

# Introduction to ML and Support Vector Machines

- Vikas Thammanna Gowda

# Agenda

- **What is ML? Why ML?**
- **Categories of ML**
- **Support Vector Machines**
  - ◆ **Basic idea**
  - ◆ **Special Cases**
  - ◆ **History and Development**
  - ◆ **Math**

# What is Machine Learning?

**Arthur Samuel:** Machine Learning is the field of study that gives computers the ability to learn without being explicitly programmed.

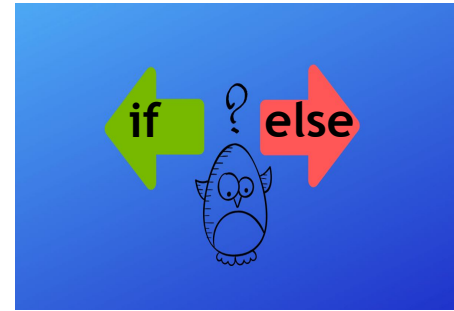
**ML** is a collection of **algorithms** and techniques used to create computational systems that **learn from data** in order to make **predictions** and inferences.



# Why Machine Learning?



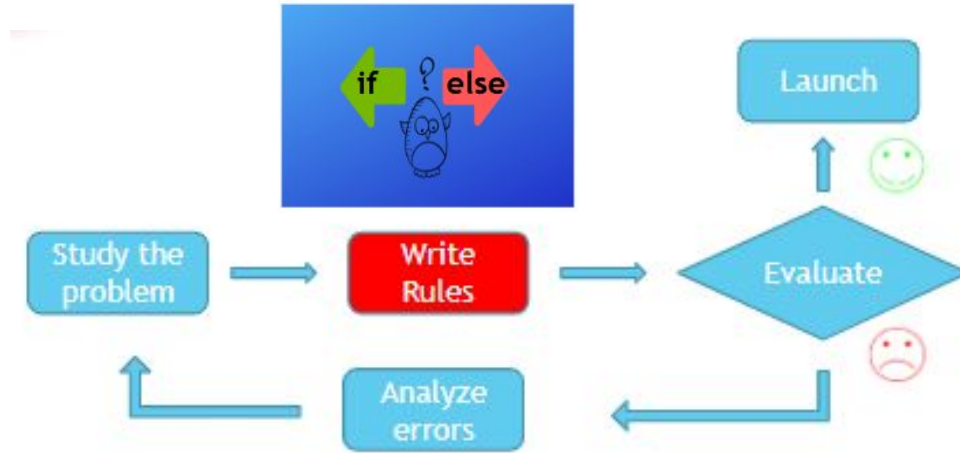
4U  
credit card  
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amazing





# Why Machine Learning?

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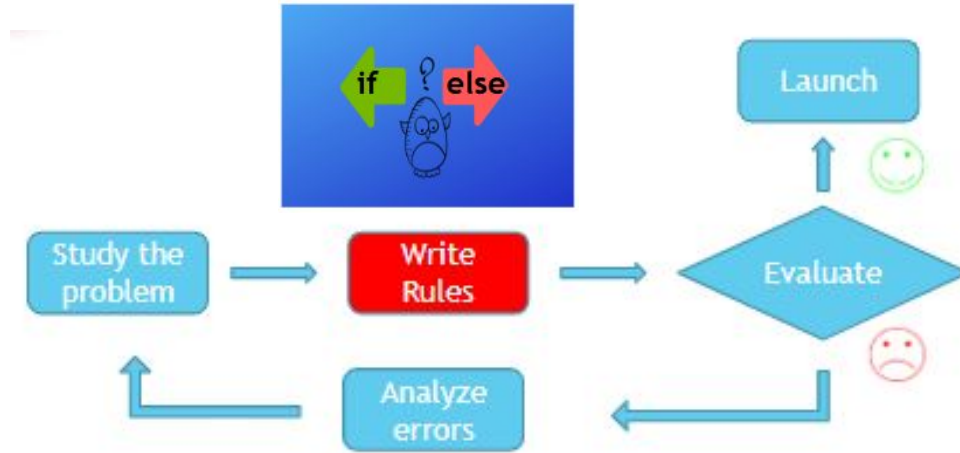


The traditional approach



# Why Machine Learning?

**For U**  
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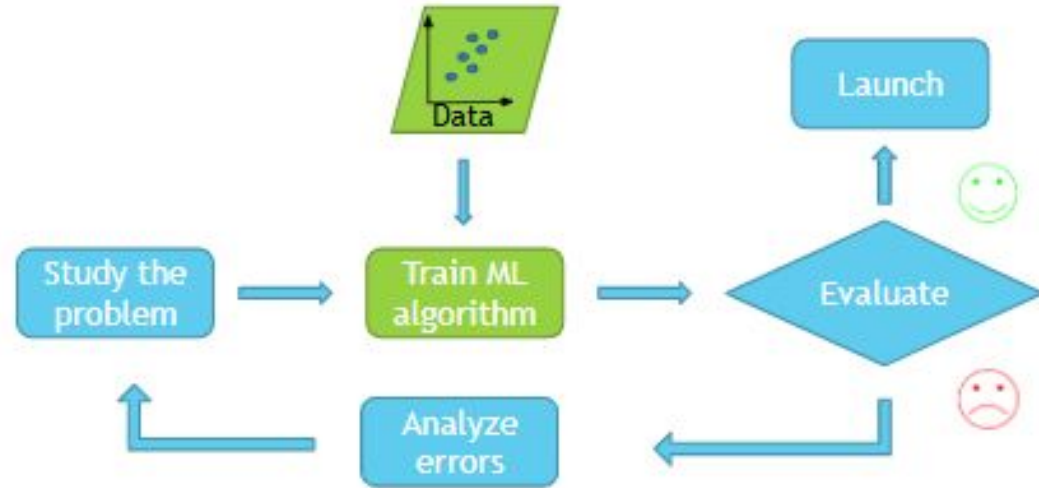


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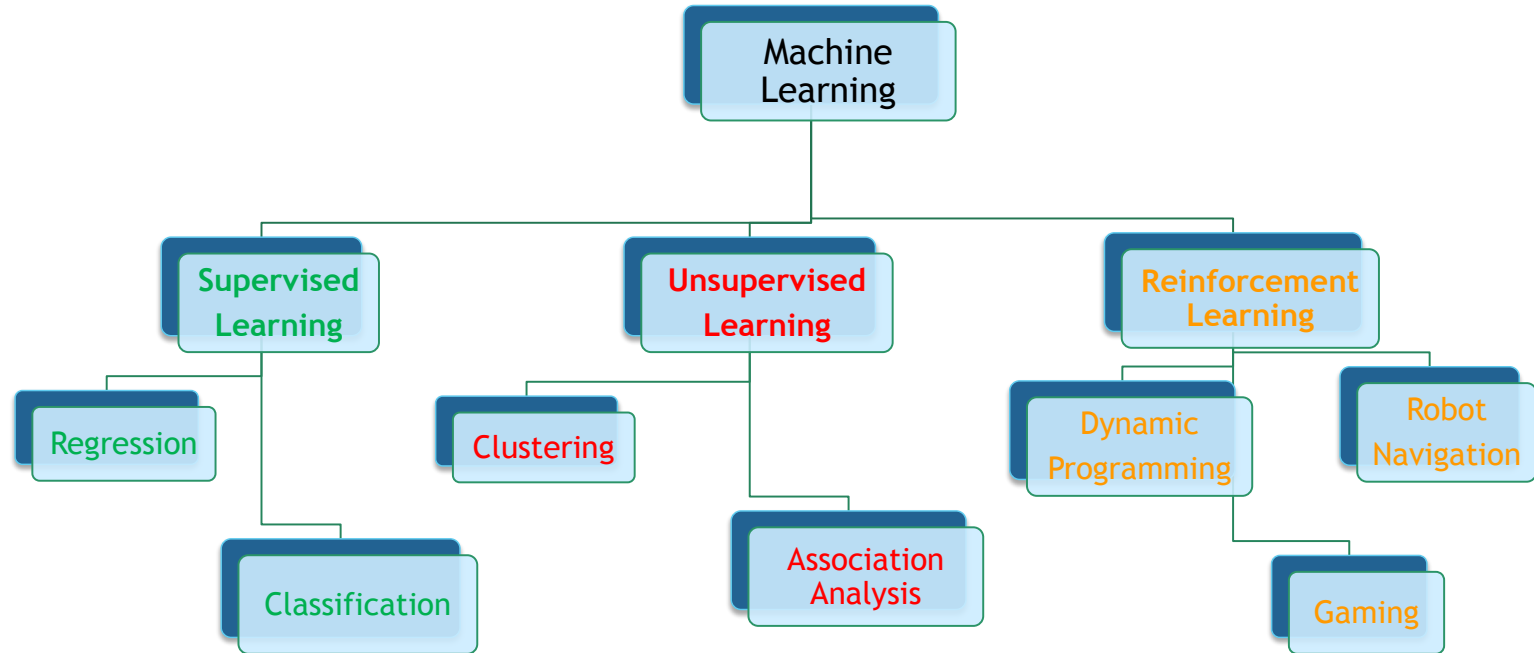
Machine Learning approach

