

Bike Rentals

Data Analysis

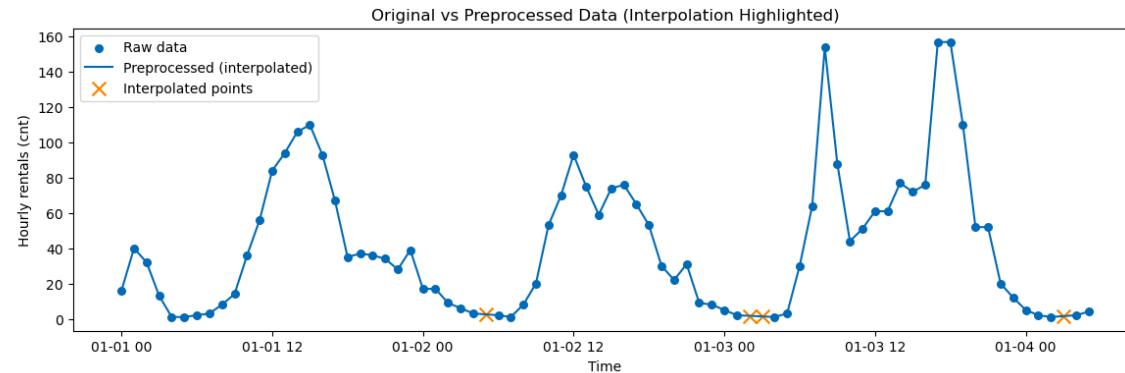
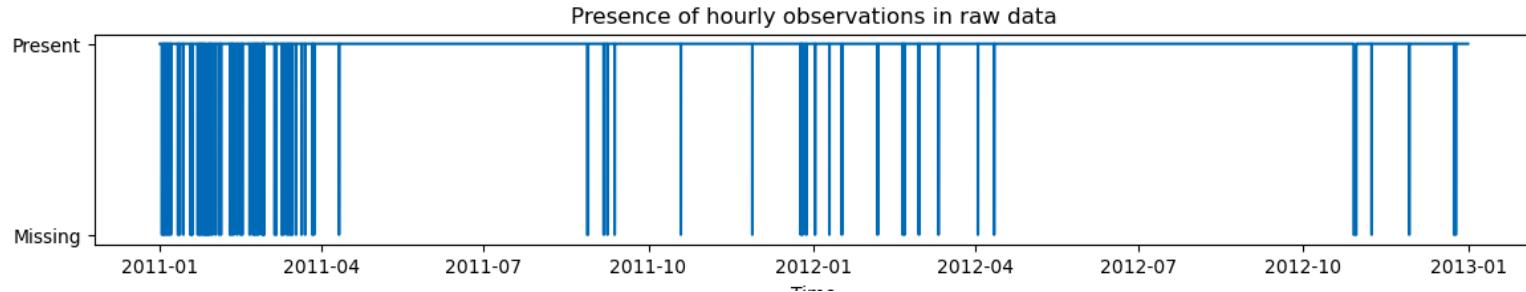
Current Catalysts:

