
ACCOUNTING FOR VARIANCE IN MACHINE LEARNING BENCHMARKS

Xavier Bouthillier^{1,2} Pierre Delaunay³ Mirko Bronzi¹ Assya Trofimov^{1,2,4} Brennan Nichyporuk^{1,5,6}
Justin Szeto^{1,5,6} Naz Sepah^{1,5,6} Edward Raff^{7,8} Kanika Madan^{1,2} Vikram Voleti^{1,2}
Samira Ebrahimi Kahou^{1,6,9,10} Vincent Michalski^{1,2} Dmitriy Serdyuk^{1,2} Tal Arbel^{1,5,6,10} Chris Pal^{1,11,12}
Gaël Varoquaux^{1,6,13} Pascal Vincent^{1,2,10}

ABSTRACT

Strong empirical evidence that one machine-learning algorithm A outperforms another one B ideally calls for multiple trials optimizing the learning pipeline over sources of variation such as data sampling, augmentation, parameter initialization, and hyperparameters choices. This is prohibitively expensive, and corners are cut to reach conclusions. We model the whole benchmarking process, revealing that variance due to data sampling, parameter initialization and hyperparameter choice impact markedly the results. We analyze the predominant comparison methods used today in the light of this variance. We show a counter-intuitive result that adding more sources of variation to an imperfect estimator approaches better the ideal estimator at a $51\times$ reduction in compute cost. Building on these results, we study the error rate of detecting improvements, on five different deep-learning tasks/architectures. This study leads us to propose recommendations for performance comparisons.

1 INTRODUCTION: TRUSTWORTHY BENCHMARKS ACCOUNT FOR FLUCTUATIONS

Machine learning increasingly builds upon empirical evidence, to motivate publications or a production pipeline. The value of a new method or algorithm A is often established by empirical benchmarks comparing it to prior work. Although such benchmarks are built on quantitative measures of performance, uncontrolled factors can impact these measures and dominate the meaningful difference between the methods. In particular, recent studies have shown that loose choices of hyper-parameters lead to non-reproducible benchmarks and unfair comparisons (Raff, 2019; 2021; Lucic et al., 2018; Henderson et al., 2018; Kadlec et al., 2017; Melis et al., 2018; Bouthillier et al., 2019; Reimers & Gurevych, 2017; Gorman & Bedrick, 2019). Properly accounting for these factors may go as far as changing the conclusions for the comparison, as shown for recommender systems (Dacrema et al., 2019), neural architecture pruning (Blalock et al., 2020), and metric learning (Musgrave et al.,

2020).

The steady increase in complexity –e.g. neural-network depth– and number of hyper-parameters of learning pipelines increases computational costs of models, making brute-force approaches prohibitive. Indeed, robust conclusions on comparative performance of models A and B would require multiple training of the full learning pipelines, including hyper-parameter optimization and random seeding. Unfortunately, since the computational budget of most researchers can afford only a small number of model fits (Bouthillier & Varoquaux, 2020), many sources of variances are not probed via repeated experiments. Rather, sampling several model initializations is often considered to give enough evidence. As we will show, there are other, larger, sources of uncontrolled variation and the risk is that conclusions are driven by differences due to arbitrary factors, such as data order, rather than model improvements.

The seminal work of Dietterich (1998) studied statistical tests for comparison of supervised classification learning algorithms focusing on variance due to data sampling. Following works (Nadeau & Bengio, 2000; Bouckaert & Frank, 2004) perpetuated this focus, including a series of work in NLP (Riezler & Maxwell, 2005; Taylor Berg-Kirkpatrick & Klein, 2012; Anders Sogaard & Alonso, 2014) which ignored variance extrinsic to data sampling. Most of these works recommended the use of paired tests to mitigate the issue of extrinsic sources of variation, but Hothorn et al. (2005) then proposed a theoretical framework encompassing all sources of variation. This framework addressed the

¹Mila, Montréal, Canada ²Université de Montréal, Montréal, Canada ³Independent ⁴IRIC ⁵Centre for Intelligent Machines ⁶McGill University, Montréal, Canada ⁷Booz Allen Hamilton ⁸University of Maryland, Baltimore County ⁹École de technologie supérieure ¹⁰CIFAR ¹¹Polytechnique Montréal, Montréal, Canada ¹²ElementAI ¹³Inria, Saclay, France. Correspondence to: Xavier Bouthillier <xavier.bouthillier@umontreal.ca>.

issue of extrinsic sources of variation by marginalizing all of them, including the hyper-parameter optimization process. These prior works need to be confronted to the current practice in machine learning, in particular deep learning, where 1) the machine-learning pipelines has a large number of hyper-parameters, including to define the architecture, set by uncontrolled procedures, sometimes manually, 2) the cost of fitting a model is so high that train/validation/test splits are used instead of cross-validation, or nested cross-validation that encompasses hyper-parameter optimization (Bouthillier & Varoquaux, 2020).

In **Section 2**, we study the different source of variation of a benchmark, to outline which factors contribute markedly to uncontrolled fluctuations in the measured performance. **Section 3** discusses estimation the performance of a pipeline and its uncontrolled variations with a limited budget. In particular we discuss this estimation when hyper-parameter optimization is run only once. Recent studies emphasized that model comparisons with uncontrolled hyper-parameter optimization is a burning issue (Lucic et al., 2018; Henderson et al., 2018; Kadlec et al., 2017; Melis et al., 2018; Bouthillier et al., 2019); here we frame it in a statistical context, with explicit bias and variance to measure the loss of reliability that it incurs. In **Section 4**, we discuss criterion using these estimates to conclude on whether to accept algorithm A as a meaningful improvement over algorithm B , and the error rates that they incur in the face of noise.

Based on our results, we issue in **Section 5** the following recommendations:

- 1) As many sources of variation as possible should be randomized whenever possible. These include weight initialization, data sampling, random data augmentation and the whole hyperparameter optimization. This helps decreasing the standard error of the average performance estimation, enhancing precision of benchmarks.
- 2) Deciding of whether the benchmarks give evidence that one algorithm outperforms another should not build solely on comparing average performance but account for variance. We propose a simple decision criterion based on requiring a high-enough probability that in one run an algorithm outperforms another.
- 3) Resampling techniques such as out-of-bootstrap should be favored instead of fixed held-out test sets to improve capacity of detecting small improvements.

Before concluding, we outline a few additional considerations for benchmarking in **Section 6**.

2 THE VARIANCE IN ML BENCHMARKS

Machine-learning benchmarks run a complete learning pipeline on a finite dataset to estimate its performance. This performance value should be considered the realization of

a random variable. Indeed the dataset is itself a random sample from the full data distribution. In addition, a typical learning pipeline has additional sources of uncontrolled fluctuations, as we will highlight below. A proper evaluation and comparison between pipelines should thus account for the *distributions* of such metrics.

2.1 A model of the benchmarking process that includes hyperparameter tuning

Here we extend the formalism of Hothorn et al. (2005) to model the different sources of variation in a machine-learning pipeline and that impact performance measures. In particular, we go beyond prior works by accounting for the choice of hyperparameters in a probabilistic model of the whole experimental benchmark. Indeed, choosing good hyperparameters –including details of a neural architecture– is crucial to the performance of a pipeline. Yet these hyperparameters come with uncontrolled noise, whether they are set manually or with an automated procedure.

The training procedure We consider here the familiar setting of supervised learning on i.i.d. data (and will use classification in our experiments) but this can easily be adapted to other machine learning settings. Suppose we have access to a dataset $S = \{(x_1, y_1), \dots, (x_n, y_n)\}$ containing n examples of (input, target) pairs. These pairs are i.i.d. and sampled from an unknown data distribution \mathcal{D} , i.e. $S \sim \mathcal{D}^n$. The goal of a learning pipeline is to find a function $h \in \mathcal{H}$ that will have good prediction performance in expectation over \mathcal{D} , as evaluated by a metric of interest e . More precisely, in supervised learning, $e(h(x), y)$ is a measure of how far a prediction $h(x)$ lies from the target y associated to the input x (e.g., classification error). The goal is to find a predictor h that minimizes the *expected risk* $R_e(h, \mathcal{D}) = \mathbb{E}_{(x,y) \sim \mathcal{D}}[e(h(x), y)]$, but since we have access only to finite datasets, all we can ever measure is an *empirical risk* $\hat{R}_e(h, S) = \frac{1}{|S|} \sum_{(x,y) \in S} e(h(x), y)$. In practice training with a training set S^t consists in finding a function (hypothesis) $h \in \mathcal{H}$ that minimizes a trade-off between a data-fit term –typically the empirical risk of a differentiable surrogate loss e' – with a regularization $\Omega(h, \lambda)$ that induces a preference over hypothesis functions:

$$\text{Opt}(S^t, \lambda) \approx \arg \min_{h \in \mathcal{H}} \hat{R}_{e'}(h, S^t) + \Omega(h, \lambda), \quad (1)$$

where λ represents the set of hyperparameters: regularization coefficients (s.a. strength of weight decay or the ridge penalty), architectural hyperparameters affecting \mathcal{H} , optimizer-specific ones such as the learning rate, etc... Note that Opt is a random variable whose value will depend also on other additional random variables that we shall collectively denote ξ_O , sampled to determine parameter initializa-

tion, data augmentation, example ordering, etc.*.

Hyperparameter Optimization The training procedure builds a predictor given a training set S^t . But since it requires specifying hyperparameters λ , a complete learning pipeline has to tune all of these. A complete pipeline will involve a hyper-parameter optimization procedure, which will strive to find a value of λ that minimizes objective

$$r(\lambda) = \mathbb{E}_{(S^t, S^v) \sim \text{sp}(S^{tv})} \left[\hat{R}_e(\text{Opt}(S^t, \lambda), S^v) \right] \quad (2)$$

where $\text{sp}(S^{tv})$ is a distribution of random splits of the data set S^{tv} between training and validation subsets S^t, S^v . Ideally, hyperparameter optimization would be applied over random dataset samples from the true distribution \mathcal{D} , but in practice the learning pipeline only has access to S^{tv} , hence the expectation over dataset splits. An ideal hyper-parameter optimization would yield $\lambda^*(S^{tv}) = \arg \min_{\lambda} r(\lambda)$. A concrete hyperparameter optimization algorithm HOpt will however use an average over a small number of train-validation splits (or just 1), and a limited training budget, yielding $\hat{\lambda}^*(S^{tv}) = \text{HOpt}(S^{tv}) \approx \lambda^*(S^{tv})$. We denoted earlier the sources of random variations in Opt as ξ_O . Likewise, we will denote the sources of variation inherent to HOpt as ξ_H . These encompass the sources of variance related to the procedure to optimize hyperparameters HOpt, whether it is manual or a search procedure which has its arbitrary choices such as the splitting and random exploration.

After hyperparameters have been tuned, it is often customary to retrain the predictor using the full data S^{tv} . The complete learning pipeline \mathcal{P} will finally return a single predictor:

$$\hat{h}^*(S^{tv}) = \mathcal{P}(S^{tv}) = \text{Opt}(S^{tv}, \text{HOpt}(S^{tv})) \quad (3)$$

Recall that $\hat{h}^*(S^{tv})$ is the result of Opt which is not deterministic, as it is affected by arbitrary choices ξ_O in the training of the model (random weight initialization, data ordering...) and now additionally ξ_H in the hyperparameter optimization. We will use ξ to denote the set of all random variations sources in the learning pipeline, $\xi = \xi_H \cup \xi_O$. Thus ξ captures all sources of variation in the learning pipeline from data S^{tv} , that are not configurable with λ .

The performance measure The full learning procedure \mathcal{P} described above yields a model \hat{h}^* . We now must define a metric that we can use to evaluate the performance of this model with statistical tests. For simplicity, we will use the same evaluation metric e on which we based hyperparameter

optimization. The expected risk obtained by applying the full learning pipeline \mathcal{P} to datasets $S^{tv} \sim \mathcal{D}^n$ of size n is:

$$R_{\mathcal{P}}(\mathcal{D}, n) = \mathbb{E}_{S^{tv} \sim \mathcal{D}^n} \left[R_e(\hat{h}^*(S^{tv}), \mathcal{D}) \right] \quad (4)$$

where the expectation is also over the random sources ξ that affect the learning procedure (initialization, ordering, data-augmentation) and hyperparameter optimization.

As we only have access to a single finite dataset S , the performance of the learning pipeline can be evaluated as the following expectation over splits:

$$\mu = \hat{R}_{\mathcal{P}}(S, n, n') = \mathbb{E}_{(S^{tv}, S^o) \sim \text{sp}_{n, n'}(S)} \left[\hat{R}_e(\hat{h}^*(S^{tv}), S^o) \right] \quad (5)$$

where sp is a distribution of random splits or bootstrap resampling of the data set S that yield sets S^{tv} (train+valid) of size n and S^o (test) of size n' . We denote as σ^2 the corresponding variance of $\hat{R}_e(\hat{h}^*(S^{tv}), S^o)$. The performance measures vary not only depending on how the data was split, but also on all other random factors affecting the learning procedure (ξ_O) and hyperparameters optimization (ξ_H).