# Agenda

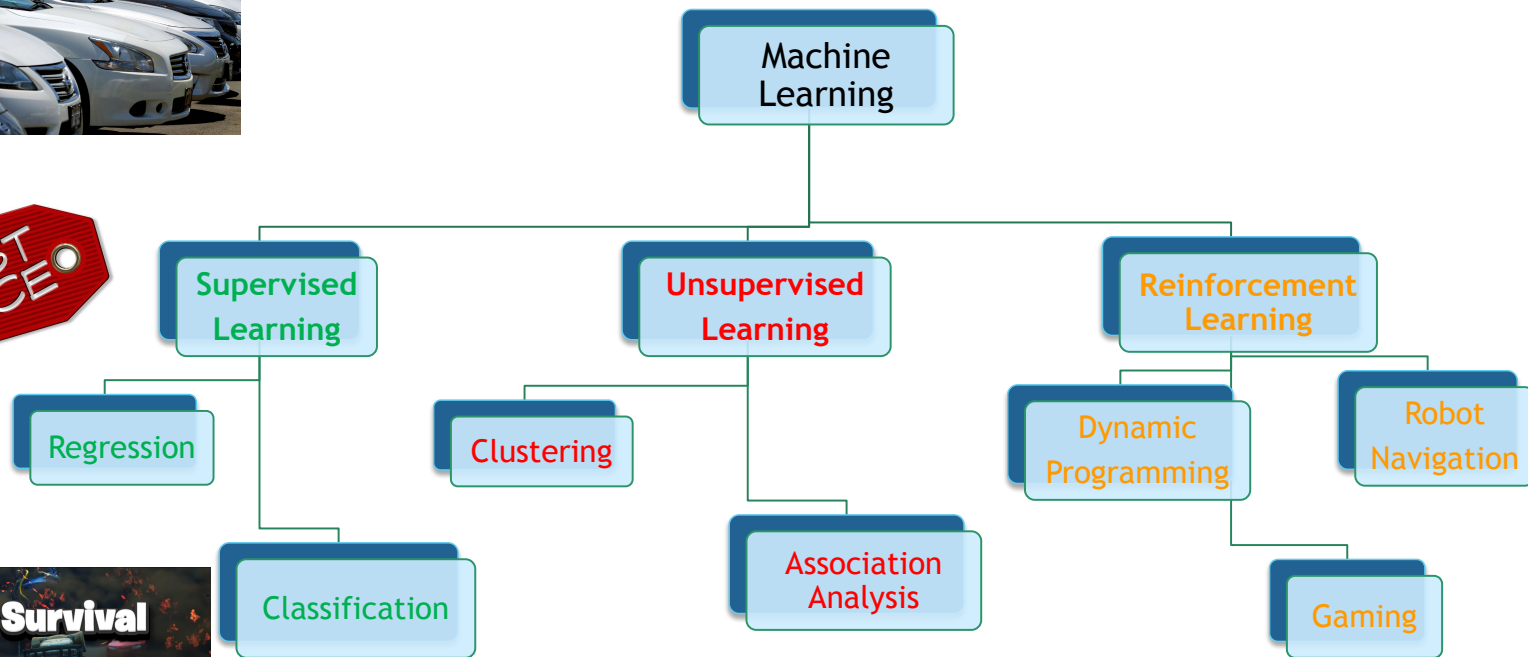
- What is ML? Why ML?
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- Support Vector Machines
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# Categories of Machine Learning



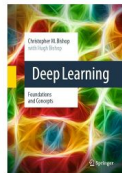
# Categories of Machine Learning



# Categories of Machine Learning

## Products related to this item

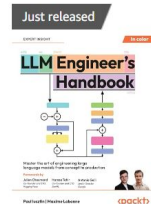
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Machine Learning

Unsupervised Learning

Regression

Clustering

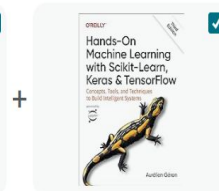
Classification

Association Analysis

Frequently bought together



**This item:** Deep Learning (Adaptive Computation and Machine Learning series)  
\$60<sup>00</sup>



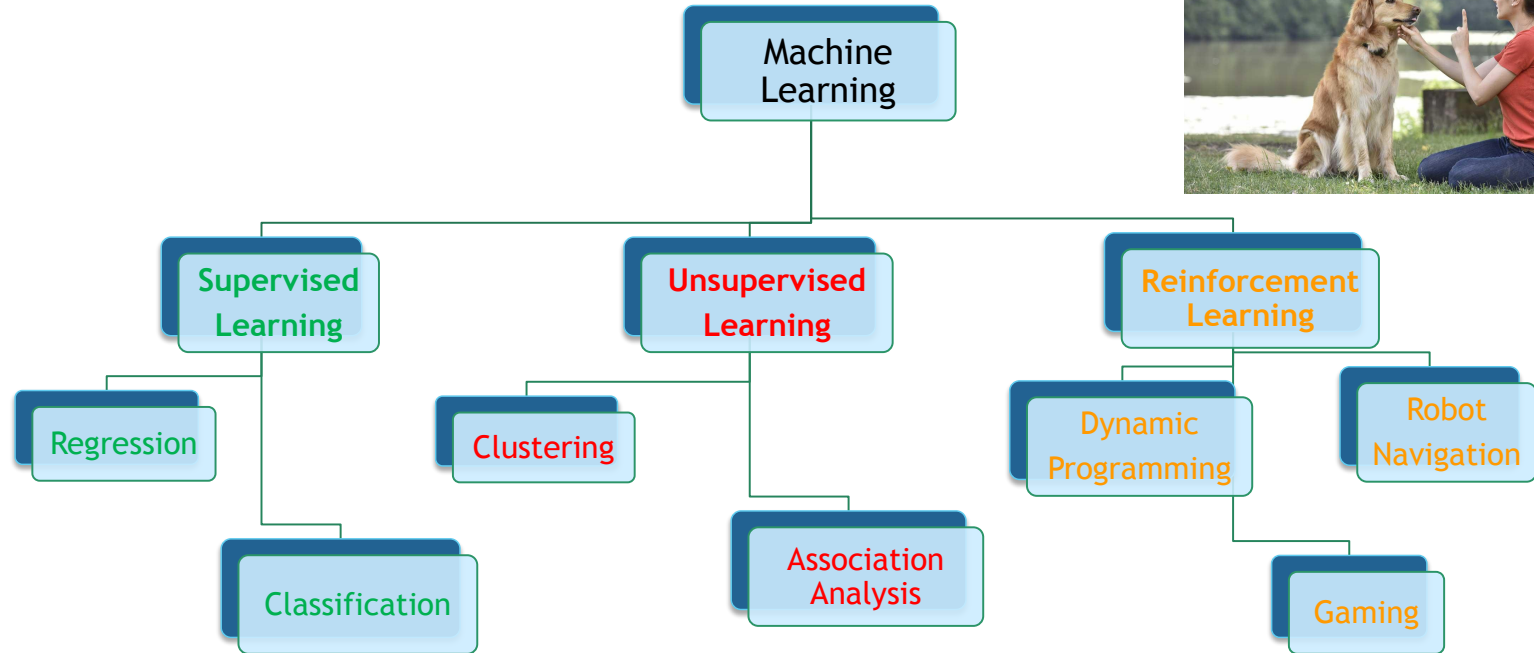
Hands-On Machine Learning with Scikit-Learn, Keras and TensorFlow: Concepts, Tool...  
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Gaming

