

1. DiffK ||

$$\langle 0, 1, 2, 3, \dots \rangle$$

Given an array A of integers and another non-negative integer K, find if there exists 2 indices i and j such that $A[i] - A[j] = K$, $i \neq j$.

Given :- A = < T

$$k \geq 0$$

Output - 1 / 0

$$E_x - A = \langle 1, 5, 3 \rangle$$
$$k = 2$$

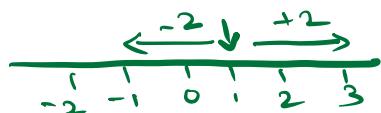
1st approach → consider all pairs

- $\begin{pmatrix} 1, 5 \end{pmatrix} \xrightarrow{4} \begin{pmatrix} 1, 3 \end{pmatrix} \xrightarrow{2}$
 - $\begin{pmatrix} 5, 3 \end{pmatrix} \rightarrow 2$

$$TC: O(n^2)$$

Scout

2nd approach →



$\lambda a_1 \dots \gamma$ search atK & a-K

If we sort arr, search on right

1, 3, 5 → search -1 and 3

$$TC: O(m \log n)$$
$$SC: O(m)$$

$$A = \langle \underline{1, 3, 5} \rangle \quad k=2$$

15x 2mg

Sct
 $\langle 1, 3, 5 \rangle$
↓

2nd
 $A = \underline{1, 3, 5}$

TC : $O(n) \rightarrow O(1)$

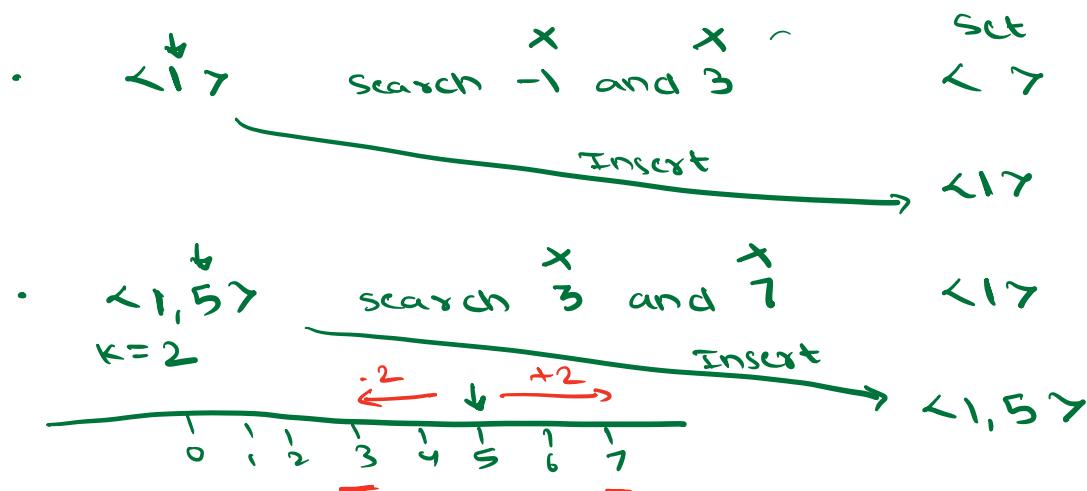
Step 1: Insertion in set $\rightarrow n$

