



Data Structure & Algorithms

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Linked List – Competitive programming

- Sort the singly linked list.



Given a string, count occurrence of each alphabet.

ABCBCDADE

A → 2✓

B → 2✓

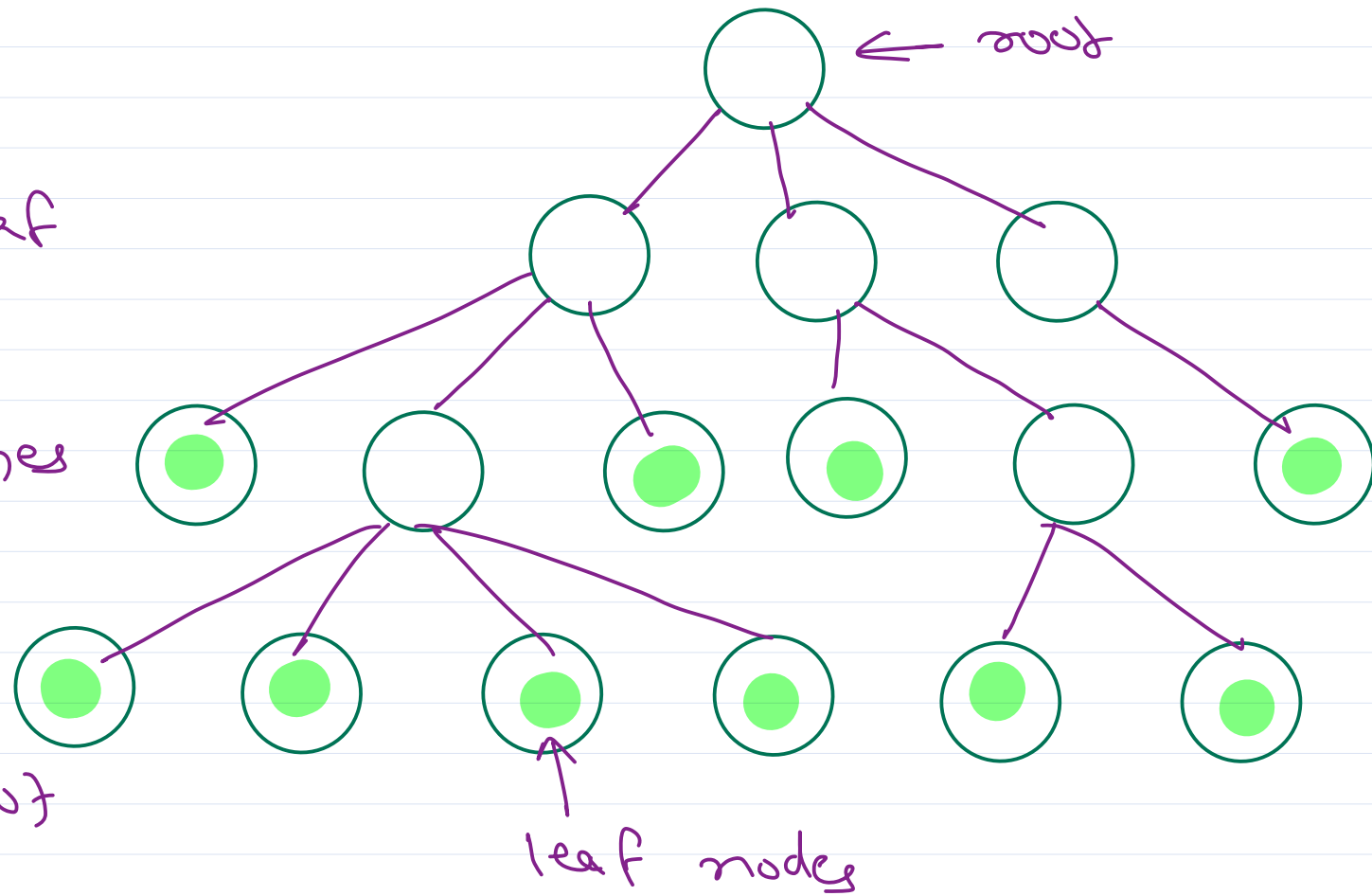
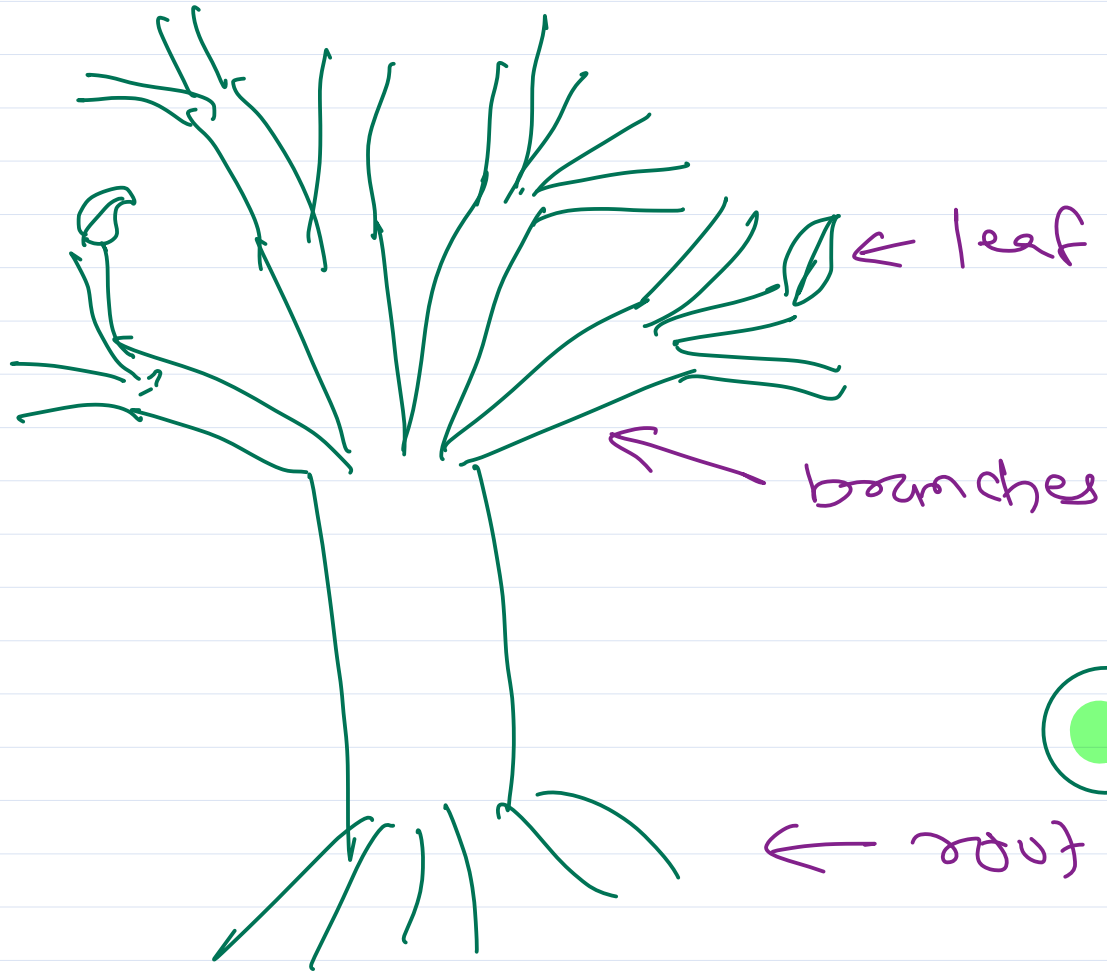
C → 3✓