# Categories of Machine Learning

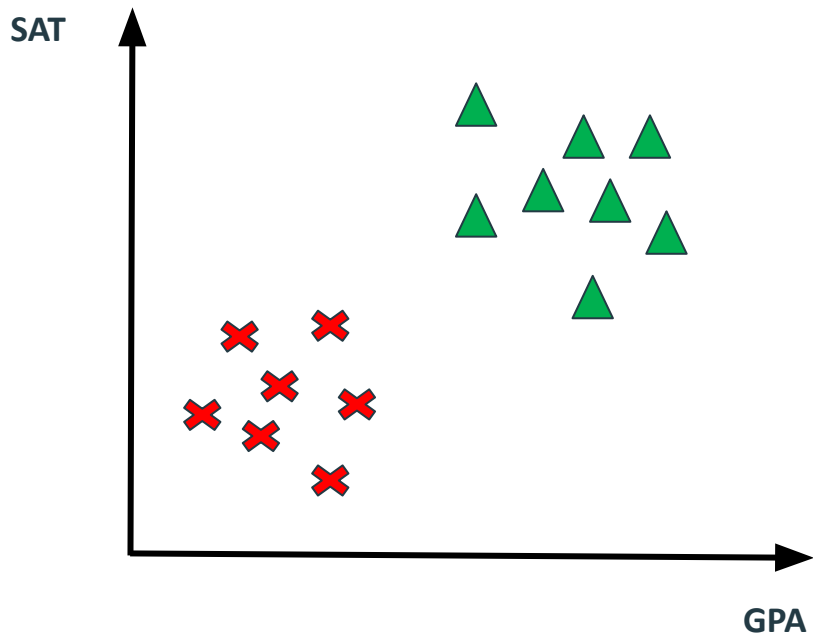


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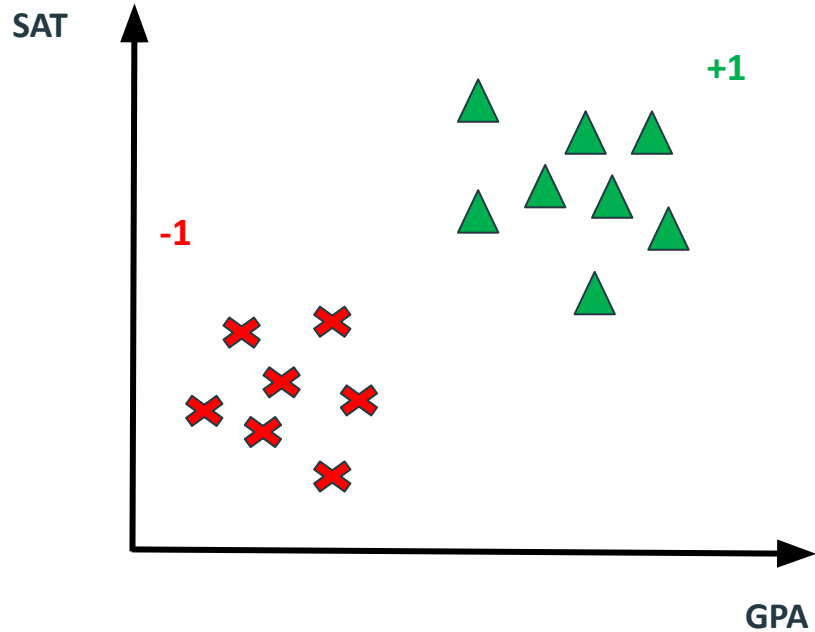
# Support Vector Machines

## The basic idea



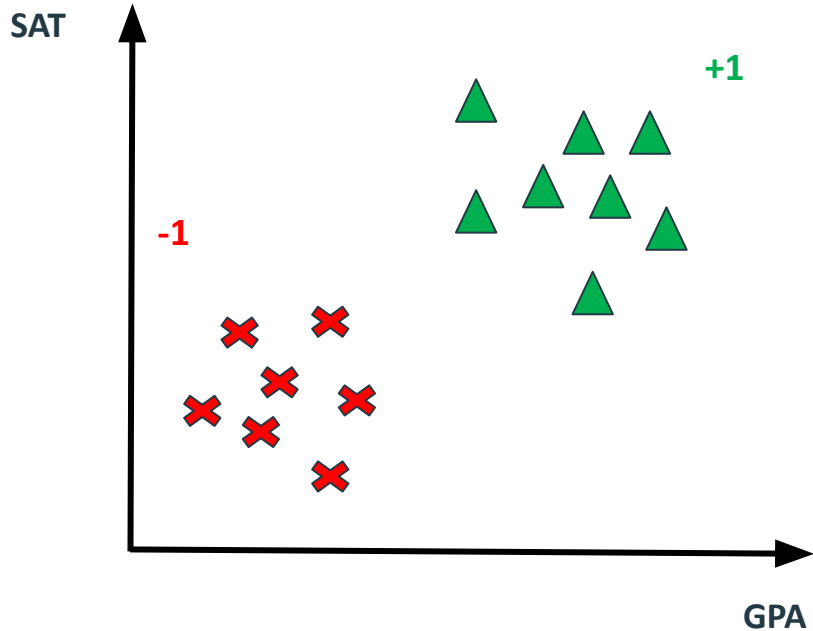
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## The basic idea



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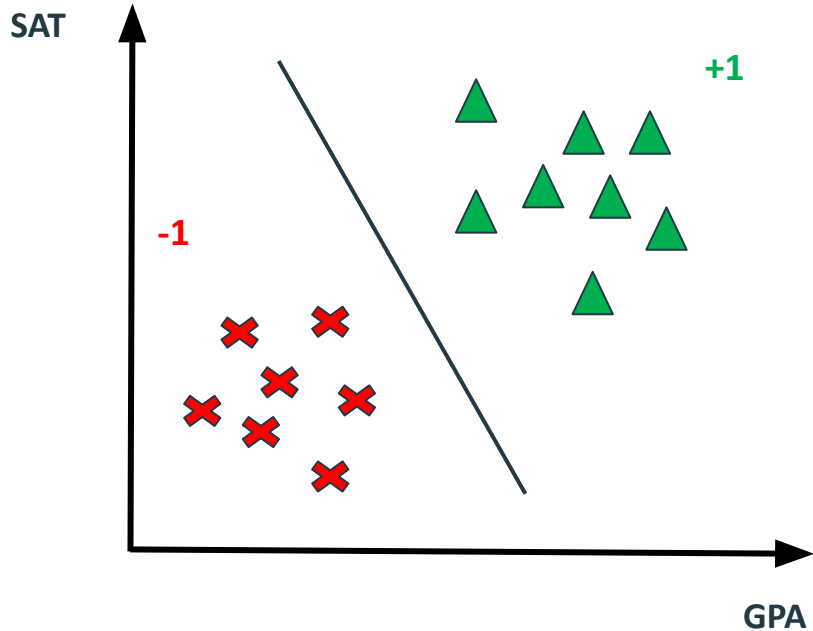


Can we find a straight line that separates the two classes?