2.2 Empirical evaluation of variance in benchmarks

We conducted thorough experiments to probe the different sources of variance in machine learning benchmarks.

Cases studied We selected i) the CIFAR10 (Krizhevsky et al., 2009) image classification with VGG11 (Simonyan & Zisserman, 2014), ii) PascalVOC (Everingham et al.) image segmentation using an FCN (Long et al., 2014) with a ResNet18 (He et al., 2015a) backbone pretrained on imagenet (Deng et al., 2009), iii-iv) Glue (Wang et al., 2019) SST-2 (Socher et al., 2013) and RTE (Bentivogli et al., 2009) tasks with BERT (Devlin et al., 2018) and v) peptide to major histocompatibility class I (MHC I) binding predictions with a shallow MLP. All details on default hyperparameters used and the computational environments –which used ~ 8 GPU years– can be found in Appendix C.

Variance in the learning procedure: ξ_O For the sources of variance from the learning procedure (ξ_O), we identified: i) the data sampling, ii) data augmentation procedures, iii) model initialization, iv) dropout, and v) data visit order in stochastic gradient descent. We model the data-sampling variance as resulting from training the model on a finite dataset S of size n , sampled from an unknown true distribution. $S \sim \mathcal{D}^n$ is thus a random variable, the standard source of variance considered in statistical learning. Since we have a single finite dataset in practice, we evaluate this variance by repeatedly generating a train set from bootstrap replicates of the data and measuring the out-of-bootstrap

*If stochastic data augmentation is used, then optimization procedure Opt for a given training set S^t has to be changed to an expectation over $\tilde{S}^t \sim P^{\text{aug}}(\tilde{S}^t | S^t; \lambda_{\text{aug}})$ where P^{aug} is the data augmentation distribution. This adds additional stochasticity to the optimization, as we will optimize this through samples from P^{aug} obtained with a random number generator.

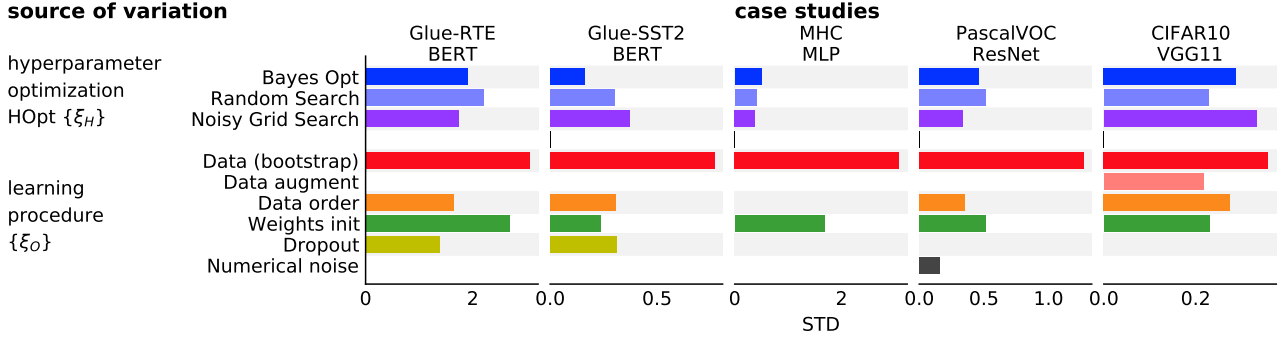


Figure 1. **Different sources of variation of the measured performance:** across our different case studies, as a fraction of the variance induced by bootstrapping the data. For hyperparameter optimization, we studied several algorithms.

error (Hothorn et al., 2005)[†].

We first fixed hyperparameters to pre-selected reasonable choices[‡]. Then, iteratively for each sources of variance, we randomized the seeds 200 times, while keeping all other sources fixed to initial values. Moreover, we measured the numerical noise with 200 training runs with all fixed seeds.

Figure 1 presents the individual variances due to sources from within the learning algorithms. Bootstrapping data stands out as the most important source of variance. In contrast, model initialization generally is less than 50% of the variance of bootstrap, on par with the visit order of stochastic gradient descent. Note that these different contributions to the variance are not independent, the total variance cannot be obtained by simply adding them up.

For classification, a simple binomial can be used to model the sampling noise in the measure of the prediction accuracy of a trained pipeline on the test set. Indeed, if the pipeline has a chance τ of giving the wrong answer on a sample, makes i.i.d. errors, and is measured on n samples, the observed measure follows a binomial distribution of location parameter τ with n degrees of freedom. If errors are correlated, not i.i.d., the degrees of freedom are smaller and the distribution is wider. Figure 2 compares standard deviations of the performance measure given by this simple binomial model to those observed when bootstrapping the data on the three classification case studies. The match between the model and the empirical results suggest that the variance due to data sampling is well explained by the limited statistical power in the test set to estimate the true performance.

Variance induced by hyperparameter optimization: ξ_H
To study the ξ_H sources of variation, we chose three of the

[†]The more common alternative in machine learning is to use cross-validation, but the latter is less amenable to various sample sizes. Bootstrapping is discussed in more detail in Appendix B.

[‡]This choice is detailed in Appendix C.

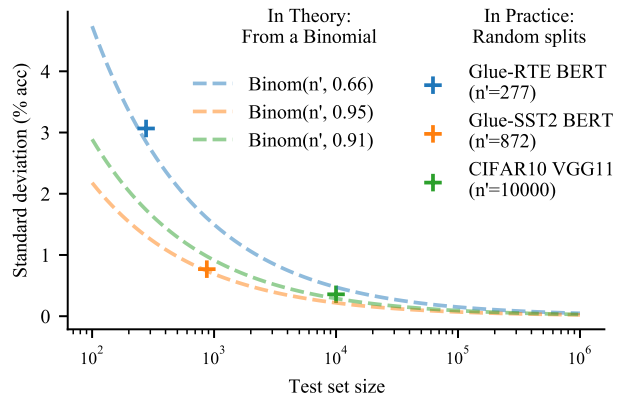


Figure 2. **Error due to data sampling:** The dotted lines show the standard deviation given by a binomial-distribution model of the accuracy measure; the crosses report the standard deviation observed when bootstrapping the data in our case studies, showing that the model is a reasonable.

most popular hyperparameter optimization methods: i) random search, ii) grid search, and iii) Bayesian optimization. While grid-search in itself has no random parameters, the specific choice of the parameter range is arbitrary and can be an uncontrolled source of variance (e.g., does the grid size step by powers of 2, 10, or increments of 0.25 or 0.5). We study this variance with a *noisy grid search*, perturbing slightly the parameter ranges (details in Appendix D).

For each of these tuning methods, we held all ξ_O fixed to random values and executed 20 independent hyperparameter optimization procedures up to a budget of 200 trials. This way, all the observed variance across the hyperparameter optimization procedures is strictly due to ξ_H . We were careful to design the search space so that it covers the optimal hyperparameter values (as stated in original studies) while being large enough to cover suboptimal values as well.

Results in figure 1 show that hyperparameter choice induces

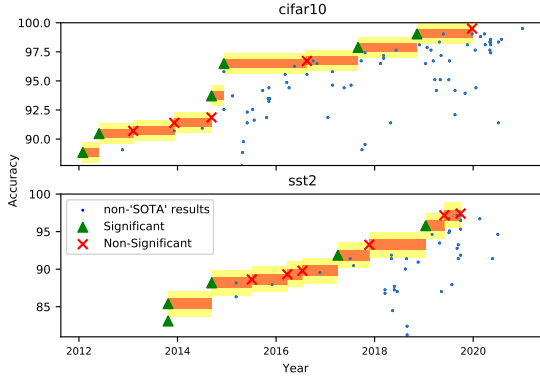


Figure 3. Published improvements compared to benchmark variance The dots give the performance of publications, function of year, as reported on paperswithcode.com; red band shows our estimated σ , and the yellow band the resulting significance threshold. Green marks are results likely significant compared to prior 'State of the Art', and red "x" appear non-significant.

a sizable amount of variance, not negligible in comparison to the other factors. The full optimization curves of the 320 HPO procedures are presented in Appendix E. The three hyperparameter optimization methods induce on average as much variance as the commonly studied weights initialization. These results motivate further investigation the cost of ignoring the variance due to hyperparameter optimization.

The bigger picture: Variance matters For a given case study, the total variance due to arbitrary choices and sampling noise revealed by our study can be put in perspective with the published improvements in the state-of-the-art. Figure 3 shows that this variance is on the order of magnitude of the individual increments. In other words, the variance is not small compared to the differences between pipelines. It must be accounted for when benchmarking pipelines.

3 ACCOUNTING FOR VARIANCE TO RELIABLY ESTIMATE PERFORMANCE $\hat{R}_{\mathcal{P}}$

This section contains 1) an explanation of the counter intuitive result that accounting for more sources of variation reduces the standard error for an estimator of $\hat{R}_{\mathcal{P}}$ and 2) an empirical measure of the degradation of expected empirical risk estimation due to neglecting HOpt variance.

We will now consider different *estimators* of the average performance $\mu = \hat{R}_{\mathcal{P}}(S, n, n')$ from Equation 5. Such estimators will use, in place of the expectation of Equation 5, an empirical average over k (train+test) splits, which we will denote $\hat{\mu}_{(k)}$ and $\hat{\sigma}_{(k)}^2$ the corresponding empirical variance. We will make an important distinction between an estimator which encompasses all sources of variation, the *ideal estimator* $\hat{\mu}_{(k)}$, and one which accounts only for a portion of

these sources, the *biased estimator* $\tilde{\mu}_{(k)}$.

But before delving into this, we will explain why many splits help estimating the expected empirical risk ($\hat{R}_{\mathcal{P}}$).

3.1 Multiple data splits for smaller detectable improvements

The majority of machine-learning benchmarks are built with fixed training and test sets. The rationale behind this design, is that learning algorithms should be compared on the same grounds, thus on the same sets of examples for training and testing. While the rationale is valid, it disregards the fact that the fundamental ground of comparison is the true distribution from which the sets were sampled. This finite set is used to compute the expected empirical risk ($\hat{R}_{\mathcal{P}}$ Eq 5), failing to compute the expected risk ($R_{\mathcal{P}}$ Eq 4) on the whole distribution. This empirical risk is therefore a noisy measure, it has some uncertainty because the risk on a particular test set gives limited information on what would be the risk on new data. This uncertainty due to data sampling is not small compared to typical improvements or other sources of variation, as revealed by our study in the previous section. In particular, figure 2 suggests that the size of the test set can be a limiting factor.

When comparing two learning algorithms A and B , we estimate their expected empirical risks $\hat{R}_{\mathcal{P}}$ with $\hat{\mu}_{(k)}$, a noisy measure. The uncertainty of this measure is represented by the standard error $\frac{\sigma}{\sqrt{k}}$ under the normal assumption[§] of \hat{R}_e . This uncertainty is an important aspect of the comparison, for instance it appears in statistical tests used to draw a conclusion in the face of a noisy evidence. For instance, a z-test states that a difference of expected empirical risk between A and B of at least $z_{0.05} \sqrt{\frac{\sigma_A^2 + \sigma_B^2}{k}}$ must be observed to control false detections at a rate of 95%. In other words, a difference smaller than this value could be due to noise alone, e.g. different sets of random splits may lead to different conclusions.

With $k = 1$, algorithms A and B must have a large difference of performance to support a reliable detection. In order to detect smaller differences, k must be increased, i.e. $\hat{\mu}_{(k)}$ must be computed over several data splits. The estimator $\hat{\mu}_{(k)}$ is computationally expensive however, and most researchers must instead use a biased estimator $\tilde{\mu}_{(k)}$ that does not probe well all sources of variance.

3.2 Bias and variance of estimators depends on whether they account for all sources of variation

Probing all sources of variation, including hyperparameter optimization, is too computationally expensive for most

[§]Our extensive numerical experiments show that a normal distribution is well suited for the fluctuations of the risk—figure F.2

researchers. However, ignoring the role of hyperparameter optimization induces a bias in the estimation of the expected empirical risk. We discuss in this section the expensive unbiased ideal estimator and the cheap biased estimator. We explain as well why accounting for many sources of variation improves the biased estimator by reducing its bias.