D → 2✓

→ 0	0 2	A
1	0 2	B
2	0 1 3	C
3	0 1 2	D
4	0	E
5	0	F
	⋮	
	⋮	
	⋮	
	⋮	
25	0	Z

$T \propto n$ (n is length of string).
→ $O(n)$.





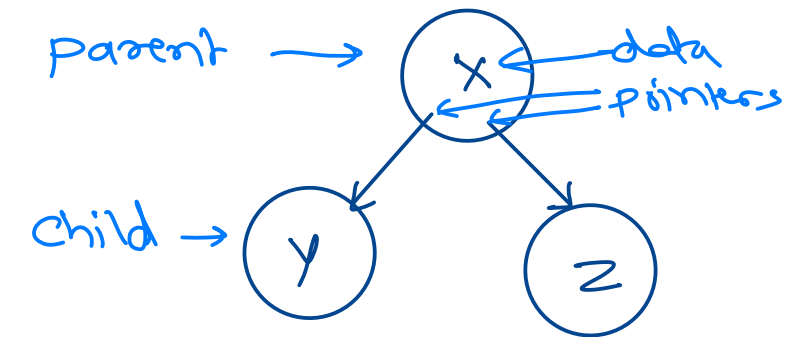
Tree Definition

- Tree is a finite set of nodes with one specially designated node called the “**root**” and the remaining node are partitioned into disjoint sets T_1 to T_n , where each of those sets is a TREE.

degree

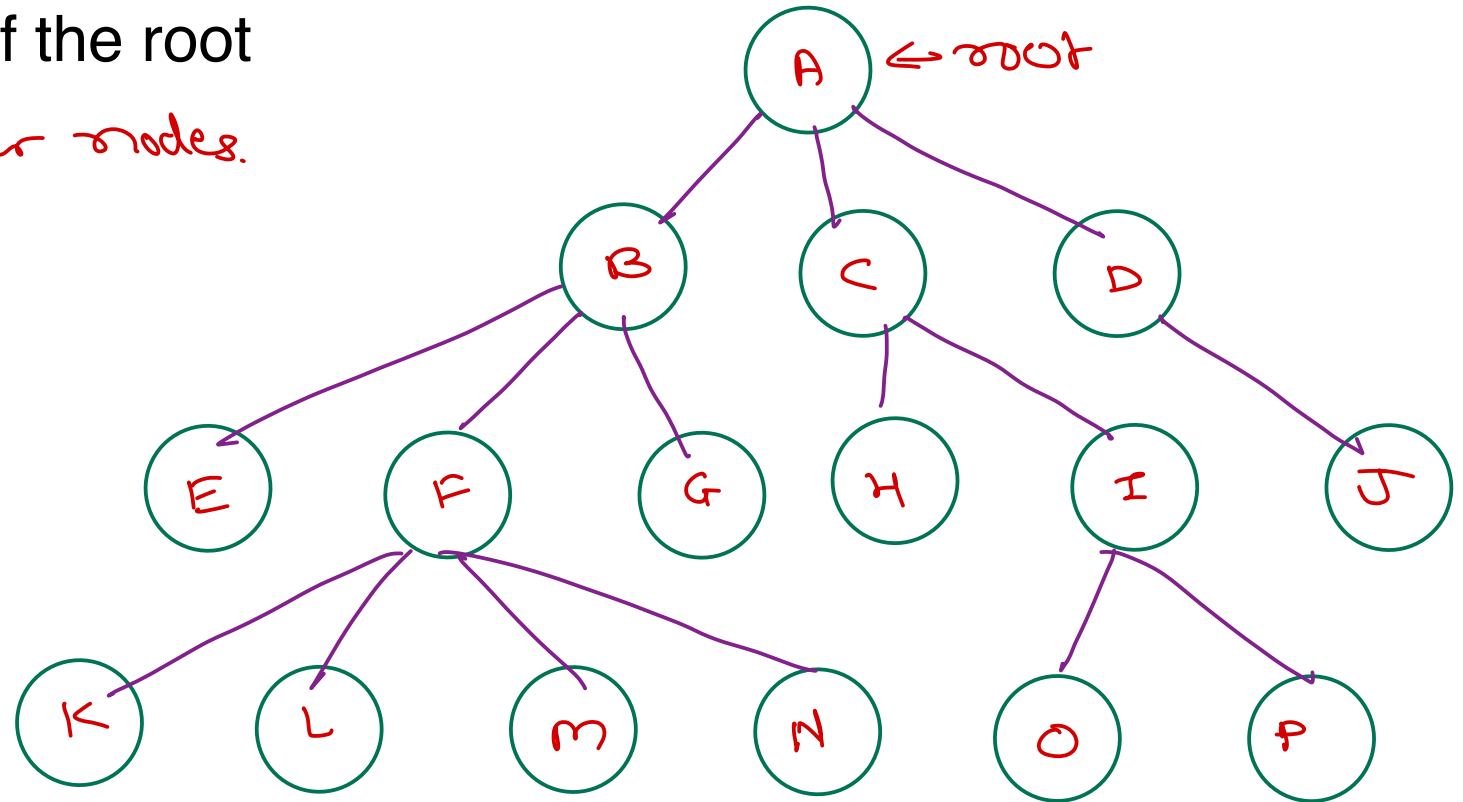
- T_1 to T_n are called sub-trees of the root

