

Bitmasking

& and
 | or
 ^ xor
 ~ not

done

<< Left Shift
 >> Right Shift

directly on bit

5



0000 101
 ← 32 bit →

Left Shift (<<) → Two operands

$a \ll b$

5

5

→

0000 000 101
 ← fill with 1 on right

5 << 1

→

0000 0101 0
 ⇒ 10

$$13 \Rightarrow \boxed{x}$$

$$\downarrow$$

$$13 \ll 1 = 26$$

$$\boxed{y}$$

$$\begin{array}{cccc} 8 & 4 & 2 & 1 \\ 0 & 1 & 0 & 1 \end{array} = 8 + 4 + 1 = \boxed{13}$$

$$\leftarrow$$

$$\begin{array}{cccc} 16 & 8 & 4 & 2 & 1 \\ 1 & 1 & 0 & 1 & 0 \end{array} = 16 + 8 + 2 = 26$$

$$x = 2^3 + 2^2 + 2^0$$

Doing
left
by 1
multiplies the
no by 2

$$y = 2^4 + 2^3 + 2^1$$

$$= 2(2^3 + 2^2 + 2^0)$$

$$= \boxed{y = 2x}$$

$$5 \rightarrow 101$$

$$5 \ll 1 \rightarrow \underline{1010}$$

$$10 \ll 1 \rightarrow 10100$$

$$\begin{array}{c} \textcircled{5} \\ \textcircled{10} \\ \boxed{20} \end{array}$$

Loss of
data
for
range
no

0000

New No is outside the range of int. \otimes

$$5 \ll 2 \rightarrow \underline{10100} = \boxed{20}$$

$$\rightarrow \boxed{a \ll b \Rightarrow a \times 2^b}$$

left shift operator

$$5 \ll 1 \text{ ? Two times}$$

$$\boxed{5 \ll 2}$$

$$5 \times 2 \times 2$$

$$5 \times 2^2$$

$$= \boxed{20}$$

[illegible]

$$8 << (2) \Rightarrow \begin{array}{c} \boxed{1000} \\ 2^8 \ 2^4 \ 2^2 \ 2^1 \ 2^0 \end{array} \begin{array}{c} 00 \\ 00 \end{array} \curvearrowright$$

$$2^3 \curvearrowright 2^5$$

Right Shift Operator

↳ Divide by Powers of 2

20
↓

10100
16 8 4 2 1
→
0

$20 \gg 1$

01010
→
0

$= 10 \gg 1 \leftarrow$

00101
→
0

$= 5 \gg 1 \leftarrow$

$5 \gg 1 = \frac{5}{2}$ ^{int div}

00010
→
0

$= 2 \gg 1 \leftarrow$

00001
→
0

$= 1 \gg 1$

$= 0$

$$a \gg b = \frac{a}{2^b}$$

Result

$$20 \gg 3 = \frac{20}{2 \cdot 2 \cdot 2} = \frac{20}{2^3} = \frac{20}{8} = 2$$

Java
(specific)

"Signed" Right Shift

$>>$

Unsigned Right Shift

$>>>$

mean the MSB (32nd bit) denotes

the sign of no

+ve



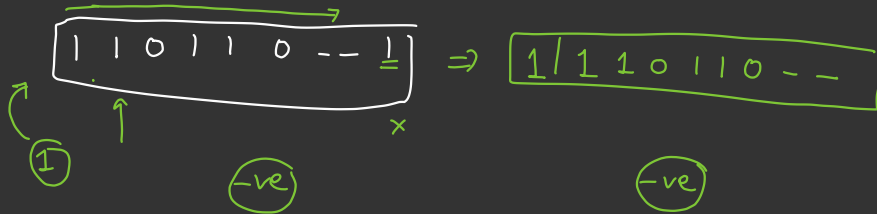
-ve



uses the MSB/left most bit to fill
trailing positions after the shift.