3.2.1 Ideal estimator: sampling multiple HOpt

The ideal estimator $\hat{\mu}_{(k)}$ takes into account all sources of variation. For each performance measure \hat{R}_e , all ξ_O and ξ_H are randomized, each requiring an independent hyperparameter optimization procedure. The detailed procedure is presented in Algorithm 1. For an estimation over k splits with hyperparameter optimization for a budget of T trials, it requires fitting the learning algorithm a total of $O(k \cdot T)$ times. The estimator is unbiased, with $\mathbb{E}[\hat{\mu}_{(k)}] = \mu$.

For a variance of the performance measures $\text{Var}(\hat{R}_e) = \sigma^2$, we can derive the variance of the ideal estimator $\text{Var}(\hat{\mu}_{(k)}) = \frac{\sigma^2}{k}$ by taking the sum of the variances in $\hat{\mu}_{(k)} = \frac{1}{k} \sum_{i=1}^k \hat{R}_{ei}$. We see that with $\lim_{k \rightarrow \infty} \text{Var}(\hat{\mu}_{(k)}) = 0$. Thus $\hat{\mu}_{(k)}$ is a well-behaved unbiased estimator of μ , as its mean squared error vanishes with k infinitely large:

$$\begin{aligned} \mathbb{E}[(\hat{\mu}_{(k)} - \mu)^2] &= \text{Var}(\hat{\mu}_{(k)}) + (\mathbb{E}[\hat{\mu}_{(k)}] - \mu)^2 \\ &= \frac{\sigma^2}{k} \end{aligned} \quad (6)$$

Note that T does not appear in these equations. Yet it controls HOpt's runtime cost (T trials to determine $\hat{\lambda}^*$), and thus the variance σ^2 is a function of T .

3.2.2 Biased estimator: fixing HOpt

A computationally much cheaper but biased estimator consists in re-using the hyperparameters obtained from a *single* hyperparameter optimization to generate k subsequent performance measures \hat{R}_e where only ξ_O (or a subset of ξ_O) is randomized. This procedure is presented in Algorithm 2. It requires only $O(k + T)$ fittings, substantially less than the ideal estimator. The estimator is biased with $k > 1$, $\mathbb{E}[\hat{\mu}_{(k)}] \neq \mu$. A bias will occur when a set of hyperparameters $\hat{\lambda}^*$ are optimal for a particular instance of ξ_O but not over most others.

When we fix sources of variation ξ to arbitrary values (e.g. random seed), we are conditioning the distribution of \hat{R}_e on some arbitrary ξ . Intuitively, holding fix some sources of variations should reduce the variance of the whole process. What our intuition fails to grasp however, is that this conditioning to arbitrary ξ induces a correlation between the trainings which in turns increases the variance of the estimator. Indeed, a sum of correlated variables increases with the strength of the correlations.

Algorithm 1 IdealEst

Ideal Estimator $\hat{\mu}_{(k)}, \hat{\sigma}_{(k)}$

Input:

dataset S
sample size k

for i in $\{1, \dots, k\}$ **do**

$\xi_O \sim \text{RNG}()$
 $\xi_H \sim \text{RNG}()$
 $S^{tv}, S^o \sim \text{sp}(S; \xi_O)$

$\hat{\lambda}^* = \text{HOpt}(S^{tv}, \xi_O, \xi_H)$

$\hat{h}^* = \text{Opt}(S^{tv}, \hat{\lambda}^*)$

$p_i = \hat{R}_e(\hat{h}^*, S^o)$

end for

Return $\hat{\mu}_{(k)} = \text{mean}(p)$,
 $\hat{\sigma}_{(k)} = \text{std}(p)$

Algorithm 2 FixHOptEst

Biased Estimator $\tilde{\mu}_{(k)}, \tilde{\sigma}_{(k)}$

Input:

dataset S
sample size k

$\xi_O \sim \text{RNG}()$

$\xi_H \sim \text{RNG}()$

$S^{tv}, S^o \sim \text{sp}(S; \xi_O)$

$\hat{\lambda}^* = \text{HOpt}(S^{tv}, \xi_O, \xi_H)$

for i in $\{1, \dots, k\}$ **do**

$\xi_O \sim \text{RNG}()$

$S^{tv}, S^o \sim \text{sp}(S; \xi_O)$

$\hat{h}^* = \text{Opt}(S^{tv}, \hat{\lambda}^*)$

$p_i = \hat{R}_e(\hat{h}^*, S^o)$

end for

Return $\tilde{\mu}_{(k)} = \text{mean}(p)$,
 $\tilde{\sigma}_{(k)} = \text{std}(p)$

Figure 4. Estimators of the performance of a method, and its variation. We represent the seeding of sources of variations with $\xi \sim \text{RNG}()$, where $\text{RNG}()$ is some random number generator. Their difference lies in the hyper-parameter optimization step (HOpt). The ideal estimator requires executing k times HOpt, each requiring T trainings for the hyperparameter optimization, for a total of $O(k \cdot T)$ trainings. The biased estimator requires executing only 1 time HOpt, for $O(k + T)$ trainings in total.

Let $\text{Var}(\hat{R}_e | \xi)$ be the variance of the conditioned performance measures \hat{R}_e and ρ the average correlation among all pairs of \hat{R}_e . The variance of the biased estimator is then given by the following equation.

$$\text{Var}(\tilde{\mu}_{(k)} | \xi) = \frac{\text{Var}(\hat{R}_e | \xi)}{k} + \frac{k-1}{k} \rho \text{Var}(\hat{R}_e | \xi) \quad (7)$$

We can see that with a large enough correlation, the variance $\text{Var}(\tilde{\mu}_{(k)} | \xi)$ could be dominated by the second term. In such case, increasing the number of data splits k would not reduce the variance of $\tilde{\mu}_{(k)}$. Unlike with $\hat{\mu}_{(k)}$, the mean square error for $\tilde{\mu}_{(k)}$ will not decrease with k :

$$\begin{aligned} \mathbb{E}[(\tilde{\mu}_{(k)} - \mu)^2] &= \text{Var}(\tilde{\mu}_{(k)} | \xi) + (\mathbb{E}[\tilde{\mu}_{(k)} | \xi] - \mu)^2 \\ &= \frac{\text{Var}(\hat{R}_e | \xi)}{k} + \frac{k-1}{k} \rho \text{Var}(\hat{R}_e | \xi) \\ &\quad + (\mathbb{E}[\hat{R}_e | \xi] - \mu)^2 \end{aligned} \quad (8)$$

This result has two implications, one beneficial to improving benchmarks, the other not. Bad news first, the limited effectiveness of increasing k to improve the quality of the estimator $\tilde{\mu}_{(k)}$ is a consequence of ignoring the variance induced by hyperparameter optimization. We cannot avoid this loss of quality if we do not have the budget for repeated independent hyperoptimization. The good news is that current practices generally account for only one or two sources

of variation; there is thus room for improvement. This has the potential of decreasing the average correlation ρ and moving $\tilde{\mu}_{(k)}$ closer to $\hat{\mu}_{(k)}$. We will see empirically in next section how accounting for more sources of variation moves us closer to $\hat{\mu}_{(k)}$ in most of our case studies.

3.3 The cost of ignoring HOpt variance

To compare the estimators $\hat{\mu}_{(k)}$ and $\tilde{\mu}_{(k)}$ presented above, we measured empirically the statistics of the estimators on budgets of $k = (1, \dots, 100)$ points on our five case studies. The ideal estimator is asymptotically unbiased and therefore only one repetition is enough to estimate $\text{Var}(\hat{\mu}_{(k)})$ for each task. For the biased estimator we run 20 repetitions to estimate $\text{Var}(\tilde{\mu}_{(k)} \mid \xi)$. We sample 20 arbitrary ξ (random seeds) and compute the standard deviation of $\tilde{\mu}_{(k)}$ for $k = (1, \dots, 100)$.

We compared the biased estimator `FixedHOptEst()` while varying different subset of sources of variations to see if randomizing more of them would help increasing the quality of the estimator. We note `FixedHOptEst(k, Init)` the biased estimator $\tilde{\mu}_{(k)}$ randomizing only the weights initialization, `FixedHOptEst(k, Data)` the biased estimator randomizing only data splits, and `FixedHOptEst(k, All)` the biased estimator randomizing all sources of variation ξ_O except for hyperparameter optimization.

We present results from a subset of the tasks in Figure 5 (all tasks are presented in Figure G.3). Randomizing weights initialization only (`FixedHOptEst(k, init)`) provides only a small improvement with $k > 1$. In the task where it best performs (Glue-RTE), it converges to the equivalent of $\hat{\mu}_{(k=2)}$. This is an important result since it corresponds to the predominant approach used in the literature today. Bootstrapping with `FixedHOptEst(k, Data)` improves the standard error for all tasks, converging to equivalent of $\hat{\mu}_{(k=2)}$ to $\hat{\mu}_{(k=10)}$. Still, the biased estimator including all sources of variations excluding hyperparameter optimization `FixedHOptEst(k, All)` is by far the best estimator after the ideal estimator, converging to equivalent of $\hat{\mu}_{(k=2)}$ to $\hat{\mu}_{(k=100)}$.

This shows that accounting for all sources of variation reduces the likelihood of error in a computationally achievable manner. `IdealEst(k = 100)` takes 1 070 hours to compute, compared to only 21 hours for each `FixedHOptEst(k = 100)`. Our study paid the high computational cost of multiple rounds of `FixedHOptEst(k, All)`, and the cost of `IdealEst(k)` for a total of 6.4 GPU years to show that `FixedHOptEst(k, All)` is better than the status-quo and a satisfying option for statistical model comparisons without these prohibitive costs.

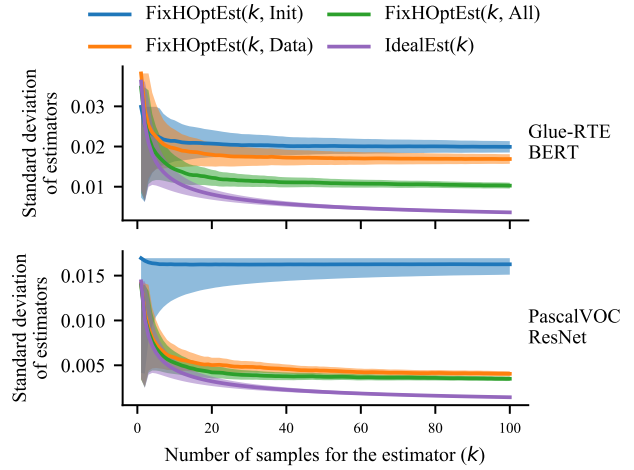


Figure 5. **Standard error of biased and ideal estimators with k samples.** Top figure presents results from BERT trained on RTE and bottom figure VGG11 on CIFAR10. All other tasks are presented in Figure G.3. On x axis, the number of samples used by the estimators to compute the average classification accuracy. On y axis, the standard deviation of the estimators. Uncertainty represented in light color is computed analytically as the approximate standard deviation of the standard deviation of a normal distribution computed on k samples. For most case studies, **accounting for more sources of variation reduces the standard error of $\hat{\mu}_{(k)}$** . This is caused by the decreased correlation ρ thanks to additional randomization in the learning pipeline. `FixHOptEst(k, All)` provides an improvement towards `IdealEst(k)` for no additional computational cost compared to `FixHOptEst(k, Init)` which is currently considered as a good practice. **Ignoring variance from HOpt is harmful for a good estimation of $\hat{R}_{\mathcal{P}}$.**

4 ACCOUNTING FOR VARIANCE TO DRAW RELIABLE CONCLUSIONS

4.1 Criteria used to conclude from benchmarks

Given an estimate of the performance of two learning pipelines and their variance, are these two pipelines different in a meaningful way? We first formalize common practices to draw such conclusions, then characterize their error rates.

Comparing the average difference A typical criterion to accept a pipeline as an improvement is to compare the difference to the baseline to an acceptance threshold δ , sometimes implicit. The choice of the threshold δ can be arbitrary, but a reasonable one is to consider previous accepted improvements, e.g. in publications on the same task.

This difference in performance is sometimes computed across a single run of the two pipelines, but a better practice used in the deep-learning community is to average multiple seeds (Bouthillier & Varoquaux, 2020). Typically hyperparameter optimization is performed for each learning

algorithm and then several weights initializations or other sources of fluctuation are sampled, giving k estimates of the risk \hat{R}_e – note that these are biased as detailed in [subsection 3.2.2](#). If algorithm A performs better than algorithm B by at least δ on average, it is considered as a better algorithm than B for the task at hand. This method is simple but does not conclude on whether the difference stands out from the fluctuations: it has no control on false detections.

Assuming that the fluctuations of the performance estimates are normally distributed –as observed in our extensive numerical experiments, on figure [F.2](#)–, we can model the rate of positive comparisons. Let $\hat{R}_e^A = \frac{1}{k} \sum_{i=1}^k \hat{R}_{ei}^A$, where \hat{R}_{ei}^A is the empirical risk of algorithm A on the i -th split, be the mean performance of algorithm A , and similarly for B . The decision whether A outperforms B is then determined by $(\hat{R}_e^A - \hat{R}_e^B > \delta)$.

