

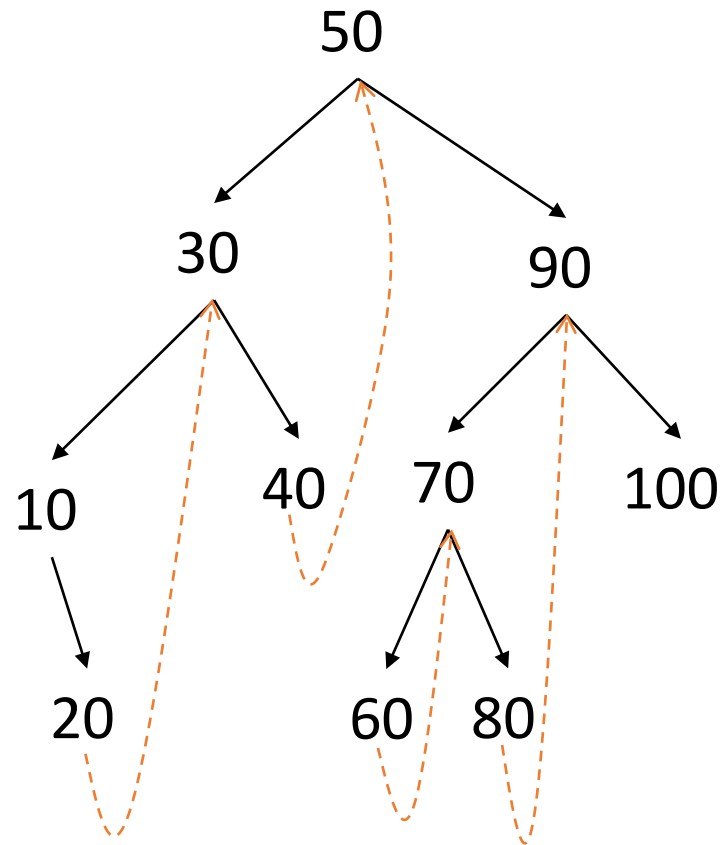


Data Structure & Algorithms

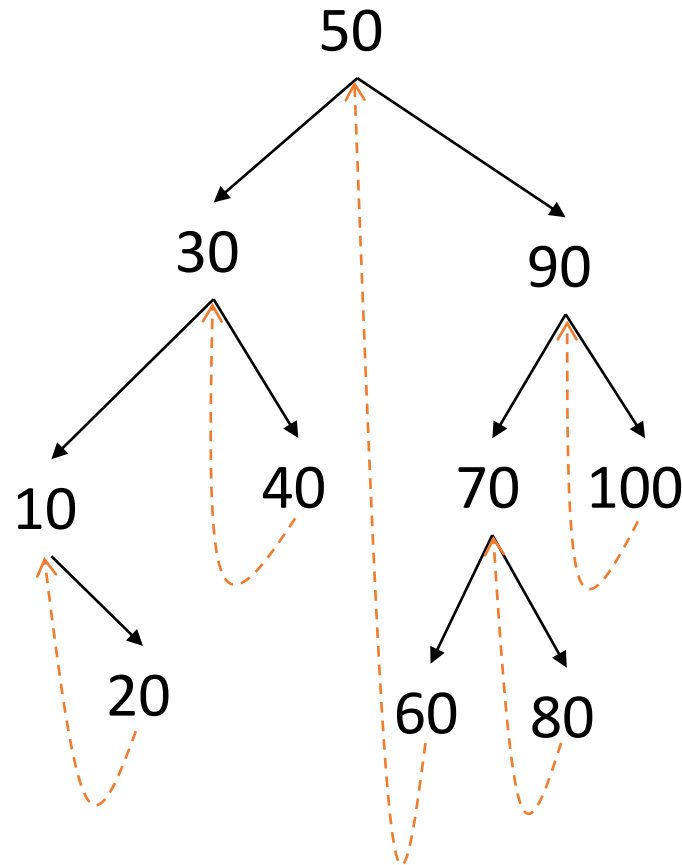
Nilesh Ghule



Threaded BST - fast in-order traversal



right-threaded
BST

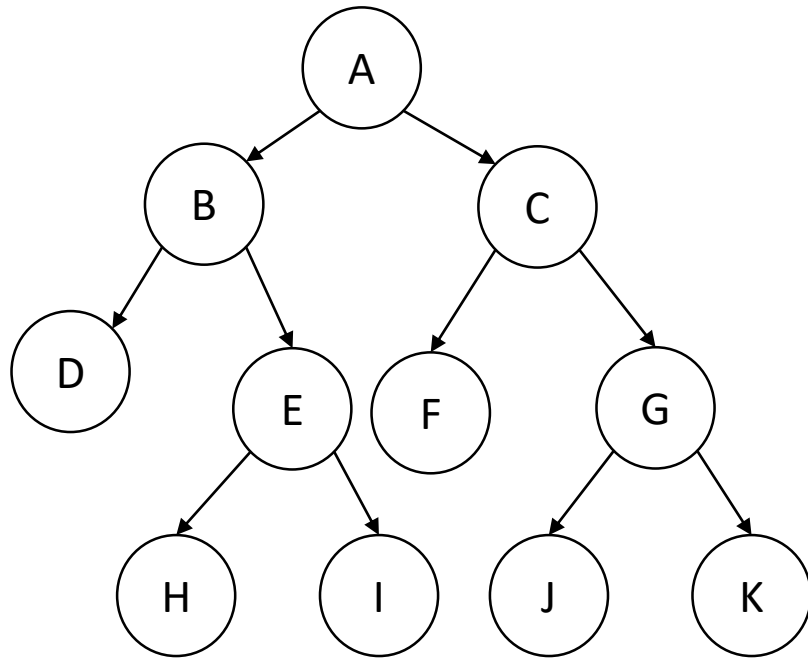


left-threaded
BST

- Typical BST in-order traversal involves recursion or stack. It slows execution and also need more space.
- Threaded BST keep address of in-order successor or predecessor addresses instead of NULL to speed up in-order traversal (using a loop).
- Left threaded BST +
- Right threaded BST
- In-threaded BST =



Strict/Full Binary Tree



- Binary tree in which each non-leaf node has exactly two child nodes.

single child node is not allowed,
either 0 or 2 child nodes.