if you have negative, then filler \rightarrow 1

positive, then filler \rightarrow 0



$$x = -9$$

$$y = 9$$

$$x \gg 2$$

$$y \gg 2$$

$$\Rightarrow \frac{-9}{2^2} = \frac{-9}{4} = \boxed{-2}$$

$$\frac{9}{2^2} = \boxed{2}$$

Q. $\boxed{-5} \rightarrow$ stored \rightarrow 2's complement form

$$\begin{array}{l} 5 \rightarrow \boxed{0101} \\ -5 \rightarrow \end{array}$$

$$\begin{array}{l} \text{① } -5 \rightarrow \boxed{1011} \end{array}$$

$$\begin{array}{l} \text{③ } \leftarrow \boxed{-5 \gg 1} \end{array}$$

$$\begin{array}{r} -a \gg b \\ \hline \rightarrow a \\ \hline 2b \end{array}$$

$$\begin{array}{l} -(-x) \\ || \\ + \boxed{x} \\ \hline \text{③} \end{array}$$

$$\begin{array}{r} \text{flip all} \\ \boxed{0}010 \\ + \quad \quad \quad 1 \\ \hline 0011 \end{array}$$

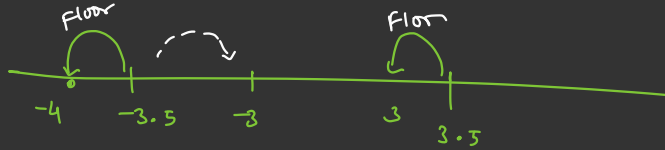
$$\begin{array}{l} \xrightarrow{\quad} 101x \\ \text{filler} \\ \text{①} \end{array}$$

$$\rightarrow \text{ve } \text{①} -(-x)$$

$$\begin{array}{l} \text{2s complement for} \\ \downarrow \\ \text{flip +1} \end{array}$$

$$\rightarrow \text{③}$$

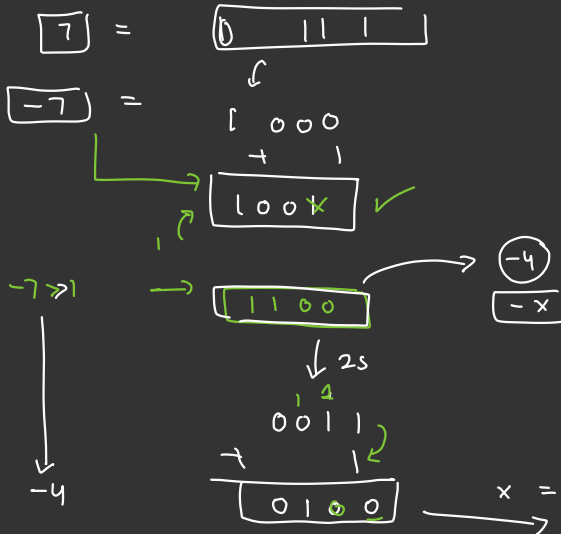
$$a \gg b = \text{floor} \left(\frac{a}{2^b} \right) \quad \begin{array}{l} \text{for both} \\ \text{+ve \&} \\ \text{-ve} \\ \text{no's} \end{array}$$



