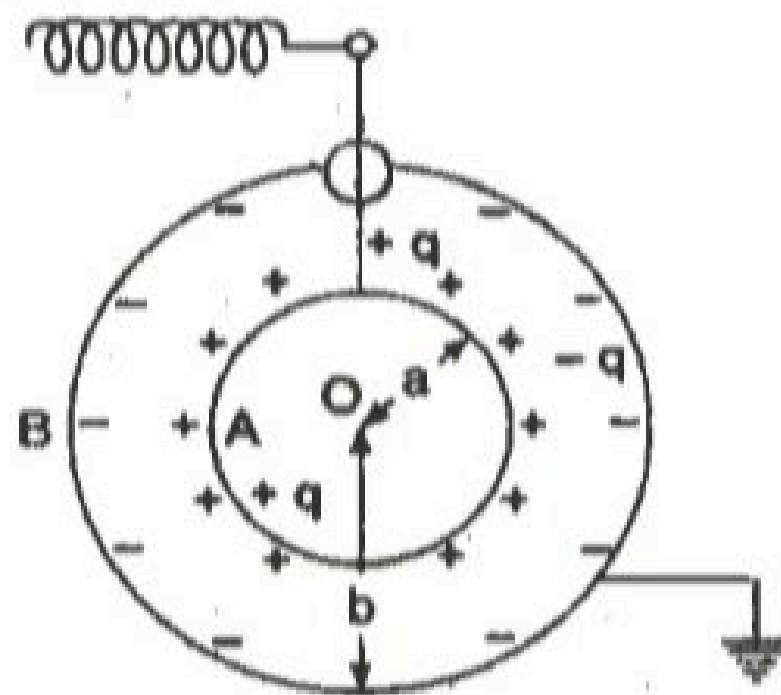


**(Capacitance of Spherical Capacitor)**

$$C = 4 \pi \epsilon_0 K \left( \frac{ab}{b - a} \right)$$

if  $K = 1$

$$C_0 = 4 \pi \epsilon_0 \left( \frac{ab}{b - a} \right)$$

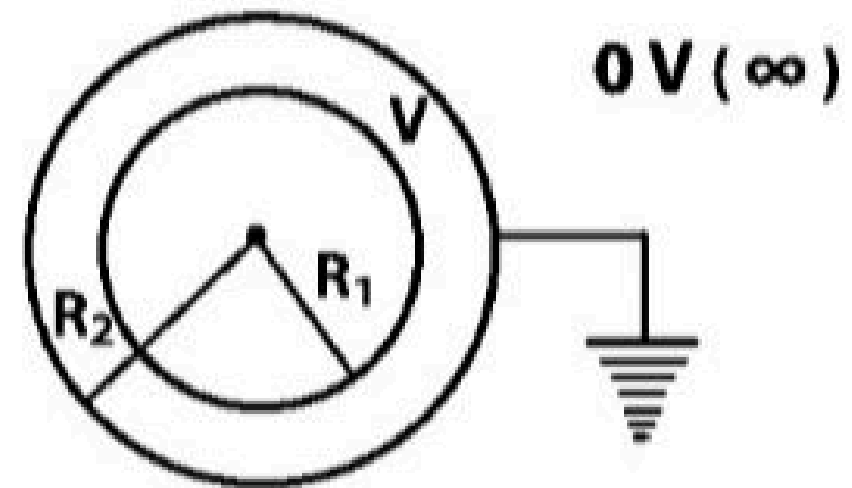




## Capacitance of spherical capacitor under different earthing condition :-

1) no electric field between outer plate and  $\infty$

$$C = \frac{4\pi\epsilon_0 R_2 R_1}{R_2 - R_1}$$

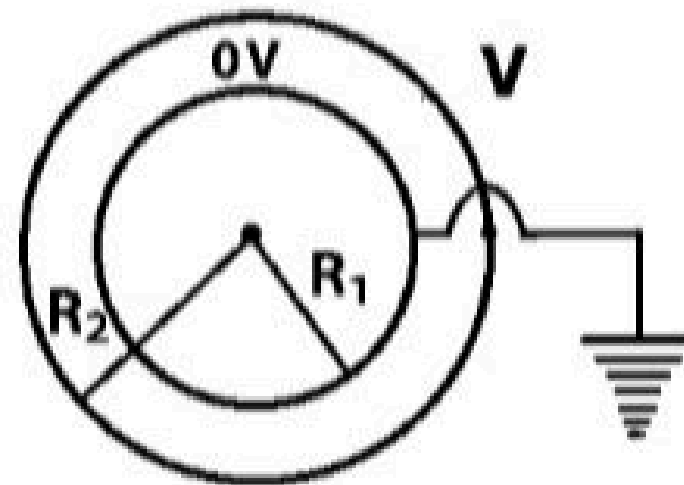


2) Two capacitors present between inner and outer and Infinity ( In Parallel ) with Potential Difference