# Support Vector Machines

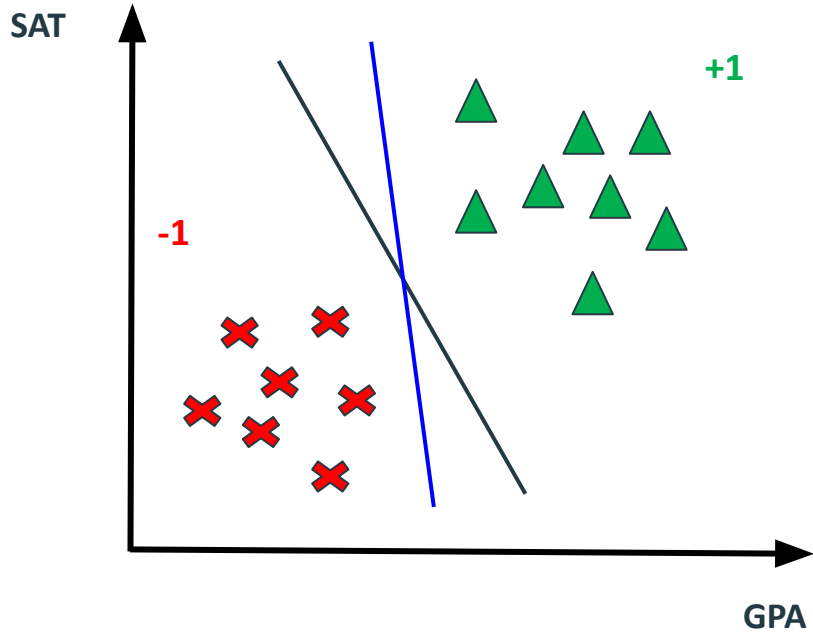
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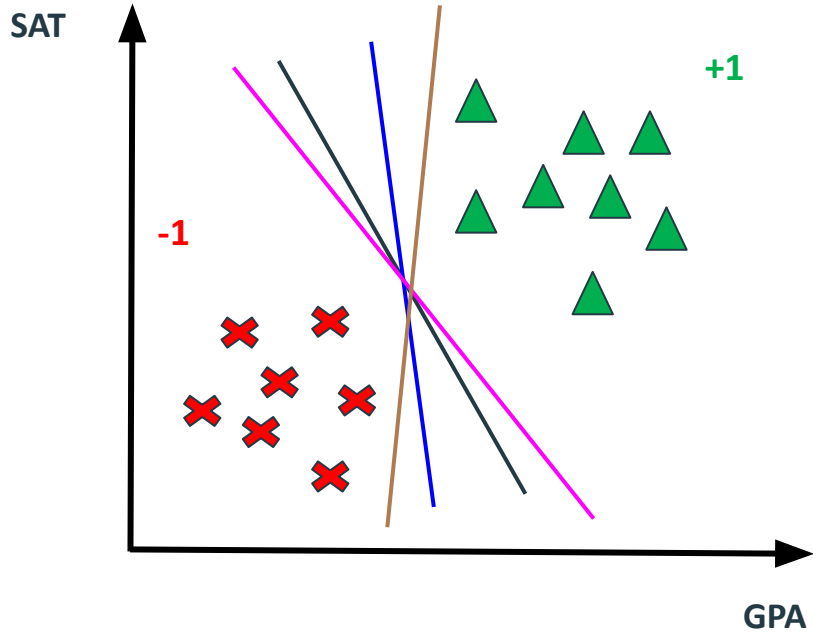
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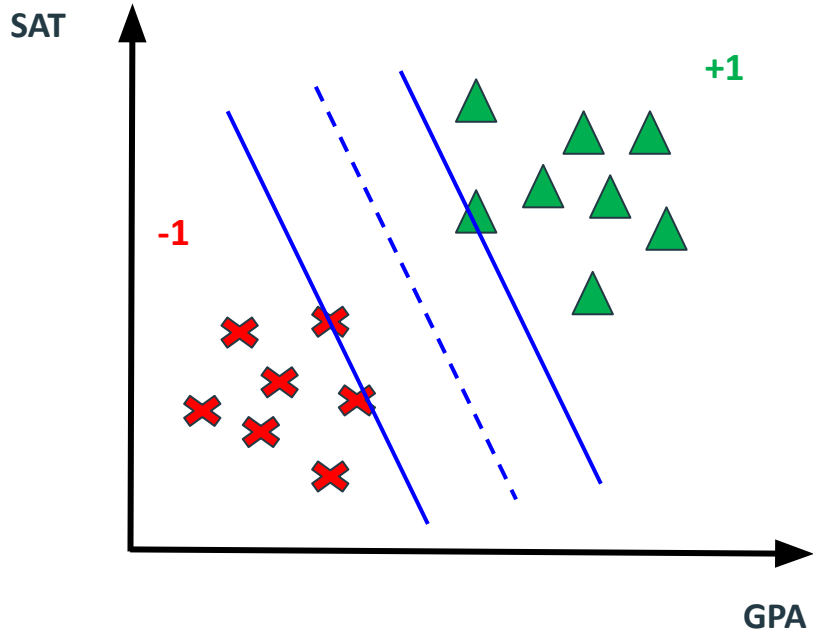
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Can we find a straight line that separates the two classes?