$$-7 \gg 1 = -4$$

$$+7 \gg 1 = 3$$

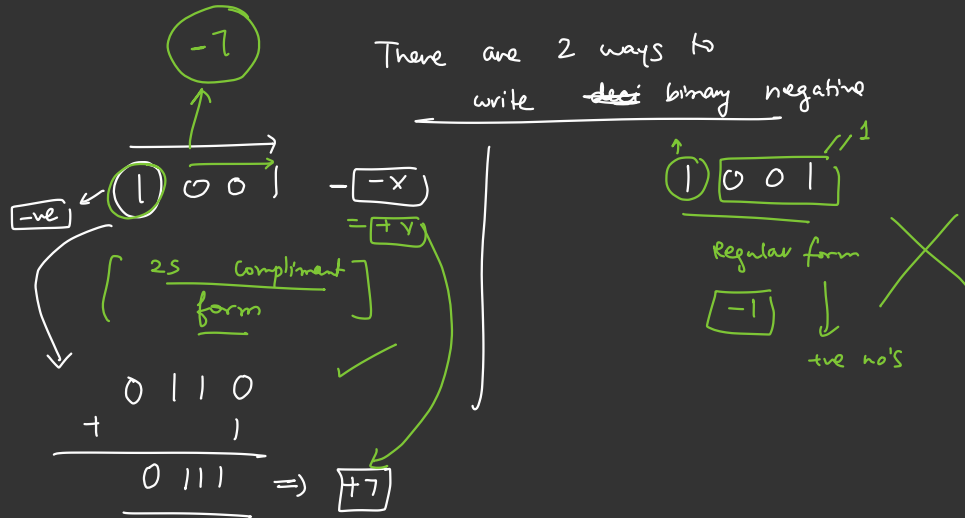
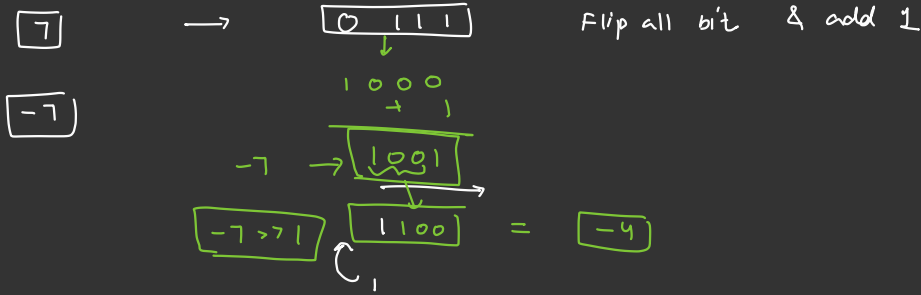
Reap



$$-(-x) = +x$$

$$\begin{array}{l} 1+1 = 10 \\ 0+1 = 1 \\ 1+0 = 0 \\ 0+0 = 0 \end{array}$$

Give a no, how to find in 2's complement

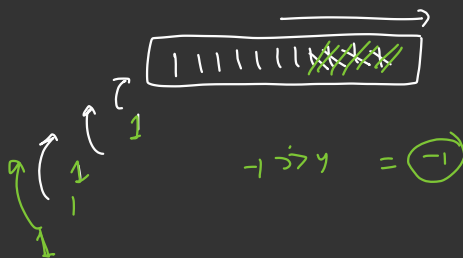


$$x = -1$$



Guess the output

$$-1 \gg 4$$



$$\begin{array}{r} +1 \quad 00000 \downarrow \\ \downarrow \\ -ve \quad 111110 \\ + \quad 1 \\ \hline 111111 \end{array}$$

$$1 \gg 4 = \frac{1}{2^4} = 0$$

$$00000 \gg 4 = 0$$

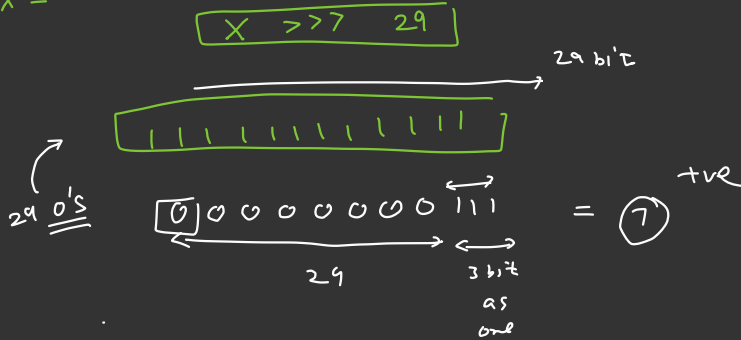
doesn't differentiate b/w +ve & -ve no

Unsigned Right Shift \ggg

filler $\rightarrow 0 \rightarrow +ve$
 $\rightarrow 1 \rightarrow -ve$

Filler is always 0

$x = -1$

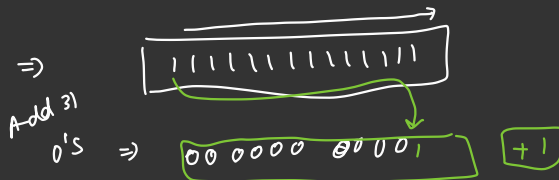


$(5) \gg 1 \rightarrow$

$010x$

\gg, \ggg

$-1 \gg 31$



$\begin{matrix} \text{unsigned} \\ \downarrow \\ -5 \gg 2 \end{matrix} \rightarrow \begin{matrix} 10 ** \\ 0010 \\ = 2 \end{matrix}$