Vikram Anand, Umer Farooq

Data Set

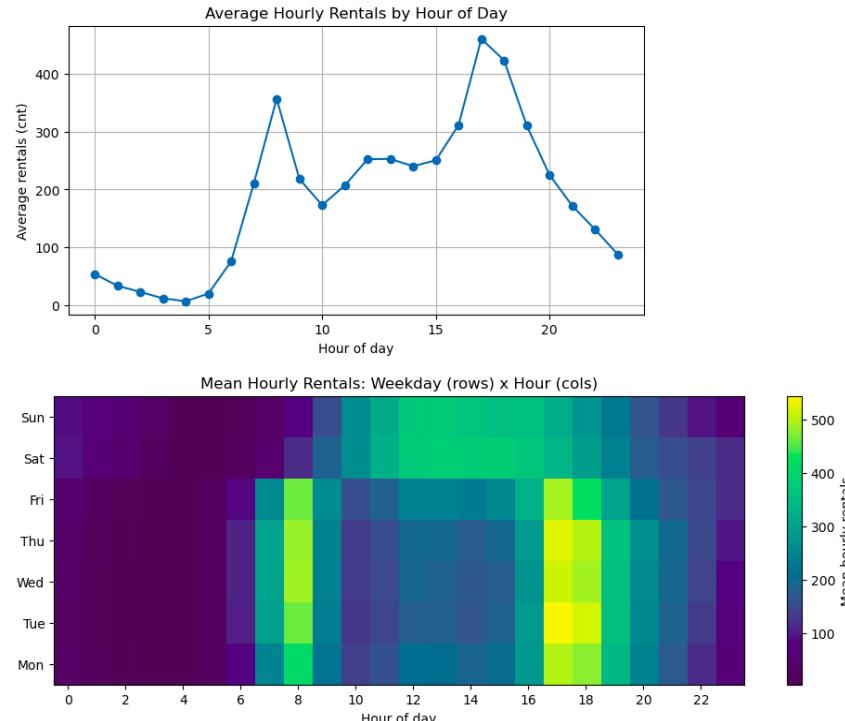
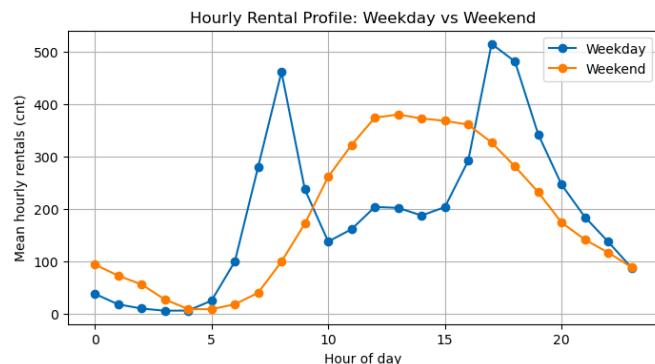
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7 26,2011-01-02,1,0,1,1,0,0,0,0,2,0.44,0.4394,0.94,0.2537,0,1,16,17
8 27,2011-01-02,1,0,1,2,0,0,0,0,2,0.42,0.4242,1,0,0.2836,0,1,8,9
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Missing Timestamps in Data and Interpolation

