

Recursion-3 (26 June)

⑦ Recording

↳ Problem, Assignment, Doubts

_____ x _____ x _____ x _____ x _____

⇒ Linked List (Introduction) ↑
↑ understand

+ Move in Advanced Batch

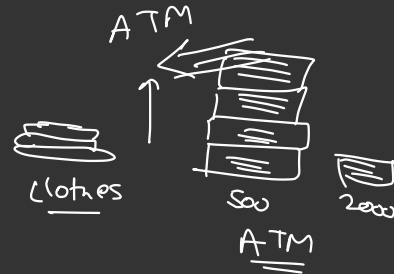
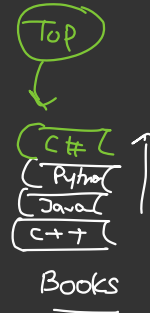
_____ x _____ x _____ x _____

Stacks & Queues

Stack

Data Structure / Container
data is stored in LIFO
fashion

↑
Last In
First out



Push / Insert() from Top $O(1)$

Pop / Remove() → from Top $O(1)$

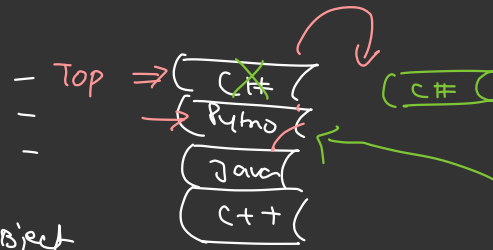
Top() → get the value from Top most object
Read

Remove
the
top most
element.

Remove a particular element

↓
not supported directly

↓
loop → $O(N)$



→ insert("C#") ✓

→ pop() ✗

→ top() Python

→ pop()

→ top() → Java

Real life in software

① Recursion

Implicit Stack

[Function
Call]

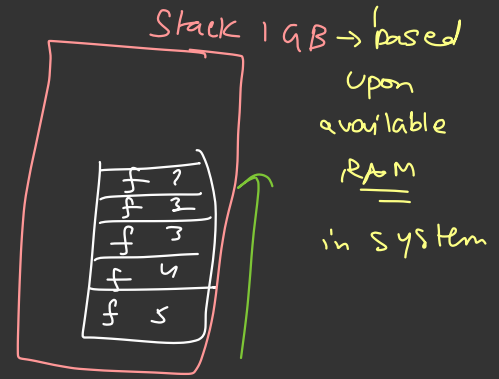
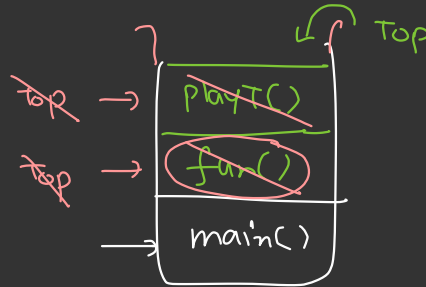
Automatically created
in memory.

fn() {
fn()
}

playTennis() when ~~rec~~ function calls

↑
fn() { ≡ }

↑
main() {
 ≡ fn()
}

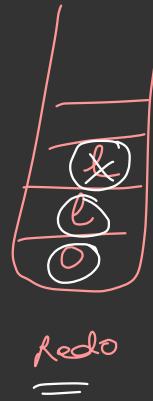


1GB, 20MB, ---, ---

→ ∞ Recursion
→ very large size containers

Stack overflow

~~hello~~
 xxx
 hello
 ==>
 ->



Ctrl + Z

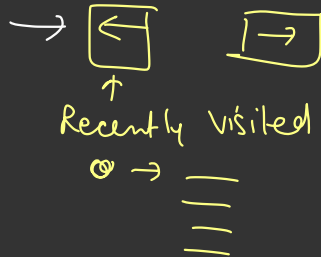
Cmd + Shift + Z

hello

Some limit

↑
 Steps we can
undo & Redo

Q) Web Browsers



Stack

open-web-page

stack.push(web url),

Stack of Integers

push(40)

push(20)

push(8)

push(9)