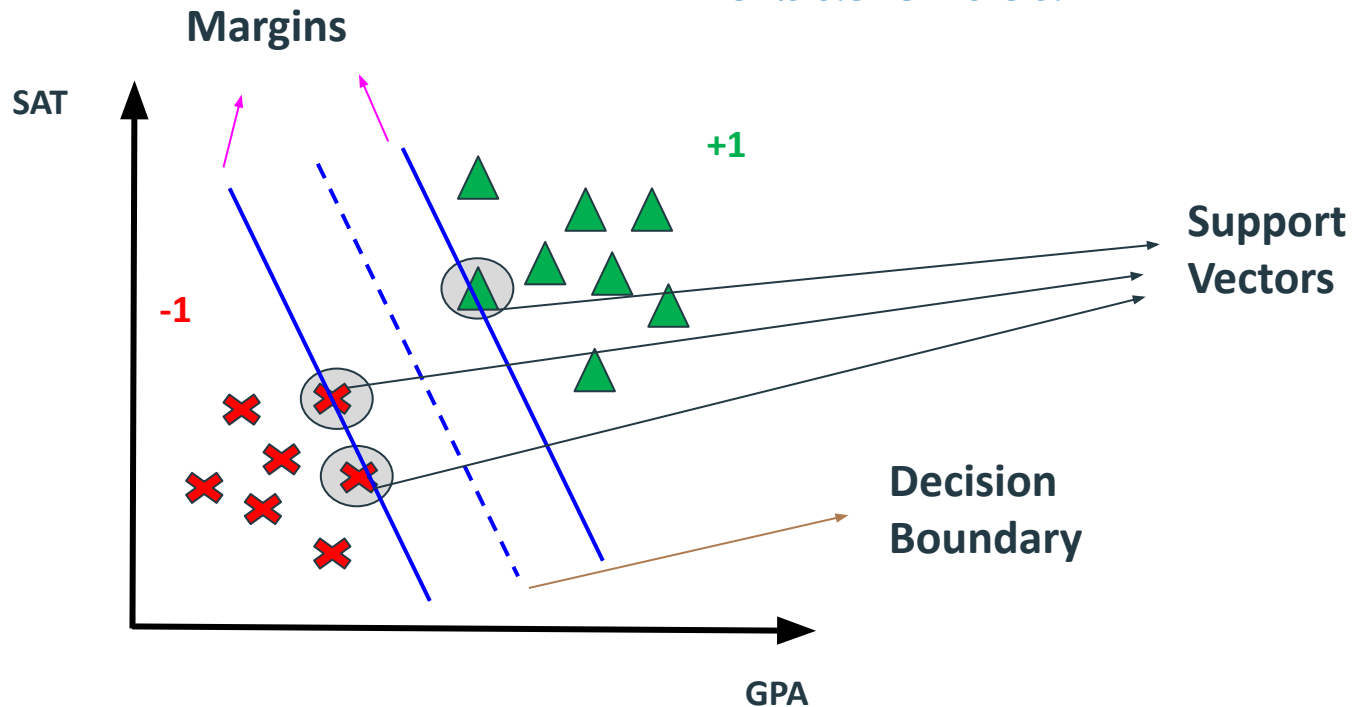
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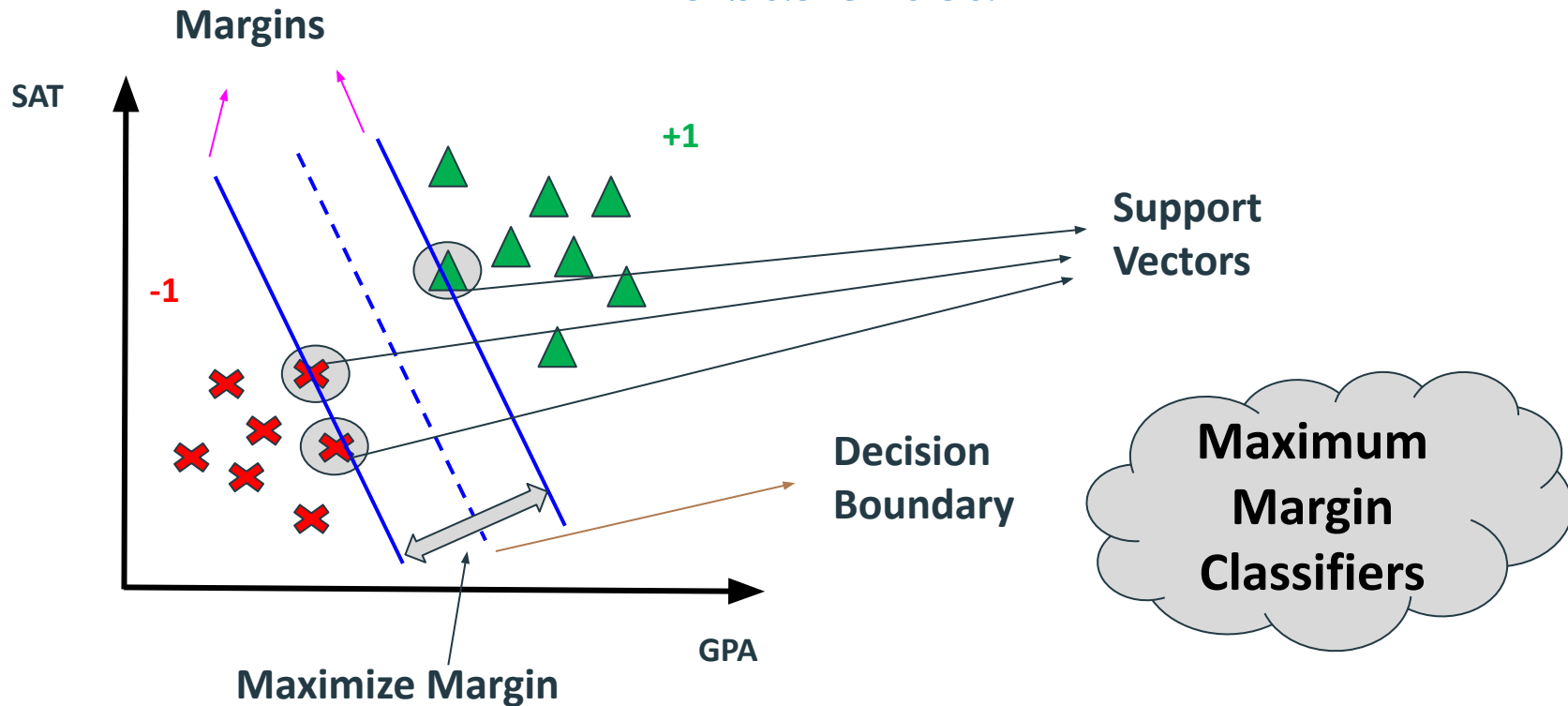
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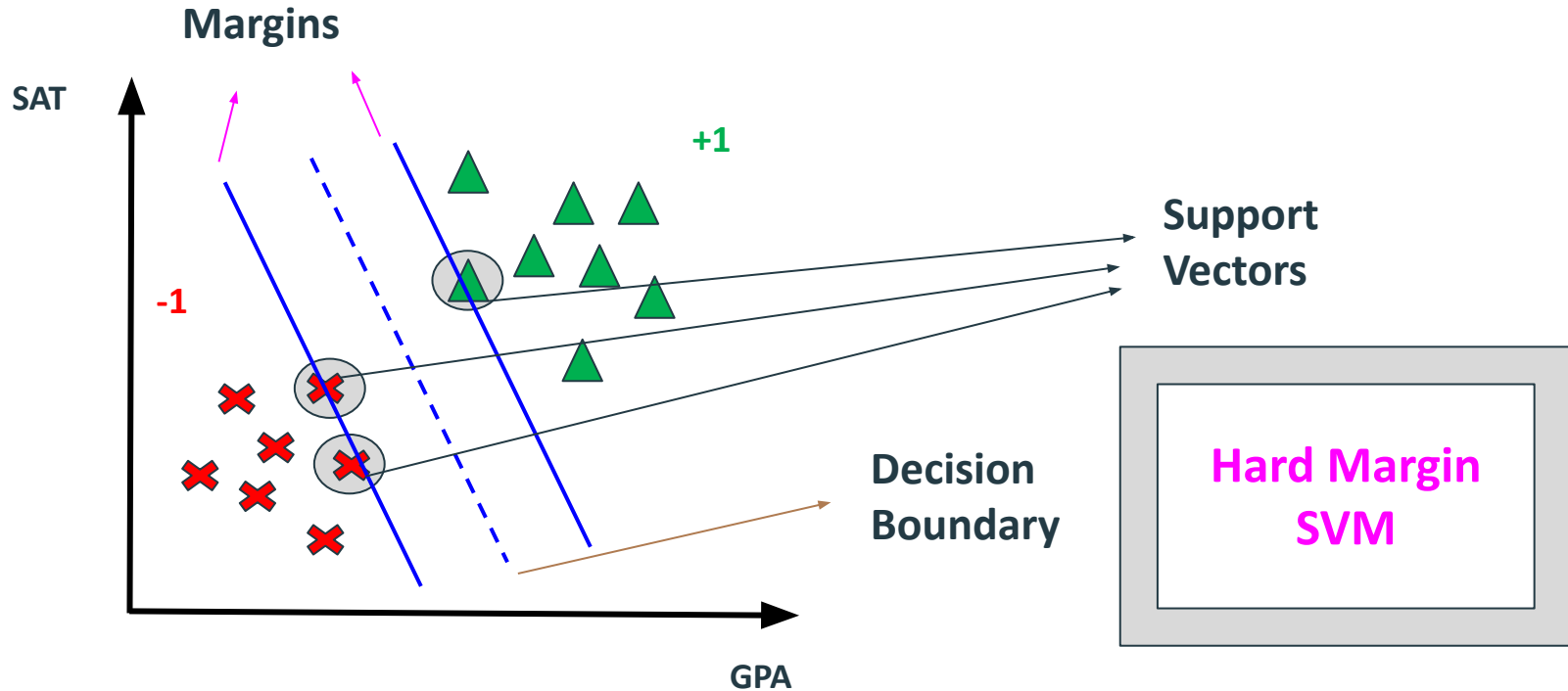


