

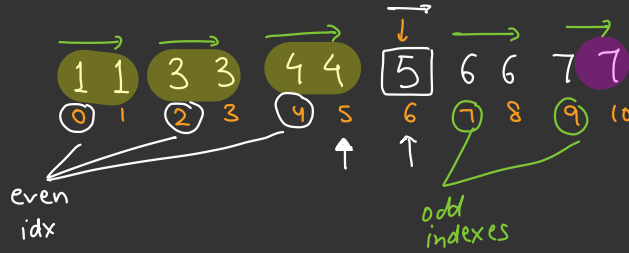
Good evening



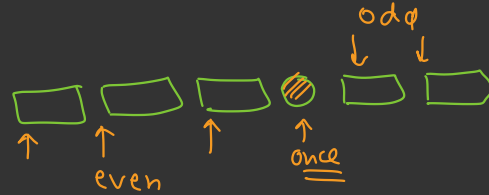
Q) Sorted Array with $2N+1$ elements, find out unique element.

odd

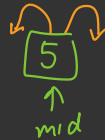
Repeating Unique



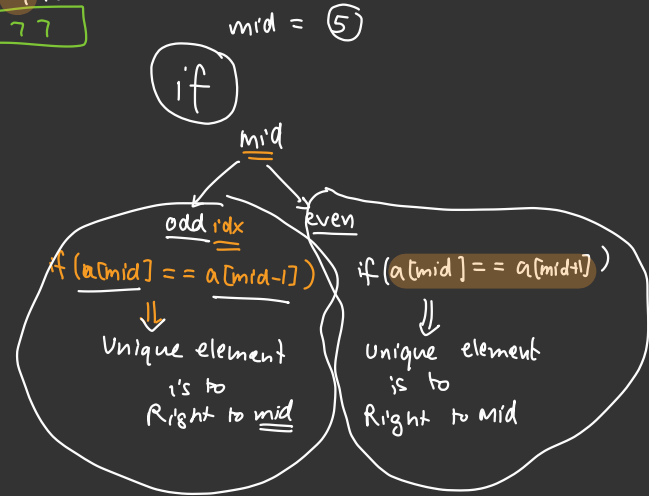
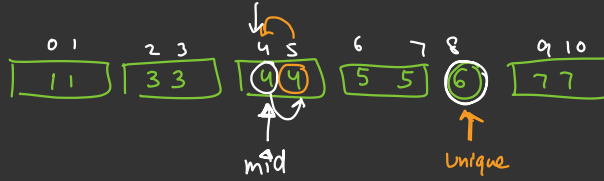
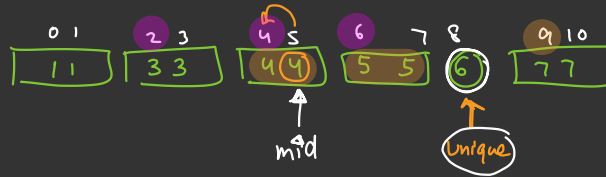
$s=0$ $e=10$ $mid=5$



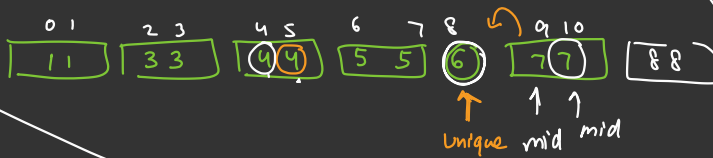
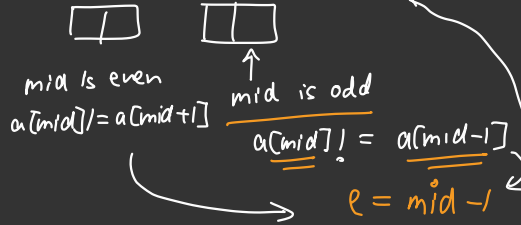
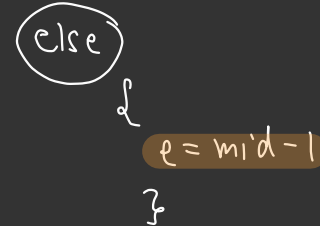
$mid \rightarrow 6$



if $(a[mid] \neq a[mid+1] \text{ and } a[mid] \neq a[mid-1])$ {
 return $a[mid]$;
}



$$s = mid + 1$$



Code

$S = 0$

$e = arr.length - 1$

unique start → unique end

5 5 6

6 7 7

↑↑ ↑ ↑
20 mid 2

5

↑ ↑
s e

log₂ C

// single size array

if ($a[0] == a[1]$) return $a[0]$;
if ($a[n-1] == a[n-2]$) return $a[n-1]$;
while ($S \leq e$) {