→ pop() → Remove = 9

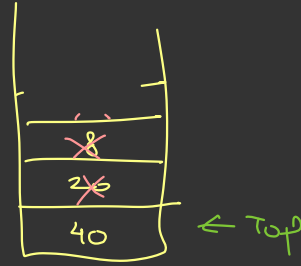
→ pop() → — = 8

→ pop() = 1 → 20

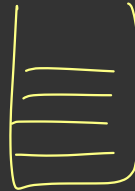
top() ⇒ 40 (Reads)

pop() → → 40

top() → error

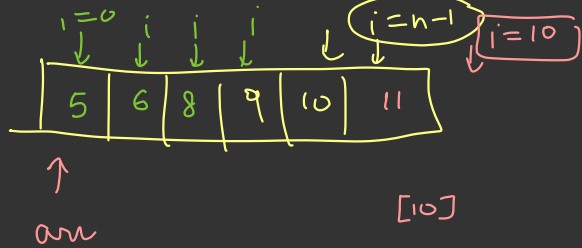


ans = S.top()
S.pop(),
S.pop(),
S.push(ans)



Stack Implementation

Stack using a array (Fixed / Dynamic \rightarrow ArrayList)

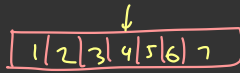


```
void push(int data) {  
    if ( $i == \text{array.size()}$ ) {  
        print("Stack is full");  
    }  
    else {  
        arr[i] = data;  
        i++;  
    }  
}
```

3

array
(powerful)

→ Stack
(less powerful)



→ iterate
& see
all

→ arr[i]

→ insert in
middle (=)

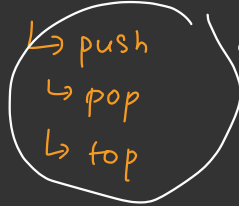
Limiting the

ops we
can do
on arrays

just to provide
LIFO

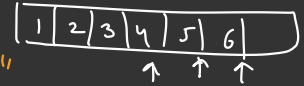
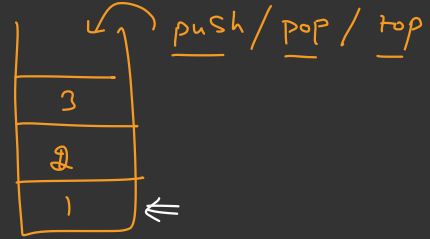


use



← Abstraction

to build a behaviour for "stack"



Stack s;

{ s.push()
- s.pop()
s.top()

class Stack {

ArrayList<Integer> arr;

Stack() { arr = new ArrayList<>(); }

push(int data) {

arr.add(data);

hidden

pop() { int n = arr.size();

arr.remove(n-1);

int top() {

return arr.get(n-1);

}



n=2

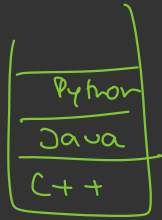


if(n==0) { print("Empty Stack",

Any stack problem can be solve using array.

Advantage

↳ Code would be simplified.



hiding the
details of
insertion behind the push
fn

predefined

Stack s = new Stack();

s.push("C++")

s.push("Java")

s.push("Python")

s.pop()

C++ | Java | ?

Array

String books[10];

int i=0,

books[i] = "C++" loop

i++

books[i] = Java,

i++

books[i] = Python

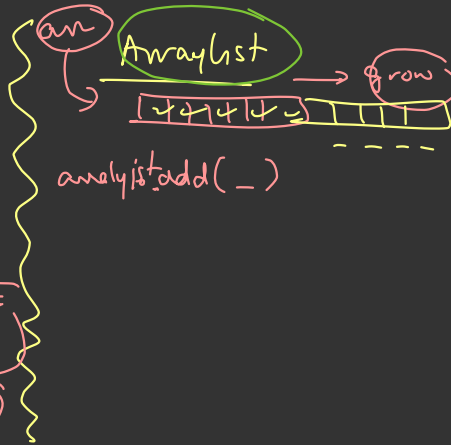
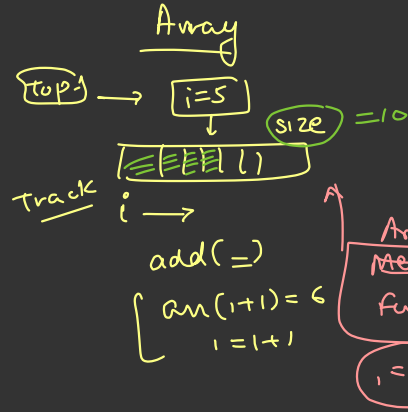
i++