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# Support Vector Machines

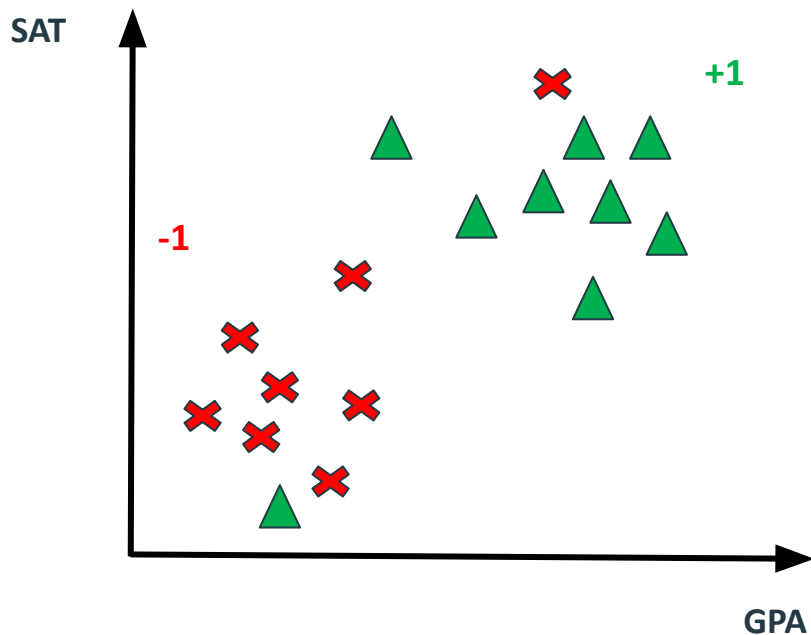
## Case 1: Linearly Separable Data





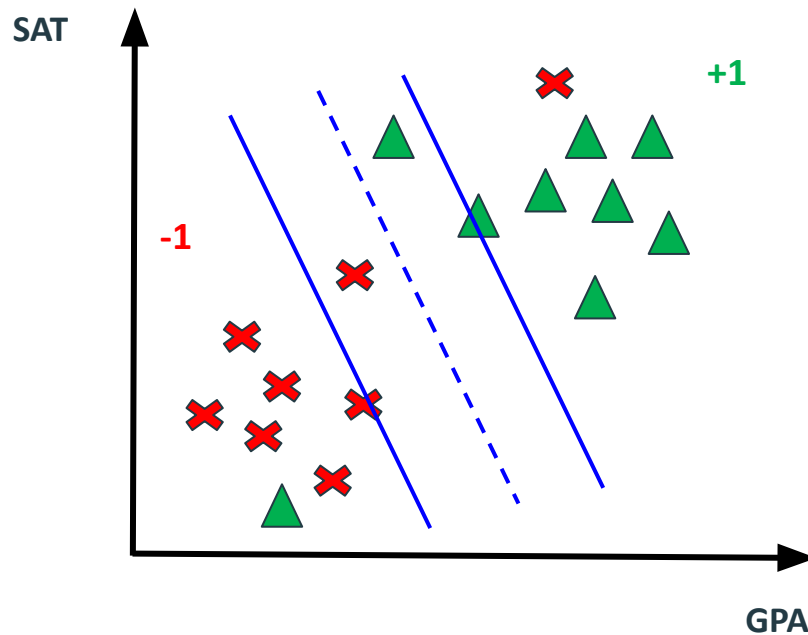
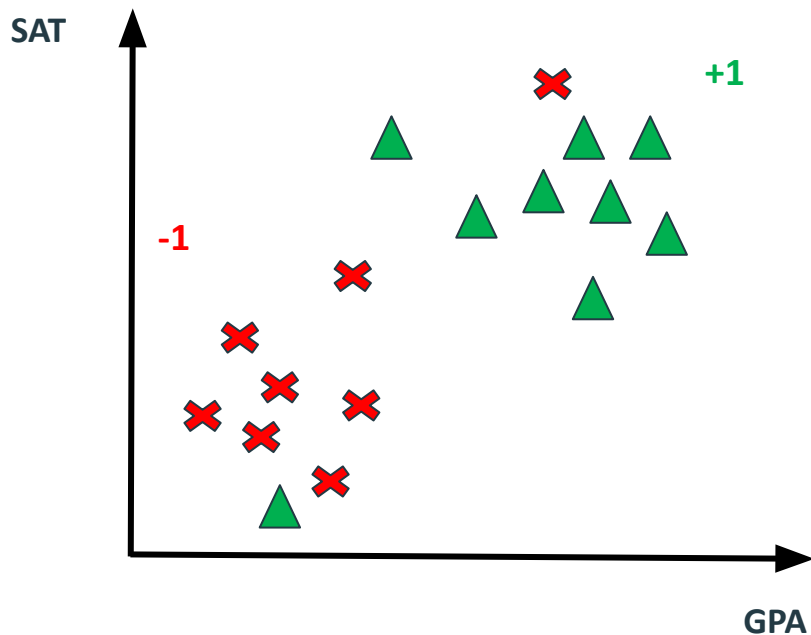
# Support Vector Machines

## Case 2a: Linearly Inseparable



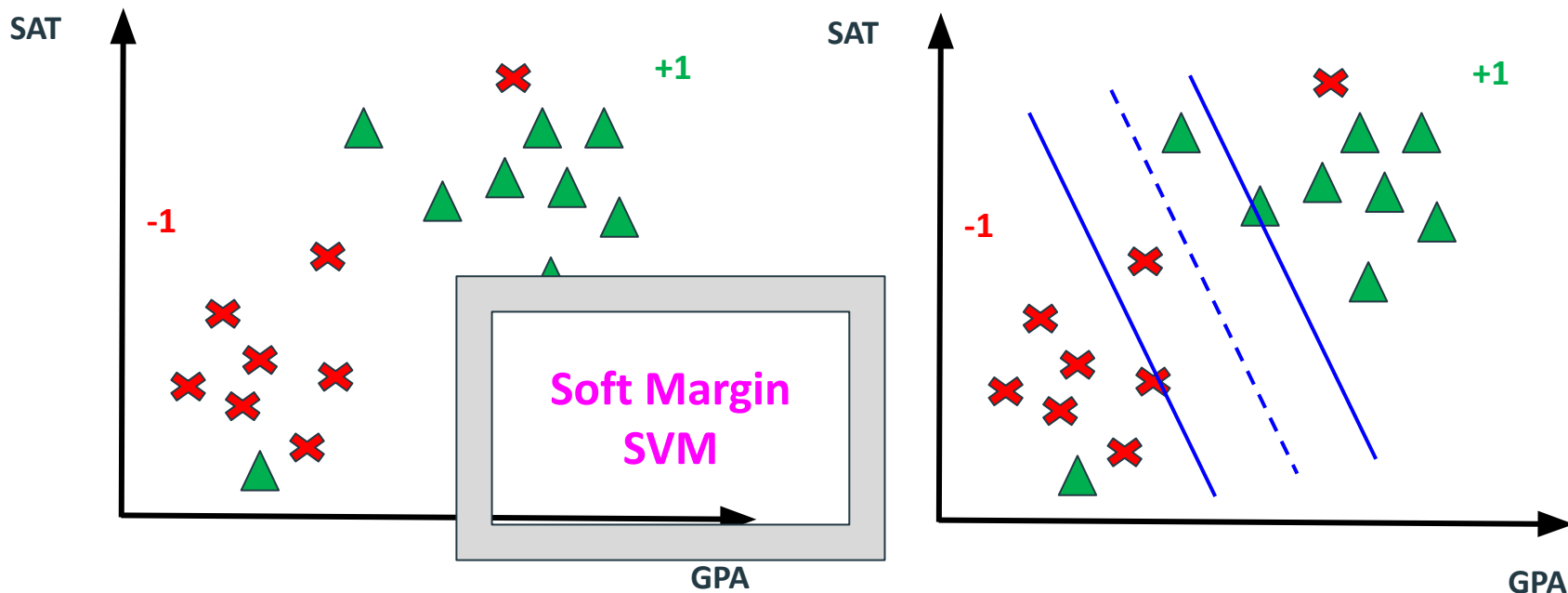
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## Case 2a: Linearly Inseparable