Node = Data + Pointers to other nodes.



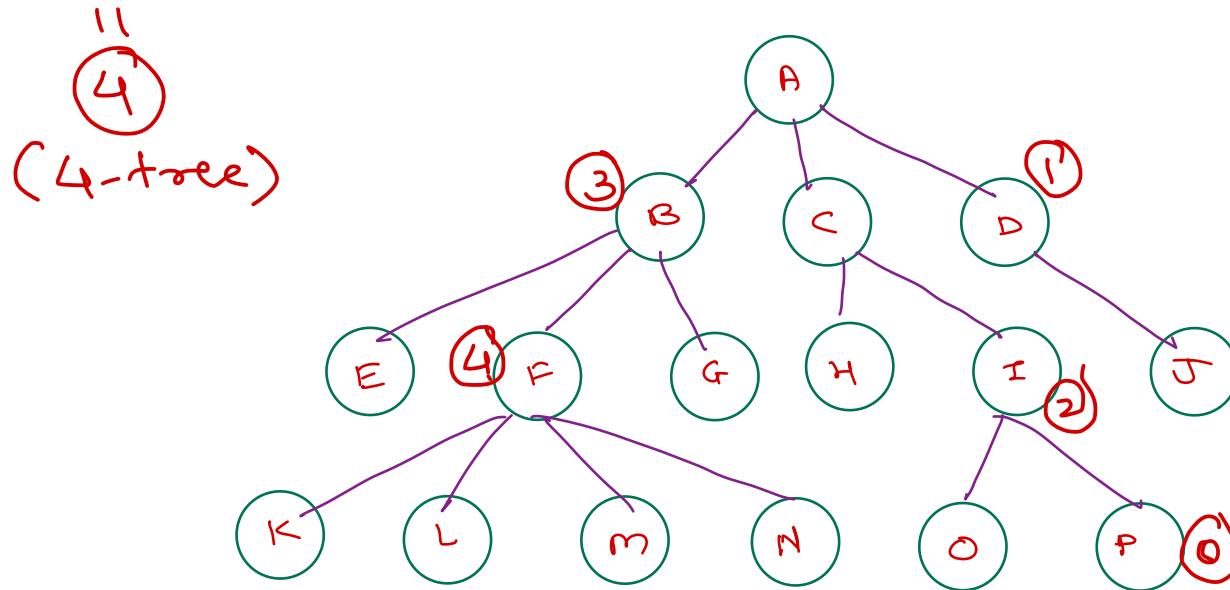
Tree is a non-linear data structure.

Tree is used to represent hierarchical data. leaf nodes →



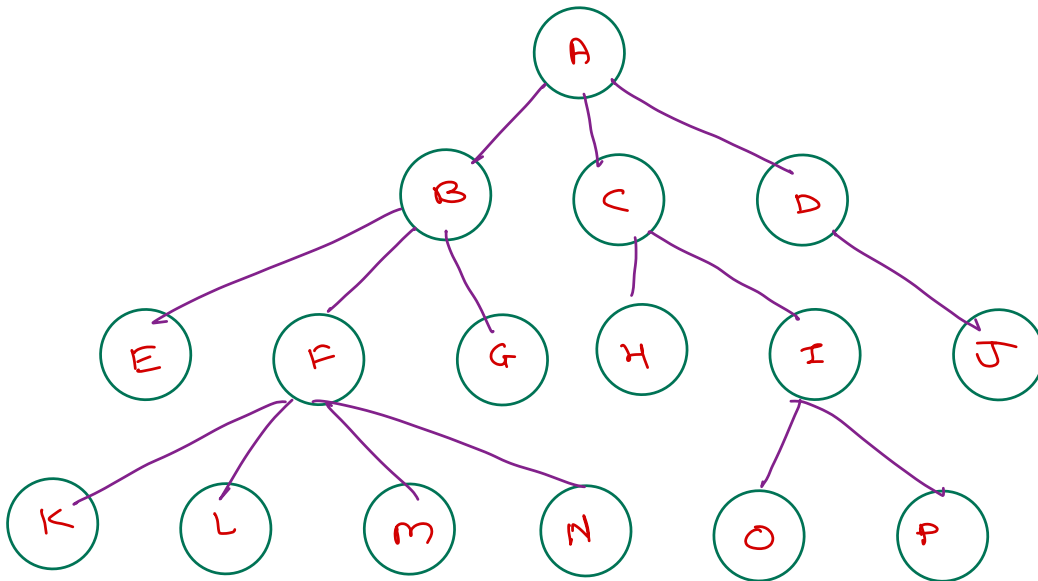
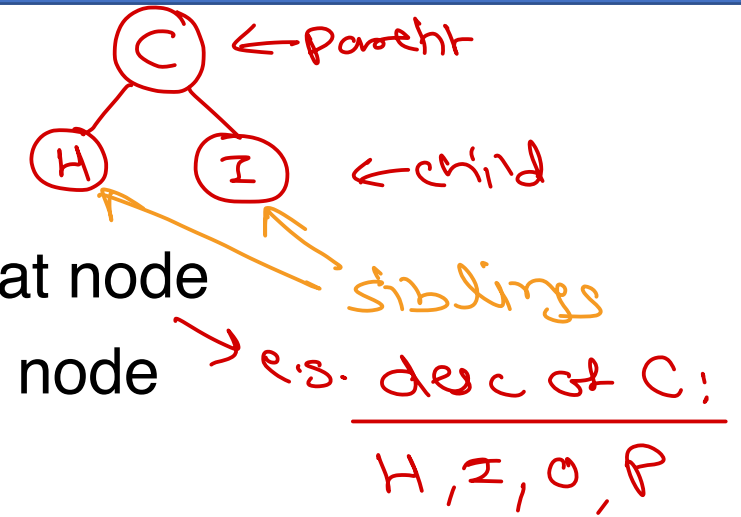
Tree terminologies