~~to~~ i = i - 1

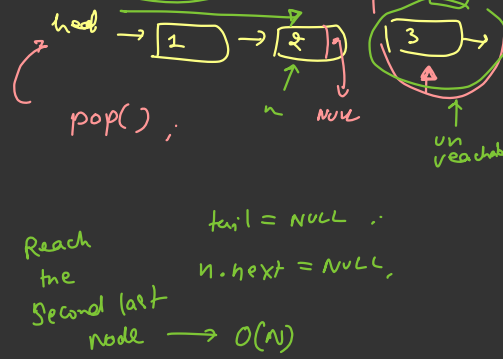
Maintain
i

enclosed
in
push
fn of stack

Stack

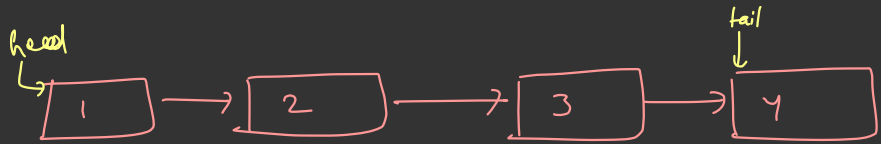


Linked List



3
2
1

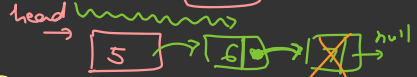
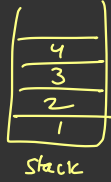
l.h.o



X

Insertion

$O(1)$ $\left[\begin{array}{l} \text{push(int d) \{ \\ if(head == null) \{ head = new Node(d); \\ tail = head, \\ tail.next = new Node(d), \\ tail = tail.next \\ \} \} \end{array} \right.$



Can't move Backward

PROBLEM

pop() {

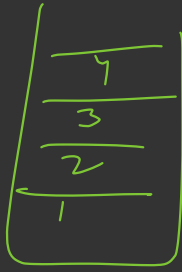
tail = null
SL.next = null

$O(N)$ Bad \odot

Iterate from the front to get SL

tail = SL,

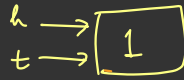
SL, tail, SL, tail, tail



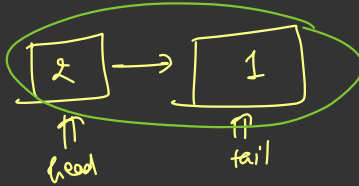
pop()

linked list

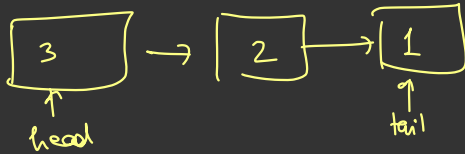
$h \rightarrow \text{null}$



$\leftarrow s.push(1)$

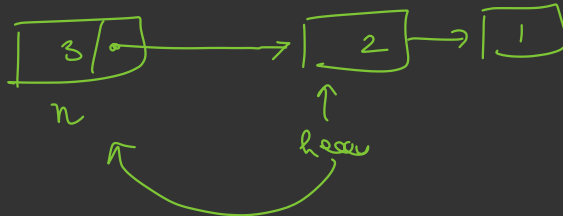


$\leftarrow s.push(2)$



$\leftarrow s.push(3)$

$O(1)$



insert At head(d) {

if(head == null) {

head = new Node(d);

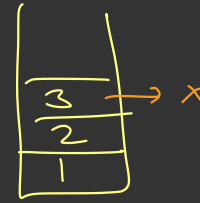
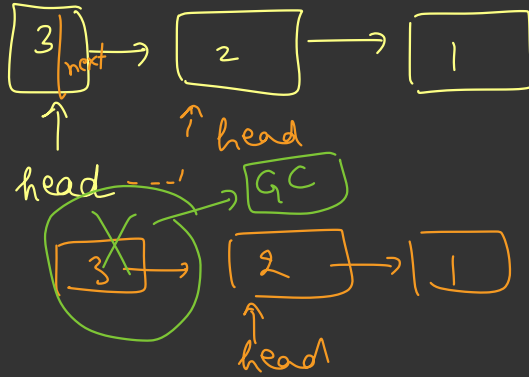
}

Node n = new Node(d)

n.next = head,

head = n,

}



pop() {

head = head.next,

}

top() {

if (head != null) {
return head.data;

}

}

O(1)

insertion / pop
at
head
O(1)



Interview Question on Stack

↳ Design A Stack, TC of Pop / Push

↳ Solve XYZ Problem. \Rightarrow Use case of Stack

↳ inbuilt stack (Java library)

 10.45



Gray Code

The gray code is a binary numeral system where two successive values differ in only one bit.