The variance is not accounted for in the average comparison. We will now present a statistical test accounting for it. Both comparison methods will next be evaluated empirically using simulations based on our case studies.

Probability of outperforming The choice of threshold δ to compare the average difference to is problem-specific and does not relate well to a statistical improvement. Rather, we propose to formulate the comparison in terms of probability of improvement. Instead of comparing the average performances, we compare their distributions altogether. Let $\mathbb{P}(A > B)$ be the probability of measuring a better performance for A than B across fluctuations such as data splits and weights initialization. To consider an algorithm A significantly better than B , we ask that A outperforms B *often enough*: $\mathbb{P}(A > B) \geq \gamma$. Often enough, as set by γ , needs to be defined by community standards, which we will revisit below. This probability can simply be computed as the proportion of successes, $\hat{R}_{ei}^A > \hat{R}_{ei}^B$, where $(\hat{R}_{ei}^A, \hat{R}_{ei}^B), i \in \{1, \dots, k\}$ are pairs of empirical risks measured on k different data splits for algorithms A and B .

$$\mathbb{P}(A > B) = \frac{1}{k} \sum_{i=1}^k I_{\{\hat{R}_{ei}^A > \hat{R}_{ei}^B\}} \quad (9)$$

where I is the indicator function. We will build upon the non-parametric Mann-Whitney test to produce decisions about whether $\mathbb{P}(A > B) \geq \gamma$ ([Perme & Manevski, 2019](#)).

The problem is well formulated in the Neyman-Pearson view of statistical testing ([Neyman & Pearson, 1928](#); [Perez-gonzalez, 2015](#)), which requires the explicit definition of both a null hypothesis H_0 to control for *statistically significant* results, and an alternative hypothesis H_1 to declare results *statistically meaningful*. A *statistically significant* result is one that is not explained by noise, the null-hypothesis $H_0 : \mathbb{P}(A > B) = 0.5$. With large enough sample size, any

arbitrarily small difference can be made *statistically significant*. A *statistically meaningful* result is one large enough to satisfy the alternative hypothesis $H_1 : \mathbb{P}(A > B) = \gamma$. Recall that γ is a threshold that needs to be defined by community standards. We will discuss reasonable values for γ in next section based on our simulations.

We suggest to conclude that algorithm A is better than B on a given task if the result is both *statistically significant* and *meaningful*. The reliability of the estimation of $\mathbb{P}(A > B)$ can be quantified using confidence intervals, computed with the non-parametric percentile bootstrap ([Efron, 1982](#)). The lower bound of the confidence interval CI_{\min} controls if the result is *significant* ($\mathbb{P}(A > B) - \text{CI}_{\min} > 0.5$), and the upper bound of the confidence interval CI_{\max} controls if the result is *meaningful* ($\mathbb{P}(A > B) + \text{CI}_{\max} > \gamma$).

If the number of draws k is small, counting as in equation 9 gives imprecise estimates of this probability. An alternative is then to rely on a normal model, and the decision criteria then becomes:

$$\text{Accept } A \text{ over } B \text{ if } \frac{\mu_A - \mu_B}{\sqrt{(\sigma_A^2 + \sigma_B^2)}} > \Phi^{-1}(1 - \gamma) \quad (10)$$

where Φ^{-1} is the inverse cumulative distribution function of the normal distribution. The above formula is easy to compute and is related to the Neyman-Pearson view on the t-test. In addition, it motivates a popular decision rule: checking to see if the observed standard deviations in results overlaps the observed means.

4.2 Characterizing errors of these conclusion criteria

We now run an empirical study of the two conclusion criteria present above, the popular “comparing the average difference” and our new “probability of outperforming”. We will re-use mean and variance estimates from [subsection 3.3](#) with the Ideal and biased estimators so that we can show that our proposed method has a higher rate of detecting significant improvement compared to the current approaches and is closer to the ideal case.

Computing error rates using plug-in estimators In order to test the reliability of the comparison methods, we run simulations based on the variances measured in Section 2.

We simulate realizations of the ideal estimator $\hat{\mu}_{(k)}$ and the biased estimator $\tilde{\mu}_{(k)}$ with a budget of $k = 50$ data splits. For the ideal estimator, we model $\hat{\mu}_{(k)}$ with a normal distribution $\hat{\mu}_{(k)} \sim \mathcal{N}(\mu, \frac{\sigma^2}{k})$, where σ^2 is the variance measured with the ideal estimator in our case studies, and μ is the empirical risk \hat{R}_e . Our experiments consist in varying the difference in μ for the two algorithms, to span from identical to widely different performance ($\mu_A \gg \mu_B$).

For the biased estimator, we rely on a two stage sampling

process for the simulation. First, we sample the bias of $\tilde{\mu}_{(k)}$ based on the variance $\text{Var}(\tilde{\mu}_{(k)} \mid \xi)$ measured in our case studies, $B \sim \mathcal{N}(0, \text{Var}(\tilde{\mu}_{(k)} \mid \xi))$. Given b , a sample of B , we sample k empirical risks following $\hat{R}_e \sim \mathcal{N}(\mu + b, \text{Var}(\hat{R}_e \mid \xi))$, where $\text{Var}(\hat{R}_e \mid \xi)$ is the variance of \hat{R}_e averaged across 20 realizations of $\tilde{\mu}_{(k)}$ that we measured in our case studies. In simulation we vary the mean performance of A with respect to the mean performance of B so that $\mathbb{P}(A > B)$ varies from 0.4 to 1 to test three regions: H_0 is true ($\mathbb{P}(\mathbb{P}(A > B) - \text{CI}_{\min} \geq 0.5)$), H_1 is true (i.e., significant and meaningful) $\mathbb{P}(\mathbb{P}(A > B) - \text{CI}_{\min} > 0.5 \wedge \mathbb{P}(A > B) + \text{CI}_{\min} > \gamma)$, and a middle region (i.e., significant but not meaningful: $\mathbb{P}(\mathbb{P}(A > B) - \text{CI}_{\min} \geq 0.5)$).

For decisions based on comparing averages, we set $\delta = 1.9952\sigma$ where σ is the standard deviation measured in our case studies with the ideal estimator. The value 1.9952 is set by linear regression so that δ matches the average improvements obtained from paperswithcode.com. This provides a threshold δ representative of the published improvements. For the probability of outperforming, we use a threshold of $\gamma = 0.75$ which we have observed to be robust across all case studies (See Appendix H).

Observations Figure 6 reports results for different decision criteria, using the ideal estimator and the biased estimator, as the difference in performance of the algorithms A and B increases. The input is broken into three regions, leftmost is when H_0 is true (not-significant), the grey middle when the result is significant, but not meaningful in our framework, and the rightmost is when H_1 is true (significant and meaningful). The single point comparison leads to the worst decision by far. It suffers from both high false positives ($\approx 10\%$) and high false negatives ($\approx 75\%$). The average with $k = 50$, on the other hand, is very conservative with low false positives ($< 5\%$) but very high false negatives ($\approx 90\%$). Using the probability of outperforming leads to better balanced decisions, with a reasonable rate of false positives ($\approx 5\%$) on the left and a reasonable rate of false negatives on the right ($\approx 30\%$).

The main problem with the average comparison is the threshold. A t-test only differs from an average in that the threshold is computed based on the variance of the model performances and the sample size.

Finally, we observe that the test of probability of outperforming ($\mathbb{P}(A > B)$) controls well the error rates even when used with a biased estimator. Its performance is nevertheless slightly impacted by the biased estimator compared to the ideal estimator. Although we cannot guarantee a nominal control, we confirm that it is a major improvement compared to the commonly used comparison method at no additional cost.

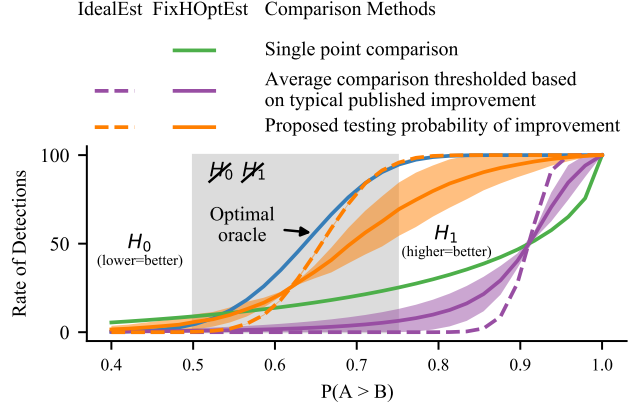


Figure 6. Rate of detections of different comparison methods. x axis is the true simulated probability of a learning algorithm A to outperform another algorithm B across random fluctuations (ex: random data splits). We vary the mean performance of A with respect to that of B so that $\mathbb{P}(A > B)$ varies from 0.4 to 1. The blue line is the optimal oracle, with perfect knowledge of the variances. The single-point comparison (green line) has both a high rate of false positives in the left region ($\approx 10\%$) and a high rate of false negative on the right ($\approx 75\%$). The orange and purple lines show the results for the *average comparison method* (prevalent in the literature) and our proposed *probability of outperforming* method respectively. The solid versions are using the expensive ideal estimator, and the dashed line our $51\times$ cheaper, but biased, estimator. The average comparison is highly conservative with a low rate of false positives ($< 5\%$) on the left and a high rate of false negative on the right ($\approx 90\%$), even with the expensive and exhaustive simulation. Using the probability of outperforming has both a reasonable rate of false positives ($\approx 5\%$) on the left and a reasonable rate of false negatives on the right ($\approx 30\%$) even when using our biased estimator, and approaches the oracle when using the expensive estimator.

5 OUR RECOMMENDATIONS: GOOD BENCHMARKS WITH A BUDGET

We now distill from the theoretical and empirical results of the previous sections a set of practical recommendations to benchmark machine-learning pipelines. Our recommendations are pragmatic in the sense that they are simple to implement and cater for limited computational budgets.

Randomize as many sources of variations as possible

Fitting and evaluating a modern machine-learning pipeline comes with many arbitrary aspects, such as the choice of initializations or the data order. Benchmarking a pipeline given a specific instance of these choices will not give an evaluation that generalize to new data, even drawn from the same distribution. On the opposite, a benchmark that varies these arbitrary choices will not only evaluate the associated variance (section 2), but also reduce the error on the expected performance as they enable measures of performance on the test set that are less correlated (3). This counter-intuitive

phenomenon is related to the variance reduction of bagging (Breiman, 1996a; Bühlmann et al., 2002), and helps characterizing better the expected behavior of a machine-learning pipeline, as opposed to a specific fit.

Account for variance to detect meaningful improvements Concluding on the significance –statistical or practical– of an improvement based on the difference between average performance requires the choice of a threshold that can be difficult to set. A natural scale is that of the variance of the benchmark, sometimes used informally. Formulating the detection threshold on the probability that on one execution a pipeline outperforms another (section 4.1 and equation 10) nicely relates this comparison of variance to a probabilistic control. In addition, using a threshold of $\mathbb{P}(A > B) > 0.75$ gives empirically a criterion that separates well benchmarking fluctuations from published improvements over the 5 case studies that we considered. We recommend to always highlight not only the best-performing procedure, but also all those within the significance bounds.

Use multiple data splits The subset of the data used as test set to validate an algorithm is arbitrary. As it is of a limited size, it comes with a limited estimation quality with regards to the performance of the algorithm on wider samples of the same data distribution (figure 2). Improvements smaller than this variance observed on a given test set will not generalize. Importantly, this variance is not negligible compared to typical published improvements or other sources of variance (figures 3 and 1). For pipeline comparisons with more statistical power, it is useful to draw multiple tests, for instance generating random splits with a out-of-bootstrap scheme (detailed in appendix B).

6 ADDITIONAL CONSIDERATIONS

There are many aspects of benchmarks which our study has not addressed. For completeness, we discuss them here.

Comparing models instead of procedures Our framework provides value when the user can control the model training process and source of variation. In cases where models are *given* but not under our control (e.g., purchased via API or a competition), the only source of variation left is the data used to test the model. Our framework and analysis does not apply to such scenarios.

Benchmarks and competitions with many contestants We focused on comparing two learning algorithms. Benchmarks – and competitions in particular – commonly involve large number of learning algorithms that are being compared. Part of our results carry over unchanged in such settings, in particular those related to variance and performance estimation. With regards to reaching a well-controlled decision,

a new challenge comes from multiple comparisons when there are many algorithms. A possible alley would be to adjust the decision threshold γ , raising it with a correction for multiple comparisons (e.g. Bonferroni) (Dudoit et al., 2003). However, as the number gets larger, the correction becomes stringent. In competitions where the number of contestants can reach hundreds, the choice of a winner comes necessarily with some arbitrariness: a different choice of test sets might have led to a slightly modified ranking.