- Node: A item storing information and branches to other nodes
- Null Tree: Tree with no node (empty tree)
- Leaf Node: Terminal node of a tree & does not have any ^{child} node connected to it → degree = 0
- Degree of a Node: No of sub trees of a node (No of child nodes)
- Degree of a tree: Degree of a tree is maximum degree of a node in the tree



Tree terminologies

- Parent Node: node having other ^{child} nodes connected to it
- Siblings: Children of the same parents
- Descendants: all those node which are reachable from that node
- Ancestor: all the node along the path from the root to that node



e.g.
Ancestors of P
A, B, F



Tree terminologies

- Level of a Node:

- Indicates the position of the node in the hierarchy
- Level of any node is level of its parent + 1
- Level of root is 1

- Depth of a node:

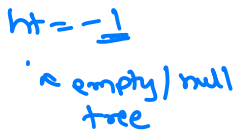
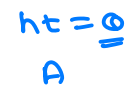
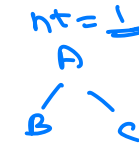
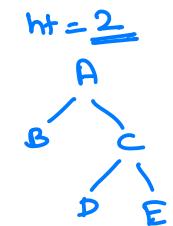
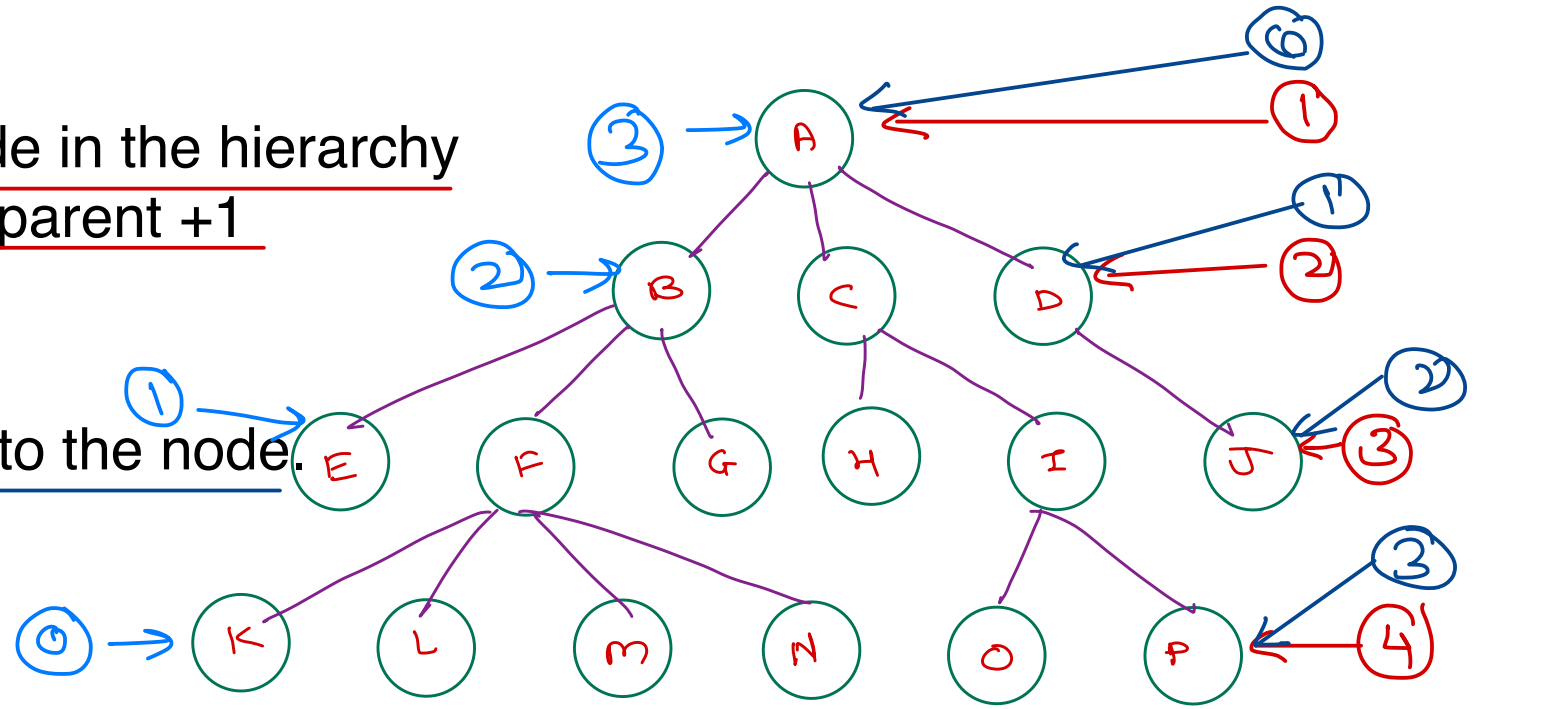
- Number of nodes from the root to the node.
- Depth of root is 0
- Level = Depth + 1