# Support Vector Machines

## Case 2a: Linearly Inseparable



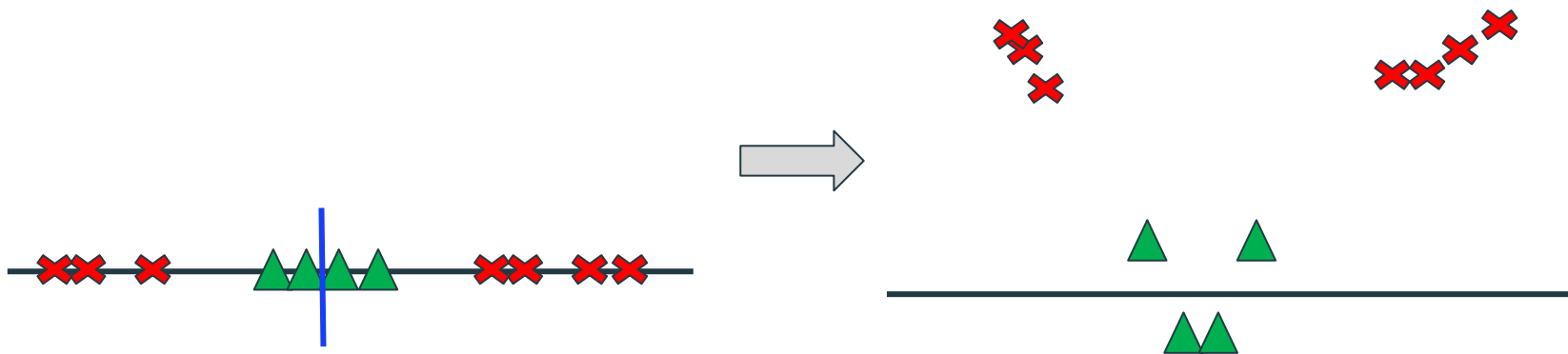
# Support Vector Machines

## Case 2b: Linearly Inseparable



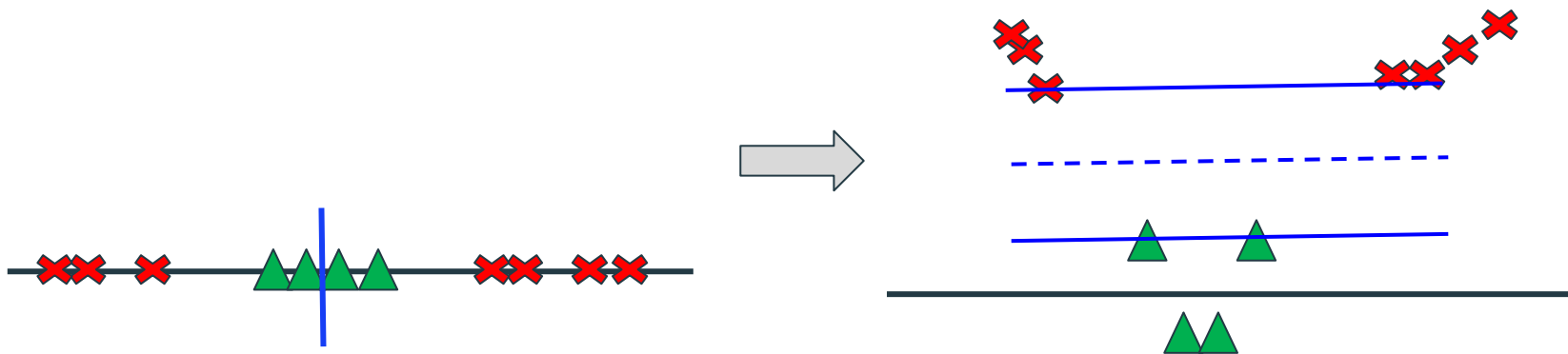
# Support Vector Machines

## Case 2b: Linearly Inseparable



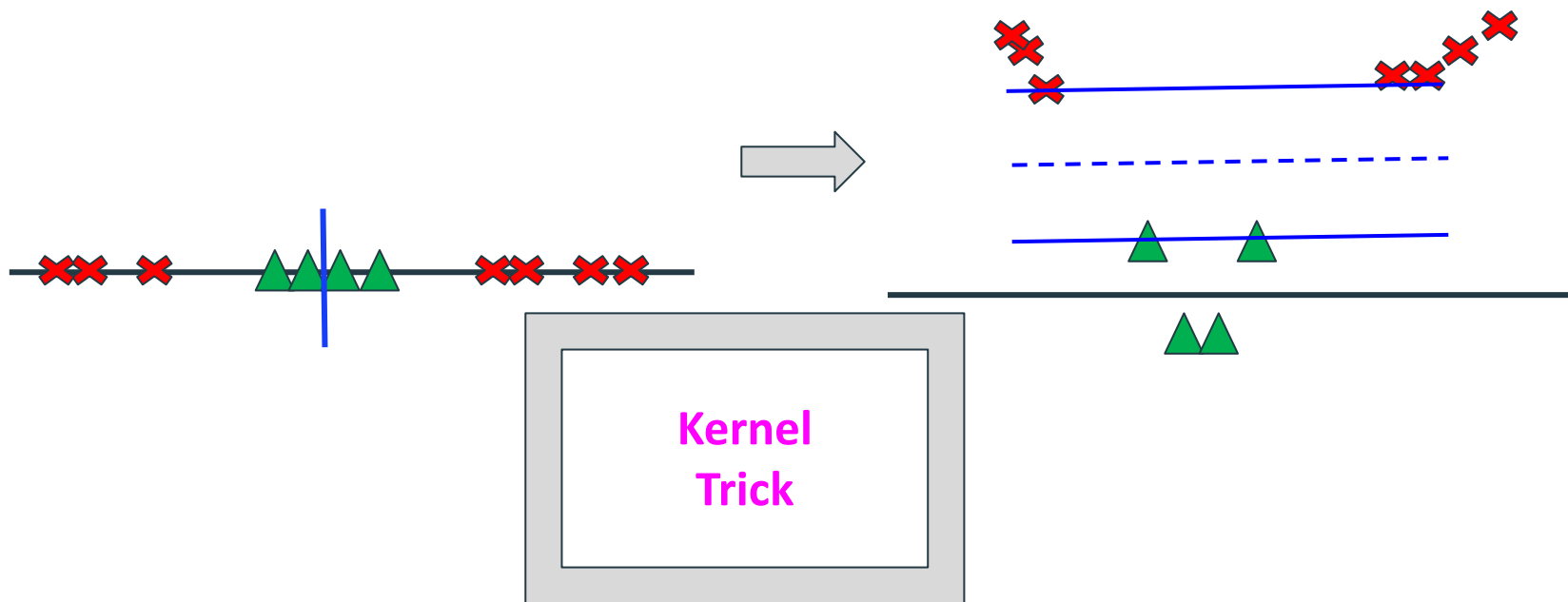
# Support Vector Machines

## Case 2b: Linearly Inseparable



# Support Vector Machines

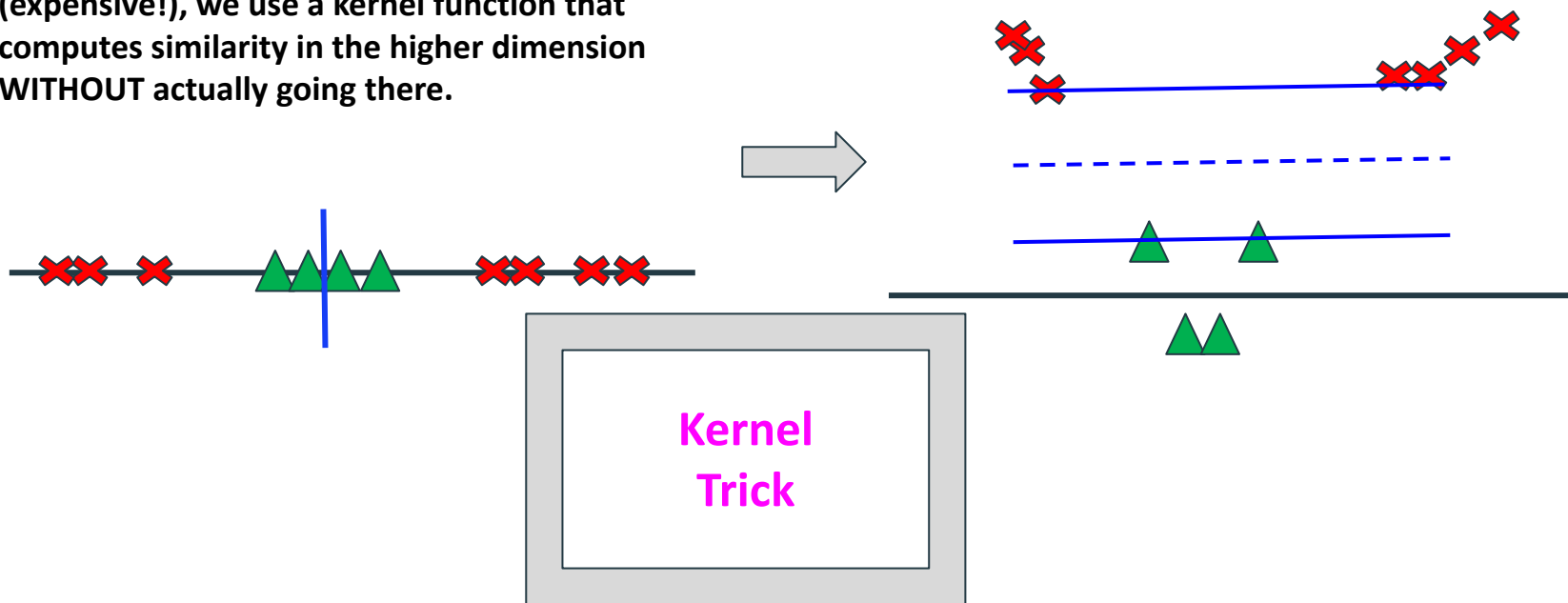
## Case 2b: Linearly Inseparable



# Support Vector Machines

## Case 2b: Linearly Inseparable

Instead of explicitly transforming data (expensive!), we use a kernel function that computes similarity in the higher dimension WITHOUT actually going there.