$\rightarrow 00000101$
 $-5 \quad 1010$
 $+1$

(a) Given a pos No., find out the No of set bits in that No
 Input $\rightarrow 5 \rightarrow 000101 \rightarrow 2$
 $\rightarrow 7 \rightarrow 000111 \rightarrow 3$

Decimal to Binary

$\begin{array}{r|l} 2 & 13 \\ \hline 2 & 6, 1 \\ 2 & 3, 0 \\ 2 & 1, 1 \\ & 0, 1 \end{array}$

1101

$n = 13, \text{cnt} = 0$
 $\text{while}(n > 0) \{$
 $\text{rem} = n \% 2;$
 $\text{cnt} = \text{cnt} + \text{rem};$
 $n = n / 2;$
 $\text{print}(\text{cnt});$

$n = 13 > 0$
 \downarrow
 $6 > 0$
 \downarrow
 $3 > 0$
 \downarrow
 $1 > 0$
 \downarrow
 0

$\text{rem} = 1$
 $= 0$

$\text{cnt} = 0$
 $= +1$
 $\rightarrow 0$

$$\begin{array}{rcl}
 3 & > 0 & = 1 \quad + 1 \\
 \downarrow & & \\
 1 & > 0 & = 1 \quad + 1 \\
 \downarrow & & \\
 0 & & \underline{\quad} \quad \text{set bit} \\
 & & \textcircled{3}
 \end{array}$$

Bitwise
way

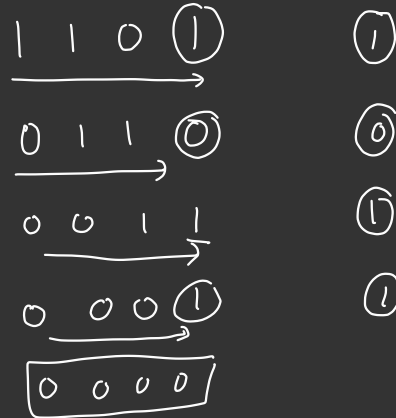
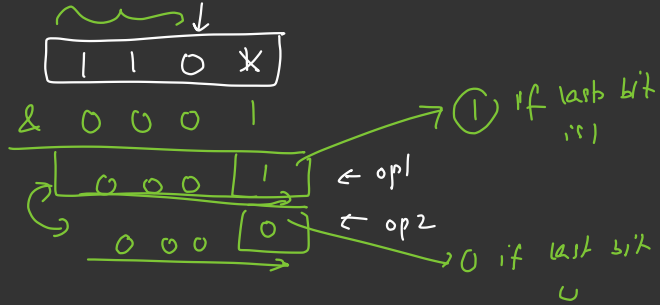
$$N = 13$$

$$n = 13, \text{ cnt} = 0$$

while(n > 0) {

$$\begin{aligned}
 \rightarrow \text{last_bit} &= n \& 1 \\
 \text{cnt} &= \text{cnt} + \text{last_bit} \\
 n &= n >> 1
 \end{aligned}$$

print(cnt)



0000000010100~~0~~

...00001010~~0~~ = 20

101~~0~~ = 10

101 = 5

10 = 2

1 = 1

0

~
↓
1/2
↓
0

→ log N

90

≤ 32
O(1)
complexity

101000
32 16 8 4 2 1

h = n > 1

20

↓

10

↓

5

↓

5

↓

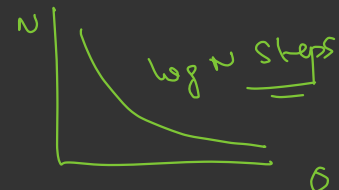
2

↓

1

↓

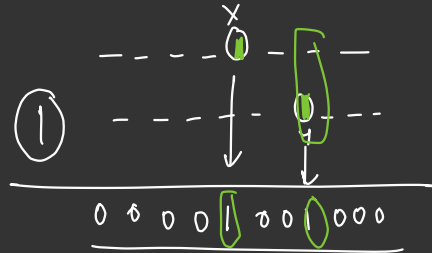
0



$$\begin{array}{r} 1000 \\ + 10 \\ \hline 1010 \\ \downarrow \\ 10 \end{array}$$

$$\begin{array}{r} 10 \\ \hline 2 \end{array}$$

$$\text{ans} = \left(\underline{1 \ll x} \right) \mid \left(\underline{1 \ll y} \right)$$