- Height of a node:

- Number of nodes from the node to its deepest leaf.
- Height of node = ^{max} height of its child + 1
- Height of empty/null tree is -1

- Height of a tree: Height of root of the tree. = 3

- Traversal: Visiting each node of tree exactly once



$$\text{height}(A) = \text{MAX}(\underset{0}{\text{height}(B)}, \underset{1}{\text{height}(C)}) + 1$$



Types of trees

- Binary Trees

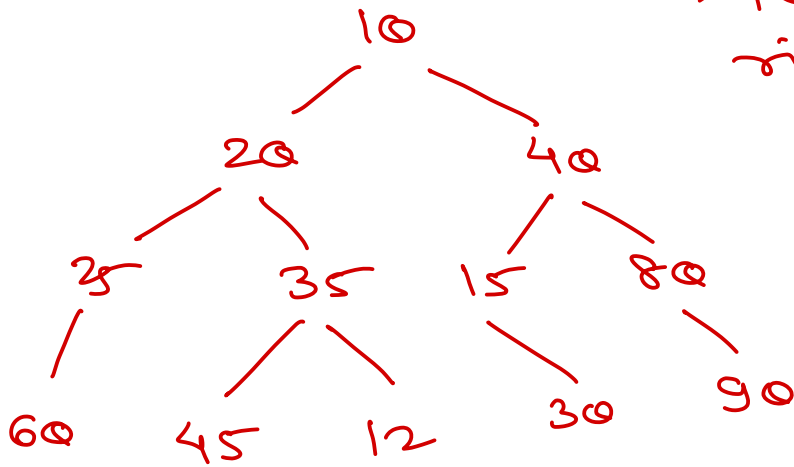
→ each node has max 2 child nodes.

- It is a finite set of nodes partitioned into three sub sets:- Root, Left sub tree, Right sub tree