$mid = (S + e) / 2;$

→ if ($a[mid] == a[mid+1]$ && $a[mid] == a[mid-1]$) { return $a[mid]$; }

→ else if (mid is odd && $a[mid] == a[mid-1]$) || (mid is even && $a[mid] == a[mid+1]$)

$S = mid + 1;$

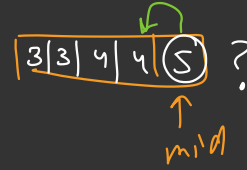
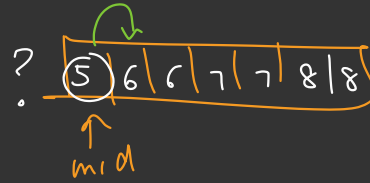
else {

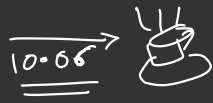
$e = mid - 1;$

}

① uniq ② Right ③ left

fail if unique element is present at start/end of array





Q2.

N tasks

K workers

Time to finish each task

times = $\left[\begin{array}{c} 3, 5, 7, 6, 2, 10 \\ \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \\ t_1 \end{array} \right]$

K = 3 workers

Conditions:

- Each worker will execute a "set of continuous tasks".
- All workers start doing tasks at same time

⇒ Find minimum time required to finish all the tasks

↑
output

min (--- max ---) optimisation →

[3, 5, 7, 6, 2, 10]

← w1 → ← w2 → ← w3 →

max (15 mins , 8 mins , 10 mins) = 15 mins

[3 5 7 6 2 10]

max (8 mins , 13 mins , 12 mins)

= 13 mins ✓

$\begin{matrix} & w1 & w2 & w3 & & \\ & \downarrow & \downarrow & \downarrow & & \\ m & 8 & & 12 & & 0 \\ & & & & & 0 \\ & & & & & 0 \\ & & & & & 0 \end{matrix}$

→ 13 → 13 mins

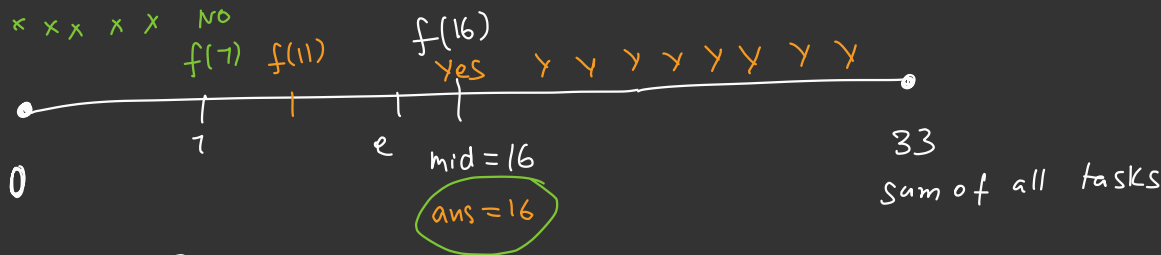
Search Space



Min
Time

if all tasks can be finished in 16 mins

↑
every workers
should do
work \leq 16 mins



$S=6$ $e=15$ $mid=(7)$

$\vec{3} \vec{5} \vec{7} \quad \overbrace{6 \ 2 \ 16}$

$w1=3$

$w2=5$

$w3=7$

$S=8$ $e=15$

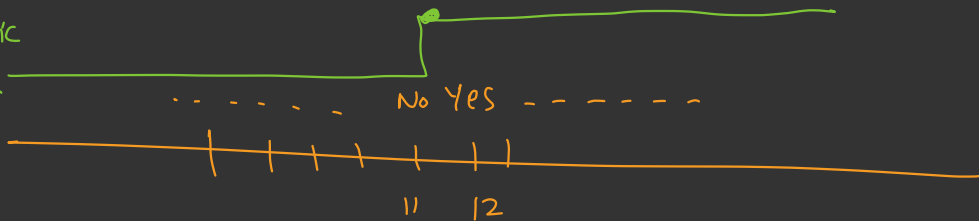
$\overbrace{3 \ 5 \ 7} \quad \overbrace{6 \ 2} \quad \overbrace{10}$

$w=3$

min Time

$$\begin{cases} w1 = 3+5+7 & \leq 16 \\ w2 = 6+2 & \leq 16 \\ w3 = 10 & \leq 16 \end{cases}$$

monotonic
search
space



10:06

5 — 10
↑
7.5
mins

tasks = [3, 5, 7, 6, 2, 10]

k = 3 (workers)