Comparisons across multiple dataset Comparison over multiple datasets is often used to accumulate evidence that one algorithm outperforms another one. The challenge is to account of different errors, in particular different levels of variance, on each dataset.

Demšar (2006) recommended Wilcoxon signed ranks test or Friedman tests to compare classifiers across multiple datasets. These recommendations are however hardly applicable on small sets of datasets – machine learning works typically include as few as 3 to 5 datasets (Bouthillier & Varoquaux, 2020). The number of datasets corresponds to the sample size of these tests, and such a small sample size gives tests with a very limited statistical power.

Dror et al. (2017) propose to accept methods that give improvements on *all* datasets, controlling for multiple comparisons. As opposed to Demšar (2006)’s recommendation, this approach performs well with a small number of datasets. On the other hand, a large number of datasets will increase significantly the severity of the family-wise error-rate correction, making Demšar’s recommendations more favorable.

Non-normal metrics We focused on model performance, but model evaluation in practice can include other metrics such as the training time to reach a performance level or the memory foot-print (Reddi et al., 2020). Performance metrics are generally averages over samples which typically makes them amenable to a reasonable normality assumption. When normality does not hold, the parametric form of the criterion judging the probability of outperforming (equation 10) cannot be used.

7 CONCLUSION

We showed that fluctuations in the performance measured by machine-learning benchmarks arise from many different sources. In deep learning, most evaluations focus on the effect of random weight initialization, which actually contribute a small part of the variance, on par with residual fluctuations of hyperparameter choices after their optimization but much smaller than the variance due to perturbing the split of the data in train and test sets. Our study clearly shows that these factors must be accounted to give reliable benchmarks. For this purpose, we study estimators of bench-

mark variance as well as decision criterion to conclude on an improvement. Our findings outline recommendations to improve reliability of machine learning benchmarks: 1) sample as many sources of variations as possible in the performance estimation; 2) account for the resulting variance when concluding on the benefit of an algorithm over another; 3) prefer resampling to fixed test sets.

REFERENCES

- Anders Sogaard, Anders Johannsen, B. P. D. H. and Alonso, H. M. What's in a p-value in nlp? In *Proceedings of the Eighteenth Conference on Computational Natural Language Learning*, pp. 1–10. Association for Computational Linguistics, 2014.
- Bentivogli, L., Dagan, I., Dang, H. T., Giampiccolo, D., and Magnini, B. The fifth PASCAL recognizing textual entailment challenge. 2009.
- Blalock, D., Gonzalez Ortiz, J. J., Frankle, J., and Gutttag, J. What is the State of Neural Network Pruning? In *Proceedings of Machine Learning and Systems 2020*, pp. 129–146. 2020.
- Bouckaert, R. R. and Frank, E. Evaluating the replicability of significance tests for comparing learning algorithms. In *Pacific-Asia Conference on Knowledge Discovery and Data Mining*, pp. 3–12. Springer, 2004.
- Bouthillier, X. and Varoquaux, G. Survey of machine-learning experimental methods at NeurIPS2019 and ICLR2020. Research report, Inria Saclay Ile de France, January 2020. URL <https://hal.archives-ouvertes.fr/hal-02447823>.
- Bouthillier, X., Laurent, C., and Vincent, P. Unreproducible research is reproducible. In Chaudhuri, K. and Salakhutdinov, R. (eds.), *Proceedings of the 36th International Conference on Machine Learning*, volume 97 of *Proceedings of Machine Learning Research*, pp. 725–734, Long Beach, California, USA, 09–15 Jun 2019. PMLR. URL <http://proceedings.mlr.press/v97/bouthillier19a.html>.
- Breiman, L. Bagging predictors. *Machine learning*, 24(2): 123–140, 1996a.
- Breiman, L. Out-of-bag estimation. 1996b.
- Bühlmann, P., Yu, B., et al. Analyzing bagging. *The Annals of Statistics*, 30(4):927–961, 2002.
- Dacrema, M. F., Cremonesi, P., and Jannach, D. Are we really making much progress? A Worrying Analysis of Recent Neural Recommendation Approaches. In *Proceedings of the 13th ACM Conference on Recommender Systems - RecSys '19*, pp. 101–109, New York, New York, USA, 2019. ACM Press. ISBN 9781450362436. doi: 10.1145/3298689.3347058. URL <http://dl.acm.org/citation.cfm?doid=3298689.3347058>.
- Demšar, J. Statistical comparisons of classifiers over multiple data sets. *Journal of Machine learning research*, 7 (Jan):1–30, 2006.
- Deng, J., Dong, W., Socher, R., Li, L.-J., Li, K., and Fei-Fei, L. ImageNet: A Large-Scale Hierarchical Image Database. In *CVPR09*, 2009.
- Devlin, J., Chang, M.-W., Lee, K., and Toutanova, K. Bert: Pre-training of deep bidirectional transformers for language understanding, 2018.
- Dietterich, T. G. Approximate statistical tests for comparing supervised classification learning algorithms. *Neural computation*, 10(7):1895–1923, 1998.
- Dror, R., Baumer, G., Bogomolov, M., and Reichart, R. Replicability analysis for natural language processing: Testing significance with multiple datasets. *Transactions of the Association for Computational Linguistics*, 5:471–486, 2017.
- Dudoit, S., Shaffer, J. P., and Boldrick, J. C. Multiple hypothesis testing in microarray experiments. *Statistical Science*, pp. 71–103, 2003.
- Efron, B. Bootstrap methods: Another look at the jackknife. *Ann. Statist.*, 7(1):1–26, 01 1979. doi: 10.1214/aos/1176344552. URL <https://doi.org/10.1214/aos/1176344552>.
- Efron, B. *The jackknife, the bootstrap, and other resampling plans*, volume 38. Siam, 1982.
- Everingham, M., Van Gool, L., Williams, C. K. I., Winn, J., and Zisserman, A. The PASCAL Visual Object Classes Challenge 2012 (VOC2012) Results. <http://www.pascal-network.org/challenges/VOC/voc2012/workshop/index.html>.
- Glorot, X. and Bengio, Y. Understanding the difficulty of training deep feedforward neural networks. In Teh, Y. W. and Titterton, M. (eds.), *Proceedings of the Thirteenth International Conference on Artificial Intelligence and Statistics*, volume 9 of *Proceedings of Machine Learning Research*, pp. 249–256, Chia Laguna Resort, Sardinia, Italy, 13–15 May 2010. PMLR. URL <http://proceedings.mlr.press/v9/glorot10a.html>.
- Gorman, K. and Bedrick, S. We need to talk about standard splits. In *Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics*,

- pp. 2786–2791, Florence, Italy, July 2019. Association for Computational Linguistics. doi: 10.18653/v1/P19-1267. URL <https://www.aclweb.org/anthology/P19-1267>.
- He, K., Zhang, X., Ren, S., and Sun, J. Deep residual learning for image recognition, 2015a.
- He, K., Zhang, X., Ren, S., and Sun, J. Delving deep into rectifiers: Surpassing human-level performance on imagenet classification. In *Proceedings of the IEEE international conference on computer vision*, pp. 1026–1034, 2015b.
- He, K., Zhang, X., Ren, S., and Sun, J. Identity mappings in deep residual networks. In *European conference on computer vision*, pp. 630–645. Springer, 2016.
- Henderson, P., Islam, R., Bachman, P., Pineau, J., Precup, D., and Meger, D. Deep reinforcement learning that matters. In *Thirty-Second AAAI Conference on Artificial Intelligence*, 2018.
- Henikoff, S. and Henikoff, J. G. Amino acid substitution matrices from protein blocks. *Proceedings of the National Academy of Sciences*, 89(22):10915–10919, 1992.
- Hothorn, T., Leisch, F., Zeileis, A., and Hornik, K. The design and analysis of benchmark experiments. *Journal of Computational and Graphical Statistics*, 14(3):675–699, 2005.
- Hutter, F., Hoos, H., and Leyton-Brown, K. An efficient approach for assessing hyperparameter importance. In *Proceedings of International Conference on Machine Learning 2014 (ICML 2014)*, pp. 754–762, June 2014.
- Jurtz, V., Paul, S., Andreatta, M., Marcatili, P., Peters, B., and Nielsen, M. Netmhcpan-4.0: improved peptide–mhc class i interaction predictions integrating eluted ligand and peptide binding affinity data. *The Journal of Immunology*, 199(9):3360–3368, 2017.
- Kadlec, R., Bajgar, O., and Kleindienst, J. Knowledge base completion: Baselines strike back. In *Proceedings of the 2nd Workshop on Representation Learning for NLP*, pp. 69–74, 2017.
- Klein, A., Falkner, S., Mansur, N., and Hutter, F. Robo: A flexible and robust bayesian optimization framework in python. In *NIPS 2017 Bayesian Optimization Workshop*, December 2017.
- Krizhevsky, A., Hinton, G., et al. Learning multiple layers of features from tiny images. 2009.
- Liu, C., Zoph, B., Neumann, M., Shlens, J., Hua, W., Li, L.-J., Fei-Fei, L., Yuille, A., Huang, J., and Murphy, K. Progressive neural architecture search. In *The European Conference on Computer Vision (ECCV)*, September 2018.
- Long, J., Shelhamer, E., and Darrell, T. Fully convolutional networks for semantic segmentation, 2014.
- Lucic, M., Kurach, K., Michalski, M., Gelly, S., and Bousquet, O. Are gans created equal? a large-scale study. In Bengio, S., Wallach, H., Larochelle, H., Grauman, K., Cesa-Bianchi, N., and Garnett, R. (eds.), *Advances in Neural Information Processing Systems 31*, pp. 700–709. Curran Associates, Inc., 2018.
- Mahajan, D., Girshick, R., Ramanathan, V., He, K., Paluri, M., Li, Y., Bharambe, A., and van der Maaten, L. Exploring the limits of weakly supervised pretraining. In *Proceedings of the European Conference on Computer Vision (ECCV)*, pp. 181–196, 2018.
- Melis, G., Dyer, C., and Blunsom, P. On the state of the art of evaluation in neural language models. *ICLR*, 2018.
- Musgrave, K., Belongie, S., and Lim, S.-N. A Metric Learning Reality Check. *arXiv*, 2020. URL <http://arxiv.org/abs/2003.08505>.
- Nadeau, C. and Bengio, Y. Inference for the generalization error. In Solla, S. A., Leen, T. K., and Müller, K. (eds.), *Advances in Neural Information Processing Systems 12*, pp. 307–313. MIT Press, 2000.
- Neyman, J. and Pearson, E. S. On the use and interpretation of certain test criteria for purposes of statistical inference: Part i. *Biometrika*, pp. 175–240, 1928.
- Nielsen, M., Lundegaard, C., Blicher, T., Lamberth, K., Harndahl, M., Justesen, S., Røder, G., Peters, B., Sette, A., Lund, O., et al. Netmhcpan, a method for quantitative predictions of peptide binding to any hla-a and-b locus protein of known sequence. *PloS one*, 2(8), 2007.
- O’Donnell, T. J., Rubinsteyn, A., Bonsack, M., Riemer, A. B., Laserson, U., and Hammerbacher, J. Mhcflurry: open-source class i mhc binding affinity prediction. *Cell systems*, 7(1):129–132, 2018.
- Pearson, H., Daouda, T., Granados, D. P., Durette, C., Bonneil, E., Courcelles, M., Rodenbrock, A., Laverdure, J.-P., Côté, C., Mader, S., et al. Mhc class i–associated peptides derive from selective regions of the human genome. *The Journal of clinical investigation*, 126(12):4690–4701, 2016.
- Perezgonzalez, J. D. Fisher, neyman-pearson or nhst? a tutorial for teaching data testing. *Frontiers in Psychology*, 6:223, 2015.