Step 2: Finding $a+k$ & $a-k$ $\rightarrow n$

TC : $O(n)$
 going through
 arr 2 times

3rd (B) approach

$A = \underline{1, 5, 3}$
 $k = 2$



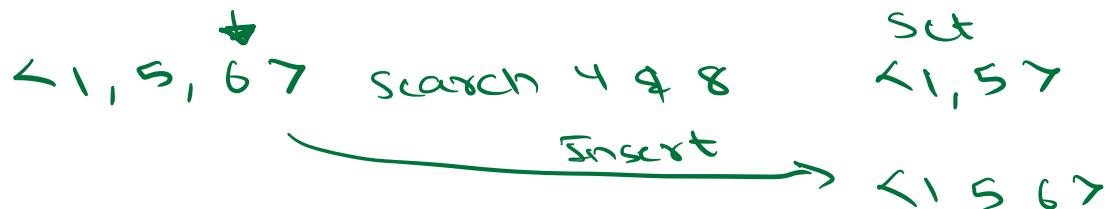
• $\underline{1, 5, 3}$ $k=2$ search $\overset{\checkmark}{1}$ and $\overset{\checkmark}{5}$ Set $\leftarrow \{1, 1, 3\}$
 $(3-2)$ $(3+2)$
 $(a-k)$ $(a+k)$

Return 1

$(3, 1 \text{ and } 3, 5)$

$A = \langle 1, 5, 6 \rangle$

$K = 2$



Reached end of A , return 0

Code:

```
public int diffPossible (final int[] A,  
                      int B) {  
  
    HashSet<Integer> s = new HashSet<Integer>();  
    for (int num : A) {  
  
        if (s.contains (num - B) ||  
            s.contains (num + B))  
            return 1;  
        s.add (num);  
    }  
    return 0;  
}
```

TC: $O(n)$
Iterating through
A once
SC: $O(n)$
 $(Set) \uparrow$

2. Largest Number $\langle 0, 1, 2, \dots \rangle$

Given an array A of non-negative integers, arrange them such that they form the largest number.
Note - The result may be very large, so return a string instead of an integer.

$$1 \leq \text{len}(A) \leq 100000$$

$$0 \leq A[i] \leq 2 \times 10^9$$

Ex $A = \langle 4, 2, 9, 1 \rangle$

$$\text{Nos.} \rightarrow 4291, 1294, \dots$$

$$\text{Total nos.} \rightarrow 4!$$

$$\text{Largest no.} \rightarrow 9421$$

$$(n!)$$

$$A = \langle 9, 4, 2, 1 \rangle$$

1. Sort \rightarrow Descending

2. Largest digit \rightarrow Left

Ex $A = \langle 3, 30, 34, 5, 9 \rangle$

$$\text{Nos.} \rightarrow 3303459, 3343059, \dots (5!)$$

Sort in descending

$$A = \langle 34, 30, 9, 5, 3 \rangle$$

No $\rightarrow 3430953 \times$ (Not largest)

Largest no $\rightarrow 9534330$

$$A = \langle 9, 5, 34, 3, 30 \rangle$$

Sort \rightarrow ↓↓↓ \times

Largest digit \rightarrow left ✓

$$A = \langle 30, 9 \rangle \rightarrow \text{Input}$$

$$\text{Nos} = 309 < 930 \checkmark$$

$$\langle 9, 30 \rangle \rightarrow \text{Output}$$

$$\begin{array}{r} x \\ 30 \\ \hline 9 \end{array}$$

$$\frac{4}{9} \frac{x}{30} > \frac{x}{30} \frac{y}{9}$$

(9 comes before 30)
y comes before x

$$\rightarrow -9--30-$$

$$2 \boxed{930} 5 > 2 \boxed{309} 5$$

$$29305 > 23095$$

$$A = \langle 3, 30, 34, 5, 9 \rangle$$

- $\langle 3, 30 \rangle$

$$\begin{array}{r} x \\ 4 \end{array}$$

$$\begin{array}{r} 330 > 303 \\ \times 4 \quad 4x \end{array}$$

x comes before 4
3 comes first

$$-3---30-$$

- $\langle 3, 34 \rangle$

$$\begin{array}{r} 334 < 343 \\ \times 4 \quad 4x \end{array}$$

y comes before x
34 comes 1st

$$\begin{array}{r} 5 \downarrow \quad 5 \downarrow \\ -34--3--30 \end{array}$$

- $\langle 3, 5 \rangle$

$$\begin{array}{r} 35 < 53 \\ \times 4 \quad 4x \end{array}$$

5 comes before 3

- $\langle 3, 9 \rangle$

$$\begin{array}{r} 39 < 93 \\ \times 4 \quad 4x \end{array}$$

9 comes before 3

$$\begin{array}{r} 9,5 \quad 9,5 \\ \downarrow \quad \downarrow \\ -34--3--30 \end{array}$$