OR → Bit Level

$$\begin{array}{rcl} 1 \ll 3 & = & \overrightarrow{1000} \\ 1 \ll 1 & = & \begin{array}{r} 0010 \\ \hline 1010 \end{array} \end{array}$$

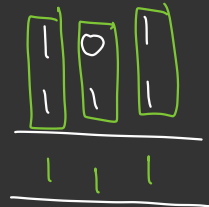
OR → no carry.

Addition
1 + 1 = 10

$$1 \mid 1 = 1$$

ORing

$$5 \mid 7 =$$



$$\left\{ \begin{array}{l} 1 \text{ or } 1 = 1 \\ 1 \text{ or } 0 = 1 \\ 0 \text{ or } 1 = 1 \\ 0 \text{ or } 0 = 0 \end{array} \right\}$$

bits

2 2 1 0
6 0 0 0 1 0 1 0

or

6000 10000
000000010

powers of 2

$$2^3 \oplus 2^1 \leftarrow$$
$$= 8 + 2$$
$$= 10$$

get i^{th} bit (no, i)

13

31 ... 7 3 2 1 0
0000 1 1 0 1

↑

→ make this bit
as last bit

no \rightarrow $\begin{matrix} 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 1 \end{matrix}$ ✓

\downarrow
 $\begin{matrix} 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \end{matrix}$ ✓

\downarrow
 $\begin{matrix} 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \end{matrix}$ ✓

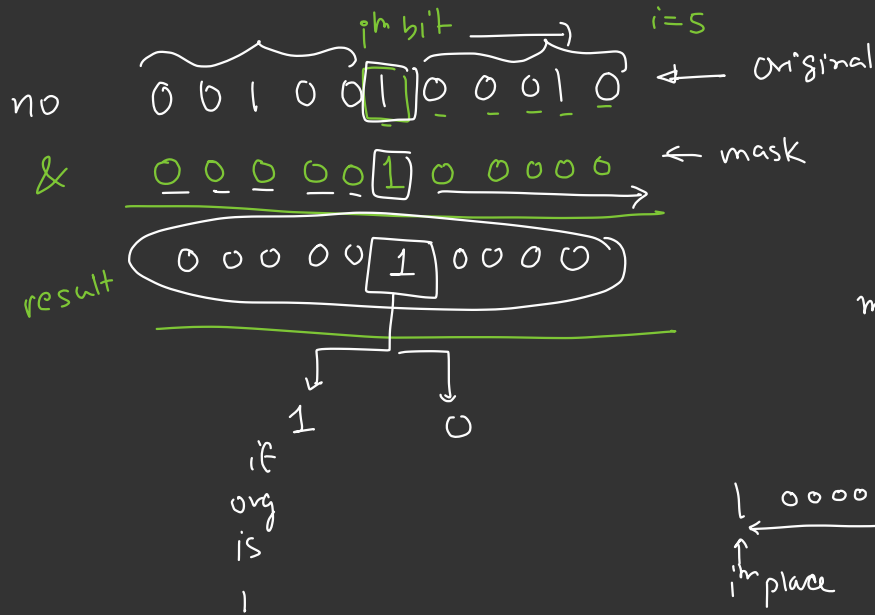
\downarrow
 $\begin{matrix} 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \end{matrix}$
 1st bit now at last

$\left. \begin{matrix} \text{1st times} \\ \text{Right} \\ \text{Shift} \end{matrix} \right\}$

Way-1

$(no \gg i) \& 1$
 $\Rightarrow 1$
 $\Rightarrow 0$

way-2



$$1 \ll 1^0$$

$$\text{mask} = (1 \ll i)$$

no & mask

$\text{result} = 0 \rightarrow 1^{\text{st}} \text{ bit } 0$
 $\text{result} > 0 \rightarrow 1^{\text{st}} \text{ bit } 1$