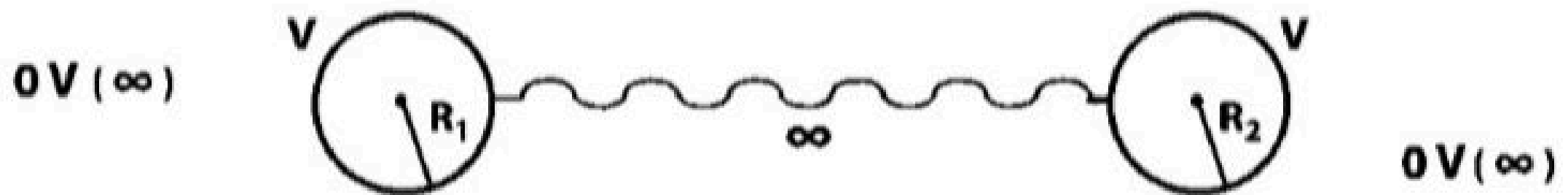
$$C = \frac{4\pi\epsilon_0 R_2 R_1}{R_2 - R_1} + 4\pi\epsilon_0 R_2$$

$0V (\infty)$

$$C = \frac{4\pi\epsilon_0 R_2^2}{R_2 - R_1}$$



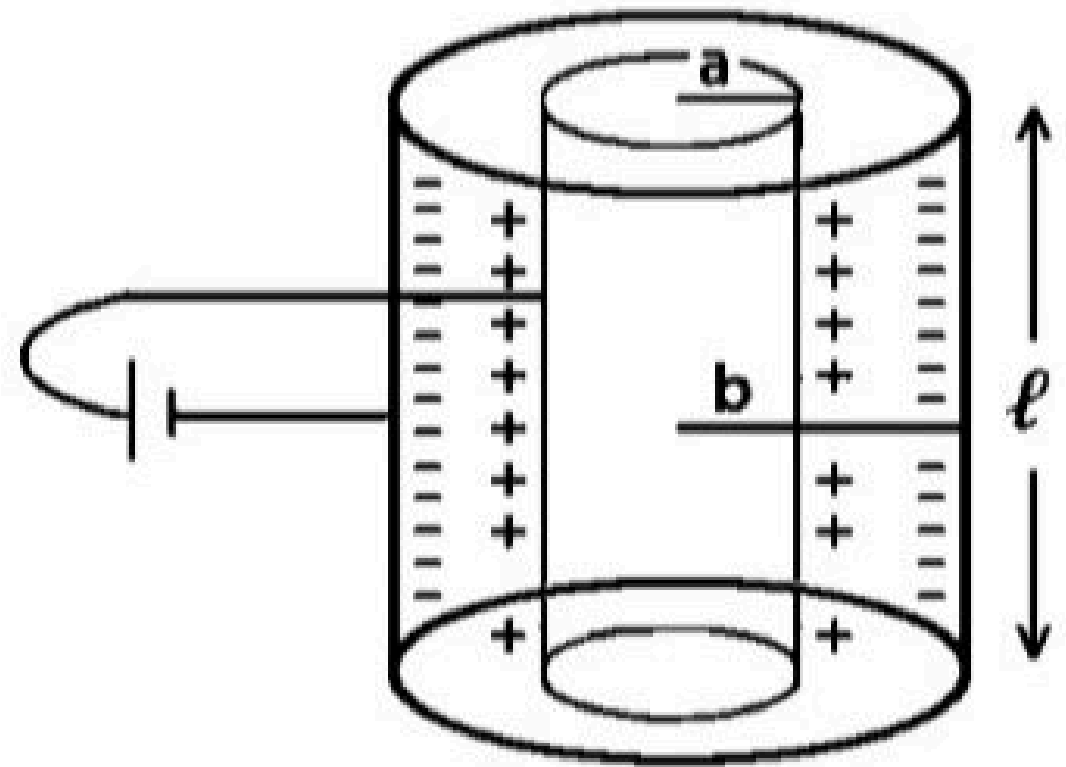
3) Two capacitors joined in parallel (Same P. D. b / w  $V$  and  $\infty$ )