- Perme, M. P. and Manevski, D. Confidence intervals for the mann–whitney test. *Statistical methods in medical research*, 28(12):3755–3768, 2019.
- Raff, E. A Step Toward Quantifying Independently Reproducible Machine Learning Research. In *NeurIPS*, 2019. URL <http://arxiv.org/abs/1909.06674>.
- Raff, E. Research Reproducibility as a Survival Analysis. In *The Thirty-Fifth AAAI Conference on Artificial Intelligence*, 2021. URL <http://arxiv.org/abs/2012.09932>.
- Reddi, V. J., Cheng, C., Kanter, D., Mattson, P., Schmuelling, G., Wu, C.-J., Anderson, B., Breughe, M., Charlebois, M., Chou, W., et al. Mlperf inference benchmark. In *2020 ACM/IEEE 47th Annual International Symposium on Computer Architecture (ISCA)*, pp. 446–459. IEEE, 2020.
- Reimers, N. and Gurevych, I. Reporting score distributions makes a difference: Performance study of LSTM-networks for sequence tagging. In *Proceedings of the 2017 Conference on Empirical Methods in Natural Language Processing*, pp. 338–348, Copenhagen, Denmark, September 2017. Association for Computational Linguistics. doi: 10.18653/v1/D17-1035. URL <https://www.aclweb.org/anthology/D17-1035>.
- Riezler, S. and Maxwell, J. T. On some pitfalls in automatic evaluation and significance testing for mt. In *Proceedings of the ACL Workshop on Intrinsic and Extrinsic Evaluation Measures for Machine Translation and/or Summarization*, pp. 57–64, 2005.
- Simonyan, K. and Zisserman, A. Very deep convolutional networks for large-scale image recognition. *arXiv preprint arXiv:1409.1556*, 2014.
- Socher, R., Perelygin, A., Wu, J., Chuang, J., Manning, C. D., Ng, A., and Potts, C. Recursive deep models for semantic compositionality over a sentiment treebank. In *Proceedings of EMNLP*, pp. 1631–1642, 2013.
- Taylor Berg-Kirkpatrick, D. B. and Klein, D. An empirical investigation of statistical significance in nlp. In *Proceedings of the 2012 Joint Conference on Empirical Methods in Natural Language Processing and Computational Natural Language Learning*, pp. 995–1005. Association for Computational Linguistics, 2012.
- Torralba, A., Fergus, R., and Freeman, W. T. 80 million tiny images: A large data set for nonparametric object and scene recognition. *IEEE transactions on pattern analysis and machine intelligence*, 30(11):1958–1970, 2008.
- Vaswani, A., Shazeer, N., Parmar, N., Uszkoreit, J., Jones, L., Gomez, A. N., Kaiser, L., and Polosukhin, I. Attention is all you need, 2017.
- Vita, R., Mahajan, S., Overton, J. A., Dhanda, S. K., Martini, S., Cantrell, J. R., Wheeler, D. K., Sette, A., and Peters, B. The immune epitope database (iedb): 2018 update. *Nucleic acids research*, 47(D1):D339–D343, 2019.
- Wang, A., Singh, A., Michael, J., Hill, F., Levy, O., and Bowman, S. R. GLUE: A multi-task benchmark and analysis platform for natural language understanding. 2019. In the Proceedings of ICLR.
- Wolf, T., Debut, L., Sanh, V., Chaumond, J., Delangue, C., Moi, A., Cistac, P., Rault, T., Louf, R., Funtowicz, M., and Brew, J. Huggingface’s transformers: State-of-the-art natural language processing. *ArXiv*, abs/1910.03771, 2019.
- Xie, Q., Hovy, E., Luong, M.-T., and Le, Q. V. Self-training with noisy student improves imagenet classification. *arXiv preprint arXiv:1911.04252*, 2019.

A NOTES ON REPRODUCIBILITY

Ensuring full reproducibility is often a tedious work. We provide here notes and remarks on the issues we encountered while working towards fully reproducible experiments.

The testing procedure To ensure proper study of the sources of variation it was necessary to control them close to perfection. For all tasks, we ran a pipeline of tests to ensure perfect reproducibility at execution and also at resumption. During the tests, each source of variation was varied with 5 different seeds, each executed 5 times. This ensured that the pipeline was reproducible for different seeds. Additionally, for each source of variation and for each seed, another training was executed but automatically interrupted after each epoch. The worker would then start the training of the next seed and iterate through the trainings for all seeds before resuming the first one. All these tests uncovered many bugs and typical reproducibility issues in machine learning. We report here some notes.

Computer architecture & drivers Although we did not measure the variance induced by different GPU architectures, we did observe that different GPU models would lead to different results. The CPU model had less impact on the Deep Learning tasks but the MLP-MHC task was sensitive to it. We therefore limited all tasks to specific computer architectures. We also observed issues when CUDA drivers were updated during preliminary experiments. We ensured all experiments were run using CUDA 10.2.

Software & seeds PyTorch versions lead to different results as well. We ran every Deep Learning experiments with PyTorch 1.2.0.

We implemented our data pipeline so that we could seed the iterators, the data augmentation objects and the splitting of the datasets. We had less control at the level of the models however. For PyTorch 1.2.0, the random number generator (RNG) must be seeded globally which makes it difficult to seed different parts separately. We seeded PyTorch’s global RNG for weight initialization at the beginning of the training process and then seeded PyTorch’s RNG for the dropout. Afterwards we checkpoint the RNG state so that we can restore the RNG states at resumption. We found that models with convolutional layers would not yield reproducible results unless we enabled `cuda.deterministic` and disabled `cuda.benchmark`.

We used the library RoBO (Klein et al., 2017) for our Bayesian Optimizer. There was no support for seeding, we therefore resorted to seeding the global seed of python and numpy random number generators. We needed again to keep track of the RNG states and checkpoint them so that we can resume the Bayesian Optimizer without harming the

reproducibility.

For one of our case study, image segmentation, we have been unable to make the learning pipeline perfectly reproducible. This is problematic because it prevents us from studying each source of variation in isolation. We thus trained our model with every seeds fixed across all 200 trainings and measured the variance we could not control. This is represented as the numerical noise in Figures 1 and F.2.

B OUR BOOTSTRAP PROCEDURE

Cross-validation with different k impacts the number of samples, it is not the case with not bootstrap. That means flexible sample sizes for statistical tests is hardly possible with cross-validation within affecting the training dataset sizes. (Hothorn et al., 2005) focuses on the dataset sampling as the most important source of variation and marginalize out all other sources by taking the average performance over multiple runs for a given dataset. This increases even more the computational cost of the statistical tests.

We probe the effect of data sampling with bootstrap, specifically by bootstrapping to generate training sets and measuring the out-of-bootstrap error, as introduced by Breiman (1996b) in the context of bagging and generalized by (Hothorn et al., 2005). For completeness, we formalize this use of the bootstrap to create training and test sets and how it can estimate the variance of performance measure due to data sampling on a finite dataset.

We assume we are seeking to generate sets of i.i.d. samples from true distribution \mathcal{D} . Ideally we would have access to \mathcal{D} and could sample our finite datasets independently from it.

$$S_b^t = \{(x_1, y_1), (x_2, y_2), \dots (x_n, y_n)\} \sim \mathcal{D} \quad (11)$$

Instead we have one dataset $S \sim \mathcal{D}^n$ of finite size n and need to sample independent datasets from it. A popular method in machine learning to estimate performance on a small dataset is cross-validation (Bouckaert & Frank, 2004; Dietterich, 1998). This method however underestimates variance because of correlations induced by the process. We instead favor bootstrapping (Efron, 1979) as used by (Hothorn et al., 2005) to simulate independent data sampling from the true distribution.

$$S_b^t = \{(x_1, y_1), (x_2, y_2), \dots (x_n, y_n)\} \sim S \quad (12)$$

Where $S_b^t \sim S$ represents sampling the b -th training set with replacement from the set S . We then turn to out-of-bootstrap to generate the held-out set. We use all remaining samples in $S \setminus S_b^t$ to sample S_b^o .

$$S_b^o = \{(x_1, y_1), (x_2, y_2), \dots (x_n, y_n)\} \sim S \setminus S_b^t \quad (13)$$

This procedure is represented as $(S^{tv}, S^o) \sim sp_{n,n'}(S)$ in the empirical average risk $\hat{R}_{\mathcal{P}}(S, n, n')$, end of Section ??.

Table 1. Computational infrastructure for CIFAR10-VGG11 experiments.

| Hardware/Software | Type/Version |
|-------------------|---|
| CPU | Intel(R) Xeon(R) Gold 6148 CPU @ 2.40GHz |
| GPU model | Tesla V100-SXM2-16GB |
| GPU driver | 440.33.01 |
| OS | CentOS 7.7.1908 Core |
| Python | 3.6.3 |
| PyTorch | 1.2.0 |
| CUDA | 10.2 |

C CASE STUDIES

C.1 CIFAR10 Image classification with VGG11

Task CIFAR10 (Krizhevsky et al., 2009) is a dataset of 60,000 32x32 color images selected from 80 million tiny images dataset (Torralba et al., 2008), divided in 10 balanced classes. The original split contains 50,000 images for training and 10,000 images for testing. We applied random cropping and random horizontal flipping data augmentations.

Bootstrapping The aggregation of all original training and testing samples are used for the bootstrap. To preserve the balance of the classes, we applied stratified bootstrap. For each class separately, we sampled with replacement 4,000 training samples, 1,000 for validation and 1,000 for testing. As for all tasks, we use out-of-bootstrap to ensure samples cannot be contained in more than one set.

Model We used VGG11 (Simonyan & Zisserman, 2014) with batch-normalization and no dropout. The weights are initialized with Glorot method based on a uniform distribution (Glorot & Bengio, 2010).

Search space for hyperparameters We focused on learning rate, weight decay, momentum and learning rate schedule. Batch-size was omitted to simplify the multi-model training on GPUs, so that memory usage was consistent and predictable across all hyperparameter settings. To ease the definition of the search space for the learning rate schedule, we used exponential decay instead of multi-step decay despite the wide use of the latter with similar tasks and models (Simonyan & Zisserman, 2014; Xie et al., 2019; Mahajan et al., 2018; Liu et al., 2018; He et al., 2016; 2015b). The former only require tuning of γ while the later requires additionally selecting number of steps. Search space for all experiments and default values used for the variance experiments are presented in Table 2.

Table 2. Search space and default values for the hyperparameters in CIFAR10-VGG11 experiments.

| Hyperparameters | Default | Space |
|-------------------------|---------|---------------------------|
| learning rate | 0.03 | $\log(0.001, 0.3)$ |
| weight decay | 0.002 | $\log(10^{-6}, 10^{-2})$ |
| momentum | 0.9 | $\text{lin}(0.5, 0.99)$ |
| γ of lr schedule | 0.97 | $\text{lin}(0.96, 0.999)$ |
| batch-size | 128 | - |

Table 3. Search space and default values for the hyperparameters in SST-2/RTE-BERT experiments.

| Hyperparameters | Default | Space |
|-----------------------|---------------|------------------------------|
| learning rate | $2 * 10^{-5}$ | $\log(10^{-5}, 10^{-4})$ |
| weight decay | 0.0 | $\log(10^{-4}, 2 * 10^{-3})$ |
| std for weights init. | 0.2 | $\log(0.01, 0.5)$ |
| β_1 | 0.9 | - |
| β_2 | 0.999 | - |
| dropout rate | 0.1 | - |
| batch size | 32 | - |

C.2 Glue-SST2 sentiment prediction with BERT

Task SST2 (Stanford Sentiment Treebank) (Socher et al., 2013) is a binary classification task included in GLUE (Wang et al., 2019). In this task, the input is a sentence from a collection of movie reviews, and the target is the associated sentiment (either positive or negative). The publicly available data contains around 68k entries.

Bootstrapping We maintained the same size ratio between train/validation (i.e., 0.013) when performing the bootstrapping analysis. We performed standard out-of-bootstrap without conserving class balance since the original dataset is not balanced and ratios between classes vary from training and validation set in the original splits. The variable ratios of classes across bootstrap samples generate additional variance in our results, but is representative of the effect of generating a dataset that is not perfectly balanced.

Model We used the BERT (Devlin et al., 2018) implementation provided by the Hugging Face (Wolf et al., 2019) repository. BERT is a Transformer (Vaswani et al., 2017) encoder pre-trained on the self-supervised Masked Language Model task (Devlin et al., 2018). We chose BERT given its importance and influence in the NLP literature. It is worthy to note that the pre-training phase of BERT is also affected by sources of variations. Nevertheless, we didn't investigate this phase given the amount of time (and resources) required to perform it. Instead, we always start from the (same) pre-trained model image provided by the Hugging Face (Wolf et al., 2019) repository. Indeed, the weight initialization was only applied to the final classifier. The initialization method used is standard Gaussian with

0.0 mean and standard deviation that depends on the related hyperparameter.

Search space of hyperparameters We ran a small-scale hyperparameter space exploration in order to select the hyperparameter search space to use in our experiments. As such, we decided to include the learning rate, weight decay and the standard deviation for the model parameter initialization (see Table 3). We fixed the dropout probability to the value of 0.1 as in the original BERT architecture. For the same reason, we fixed $\beta_1 = 0.9$ and $\beta_2 = 0.999$. Default values used for the variance experiments are also reported in Table 3. The model has been fine-tuned on SST2 for 3 epochs, with a batch size of 32. Training has been performed with mixed precision. Note that for weight decay we used the default value from the Hugging Face repository (i.e., 0.0) even if this is outside of the hyperparameter search space. We confirmed that this makes no difference by looking at the results of the small-scale hyperparameter space exploration.