- $\langle 30, 34 \rangle$

$$\begin{array}{r} 3034 < 3430 \\ \times 4 \quad 4x \end{array}$$

34 comes before 30

$$\begin{array}{r} 9,5 \quad 9,5 \\ \downarrow \quad \downarrow \\ -34--3--30 \end{array}$$

- $\langle 30, 5 \rangle$ $30 \underset{xy}{5} < 5 \underset{yx}{30}$ $\begin{array}{c} 9,5 \\ \downarrow \\ 34 \end{array} \quad \begin{array}{c} 9,5 \\ \downarrow \\ -3 \end{array} \quad \begin{array}{c} 9,5 \\ \downarrow \\ -30 \end{array}$
5 comes before 30
- $\langle 30, 9 \rangle$ $30 \underset{xy}{9} < 9 \underset{yx}{30}$ $\begin{array}{c} 9,5 \\ \downarrow \\ 34 \end{array} \quad \begin{array}{c} 9,5 \\ \downarrow \\ -3 \end{array} \quad \begin{array}{c} 9,5 \\ \downarrow \\ -30 \end{array}$
9 comes
- $\langle 34, 5 \rangle$ $34 \underset{xy}{5} < 5 \underset{yx}{43}$ $\begin{array}{c} 9 \\ \downarrow \\ 5 \end{array} \quad \begin{array}{c} 9 \\ \downarrow \\ 34 \end{array} \quad \begin{array}{c} 9 \\ \downarrow \\ -3 \end{array} \quad \begin{array}{c} 9 \\ \downarrow \\ -30 \end{array}$
5 comes before 34 ~~X~~
- $\langle 34, 9 \rangle$ $34 \underset{xy}{9} < 9 \underset{yx}{43}$ $\begin{array}{c} 9 \\ \downarrow \\ 5 \end{array} \quad \begin{array}{c} 9 \\ \downarrow \\ 34 \end{array} \quad \begin{array}{c} 9 \\ \downarrow \\ -3 \end{array} \quad \begin{array}{c} 9 \\ \downarrow \\ -30 \end{array}$
9 comes before 34 ~~X~~
- $\langle 5, 9 \rangle$ $5 \underset{xy}{9} < 9 \underset{yx}{5}$
9 comes before 5 $9 \quad 5 \quad 34 \quad -3 \quad -30$

$\langle 9, 5, 34, 3, 30 \rangle \rightarrow \text{custom sort}$
Largest no $\rightarrow 9534330$

Code :- A $\langle \underline{3}, 34, 30, 5, 9 \rangle$
Node \rightarrow any element in A

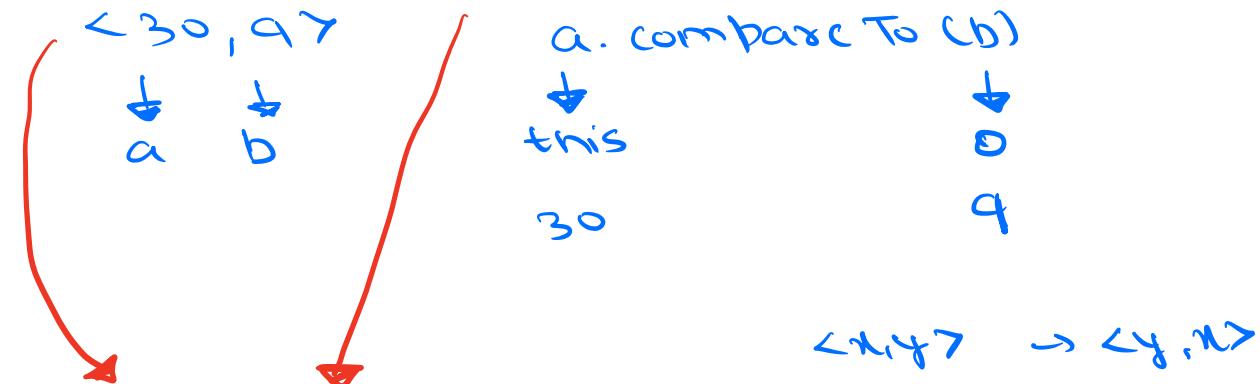
```
class Node implements Comparable<Node> {
    int number;
    public Node(int num) {
        this.number = num;
    }
}
```

```

@Override
public int compareTo(Node o) {
    // 309
    String xy = String.valueOf(this.number) +
        String.valueOf(o.number)
    // 930
    String yx = String.valueOf(o.number) +
        String.valueOf(this.number)

    return yx.compareTo(xy);
}
    "930".compareTo("309")