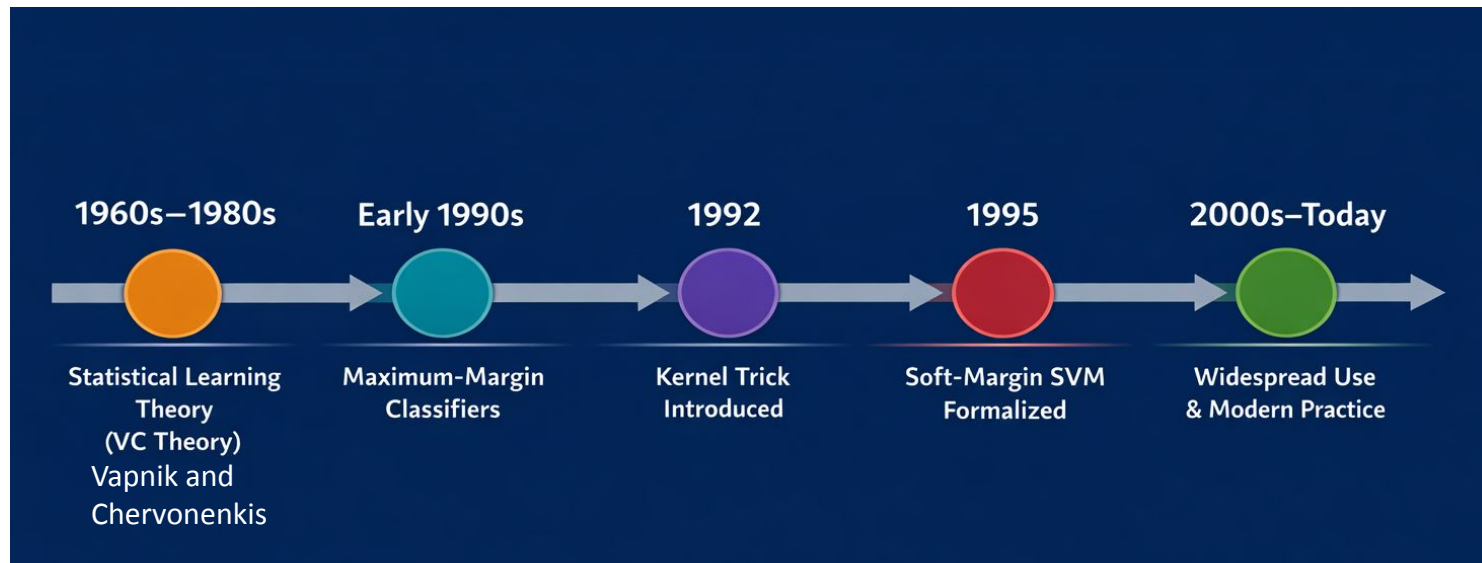


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# Support Vector Machines

## The History and Development



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# Hard Margin SVM

## The Math

### Problem Setup: Binary Classification

We want to classify data into two categories. For example, predicting whether a student gets into tech school ( $y = +1$ ) or does not ( $y = -1$ ).

The Data:

- $n$  total students
- For each student  $i$ , we have:
  - A feature vector  $x_i$  (e.g., GPA, SAT scores, ... )
  - A label  $y_i \in \{-1, +1\}$

Training data

$$\begin{bmatrix} \vec{x}_1 \\ \vec{x}_2 \\ \vdots \\ \vec{x}_n \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

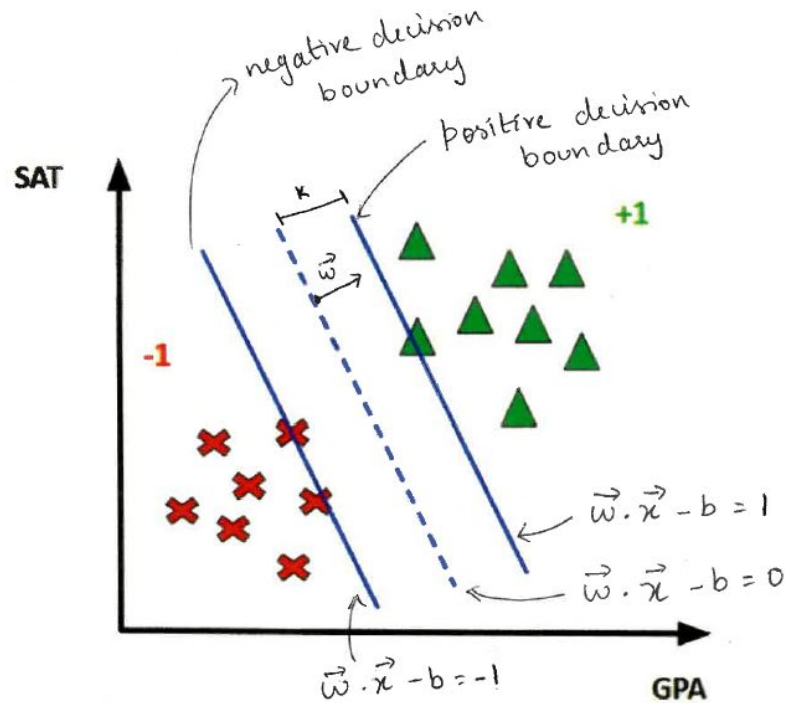
**The Goal:** Build an SVM model that creates a maximum margin classifier—a decision boundary with the largest possible "safety zone" between the two classes. This breathing room helps the model generalize better to new, unseen data.

# Hard Margin SVM

## The Math

To find the best separating boundary, we define three parallel hyperplanes

What is the distance between the two margin boundaries?



# Hard Margin SVM

## The Math

Let  $\vec{x}_0$  be any point on the decision boundary

$$\Rightarrow \vec{w} \cdot \vec{x}_0 - b = 0 \quad - (1)$$

We want to walk from  $\vec{x}_0$  in the direction of  $w$  (the perpendicular direction) until we reach the positive margin boundary.

Lets walk a distance of  $k$  units in the direction of the unit vector,  $\frac{w}{\|w\|}$

$\therefore$  the new position after walking  $k$  units:

$$\vec{x}_1 = \vec{x}_0 + k \frac{w}{\|w\|} \quad - (2)$$

Since  $x_1$  is on the positive margin boundary,

$$\vec{w} \cdot \vec{x}_1 - b = 1 \quad - (3)$$

substitute (2) in (3)

$$\vec{w} \cdot \left( \vec{x}_0 + k \frac{w}{\|w\|} \right) - b = 1$$

$$\vec{w} \cdot \vec{x}_0 + k \frac{w \cdot w}{\|w\|} - b = 1$$

$$(\vec{w} \cdot \vec{x}_0 - b) + k \frac{w \cdot w}{\|w\|} = 1 \quad - (4)$$

substitute (1) in (4),  $w \cdot w = \|w\|^2$

$$0 + k \frac{\|w\|^2}{\|w\|} = 1$$

$$\Rightarrow \boxed{k = \frac{1}{\|\vec{w}\|}}$$

$\therefore$  The margin size is  $\frac{2}{\|\vec{w}\|}$

So, we have to maximize the margin

$\Rightarrow$  minimizing  $\|\vec{w}\|$

# Hard Margin SVM

## The Math

Constraints:

1. We need every data point be correctly classified
2. Every data point be outside or on the margin

ie., for positive classes ,

$$y_i = +1, \quad \vec{w} \cdot \vec{x}_i - b \geq +1$$

for negative classes

$$y_i = -1, \quad \vec{w} \cdot \vec{x}_i - b \leq -1$$

we combine both constraints by multiplying  $y_i$

$$y_i (\vec{w} \cdot \vec{x}_i - b) \geq 1$$

$\therefore$  minimize  $\|w\|$

subject to  $y_i (\vec{w} \cdot \vec{x}_i - b) \geq 1 \quad \forall i = 1, 2, \dots, n$