C.3 Glue-RTE entailment prediction with BERT

Task RTE (Recognizing Textual Entailment) (Bentivogli et al., 2009) is also a binary classification task included in GLUE (Wang et al., 2019). The task is a collection of text fragment pairs, and the target is to predict if the first text fragment entails the second one. RTE dataset only contains around 2.5k entries.

Bootstrapping In our bootstrapping analysis we maintained the train/validation ratio of 0.1. As for Glue-SST2, we used standard out-of-bootstrap and did not preserve original class ratios.

Model & search space of hyperparameters We used the BERT (Devlin et al., 2018) model for RTE as well, trained in the same way specified in the SST-2 section. In particular, we used the same hyperparameters (see Table 3), same batch size, and we trained in the same mixed-precision environment. The model has been fine-tuned on RTE for 3 epochs.

C.4 PascalVOC image segmentation with ResNet Backbone

Task The PascalVOC segmentation task (Everingham et al.) entails generating pixel-level segmentations to classify each pixel in an image as one of 20 classes or background. This publicly available dataset contains 2913 images and associated ground truth segmentation labels. The original splits contains 2184 images for training and 729 for validation. Images were normalized and zero-padded to a final size of 512x512.

Table 4. Computational infrastructure for PASCAL VOC experiments.

| Hardware/Software | Type/Version |
|-------------------|---|
| CPU | Intel(R) Xeon(R) Silver 4216 CPU @ 2.1GHz |
| GPU model | Tesla V100 Volta 32G |
| GPU driver | 440.33.01 |
| OS | CentOS 7.7.1908 Core |
| Python | 3.6.3 |
| PyTorch | 1.2.0 |
| CUDA | 10.2 |

Table 5. Search spaces for PASCAL VOC image segmentation.

| Hyperparameters | Default | Space |
|-----------------|----------|--------------------------|
| learning rate | 0.002 | $\log(10^{-5}, 10^{-2})$ |
| momentum | 0.9 | $\text{lin}(0.50, 0.99)$ |
| weight decay | 0.000001 | $\log(10^{-8}, 10^{-1})$ |
| batch-size | 16 | - |

Bootstrapping We used a train/validation ratio of 0.25 for our bootstrap analysis, generating training sets of 2184 images, validation and test sets of 729 images each. Since multiple classes can appear in a single image, the original dataset was not balanced, we thus used standard out-of-bootstrap for our experiments.

Model We used an FCN-16s (Long et al., 2014) with a ResNet18 backbone (He et al., 2015a) pretrained on ImageNet (Deng et al., 2009). After exploring several possible backbones, ResNet18 was selected since it could be trained relatively quickly. We use weighted cross entropy, with only predictions within the original image boundary contributing to the loss. The model is optimized using SGD with momentum.

Metric The metric used is the mean Intersection over Union (mIoU) of the twenty classes and the background class. The complement of the mIoU, the mean Jaccard Distance, is the metric minimized in all HPO experiments.

Search space of hyperparameters Certain hyperparameters, such as the number of kernels, or the total number of layers, are part of the definition of the ResNet18 architecture. As a result, we explored key optimization hyperparameters including: learning rate, momentum, and weight decay. The hyperparameter ranges selected, as well as the default hyperparameters used in the variance experiments, can be found in table 5 and in table ??, respectively. A batch size of 16 was used for all experiments.

Table 6. Search spaces for the different hyperparameters for the MLP-MHC task

| Hyperparameters | Default | Space |
|-------------------|-------------------|---------------|
| hidden layer size | | lin(20, 400) |
| L2-weight decay | | log(0, 1) |
| # HPs | Hyperparameters | Default Value |
| 1 | hidden layer size | 150 |
| 2 | L2-weight decay | 0.001 |

Table 7. Defaults for MLP-MHC task.

C.5 Major histocompatibility class I-associated peptide binding prediction with shallow MLP

Task The MLP-MHC is a regression task with the goal of predicting the relative binding affinity for a given peptide and major histocompatibility complex class I (MHC) allele pair. The major histocompatibility complex (MHC) class I proteins are present on the surface of most nucleated cells in jawed vertebrates (Pearson et al., 2016). These proteins bind short peptides that arise from the degradation of intracellular proteins (Pearson et al., 2016). The complex of peptide-MHC molecule is used by immune cells to recognize healthy cells and eliminate cancerous or infected cells, a mechanism studied in the development of immunotherapy and vaccines (O’Donnell et al., 2018). The peptide binding prediction task is therefore at the base of the search for good vaccine and immunotherapy targets (O’Donnell et al., 2018; Jurtz et al., 2017).

The input data is the concatenated pairs of sequences: the MHC allele and the peptide sequence. For the MHC alleles, we restricted the sequences to the binding pocket of the peptide, as seen in (Jurtz et al., 2017). The prediction target is a normalized binding affinity score, as described in (Jurtz et al., 2017; O’Donnell et al., 2018).

Datasets and sequence encoding While both *MHCflurry* and *NetMHCpan4* models use a BLOSUM62 encoding (Henikoff & Henikoff, 1992) for the amino acids, in we chose to instead encode the amino acids as one-hot as described in (Nielsen et al., 2007).

The *NetMHCpan4* model is trained on a manually filtered dataset from the immune epitope database (Vita et al., 2019; Jurtz et al., 2017) that has been split into five folds used for cross-validation, available on the author’s website (Jurtz et al., 2017).

In contrast, the *MHCflurry* model is trained on a custom multi-source dataset (available from Mendeley data and the (O’Donnell et al., 2018) publication cite) and validated/tested on two external datasets from (Pearson et al., 2016) and an HPV peptide dataset available at the same

Table 8. Comparison of performance on datasets

| Model name | Dataset | AUC | PCC |
|------------|------------------|--------|--------|
| NetMHCpan4 | HPV | 0.53 | 0.39 |
| MHCflurry | HPV | 0.58 | 0.41 |
| MLP-MHC | HPV | 0.63 | 0.31 |
| NetMHCpan4 | NetMHC-CV splits | 0.854 | 0.620 |
| MHCflurry | NetMHC-CV splits | 0.964* | 0.671* |
| MLP-MHC | NetMHC-CV splits | 0.861 | 0.660 |

website as above.

Bootstrapping We have three different sets for training, validating and testing. We thus performed bootstrapping separately on each set for every training and evaluation.

Model The model is a shallow MLP with one hidden layer from *sklearn*. We used the default setting for the non-linearity *relu* and weight initialization strategy ((Glorot & Bengio, 2010)). The following table (Table 9) offers some comparison points between our model and the *NetMHCpan4* (Jurtz et al., 2017) and *MHCflurry* (O’Donnell et al., 2018) models.

While the *MHCflurry* model (O’Donnell et al., 2018) train only on the peptide sequences and uses ensembling to perform its predictions, training multiple models for each MHC allele, the *NetMHCpan4* model (Jurtz et al., 2017) uses the allele sequence as input and trains one single model.

We chose to retain the strategy proposed by the *NetMHCpan4* model, where a single model is trained for all alleles (Jurtz et al., 2017). As a reference, *MHCflurry* uses ensembling to perform predictions; indeed, the authors report that for each MHC allele, an ensemble of 8-16 are selected from the 320 that were trained (O’Donnell et al., 2018).

Search space of hyperparameters For the hyperparameter search, we selected hidden layer sizes between 20 and 400 (Table 6), to engulf a range slightly larger than the ones described by both (Jurtz et al., 2017; O’Donnell et al., 2018). The second hyperparameter that was explored was the L2 regularisation parameter, for which a log-uniform range between 0 and 1 was explored.

Comparison of performance We would like to state the goal of the present study was not to establish new state of the art (SOTA) on the MHC-peptide binding prediction task. However, we still report that when comparing the performance of our model to those of *NetMHCpan4* and *MHCflurry* we found the performance of our model comparable. Briefly, for the results in Table 9, we used the existing pre-trained *NetMHCpan4* and *MHCflurry* tools to predict the binding affinity of both datasets: the previously

Table 9. Comparison of models for the MLP-MHC task

| Model name | Inputs | Model design | Dataset | Sequence encoding |
|------------|----------------|--------------------------|------------------------------------|-------------------|
| NetMHCpan4 | allele+peptide | shallow MLP | custom CV split(Vita et al., 2019) | BLOSUM62 |
| MHCflurry | peptide | ensemble of shallow MLPs | (O’Donnell et al., 2018) | BLOSUM62 |
| MLP-MHC | allele+peptide | shallow MLP | same as (O’Donnell et al., 2018) | Sparse |

Table 10. Computational infrastructure for MLP-MHC experiments.

| Hardware/Software | Type/Version |
|-------------------|--|
| CPU | Intel(R) Xeon(R) CPU E5-2640 v4 320 CPU @ 2.40GHz |
| OS | CentOS 7.7.1908 Core |
| Python | 3.6.8 |
| sklearn | 0.22.2.post1 |
| BLAS | 3.4.2 |

described HPV external test data (HPV) from (O’Donnell et al., 2018) and the cross-validation test datasets from (Jurtz et al., 2017) (NetMHC-CV splits).

We would like to point out that since the *MHCflurry* model was published later than the *NetMHCpan4* one, there is a high chance that the dataset from the cross-validation splits (NetMHC-CV splits) may be contained in the dataset used to train the existing *MHCflurry* tool. The proper way to compare performances would be to re-train the *MHCflurry* model on each fold and test subsequently its performance; however, since our goal is not to reach new SOTA on this task, we leave this experiment to be performed at a later time.

This would result in a likely overestimation of the performance of *MHCflurry* on this dataset, which we noted with the * sign in Table 9.

A more in-depth study is necessary to compare in a more thorough way this performance with respect to the differences in model design, dataset encoding and other factors.

D HYPERPARAMETER OPTIMIZATION ALGORITHMS

D.1 Grid Search

Let a_i , b_i and n be the hyperparameters of the grid search, where a_i and b_i are vectors of minima and maxima for each dimension of the search space, and n is the number of values per dimension. We define Δ_i as the interval between each value on dimension i . A point on the grid is defined by $p_{ij} = a_i + \Delta_i(j - 1)$. Grid search is simply the evaluation of $r(\lambda)$ from Equation 2 on all possible combinations of values p_{ij} .

D.2 Noisy Grid Search

Grid search is a fully deterministic algorithm. Yet, it is highly sensitive to the design of the grid. To provide a variance estimate of similar choices of the grid and to be able to distinguish lucky grid, we consider a noisy version of grid search.

For the noisy grid search, we replace a_i by $\tilde{a}_i \sim U(a_i - \frac{\Delta_i}{2}, a_i + \frac{\Delta_i}{2})$ and similarly for b_i . $\tilde{\Delta}_i$ and \tilde{p}_{ij} then follows from \tilde{a}_i and \tilde{b}_i . In expectation, noisy grid search will cover the same grid as grid search, as proven below.

$$\begin{aligned}
\mathbb{E}[\tilde{p}_{ij}] &= \mathbb{E}[\tilde{a}_i + \tilde{\Delta}_i(j - 1)] \\
&= \mathbb{E}\left[\tilde{a}_i + \frac{\tilde{b} - \tilde{a}}{n - 1}(j - 1)\right] \\
&= \mathbb{E}[\tilde{a}_i] + \mathbb{E}\left[\frac{\tilde{b}}{n - 1}\right](j - 1) - \mathbb{E}\left[\frac{\tilde{a}}{n - 1}\right](j - 1) \\
&= a_i + \frac{b}{n - 1}(j - 1) - \frac{a}{n - 1}(j - 1) \\
&= a_i + \frac{b - a}{n - 1}(j - 1) \\
&= a_i + \Delta_i(j - 1) = p_{ij}
\end{aligned}$$

This provides us a variance estimate of grid search that we can compare against non-deterministic hyperparameter optimization algorithms.

D.3 Random Search

The search space of random search will be increased by $\pm \frac{\Delta_i}{2}$ as defined for the noisy grid search to ensure that they both cover the same search space. For all hyperparameters, the values are sampled from a uniform $p_i \sim U(a_i - \frac{\Delta_i}{2}, b_i + \frac{\Delta_i}{2})$. For learning rate and weight decay, values are sampled uniformly in the logarithmic space.

E HYPERPARAMETER OPTIMIZATION RESULTS

Figure E.1 presents the optimization curves of the hyperparameter optimization executions in Section 2.2.