```



- public class Solution {


```
public String largestNum (List <Integer> A){
```

```

StringBuffer strbuf = new StringBuffer();
Node num[] = new Node[A.size()];
int i=0;
num = new Node[A.size()];

```

// integers stored in nodes // $\langle 30, 9 \rangle$

```

    "for (int n : A)           → n
    <
        num[i] = new Node(n);
        i++;
    >
    // num[0] = new Node(30);   → default
                                constructor

    ↗ 30
Node{this.number}           call compareTo
                            ↑
Arrays.sort(num);          // custom sort

    for (Node n : num) < → n
        if (n.number == 0 && strbuf.length() == 1 &&
            strbuf.toString()[0] == '0')
            continue;
        strbuf.append(n.number);
    >
    return strbuf.toString();  → largest
                                no.

    ↗ edge case

```

- $A = \langle \underline{0}, 0, 0, 0 \rangle$ code $\rightarrow 0000 \times$
 Largest No. $\rightarrow 0 \checkmark$
 - $A = \langle 0, 0, 0, 0 \rangle$ strbuf \rightarrow empty
 \uparrow "0"
 - $A = \langle 0, \underline{0}, 0, 0 \rangle$ "0"
 - $A = \langle 0, 30, 0, 0 \rangle$ $\rightarrow \langle 30, 0, 0 \rangle$
 Largest No. $\rightarrow 30 \underline{\underline{0}}$

TC $O(n \log n)$ sort algo

compareTo $\rightarrow O(1)$

SC $O(n)$ no. of nodes = A.size

3. Subarray with given sum

Given an array of positive integers A and integer B, find and return first continuous subarray which adds to B. If answer doesn't exist, return an array with single element -1.

First sub-array means the sub-array for which starting index is minimum.

$$A = \langle 2, 1, 3, 1, 5 \rangle$$

$$B = 5$$

$$\langle 2, 3, 4 \rangle \quad \langle 4 \rangle$$

output $\rightarrow \langle 1, 3, 1 \rangle$

$$\min(2, 4) = 2$$

1st Approach - Consider all subarrays

	sum = 0	
• 2	sum = 2	2 ≠ 5 2 < 5
• 2, 1	sum = 3	3 ≠ 5 3 < 5
• 2, 1, 3	sum = 6	6 ≠ 5 6 > 5

$\underbrace{\langle 2, 1, 3, 1 \rangle}_> \quad X$ sum $> B$ stop
 $(i++)$

i	sum = 0	
1	sum = 1	1 ≠ 5 1 < 5
1, 3	sum = 4	4 ≠ 5 4 < 5
1, 3, 1	sum = 5	5 = 5
i i		return (1, 3, 1)

$\langle i, j \rangle$ subarray

TC $O(n^2) < i$
SC $O(1)$

$$A = \langle 1, 2, 3, 4 \rangle$$

$$B = 50$$

↓
Worst case

$$A = \langle 2, 1, 3, 4, 6, 6 \rangle$$

$$B = 12$$

$\cdot 2$

i, j

+1

$$\text{sum} = 0$$

$$\text{sum} = 2$$

$$2 < 12$$

($\text{sum} < B$
 $j++$)