Binary Search

s = 0
e = sum of tasks

ans = e

while (s <= e) {

mid = (s + e) / 2,

if (canDo (tasks, mid, k)) {

ans = mid;
e = mid - 1;

else {

$$s = mid + 1,$$

if

$$mid = 12$$

print(ans);

if all task can be done in given
by using k workers or not

→ 3, (5), (7), 6, 2, 10

Can Do
Method

bool

canDo(tasks[], mid, k)

$$\begin{array}{rcl} \text{cnt} & t = 3 & \leq 12 \\ 0 & + 5 & \end{array}$$

3 5 7 6 2 10

$$\text{cnt} = 1$$

$$t = 0$$

tasks

for(i=0; i<n-1; i++) {

if(t + time[i] ≤ mid) {

$$t = t + \text{time}[i]$$

else { t = time[i] ← Reset time for next worker

cnt++,
if(cnt > k) { return false; }

return true,

3

mid = 13

3, 5, 7, 6, 10, 18

t = 0

$$\text{cnt} = 1 \quad 3 + 5 \leq 13$$

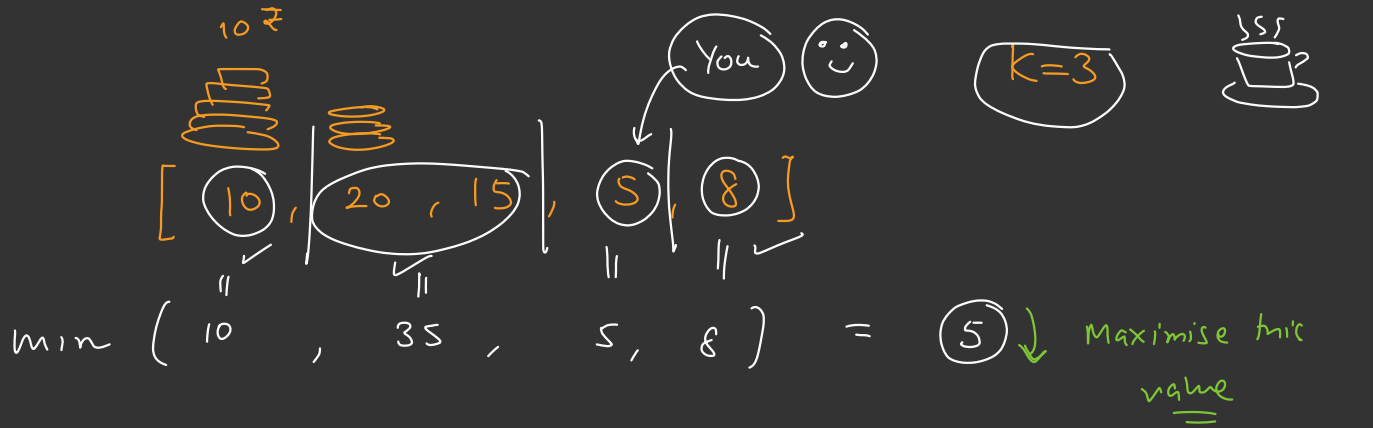
$$\text{cnt} = 2 \quad 7 + 13 \leq 13$$

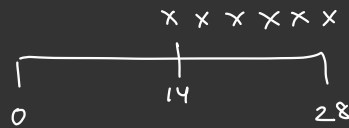
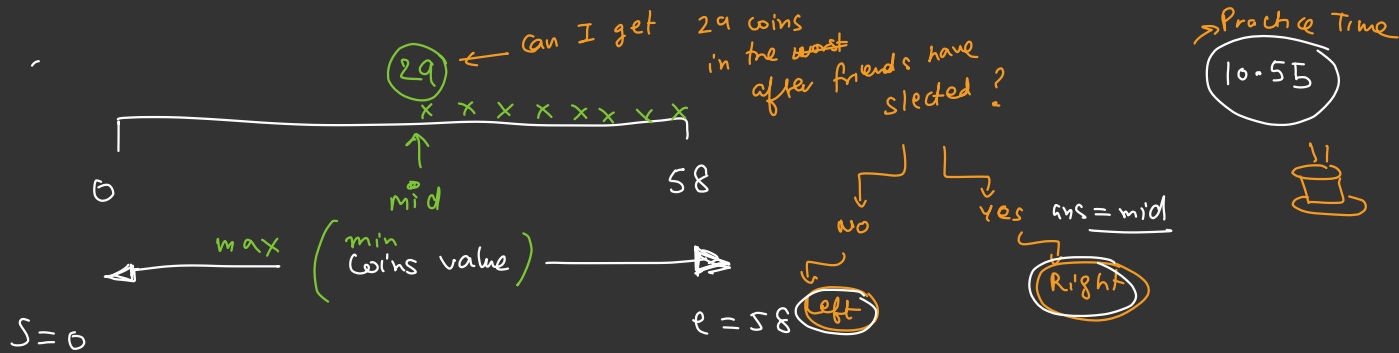
$$\text{cnt} = 3 \quad 2 + 10 \leq 13$$

Google Interview Problem

There are N stacks of coins, each stack has certain value of coins.