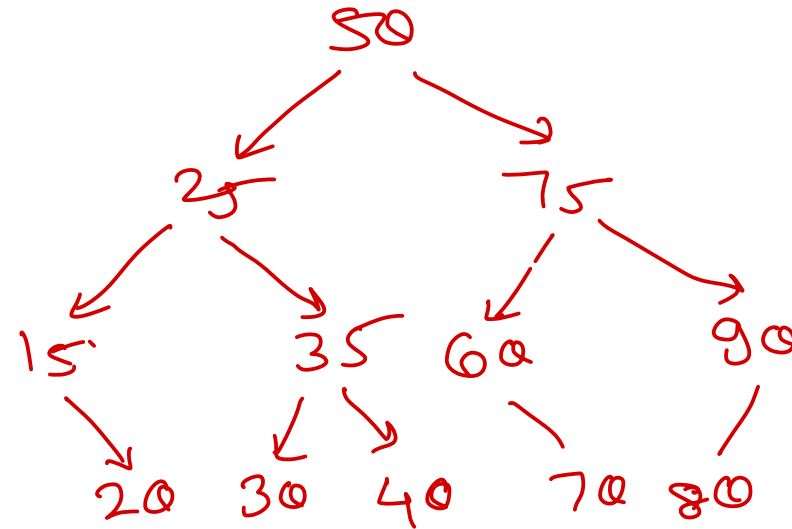
- Binary Search tree

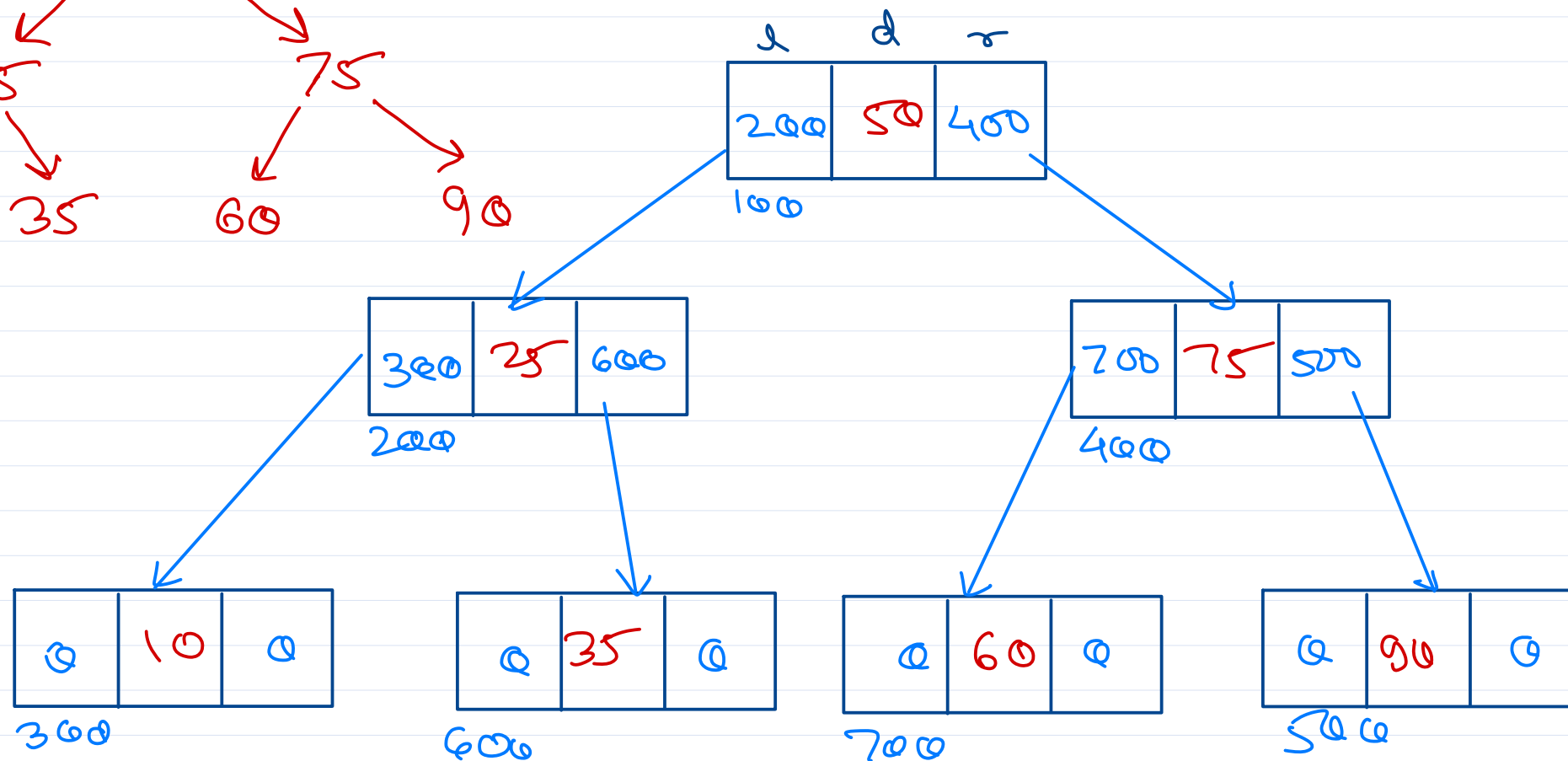
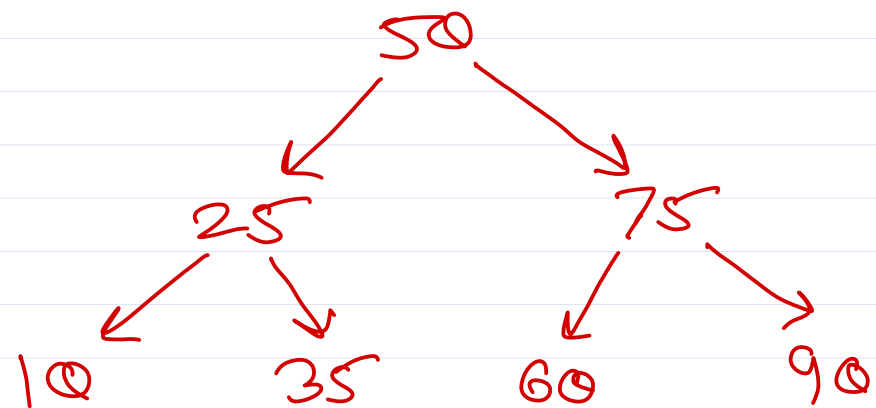
- A binary search tree is a binary tree in which the nodes are arranged according to their values.

↳ left node is smaller than parent,
right node is greater or equal to parent.