$\cdot 2, 1$

i, j

+3

$$\text{sum} = 3$$

$$3 < 12$$

$\cdot 2, 1, 3$

i, j

+4

$$\text{sum} = 6$$

$$6 < 12$$

$\cdot 2, 1, 3, 4$

i, j

+6

$$\text{sum} = 10$$

$$10 < 12$$

$\cdot 2, 1, 3, 4, 6$

i, j

-2

$$\text{sum} = 16$$

$$16 > 12 \quad X$$

stop ($\text{sum} > B$)

$\cdot 1, 3, 4, 6$

i, j

$$\text{sum} = 14$$

$$14 > 12 \quad X$$

stop

$$\begin{array}{c} 1, 3, 4, 6 \\ 1, 3, 4, 6, 6 \end{array} \quad X$$

$$\begin{array}{c} 1 \\ 1, 3 \\ 1, 3, 4 \end{array} \quad X$$

sum

$$\langle 2, 1, 3, 4 \rangle < 12$$

$\downarrow -2$

$$\text{sum } \langle 1, 3, 4 \rangle < 12$$

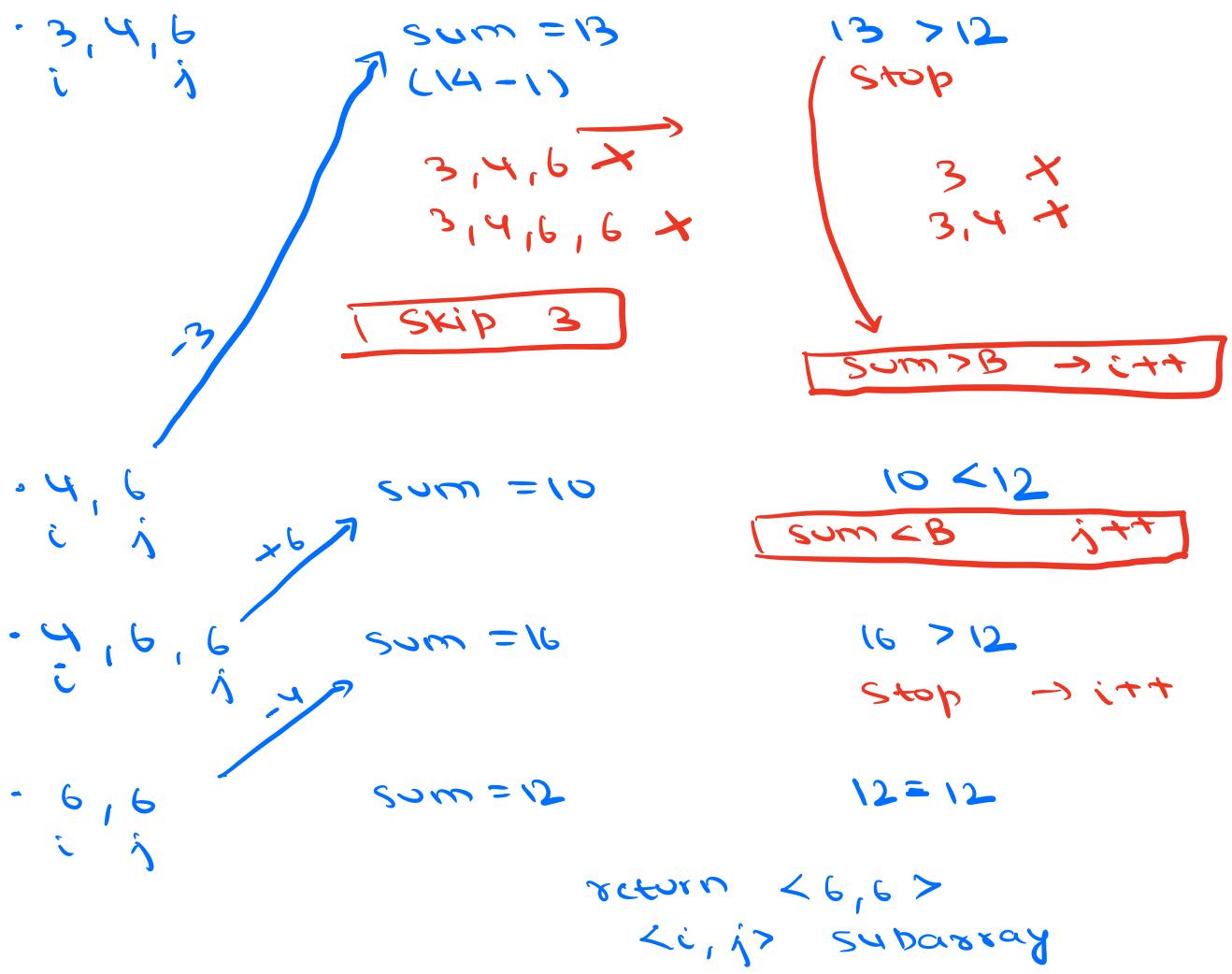
$$x < 12$$

$$x - 2 < 12$$

skip 1

sum > B

i++



sum $< B$ $j++$
 sum = B $\langle i, j \rangle$
 sum $> B$ $i++$

Code

```
public int[] solve(int[] A, int B) {  
    long n = A.length  
    int i=0, j, sum=0;  
    for(j=0; j<n; j++) {  
        sum += A[j];  
        if(sum > B) {  
            while(sum>B) {  
                sum -= A[i];  
                i++;  
            }  
        }  
        else if(sum==B) {  
            int[] ans = new int[j-i+1];  
            for(int k=i; k<=j; k++)  
                ans[k-i] = A[k];  
            return ans;  
        }  
    }  
    int[] ans = new int[1];  
    ans[0] = -1;  
    return ans;  