The stacks are ^{consecutive} lying on a straight line, you have K friends with who you can divide the stacks in $K+1$ partitions. Your friends are greedy and they will pick the best K parts and you will give the left one. Maximise the value of coins you can get.





$k=3$
 $k+1$
 4 parts

$f1 = 10 + 20 = 30$
 $f2 = 15 + 5 + 8 = 28$

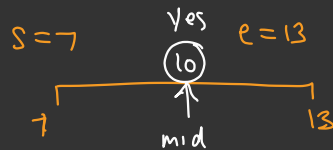
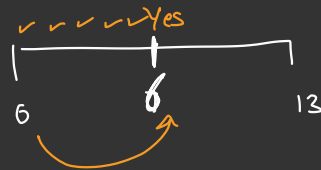
$f1 = 10 + 20 = 30$
 $f2 = 15$
 $f3 = 5 + 8 = 13$

$\vec{10}, \vec{20}, \vec{13}, 5, 8$

$f1 = 10 \checkmark$
 $f2 = 20 \checkmark$
 $f3 = 15 \checkmark$
 $f4 = 5 + 8 = 13 \checkmark$

ans = ~~5~~

ans = 10





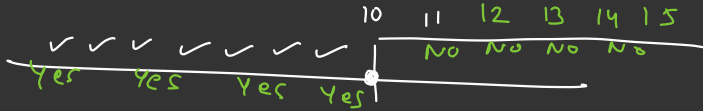
$\overrightarrow{10}, \overrightarrow{20}, \overrightarrow{15}, \overrightarrow{5}, \overrightarrow{8}$

$$f_1 = 10$$

$$f_2 = 20$$

$$f_3 = 15$$

$$f_4 = 5 + f = 13$$



→ Prata (SPOJ)
 → Painter's Partition Problem

Binary Search

$$S = 0$$

$e =$ sum of all array elements

$\xrightarrow{\log} \boxed{e}$

while ($S \leq e$) {

$$mid = (S + e) / 2,$$

$\xrightarrow{O(N)}$
if (canDivide (arr, mid, K)) {

$$ans = mid;$$

$$S = mid + 1$$

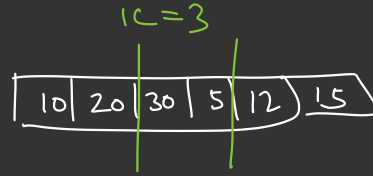
}

else {

$$e = mid - 1$$

}

}



$$O(N + \log(\text{Array Sum}))$$

Diagram illustrating the time complexity with a horizontal line and an arrow pointing to the \log term.

Can Divide (arr, mid, K) {

cnt = 0 // Partitions

S = 0

for (i = 0; i < n-1; i++) {

if (S + arr[i] > mid) {

cnt++

S = 0 // Reset sum

→ else {

S = S + arr[i];

3

3

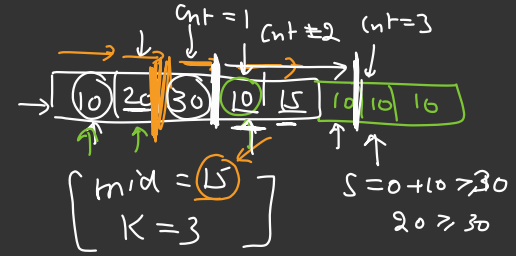
→ if (cnt >= K) { return true; }

else {

return false; }

↓

↑



→ S = 0 + 20 = 20 > mid

→ S = 30 > mid

S = 0 + 10 + 15 = 25

mid = 30

mid = 30

→ 0 + 10 > 30

S = 10 + 20 > 30

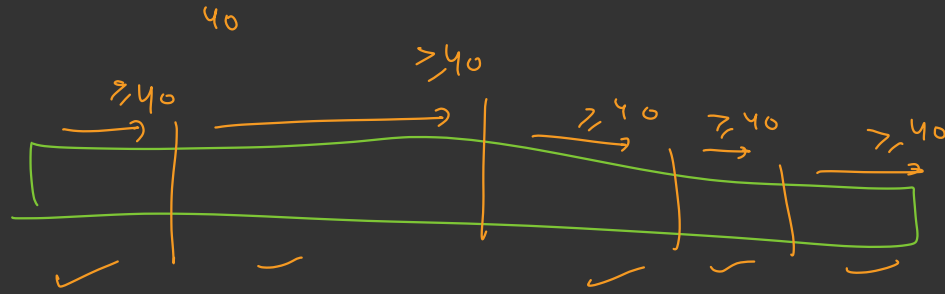
S = 0 + 30 > 30

S = 0 + 10 > 30

S = 10 + 15 > 30

S = 25 + 10 > 30

S = 0



→ 5 partitions

→ 3 partitions (yes)