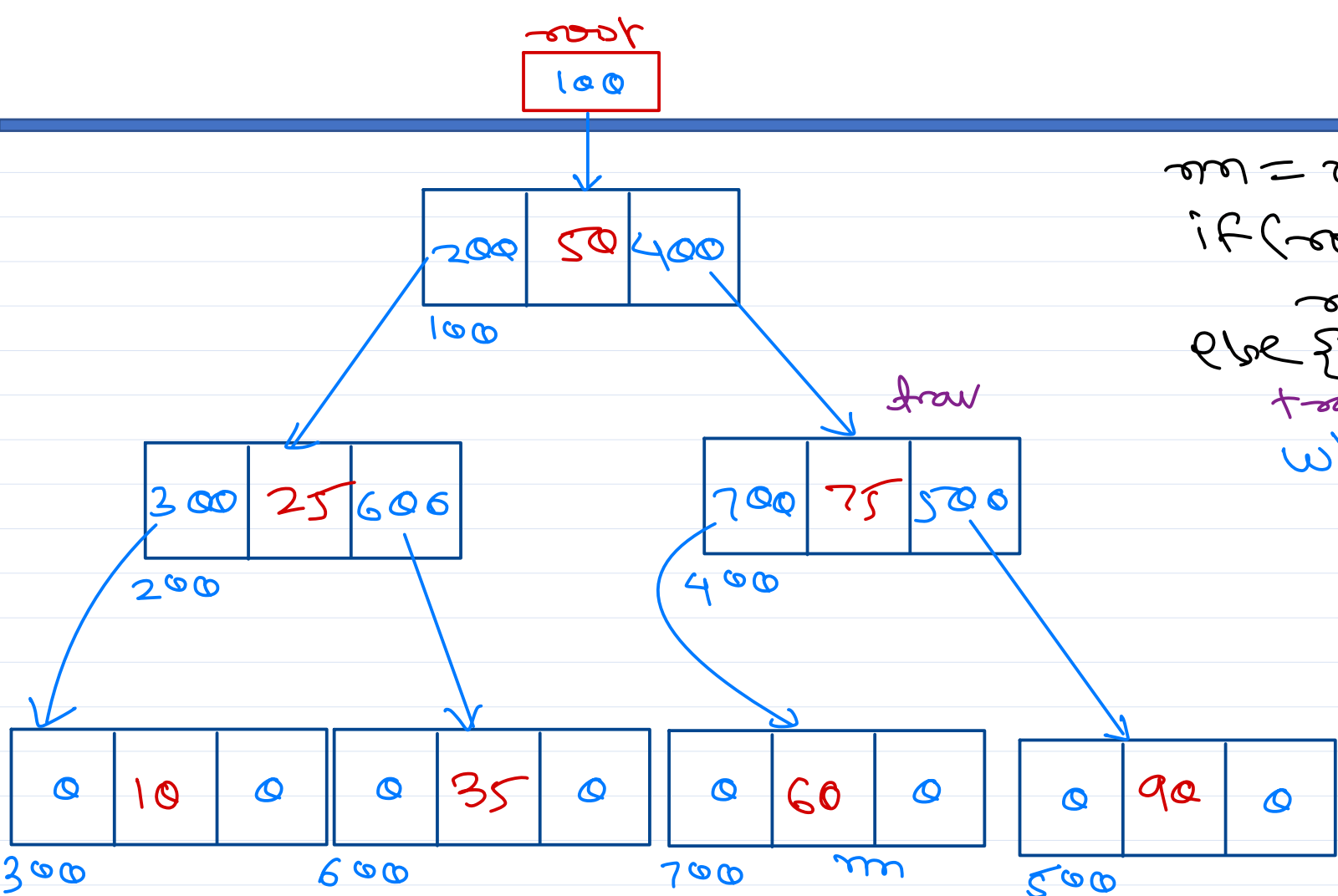
Bin Tree (2-Tree)
Degree of tree = 2





- ① 50
- ② 25
- ③ 10
- ④ 75
- ⑤ 90
- ⑥ 35
- ⑦ 60





```

nm = new Node(val);
if (root == null)
    root = nm;
else {

```

```

    trav = root;
    while (true) {
        if (val < trav.data) {
            if (trav.left == null) {
                trav.left = nm;
                break;
            } else {
                trav = trav.left;
            }
        } else {
            if (trav.right == null) {
                trav.right = nm;
                break;
            } else {
                trav = trav.right;
            }
        }
    }
}

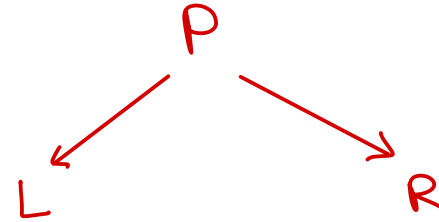
```

- ✓ 50
- ✓ 25
- ✓ 10
- ✓ 75
- ✓ 90
- ✓ 35
- ✓ 60

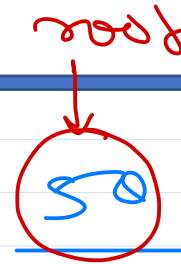
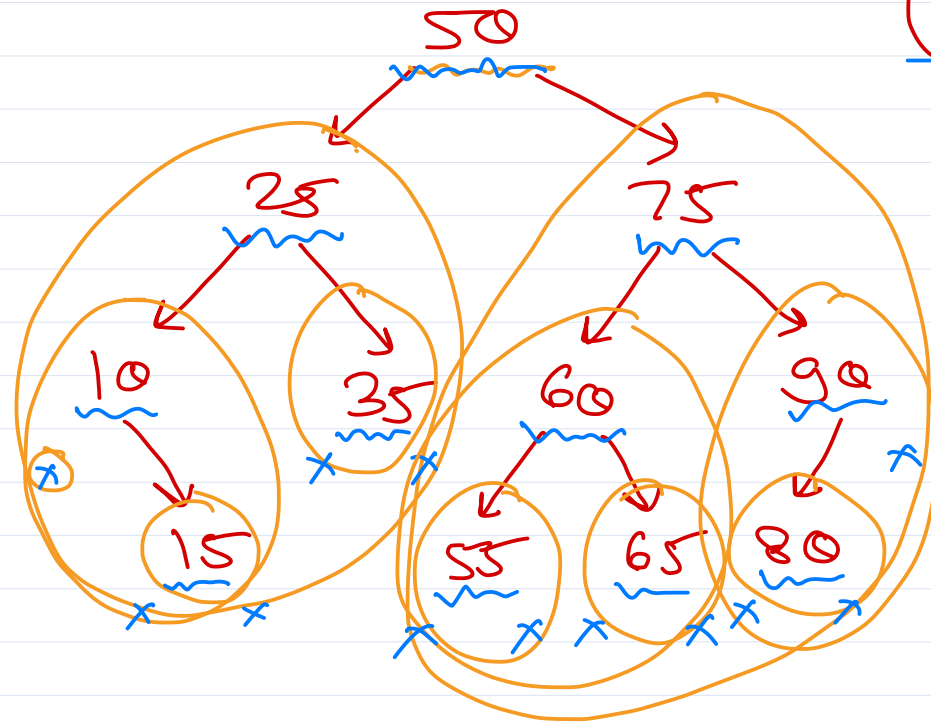


Binary Tree Traversal

- In-order: L P R
- Pre-Order: P L R
- Post-Order: L R P
- The traversal algorithms can be implemented easily using recursion.
- Non-recursive algorithms for implementing traversal needs stack to store node pointers.