Perfect Binary Tree

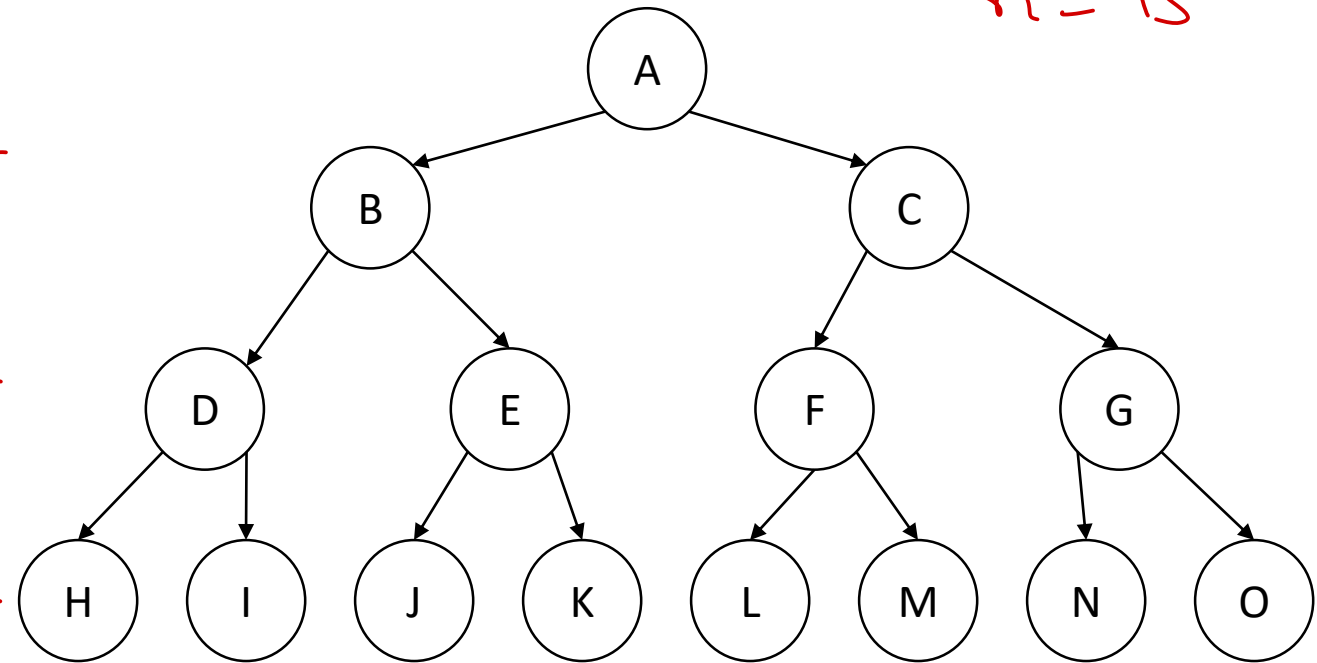
null tree height = -1

3 -

2 -

1 -

0 -



$n = 15$

- Binary tree which is full for the given height i.e. contains maximum possible nodes.