$$C = 4\pi\epsilon_0 R_1 + 4\pi\epsilon_0 R_2$$

# Cylindrical capacitor

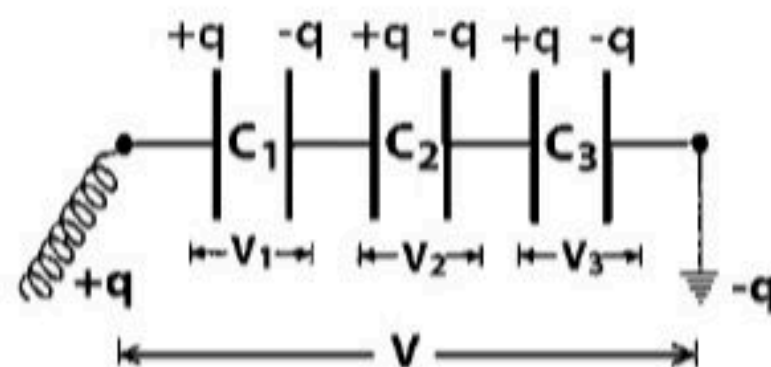
$$C = \frac{2 \pi \epsilon_0 \ell}{\ln(b/a)}$$



## Capacitor connected in Series.

$$V_1 = \frac{q}{C_1}, \quad V_2 = \frac{q}{C_2}, \quad V_3 = \frac{q}{C_3}$$

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$



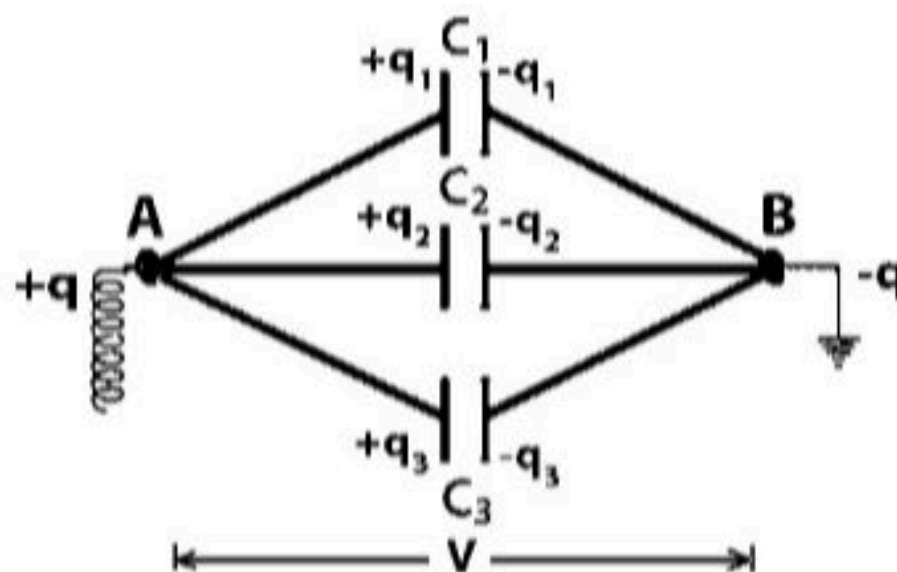
## Capacitor connected in Parallel

$$q_1 = C_1 V$$

$$q_2 = C_2 V$$

$$q_3 = C_3 V$$

