

Problem A 3.2

A function to find the norm of an input vector:

```
In [ ]: function norm(a)
        sum = 0
        for i in 1:length(a)
            sum += (a[i] * a[i])
        end
        return sqrt(sum)
    end
```

```
Out[ ]: norm (generic function with 1 method)
```

A function to find the distance between two vectors:

```
In [ ]: function distanceBetween(a, b)
        return norm(a-b)
    end
```

```
Out[ ]: distanceBetween (generic function with 1 method)
```

A function to find the angle between two vectors:

```
In [ ]: function angleBetween(a, b)
        return acos(a'b/(norm(a)norm(b)))
    end
```

```
Out[ ]: angleBetween (generic function with 1 method)
```

All the vectors from the problem statement:

```
In [ ]: a = [1, 3, 4]
        x1 = [4, 3, 5]
        x2 = [0.4, 10, 50]
        x3 = [1, 4, 10]
        x4 = [30, 40, 50]
```

```
Out[ ]: 3-element Vector{Int64}:
        30
        40
        50
```

Vector containing the names of the vectors:

```
In [ ]: vectors = ["x1", "x2", "x3", "x4"]
```

```
Out[ ]: 4-element Vector{String}:
        "x1"
        "x2"
        "x3"
        "x4"
```

Finding distance between a vector and the vectors x1, x2, x3, x4

```
In [ ]: distance_between_a_and_x1 = distanceBetween(a, x1)
```

Out[]: 3.1622776601683795

```
In [ ]: distance_between_a_and_x2 = distanceBetween(a,x2)
```

Out[]: 46.53342884421908

```
In [ ]: distance_between_a_and_x3 = distanceBetween(a,x3)
```

Out[]: 6.082762530298219

```
In [ ]: distance_between_a_and_x4 = distanceBetween(a,x4)
```

Out[]: 65.7723346096214

Finding the least distant vector from a among x1, x2, x3, x4

```
In [ ]: leastDistance = min(distance_between_a_and_x1, distance_between_a_and_x2, c
```

Out[]: 3.1622776601683795

```
In [ ]: distances = [distance_between_a_and_x1, distance_between_a_and_x2, distance
println("The vector that is least distant from 'a' is ", vectors[argmin(dis
```

The vector that is least distant from 'a' is x1 and the distance is 3.1622776601683795

Finding angle between 'a' vector and the vectors x1, x2, x3, x4

```
In [ ]: angle_between_a_and_x1 = angleBetween(a,x1)
```

Out[]: 0.4146551062003066

```
In [ ]: angle_between_a_and_x2 = angleBetween(a,x2)
```

Out[]: 0.4818770434517026

```
In [ ]: angle_between_a_and_x3 = angleBetween(a,x3)
```

Out[]: 0.2804174688623895

```
In [ ]: angle_between_a_and_x4 = angleBetween(a,x4)
```

Out[]: 0.24256387409548533

Finding the vector with least angle among x1, x2, x3, x4 and 'a'

```
In [ ]: leastAngle = min(angle_between_a_and_x1, angle_between_a_and_x2, angle_betw
```

Out[]: 0.24256387409548533

```
In [ ]: angles = [angle_between_a_and_x1, angle_between_a_and_x2, angle_between_a_and_x3, angle_between_a_and_x4]
println("The vector that has the least angle from 'a' is ", vectors[argmin(angles)])
```

The vector that has the least angle from 'a' is x4 and the angle is 0.24256387409548533 Radians