Number of Leaf = 2^h

Number of Non-Leaf = $2^h - 1$

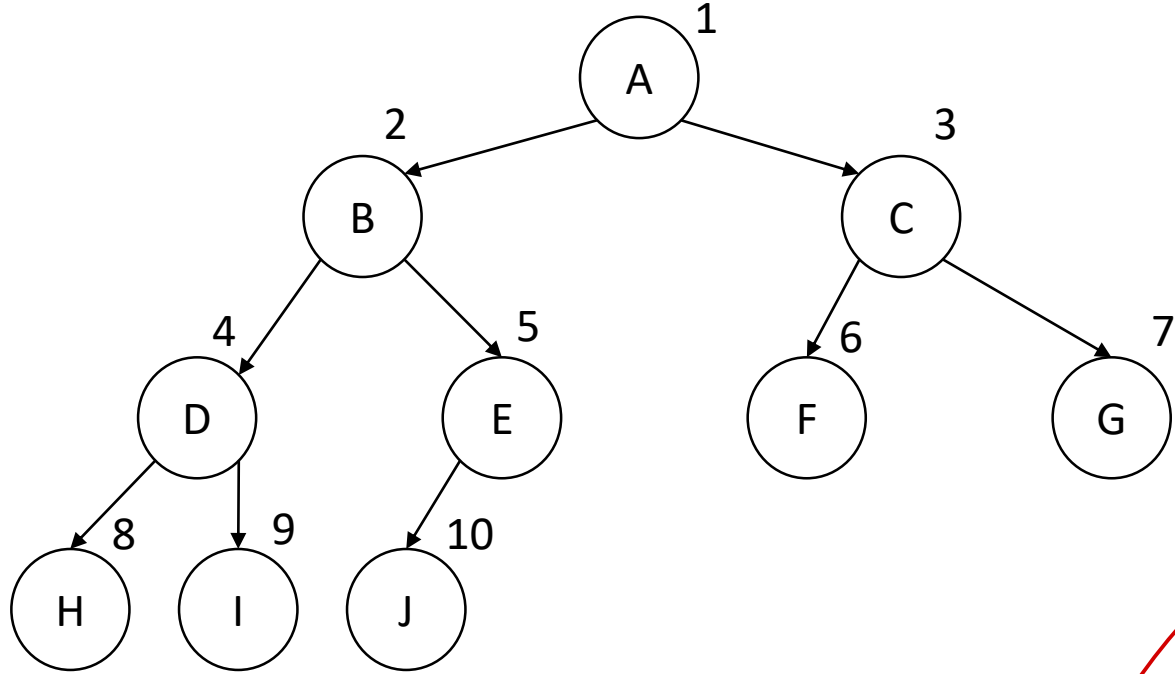
- Number of nodes = ~~$2^h - 1$~~

$2^{h+1} - 1$



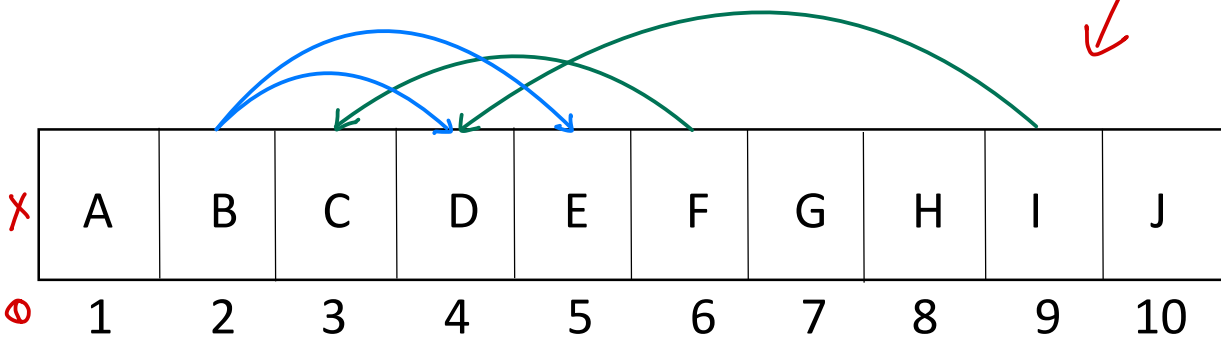
Complete Binary Tree and Heap

tree : hierarchical : parent-child

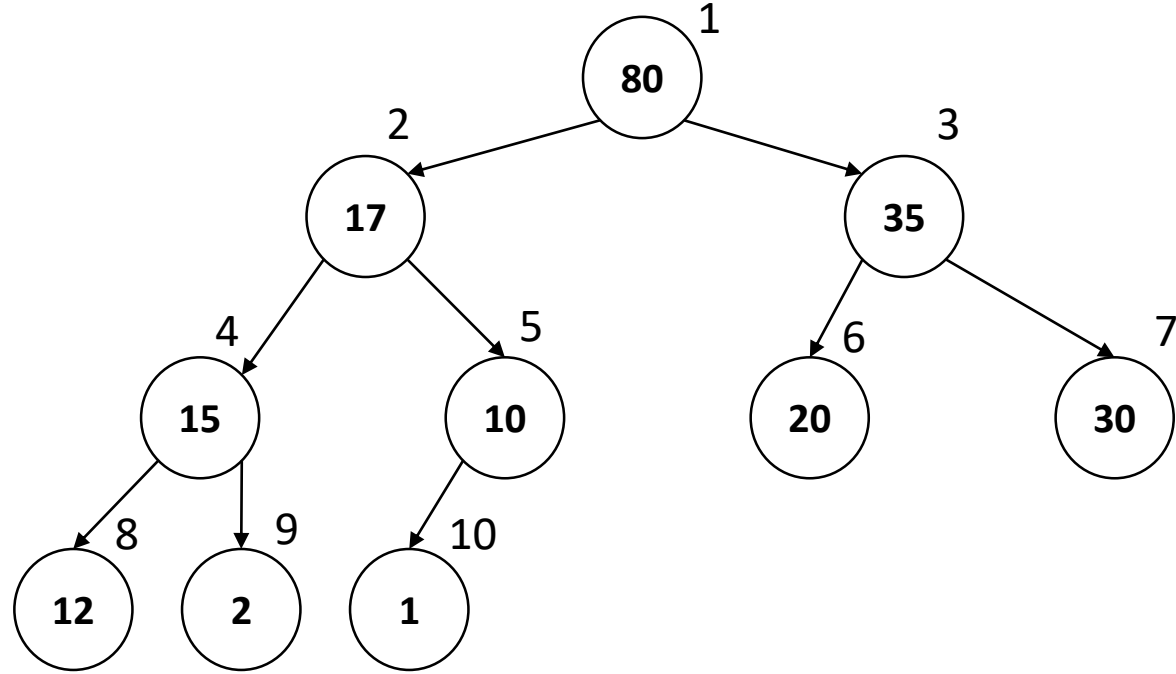


- A complete binary tree is a binary tree in which every level, except possibly the last, is completely filled, and all nodes are as far left as possible. → in last level.

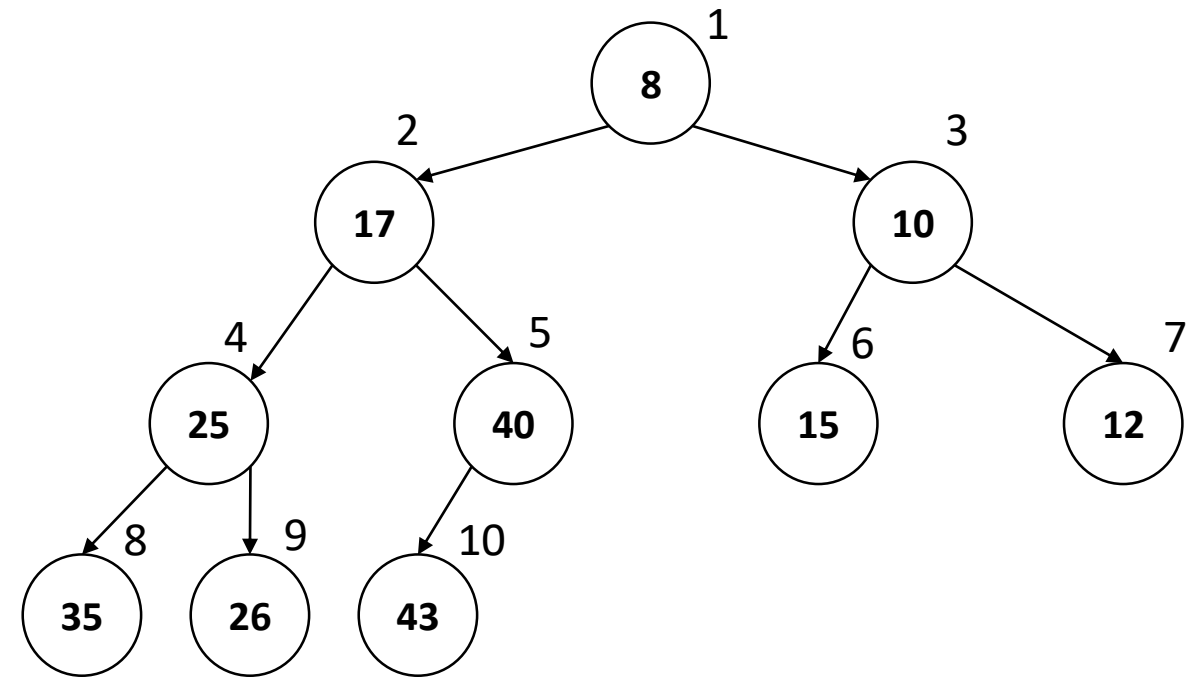
- Heap is array implementation of complete binary tree.
- Parent child relation is maintained through index calculations
 - parent index = child index / 2
 - left child index = parent index * 2
 - right child index = parent index * 2 + 1