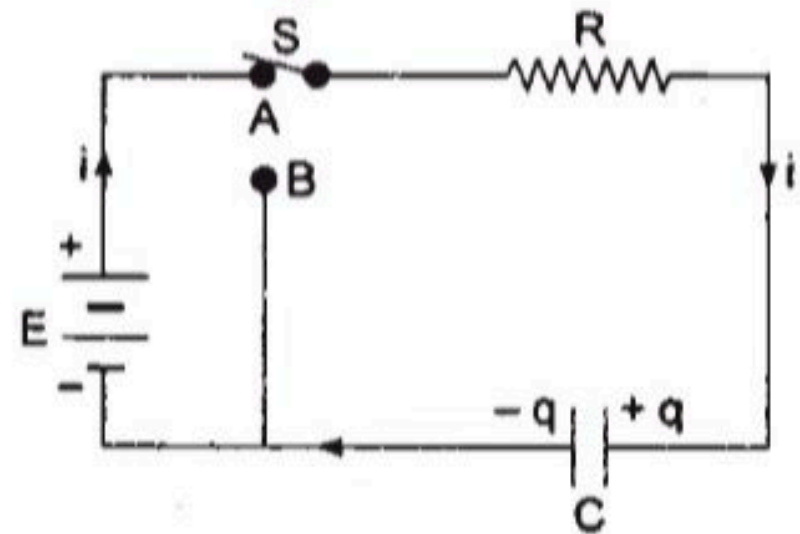
$$C = C_1 + C_2 + C_3$$



## (Charging of a Capacitor through Resistance)

$$q_0 = EC \text{ Maximum Charge}$$

**CR** is the time constant of circuit

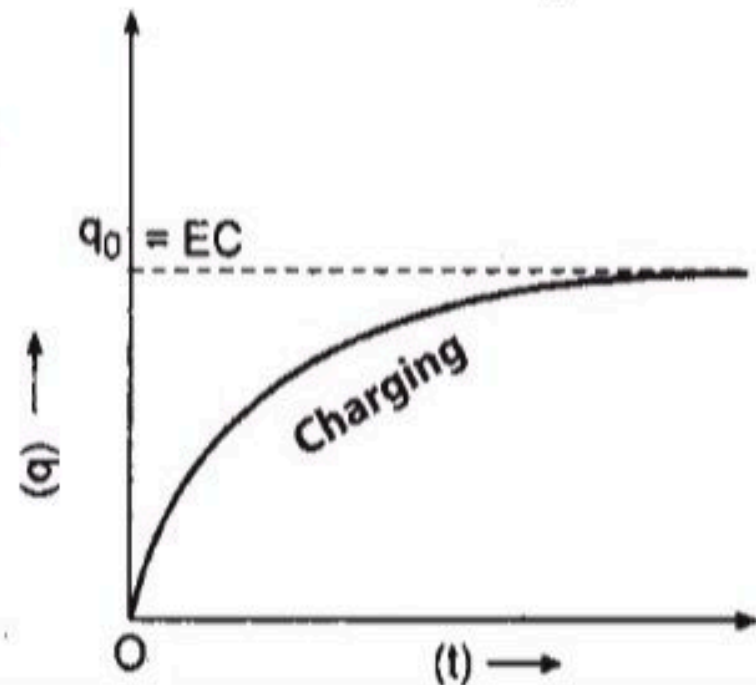


$$q = q_0 (1 - e^{-t/CR}) \longrightarrow$$

Charging current of circuit

$$i = \frac{dq}{dt} = \left( \frac{q_0}{CR} \right) e^{-t/CR}$$

$$i = i_0 e^{-t/CR} \quad i_0 = \frac{q_0}{CR}$$



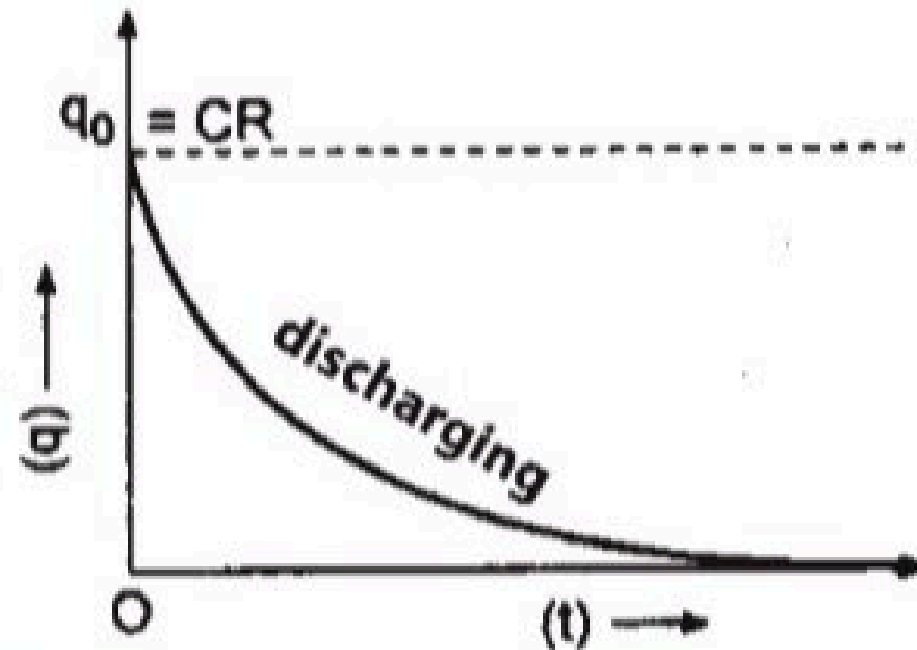