Given a non-negative integer A representing the total number of bits in the code, print the sequence of gray code.

A gray code sequence must begin with 0.

1 bit

0
—
1
—

Valid Seq

2 bit

X

0	0
0	1
1	0
1	1

1 bit
2 bits

0 0	→	0 0
0 1	→	0 1
1 1	→	1 1
1 0	→	1 0

$\begin{bmatrix} 0 \\ 1 \\ 3 \\ 2 \end{bmatrix}$

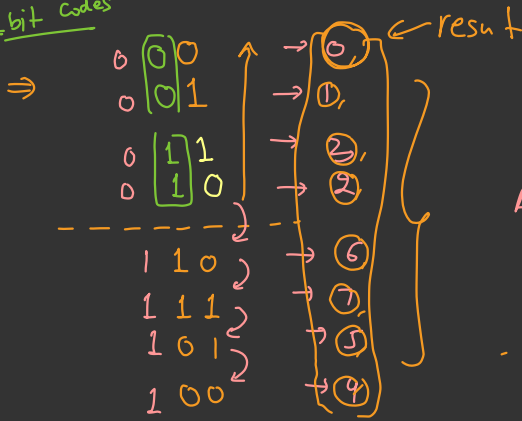


0 0	→	0
1 0	→	2
1 1	→	3
0 1	→	1

$\begin{bmatrix} 0 \\ 2 \\ 3 \\ 1 \end{bmatrix}$

Way

2 bit codes



3 bit codes

A len codes →

Bit codes of len $A-1$
↓
Bit codes of len $(A-2)$
⋮
Bit codes of len 1

Soln ⇒

array list = {0}

int n = A

for (i=0; i<n; i++) {

int currentSize = result.size();

elements
in one
array list

for (j= CS-1; j>=0; j--) {

result.add(result.get(j)
+ (1<<i))

return result.

in i^{th} iteration

↓
generate all
codes of
len $(i+1)$

$$A = 3$$

$$\text{result} = [0, 1]$$

$$\Rightarrow i = 0$$

$$\Rightarrow i = 1$$

$$\Rightarrow i = 2$$

$$cs = 1, j = 0$$

$$cs = 2, [0, 1, 11, 10]$$

$\downarrow \quad \downarrow$
 $3, 2$

$$cs = 3 [0, 1, 11, 10,$$

$$110, 111, 101, 100]$$

$$= [0, 1, 3, 2, 6, 7, 5, 4]$$

$$f(A) \rightarrow f(A-1)$$

$\text{result} \quad \text{result}$
 $\quad \quad \quad \leftarrow$

$$[0]$$

\leftarrow
 $\boxed{10} \quad \boxed{0}$
 $\quad \quad \quad \uparrow \quad \downarrow$
 $\quad \quad \quad i \quad j$

$$1 + k < 1$$

$$= 01$$

$$\rightarrow 10$$

$$\underline{11}$$

$$\begin{array}{cc} 00 & \uparrow \\ 01 & \downarrow \\ \hline 11 & \downarrow \\ 10 & \downarrow \end{array}$$

$$\begin{array}{cc} 110 \\ 111 \\ \rightarrow 101 \\ \rightarrow 100 \end{array}$$

$$\uparrow$$

$$\boxed{i=2}$$

$$k < j$$

ARRAYLIST greyCode (int A) {

if (A == 1) {

return ArrayList (0, 1)

A = [0, 1]

}

A + → (- - - - -)

A →

ArrayList < int > result = greyCode (A - 1);

int p = A - 1

for (j = result.size () - 1 , j >= 0 ; j --) {

result.add (result.get (j) + (1 << p) ,

return result,

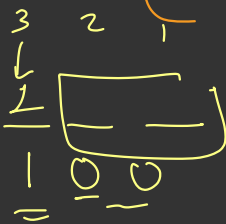
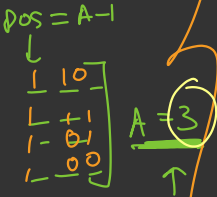
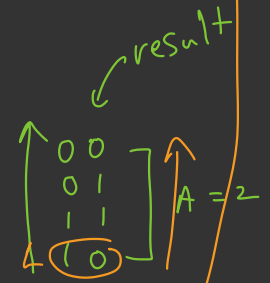
0 0 0 0
00 01 10 11

(0, 1)

10, 11

(0, 1, 2, 3)

(0, 1, 3, 2, 7, 6, 5, 4)



3

1 << 2