Max Heap & Min Heap



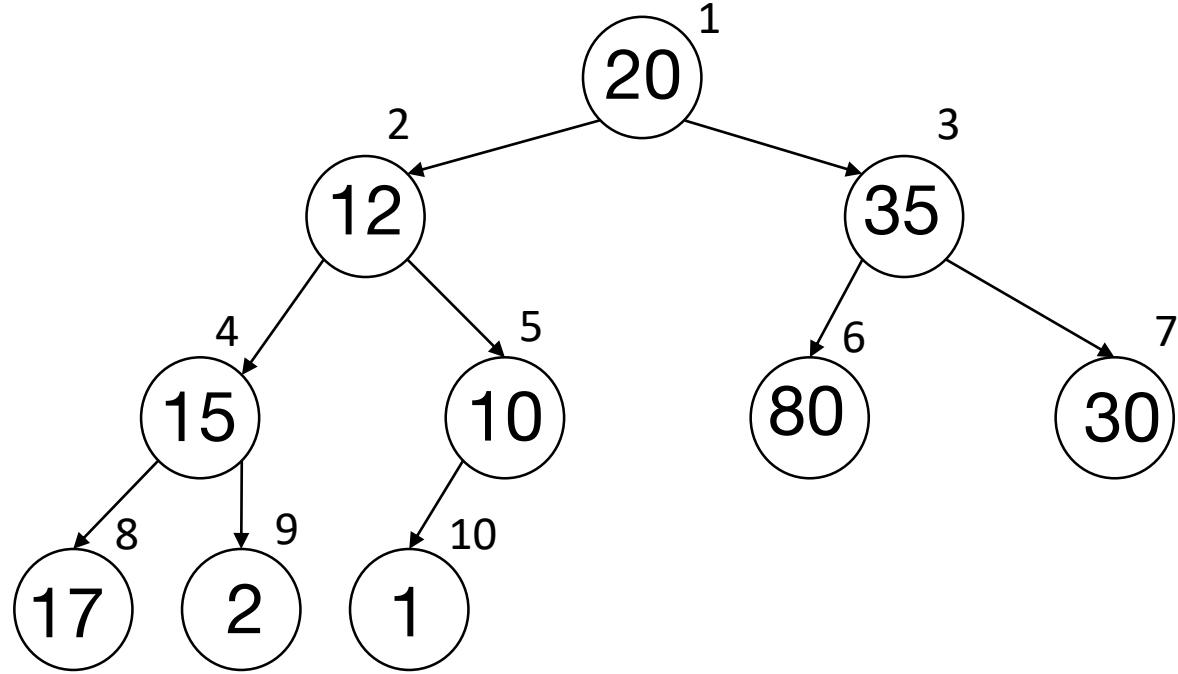
- Max heap is a heap data structure in which each node is greater than both of its child nodes.



- ~~Max~~ ^{Min} heap is a heap data structure in which each node is smaller than both of its child nodes.



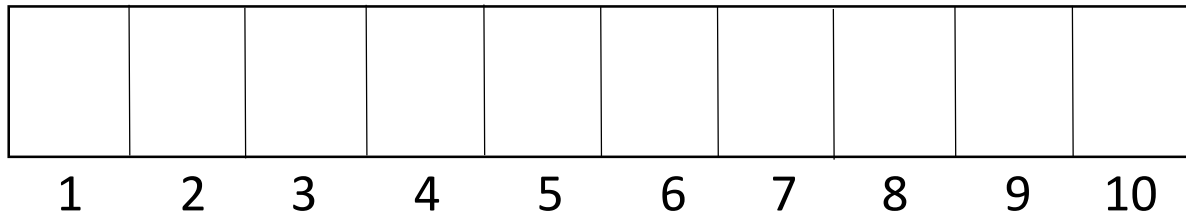
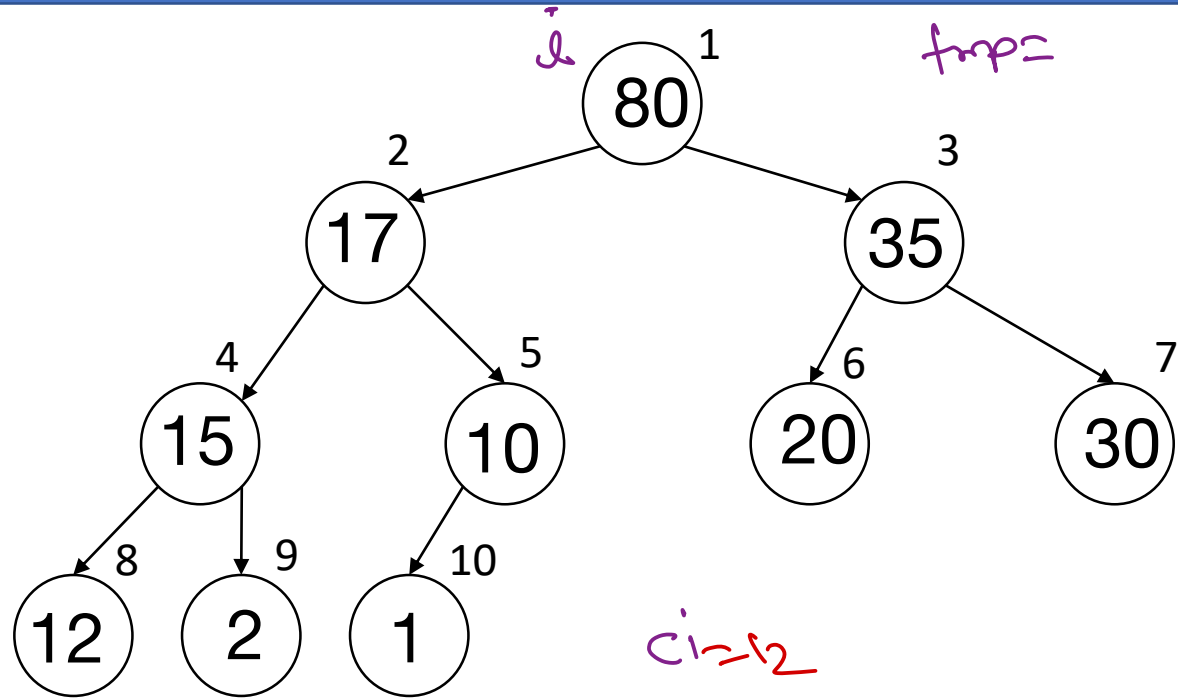
Max Heap – Initialize