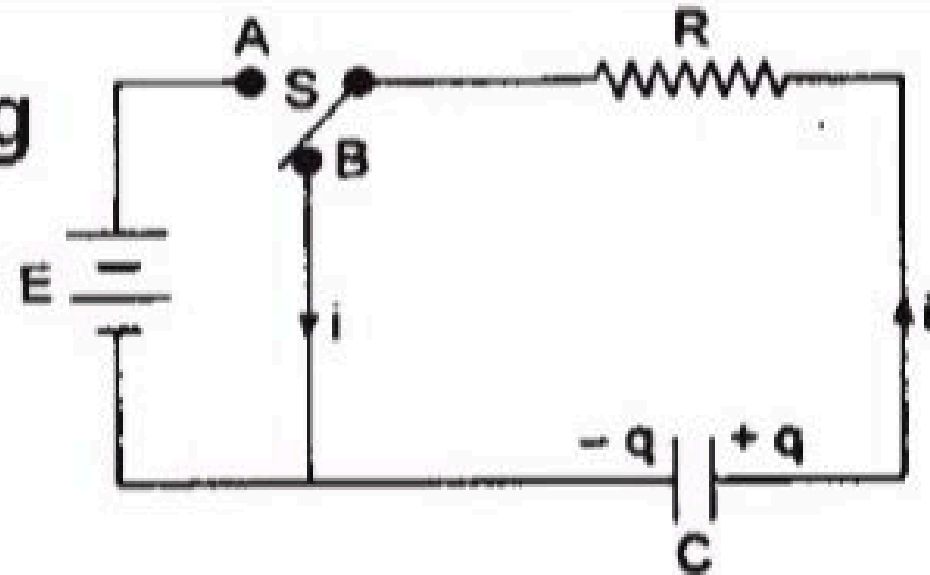
## Discharging of capacitor using Resistor

$$q = q_0 e^{-t/CR}$$

$$i = \frac{dq}{dt} = -q_0 \left( \frac{1}{CR} \right) e^{-t/CR}$$

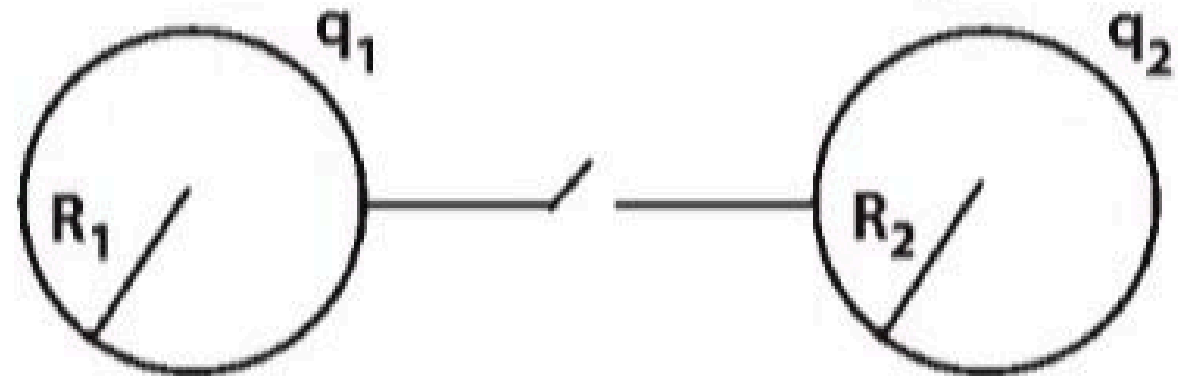
$$i = i_0 e^{-t/CR}$$

$$i_0 = \frac{q_0}{CR}$$



Conducting sphere connected to each other by a wire :-

$$\frac{\sigma_1}{\sigma_2} = \frac{R_2}{R_1}$$



$\sigma_1$  and  $\sigma_2$  is charge densities on two sphere