PreOrder



25 10 15 35
75 60 55 65 90 80

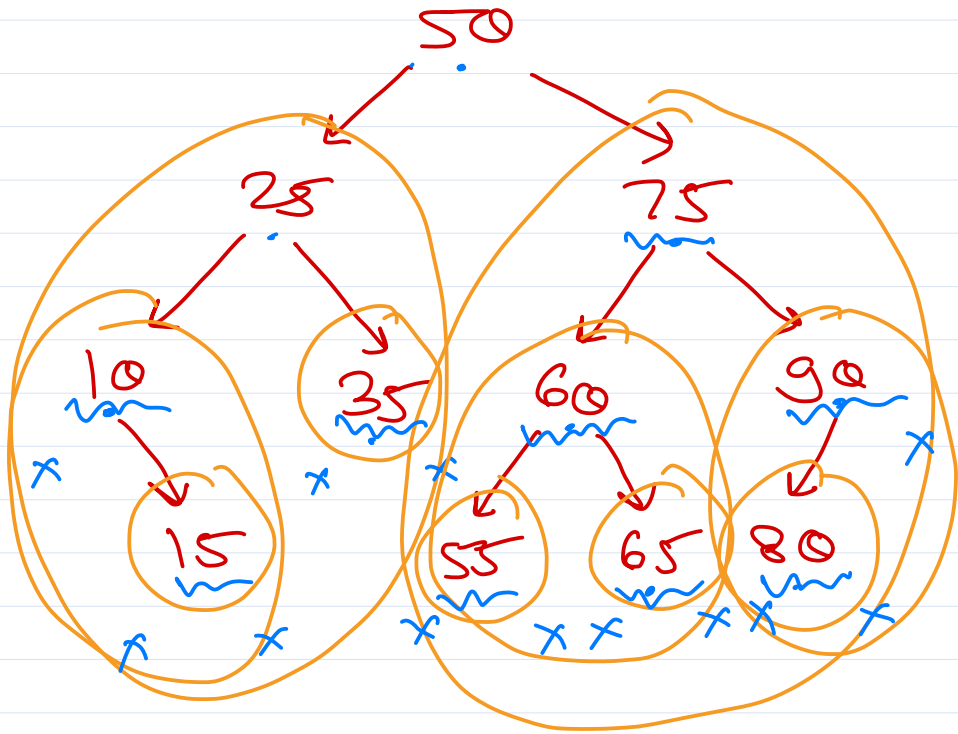
```
void preorder (Node trav) {  
    if (trav == null)  
        return;  
    print (trav.data);  
    preorder (trav.left);  
    preorder (trav.right);  
}
```



InOrder

10 15 25 35 50 → sorted output

55 60 65 75 80 90 →

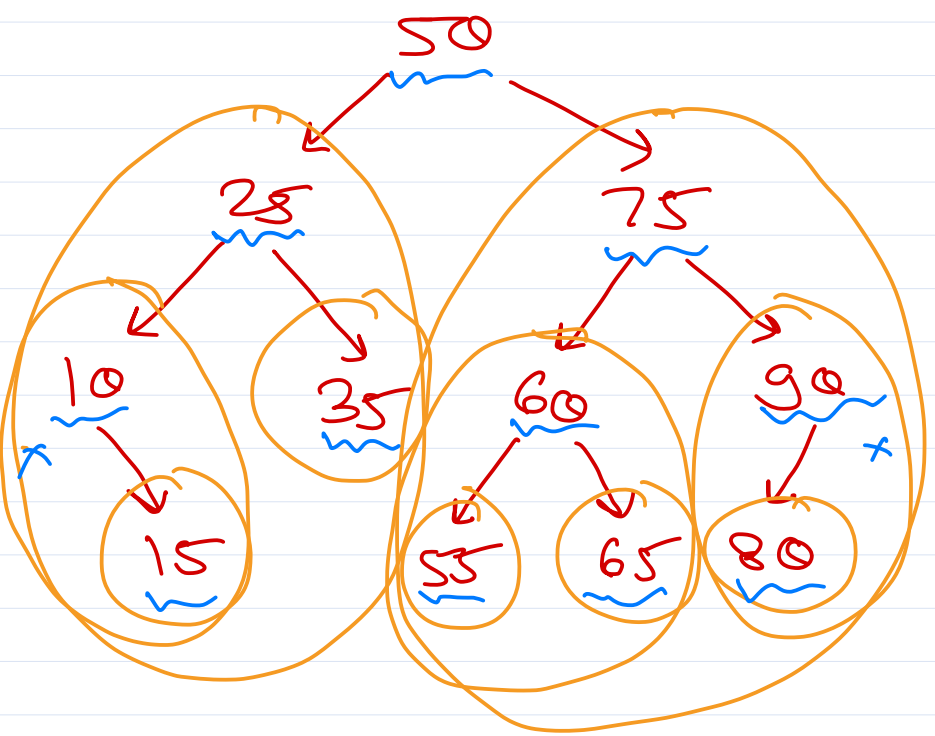


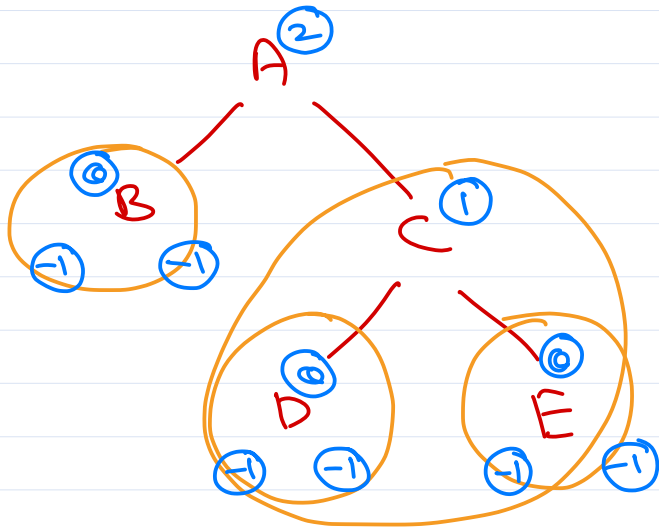
```
inorder ( trav ) {  
    if ( trav == null )  
        return;  
    inorder ( trav . left );  
    print ( trav . data );  
    inorder ( trav . right );  
}
```



PostOrder

15 10 35 25 55 65 60
80 90 75 50
↑
root





```
int height(trav) {
    if (trav == null)
        return -1;

    hl = height(trav.left);
    hr = height(trav.right);
    max = hl > hr ? hl : hr;
    return max + 1;
}
```

3





Thank you!

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