20	12	35	15	10	80	30	17	2	1
1	2	3	4	5	6	7	8	9	10



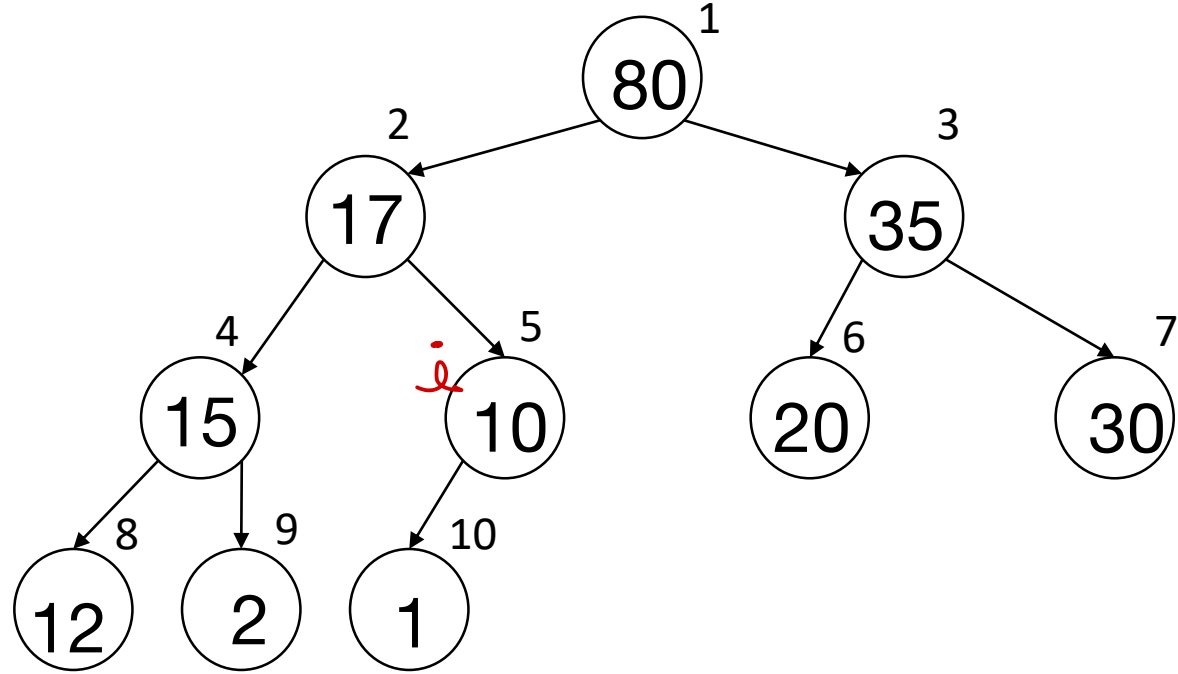
Max Heap – Initialize



```
size = arr.length - 1; → 10  
for (i = size/2; i >= 1; i--) {  
    temp = arr[i];  
    ci = i * 2;  
    while (ci <= size) {  
        if (arr[ci+1] > arr[ci])  
            ci++;  
        if (temp > arr[ci])  
            break;  
        arr[ci/2] = arr[ci];  
        ci = ci * 2;  
    }  
    arr[ci/2] = temp;  
}
```