1 (0 1 ~~0~~ ~~1~~

↑
last
bit

A_{p-1}

$\begin{array}{ccccccc} & & & 2 & 1 & 0 & \\ \times & \times & 0 & \boxed{1} & 0 & 1 & \times \end{array}$
 $\begin{array}{r} 8 \quad \boxed{000100} \\ \hline 000100 \end{array} \rightarrow \begin{array}{l} \boxed{1 < 2} \\ 70 \Rightarrow 1 \end{array}$
 $\begin{array}{r} 000000 \\ \hline \end{array} \rightarrow \textcircled{0}$

$\begin{array}{r} 00001000 \\ \hline \end{array}$
 \uparrow
 $i \text{th} \text{ bit} \Rightarrow \underline{1 < i}$

Q Given N , set i^{th} Bit in N

$N =$

3	2	1	0
1	1	0	1

\rightarrow

1	1	1	1
---	---	---	---

set \rightarrow 1st bit as 1

set \rightarrow 3rd bit as 1

i^{th} bit
 \downarrow
 i^{th} bit \rightarrow 1

1	1
---	---

1	1	1	0	1
---	---	---	---	---

0 0 1 0 0 0 0 0 $\leftarrow \text{mask} = 1 \ll i$

1 1 1 1 1 0 1

Bit
wise
OR

$N =$

N	mask
-----	---------------

$=$

N	$(1 \ll i)$
-----	-------------

$$1 \ll 0$$

$$= 1$$

$$N = 13$$

$$\begin{array}{cccc} & & i=1 \rightarrow 1 & \\ 3 & 2 & 1 & 0 \\ 1 & 1 & 0 & 1 \\ \hline 1 & 1 & 1 & 1 \\ \hline \boxed{15} \end{array}$$

$$1 \ll 1$$

$$= 10$$

$$1 \ll 2$$

$$= 100$$

$$1 \ll 3$$

$$= 1000$$

$$1 \ll 4$$

$$= 10000$$

$$1 \ll i$$

$$= \underbrace{10000000}_{\text{zeros}}$$

$$13 \mid (1 \ll 1)$$

$$= 1101 \mid 10$$

$$= \boxed{1111}$$

To Do

Unset at loc i ,

→ Given a No, make its bit as 0. ??

$$\begin{array}{c} N = \\ 13 \end{array}$$

$$\begin{array}{cccc} i=2 & i=2 & i=1 & i=0 \\ 1 & 1 & 0 & 1 \end{array}$$

$$\Rightarrow \boxed{1001}$$

Binary Addition

$$\begin{array}{r}
 \begin{array}{ccccccc}
 & 1 & & 1 & & & \\
 16 & 8 & 4 & 2 & 1 & & \\
 1 & 0 & 1 & 1 & 0 & & \\
 + & 0 & 0 & 1 & 1 & 1 & \\
 \hline
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 1 \quad 1 \quad \boxed{1} \quad 0 \quad 1 \\
 \hline
 16 \quad 8 \quad 4 \quad 2 \quad 1
 \end{array}$$

$$\rightarrow \textcircled{22}$$

$$\rightarrow \textcircled{7} = \textcircled{29}$$

$$\rightarrow \boxed{29}$$

$$\boxed{11}$$

$$\boxed{D14}$$

$$1+1 = \boxed{10}$$

↑

$$1+1 = \boxed{2}$$

$$2 \times 2 = 0$$

$$2/2 \Rightarrow 1$$

carry →
rem →

$$3 \times 2 =$$

$$3/2 \Rightarrow 1$$

$$1+1+1$$

$$= 3$$

$$= \boxed{11}$$

$$1+1+1$$

$$= 10+1$$

$$= \boxed{11}$$

Addition

$$\begin{array}{r}
 \begin{array}{cccc}
 & 1 & & 1 \\
 7 & 8 & 3 & 9 \\
 3 & 9 & 4 & 8 \\
 \hline
 11 & 7 & 8 & \textcircled{7}
 \end{array}
 \end{array}$$

$$9+8 = \boxed{17}$$

$$\text{rem} = 17 \times \textcircled{10} = \textcircled{7}$$

$$\text{carry} = 17 / \textcircled{10} = \boxed{1}$$

↑
Base