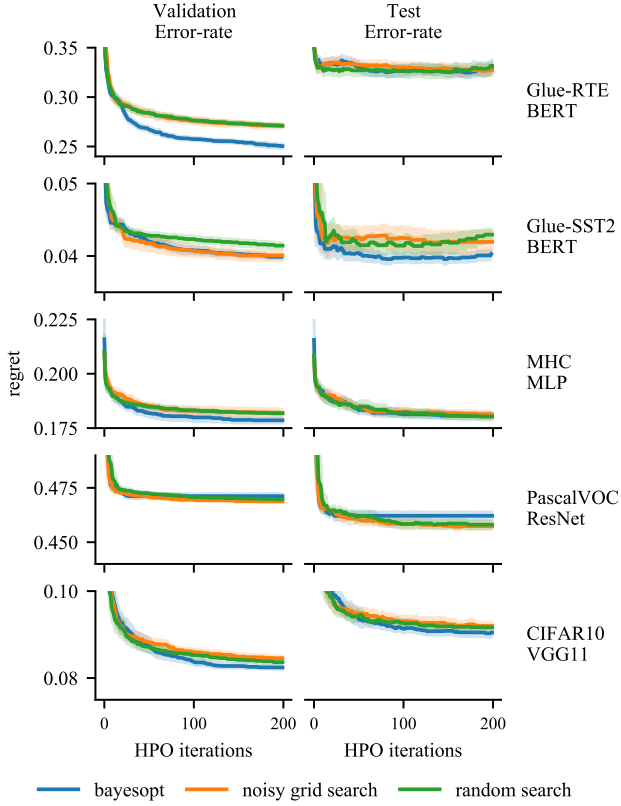


Figure E.1. Optimization curves of hyperparameter optimization executions Each row presents the result for a different task. Left column are results on validation set, the one hyperparameters were optimized on. Right column are results on the test sets. Hyperparameter optimization methods are Bayesian Optimization, Noisy Grid Search (See Section D.2), and Random Search. The y-axis are the best objectives found until an iteration i , on a different scale for each task. Left and right plots share the same scale on y-axis, so that we can easily observe whether validation error-rate corresponds to test error-rate. The bold lines are averages and the size of lighter colored areas represents the standard deviations. They are computed based on 20 independent executions for each algorithm, during which only the seed of the hyperparameter optimization is randomized. For more details on the experiments see Section 2.2. Two striking results emerge from these graphs. 1) The typical search spaces are well optimized by all algorithms, and in some cases there is even signs of slight over-fitting (on BERT tasks). 2) The standard deviation stabilizes early, before 50 iterations in most cases. These results suggests that larger budgets for hyperparameter optimization would not reduce the variability of the results in similar search spaces. This is likely not the case however for more complex search spaces such as those observed in the neural architecture search literature.

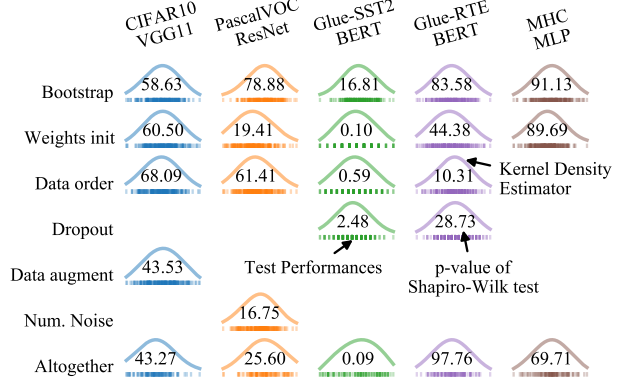


Figure F.2. Performance distributions conditional to different sources of variations. Each row is a different source of variation. For each source, all other sources are kept fix when training and evaluating models. The last row presents the distributions when all the sources of variation are randomized altogether. Each column is the results for the different tasks. We can see that except for Glue-SST2 BERT, all case studies have distributions of performances very close to normal. In the case of Glue-SST2 BERT, we note that the size of the test set is so small that it discretizes the possible performances. The distribution is nevertheless roughly symmetrical and thus amenable to many statistical tests.

F NORMALITY OF PERFORMANCE DISTRIBUTIONS IN THE CASE STUDIES

Figure F.2 presents the Shapiro-Wilk test of normality on all our results on sources of variations.

G RANDOMIZING MORE SOURCES OF VARIANCE INCREASE THE QUALITY OF THE ESTIMATOR

Figure 5 only presented the Glue-RTE and CIFAR10 tasks. We provide here a complete picture of the standard deviation of the different estimators in Figure G.3. We further present a decomposition of the mean-squared-error in Figure G.4 to help understand why accounting for more sources of variations improves the mean-squared-error of the biased estimators.

H ANALYSIS OF ROBUSTNESS OF COMPARISON METHODS

In addition to simulations described in Section 4.2, we executed experiments in which we varied the sample size and the threshold γ . To select the threshold of the average, we converted γ into the equivalent performance difference ($\delta = \Phi^{-1}(\gamma)\sigma$). Results are presented in Figure H.5

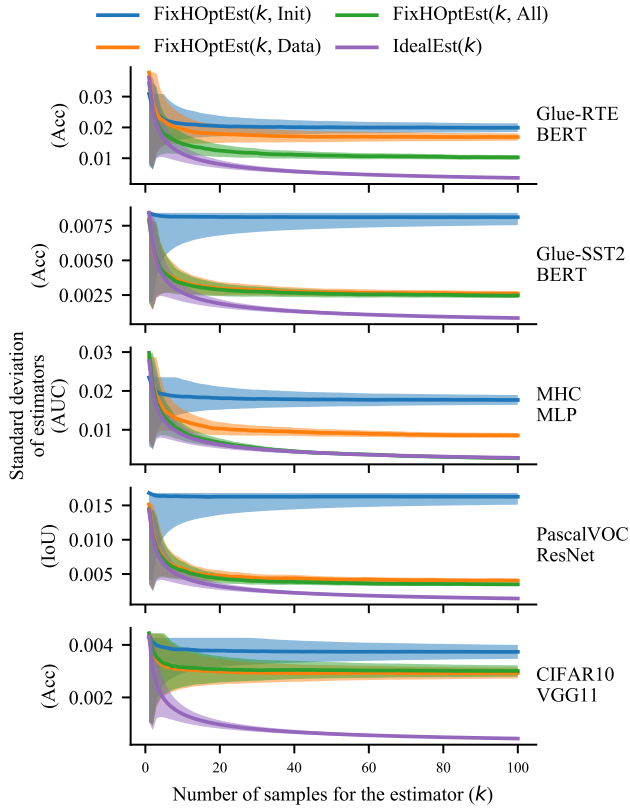


Figure G.3. Standard error of biased and ideal estimators with k samples. Each plot represents the standard error of the different tasks described in Section 2.2. On x axis, the number of samples used by the estimators to compute the average performance. On y axis, the standard deviation of the estimations, in terms of task objective; Classification accuracy (Acc), Intersection over Union (IoU), Area Under the Curve (AUC). Uncertainty represented in light color is computed analytically as the approximate standard deviation of the standard deviation of a normal distribution computed on k samples. For all case studies, **accounting for more sources of variation reduces or keeps constant the standard error of $\hat{\mu}_{(k)}$** . In all case studies, only accounting for weights initialization, $\text{FixHOptEst}(k, \text{Init})$, is by far the worst estimator. Comparatively, $\text{FixHOptEst}(k, \text{All})$ provides a systematic improvement towards $\text{IdealEst}(k)$ for no additional computational cost compared to $\text{FixHOptEst}(k, \text{Init})$. **Ignoring variance from HOpt is harmful for a good estimation of $\hat{R}_{\mathcal{P}}$** . The MHC task with MLP is the only one for which $\text{FixHOptEst}(k, \text{All})$ matches $\text{IdealEst}(k, \text{All})$. We suspect this may be explained by the relatively small standard deviation due to hyperparameter optimization observed in Figure 1. $\text{FixHOptEst}(k, \text{All})$ would have thus captured most of the variability in the learning pipeline.

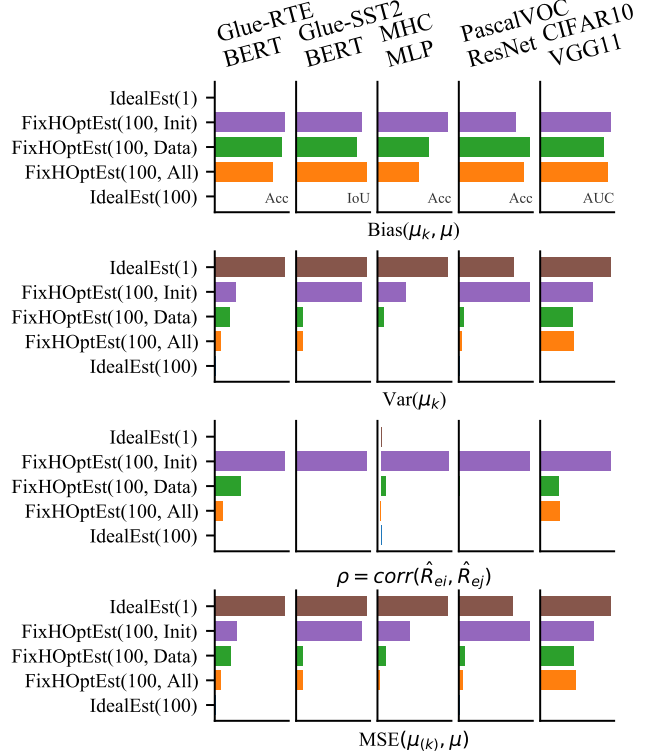


Figure G.4. Decomposition of the Mean-Squared-Error for different estimators of $\hat{R}_{\mathcal{P}}$. On each sub-figure from top to bottom, 1) bias between the estimator and the expected empirical risk $\text{Bias}(\mu_{(k)}, \mu)$, 2) variance of the estimator $\text{Var}(\mu_{(k)})$, 3) correlation between performances measures \hat{R}_e as presented in Equation 7 and 4) the mean-squared-error of the estimator $\text{MSE}(\mu_{(k)}, \mu)$. For each sub-figure, each row is a different estimator, with $\text{IdealEst}(k=1)$ as a comparison point. The experimental procedure to compute these statistics are described in section subsection 3.3. Without any surprise the $\text{IdealEst}(100, \text{All})$ minimizes the mean-squared-error so well that it looks close to 0 on the figure compared to the other estimators. Among the other estimators, the mean-squared-error is reduced most significantly by $\text{FixedHOptEst}(100, \text{All})$ on all tasks. If we look at the decomposition of the mean-squared-error, i.e., the bias and the variance, we see on first sub-figure that the bias is stable across all biased estimators on all tasks, while on second sub-figure the variance varies widely. It is thus the reduced variance of the biased estimators that leads to improved mean-squared-error. This is a counter-intuitive result because the estimator with lowest variance are these accounting for more sources of variations. The intuition is thus that they should have more variance, not less. We derived the variance of the biased estimators in Equation 7 which highlighted that the correlation among performances \hat{R}_e can increase the variance of the biased estimators. We can see in the third sub-figure that this correlation drastically drops when accounting for more sources of variances. The mean-squared-error, in other words the quality of the estimators, is thus significantly improved by decorrelating the performance measures.

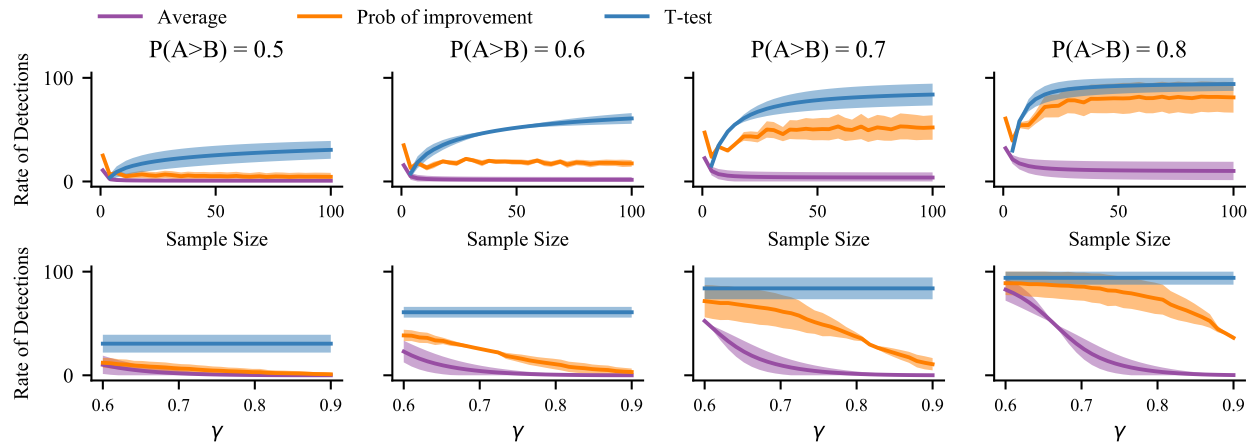


Figure H.5. Analysis of the robustness of comparison methods. On the first row, rate of detections of comparison methods in function of the sample size. On the second row, rate of detections of comparison methods in function of the threshold γ . Each column are simulations with different true simulated probability of a learning algorithm A to outperform another algorithm B across random fluctuations (ex: random data splits).