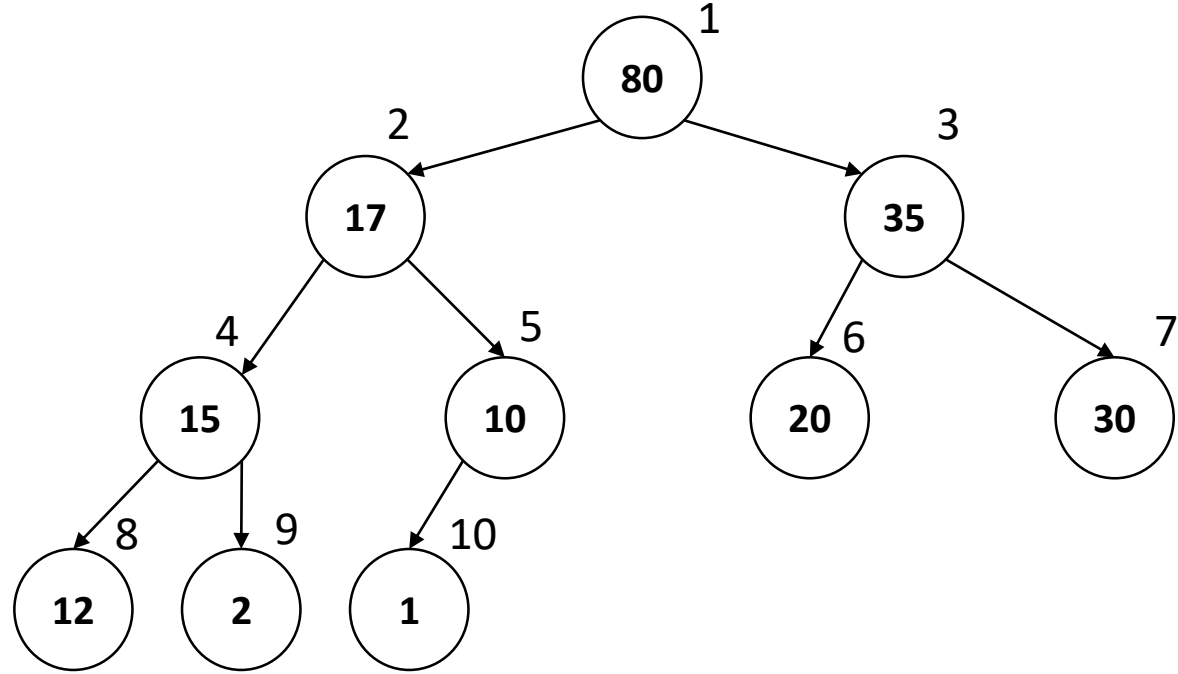
Max Heap – Initialize



80	17	35	15	10	20	30	12	2	1
1	2	3	4	5	6	7	8	9	10



Max Heap

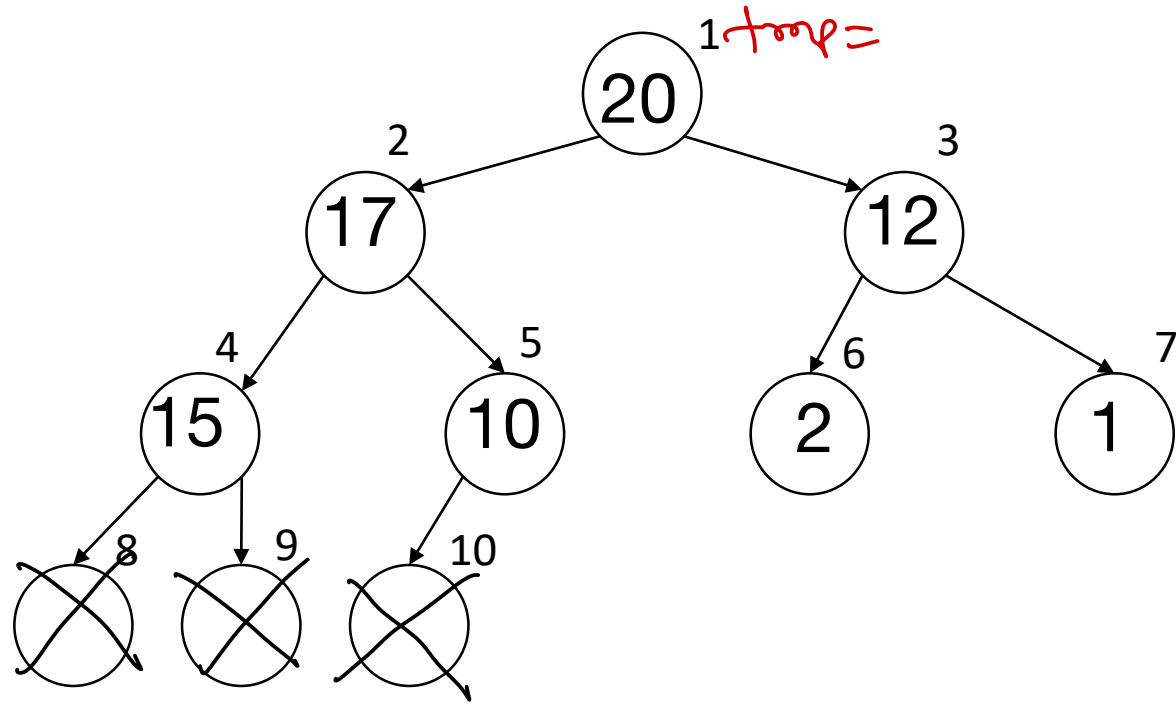


80	17	35	15	10	20	30	12	2	1
1	2	3	4	5	6	7	8	9	10



Max Heap – Delete Element

80 35 30

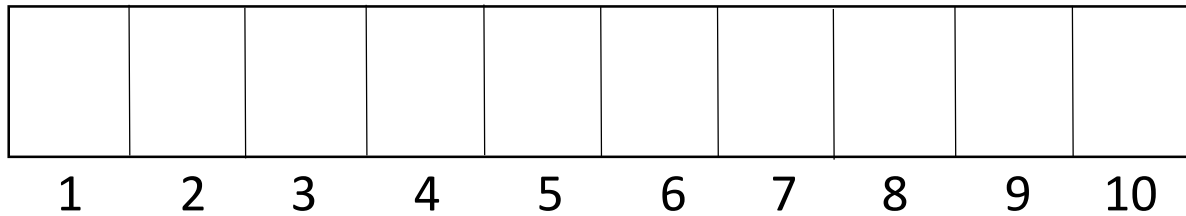


find 3rd highest elem of the array.

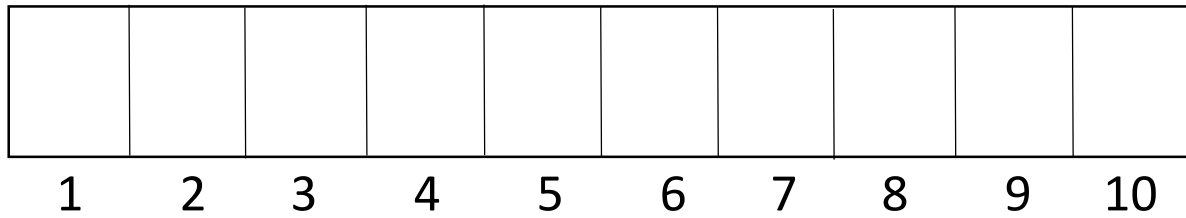
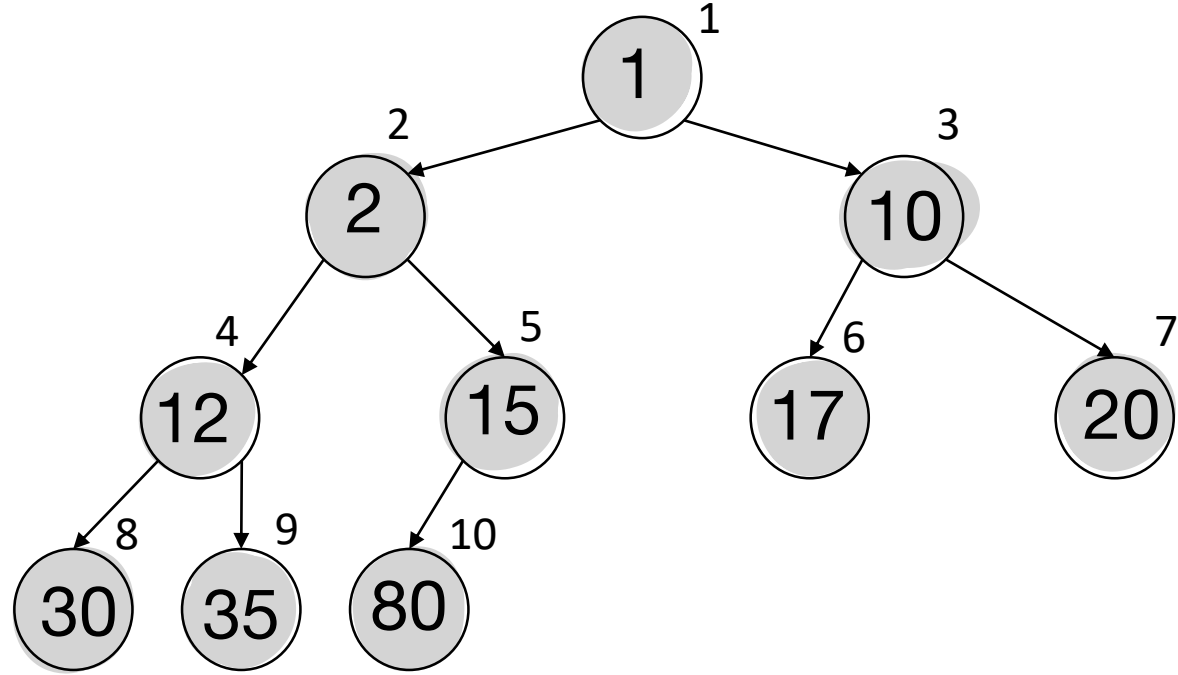
Step 1: convert into max heap.

