

50612 11.
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5.

	Abby	Bess	Cody	Dana
Abby	x		x	x
Bess		x		x
Cody			x	
Dana		x	x	

Sol:

$\text{Like} (\text{Abby}, \text{Abby})$
 $\sim \text{Like} (\text{Abby}, \text{Bess})$
 $\text{Like} (\text{Abby}, \text{Cody})$
 $\text{Like} (\text{Abby}, \text{Dana})$

$\sim \text{Like} (\text{Bess}, \text{Abby})$
 $\text{Like} (\text{Bess}, \text{Bess})$
 $\sim \text{Like} (\text{Bess}, \text{Cody})$
 $\text{Like} (\text{Bess}, \text{Dana})$

$\sim \text{Like} (\text{Cody}, \text{Abby})$
 $\sim \text{Like} (\text{Cody}, \text{Bess})$
 $\text{Like} (\text{Cody}, \text{Cody})$
 $\sim \text{Like} (\text{Cody}, \text{Dana})$

$\sim \text{Like} (\text{Dana}, \text{Abby})$
 $\text{Like} (\text{Dana}, \text{Bess})$
 $\text{Like} (\text{Dana}, \text{Cody})$
 $\sim \text{Like} (\text{Dana}, \text{Dana})$

1. $\forall x \text{ likes}(x, x)$. $\forall n \Rightarrow \text{Universal}$

$x = \text{Abby, Bess, Cody, Dana}$.

$\text{likes}(\text{Abby}, \text{Abby})$ True

$\text{likes}(\text{Bess}, \text{Bess})$ True

$\text{likes}(\text{Cody}, \text{Cody})$ True

$\text{likes}(\text{Dana}, \text{Dana})$ false.

$\forall x \text{ likes}(x, x)$ is ~~true~~ false.

2. $\forall x \exists y. \text{likes}(x, y)$. Everybody likes somebody.

$\exists y \Rightarrow \text{Existential}$.

$\exists y \text{ likes}(\text{Abby}, y)$

$\text{likes}(\text{Abby}, \text{Cody})$

$\exists y \text{ likes}(\text{Bess}, y)$

$\text{likes}(\text{Bess}, \text{Bess})$.

$\exists y \text{ likes}(\text{Cody}, y)$

$\text{likes}(\text{Cody}, \text{Cody})$

$\exists y \text{ likes}(\text{Dana}, y)$

$\text{likes}(\text{Dana}, \text{Cody})$.

$\forall x \exists y \text{ likes}(x, y)$ is true.

3. $\exists y. \forall x \text{ likes}(x, y)$. ~~There is some one everyone likes.~~

~~True~~ This is false because Dana doesn't like herself.

$\exists y \text{ likes}(\text{Abby}, \text{Abby})$ True

$\exists y \text{ likes}(\text{Bess}, \text{Bess})$ True

$\exists y \text{ likes}(\text{Cody}, \text{Cody})$ True

$\exists y \text{ likes}(\text{Dana}, \text{Dana})$ false.

$$4. \forall x \forall y \text{ likes}(x, y) \rightarrow \text{likes}(y, x).$$

$\forall x \forall y \Rightarrow$ Universal so we must check for every possibility.
for instance

$\text{likes}(\text{Abby}, \text{ody})$ True. But $\text{likes}(\text{ody}, \text{Abby})$ false

Hence.

$\forall x \forall y \text{ likes}(x, y) \rightarrow \text{likes}(y, x)$ is false.

$$5. \forall x \forall y (\exists z. \text{likes}(x, z) \wedge \text{likes}(z, y)) \rightarrow \text{likes}(x, y).$$

$\text{likes}(\text{Abby}, \text{Dana})$

$\text{likes}(\text{Dana}, \text{Ben})$

$\rightarrow \text{likes}(\text{Abby}, \text{Ben}).$

$\therefore \forall x \forall y (\exists z. \text{likes}(x, z) \wedge \text{likes}(z, y)) \rightarrow \text{likes}(x, y)$ is false.

$$1. \quad \varphi_1: P \rightarrow Q$$

$$\varphi_2: (Q \rightarrow (S \wedge T))$$

$$\varphi_3: (R \rightarrow (S \wedge T))$$

$$\varphi_4: (P \vee R)$$

$$\varphi = S \wedge T$$

$$\Phi = \{\varphi_1, \varphi_2, \varphi_3, \varphi_4\}$$

to prove that $\Phi \models \varphi$, $S \wedge T \models$

logically consequence, use resolution method. Aim is to derive the

from ~~conf~~ conf empty clause from the conf of $\Phi \cup \{\neg \varphi\}$

$$(\varphi_1 \wedge \varphi_2 \wedge \varphi_3 \wedge \varphi_4) \wedge \neg \varphi$$

$$\varphi_1: (P \rightarrow Q) \equiv (\neg P \vee Q) \quad (\because \text{logically equivalent}).$$

$$\varphi \rightarrow \psi = \neg \varphi \vee \psi \quad \begin{matrix} \Downarrow \\ \{ \neg P, Q \} \end{matrix}$$

$$\varphi_2: (Q \rightarrow (S \wedge T)) \equiv \neg Q \vee (S \wedge T)$$

$$\equiv (\neg Q \vee S) \wedge (\neg Q \vee T) \Rightarrow \begin{matrix} \{ \neg Q, S \} \\ \{ \neg Q, T \} \end{matrix}$$

$$\varphi_3: (R \rightarrow (S \wedge T)) \equiv \neg R \vee (S \wedge T)$$

$$\equiv (\neg R \vee S) \wedge (\neg R \vee T) \\ \equiv (\neg R \vee S) \wedge (\neg R \vee T)$$

ψ

$$\varphi_4: P \vee R \Rightarrow \begin{matrix} \{ \neg P, S \} \\ \{ \neg R, T \} \end{matrix}$$

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$$1. \{ \neg P, a \}$$

$$2. \{ \neg a, s \}$$

$$3. \{ \neg a, t \}$$

$$4. \{ \neg r, s \}$$

$$5. \{ \neg r, s \}$$

$$6. \{ P, r \}$$

$$7. \{ \neg r, \neg t \}$$

$$8: (1,6) \rightarrow \{ a, r \}$$

$$9: (6,7) \rightarrow \{ a, \neg t \}$$

$$10: (9,3) \rightarrow \{ \}$$

$$8: \frac{\begin{array}{l} \{ \neg P, a \} \\ \{ P, r \} \end{array}}{\{ a, r \}}$$

$$9: \frac{\begin{array}{l} \{ a, r \} \\ \{ \neg t, r \} \end{array}}{\{ a, \neg t \}}$$

If the set ϕ is not consistent we can derive every formulae ψ as a logical consequence. But there is an interpretation that satisfies $\psi_1 \wedge \psi_2 \wedge \psi_3 \wedge \psi_4$, so the set ϕ is consistent.

The interpretation is $p^i = F, q^i = F, r^i = T, s^i = T, t^i = T$.

This continue with resolution method and try to derive empty clause.

\Rightarrow The Snt is logically consequence of $\phi = \{\psi_1, \psi_2, \psi_3, \psi_4\}$.