}
```

TC $O(n)$
2 op per element
① addition
② removal
 $2n$ ops
 $\in O(1)$

4. Sort by Color

Given an array with N objects colored red, white or blue, sort them so that objects of the same color are adjacent, with colors in order red, white & blue. We will use the integers 0,1,2 to represent red, white and blue respectively.

Note - using the library sort function is not allowed.

R, W, B
[0 1 2] → output

Sort 0,1,2

A = [0, 1, 2, 0, 1, 2]

1st approach → count 0s, 1s and 2s

Step 1: $c_0 = \underline{2}$, $c_1 = 2$, $c_2 = 2$

TC $O(N)$

SC $O(1)$

Step 2: $\begin{array}{cccccc} 0 & 1 & 2 & 0 & 1 & 2 \\ \swarrow & \swarrow & \swarrow & \swarrow & \swarrow & \swarrow \\ 0 & 0 & 1 & 1 & 2 & 2 \end{array}$

2 iterations

2nd approach →

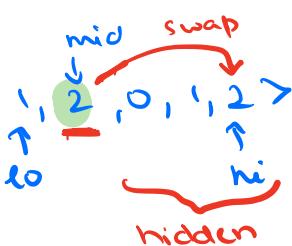
$\begin{array}{ccc} 0 & 1 & 2 \\ \text{Left} & \text{Mid} & \text{Right} \end{array}$

$\begin{array}{cccccc} 0 & 0 & \underline{1} & 1 & 2 & 2 & 2 & 2 & 2 & 2 \\ \leftarrow & \xrightarrow{\text{Mid}} & & \xrightarrow{\text{pivot}} & \longrightarrow \\ 0 \text{ to left} & & & & 2 \text{ to right} \end{array}$

\downarrow
 mid
 $A = \langle 0, 1, 2, 0, 1, 2 \rangle$
 \uparrow
 lo
 \uparrow
 hi

$lo \rightarrow 0$ is placed
 $hi \rightarrow 2$ is placed
 $mid \rightarrow$ array iteration