Step 2: delete 2 elems one by one.

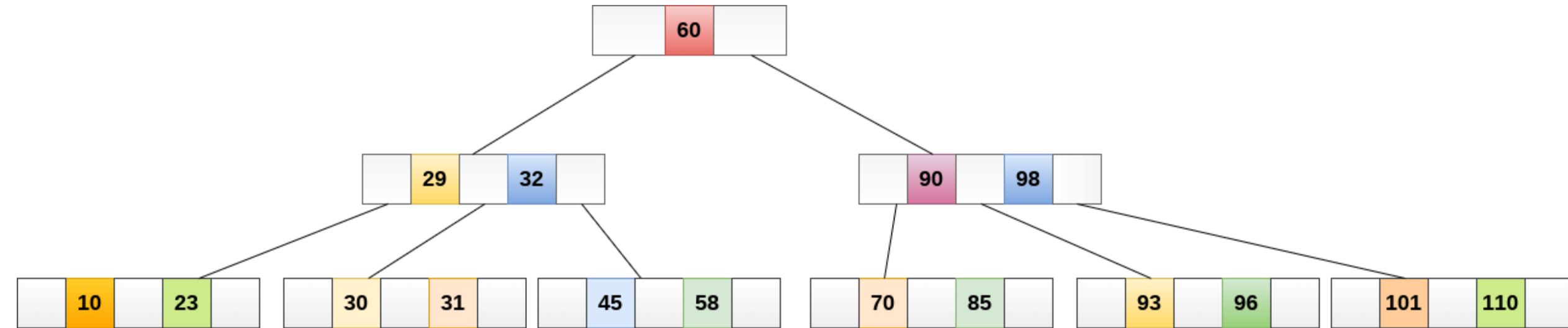
Step 3: return root → arr[0];



Heap Sort



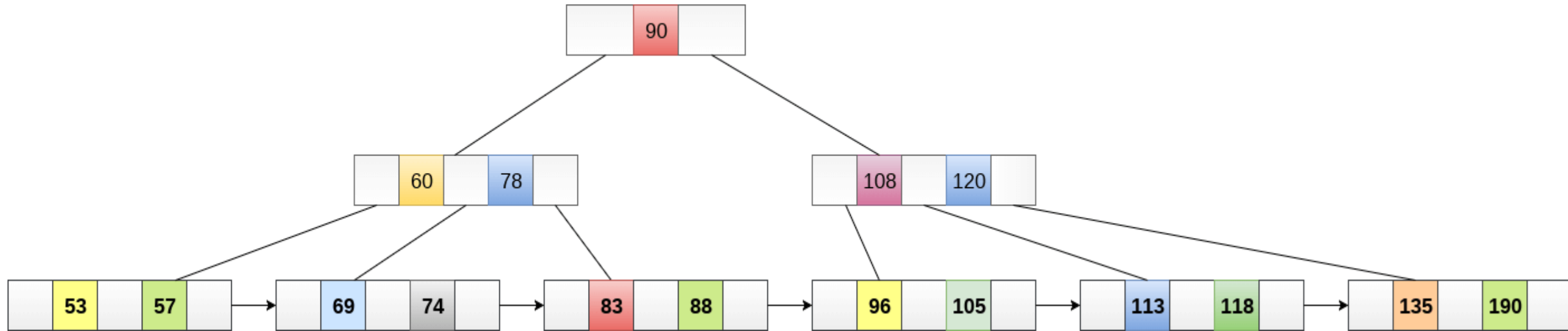
B Tree



- A B-Tree of order m can have at most $m-1$ keys and m children.
- B tree store large number of keys in a single node. This allows storing number of values keeping height minimal.
- Note that in B-Tree all leaf nodes are at same level.
- B-Tree is commonly used for indexing into file systems and databases. It ensures quick data searching and speed up disk access.



B+ Tree



- Extension of B-Tree for efficient insert, delete and search operation.
- Data is stored in leaf nodes only and all leaf nodes are linked together for sequential access.
- Search keys may be redundant.
- Faster searching, simplified deletion (as only from leaf nodes).
- B+Tree is commonly used for indexing into file systems and databases. It ensures quick data searching and speed up disk access.