- $A = \langle 0, 1, 2, 0, 1, 2 \rangle$
 \downarrow

- $A = \langle 0, 1, 2, 0, 1, 2 \rangle$
 \downarrow
 \uparrow
 mid swap
 \uparrow
 lo
 \uparrow
 hi
 \uparrow


1 starts where 0 ends
 $\boxed{\text{mid}++}$ (move to next element)

don't know $A[hi]$
 $\boxed{\text{swap}(A[mid], A[hi])}$

- $\langle 0, 1, 2, 0, 1, 2 \rangle$
 \downarrow
 mid
 \uparrow
 lo
 \uparrow
 hi
- $A = \langle 0, 1, 2, 0, 1, 2 \rangle$
 \downarrow
 \uparrow
 mid swap
 \uparrow
 lo
 \uparrow
 hi
 \uparrow
 $\langle 0, 1, 1, 0, 2, 2 \rangle$
 \uparrow
 mid hi

$hi \rightarrow$ index where 2 should be placed

$\boxed{hi - 1}$
 mid not incremented \rightarrow bcoz it is not processed

$\boxed{\text{swap}(A[mid], A[hi])}$

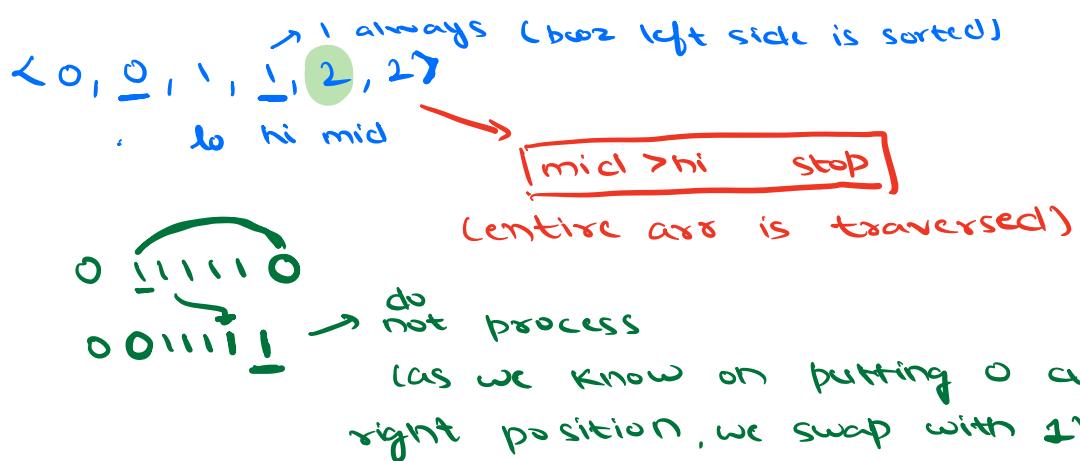
$hi = hi - 1$

- $A = \langle 0, 1, 1, 0, 2, 2 \rangle$
 \downarrow
 mid
 \uparrow
 lo
 \uparrow
 hi
- $A = \langle 0, 1, 1, 0, 2, 2 \rangle$
 \downarrow
 swap
 \uparrow
 lo
 \uparrow
 mid
 \uparrow
 hi

$\boxed{\text{mid}++}$

$\boxed{\text{swap}(A[lo], A[mid])}$

$lo++$, $mid++$



Code

```

public ArrayList<Integer> sort01
  (ArrayList<Integer> A) {
    int lo=0, hi=A.size()-1;
    for (int mid=0; mid <= hi; ) {
      if (A.get(mid) == 0) {
        int temp = A.get(lo);
        A.set(lo, 0);
        A.set(mid, temp);
        lo++;
        mid++;
      }
      else if (A.get(mid) == 2) {
        int temp = A.get(hi);
        A.set(hi, 2);
        A.set(mid, temp);
        hi--;
      }
      else
        mid++;
    }
  }
  
```

1 iteration

TC O(n)

SC O(1)

// A[mid] = 1

```
| return A;
```