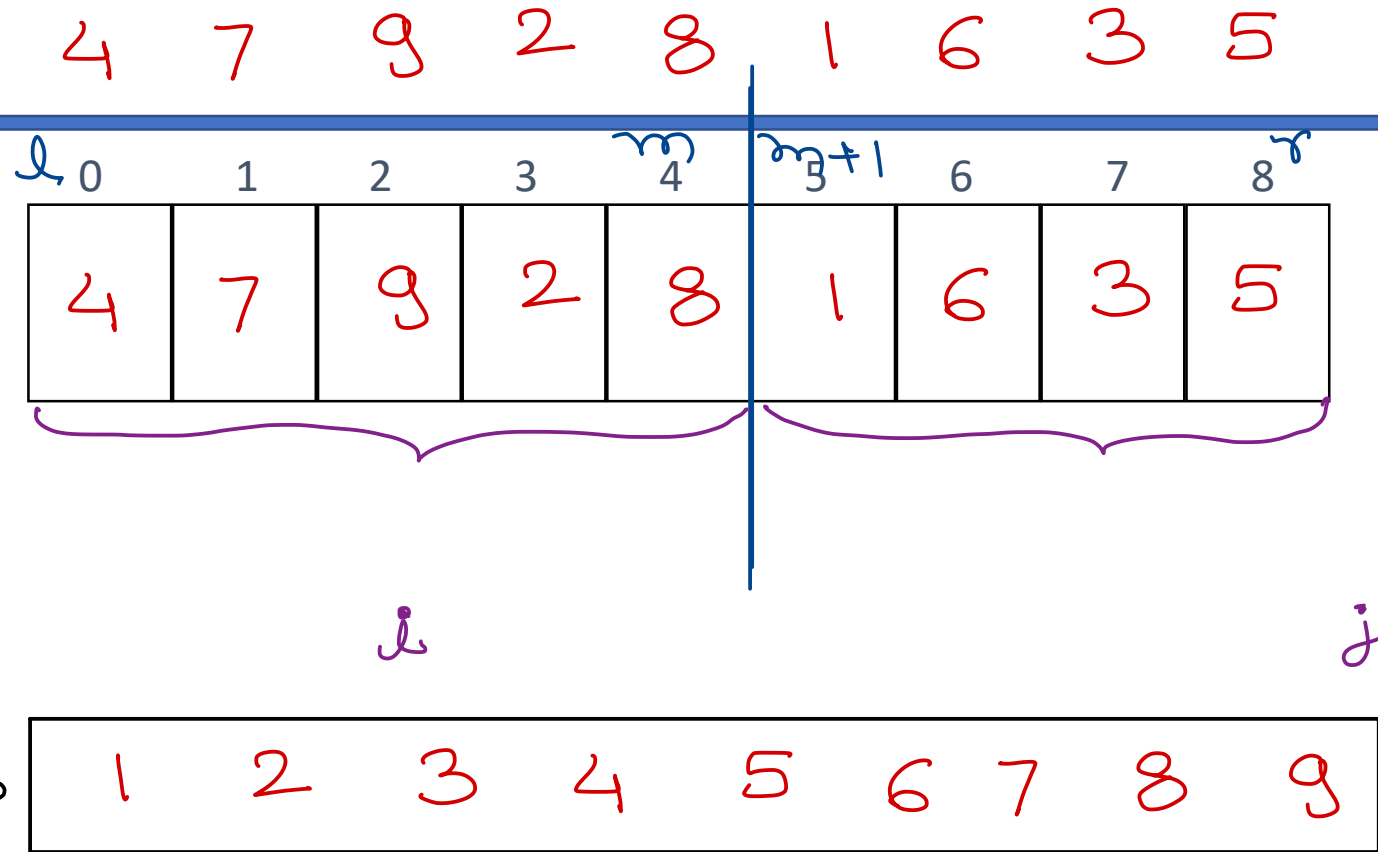
Merge Sort

merge two sorted partitions into a single array

```

if (l >= r)
    return;
m = (l + r) / 2;
mergesort(arr, l, m);
mergesort(arr, m + 1, r);
i = left; j = m + 1; k = 0;
temp = new int[r - l + 1];
while (i <= m && j <= r) {
    if (a[i] < a[j]) {
        temp[k] = a[i];
        i++; k++;
    }
    else {
        temp[k] = a[j];
        j++; k++;
    }
}

```



```

while (i <= m) {
    temp[k] = a[i];
    i++; k++;
}
while (j <= r) {
    temp[k] = a[j];
    j++; k++;
}

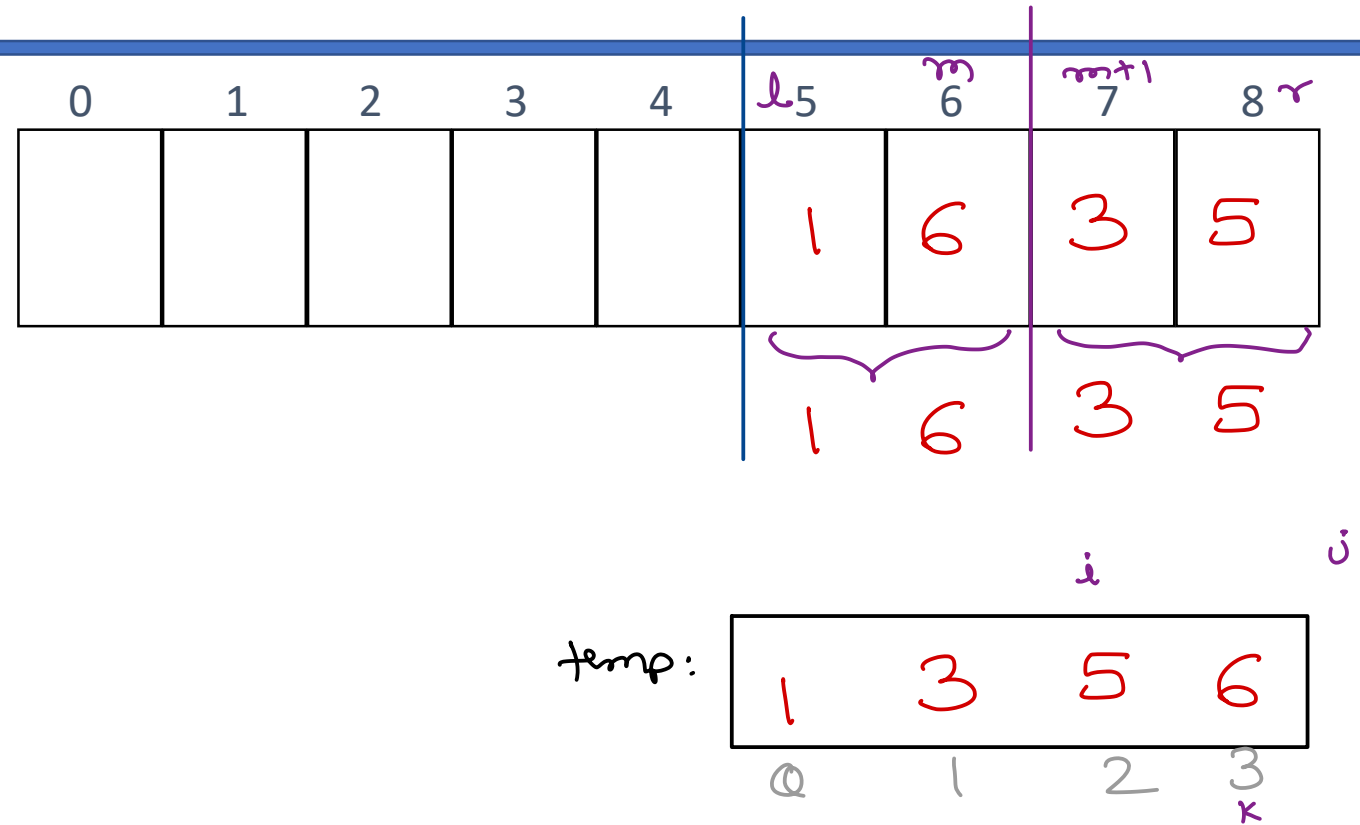
```

```

for (k = 0; k < temp.length; k++)
    a[l + k] = temp[k];

```

Merge Sort





Thank you!

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