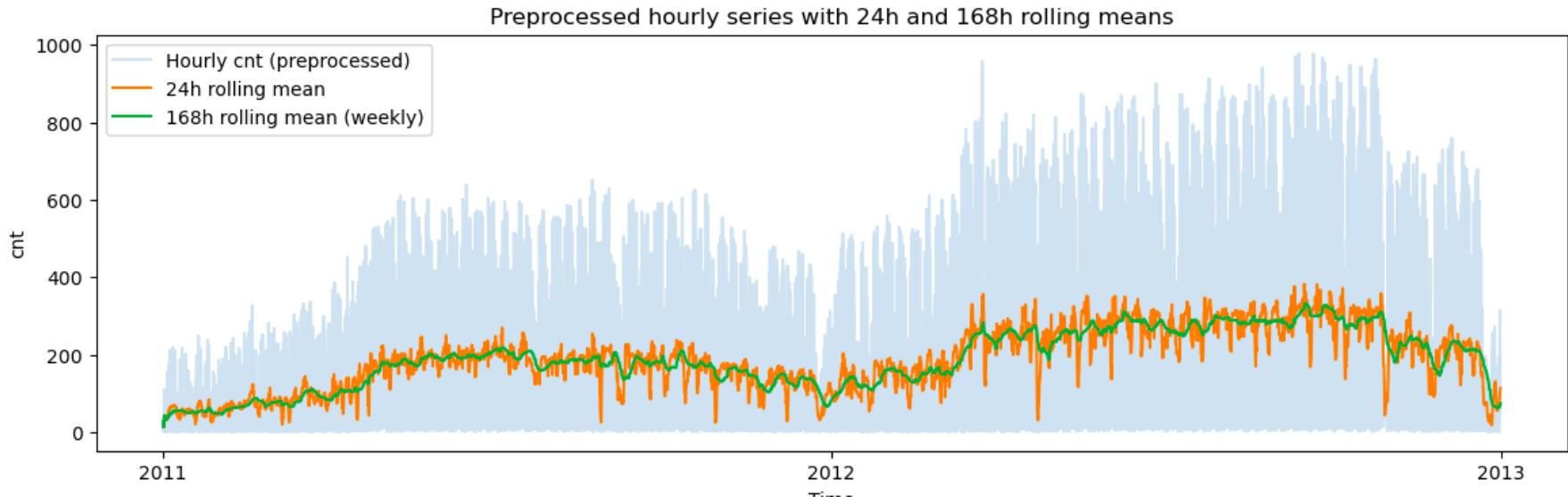


Mean Rentals of Bikes

- Peak in rentals is observed during weekdays at
 - Morning hour around 0800.
 - During evening around 1800.
- Peak rentals is observed during weekend.
 - Between 1000 hrs and 1600 hrs.

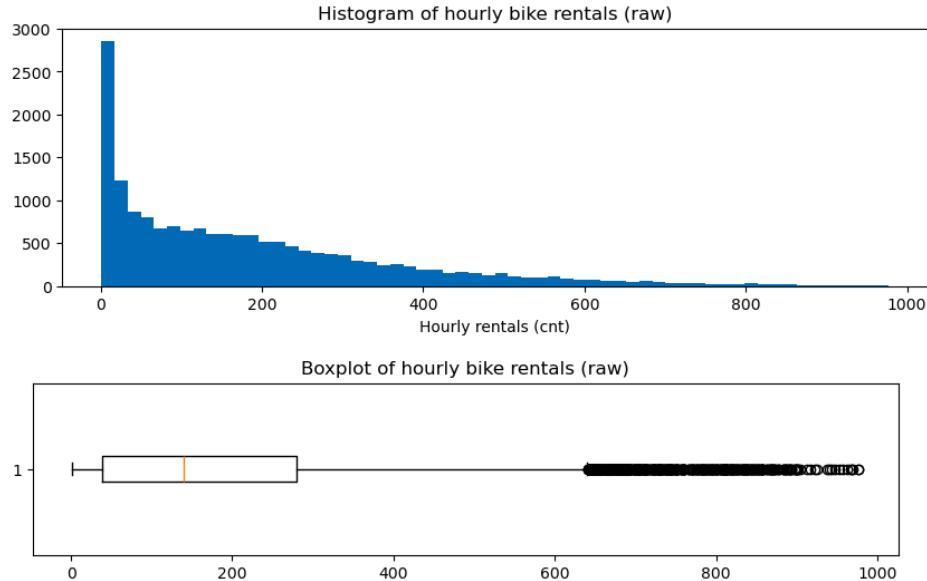


Preprocessing of data with 24h and 168h Rolling means



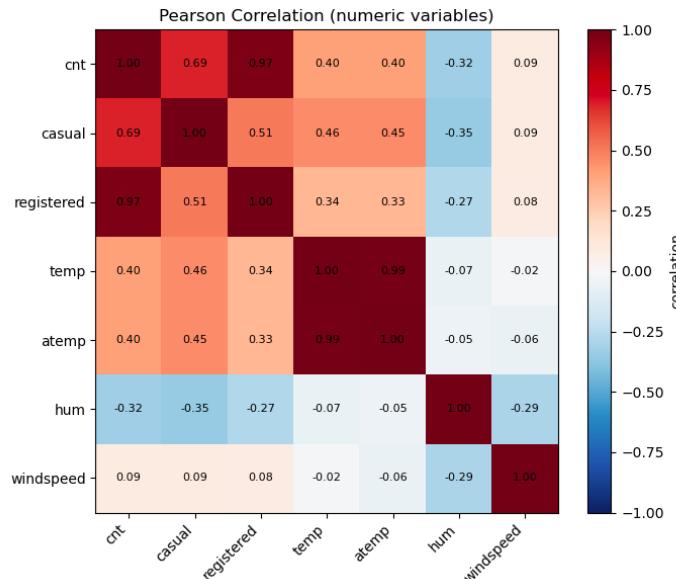
Histogram and Boxplot of Bike rentals.

- Most of the data points are centered around at 0.
- Large number of rentals are observed very less time.
- Median of data is at around 140.
- A lot of Data points are above the maximum limit of outliers.
 - These data points are still covered in the data and are not filtered.
 - We are interested in the large numbers of rentals in particular hours.

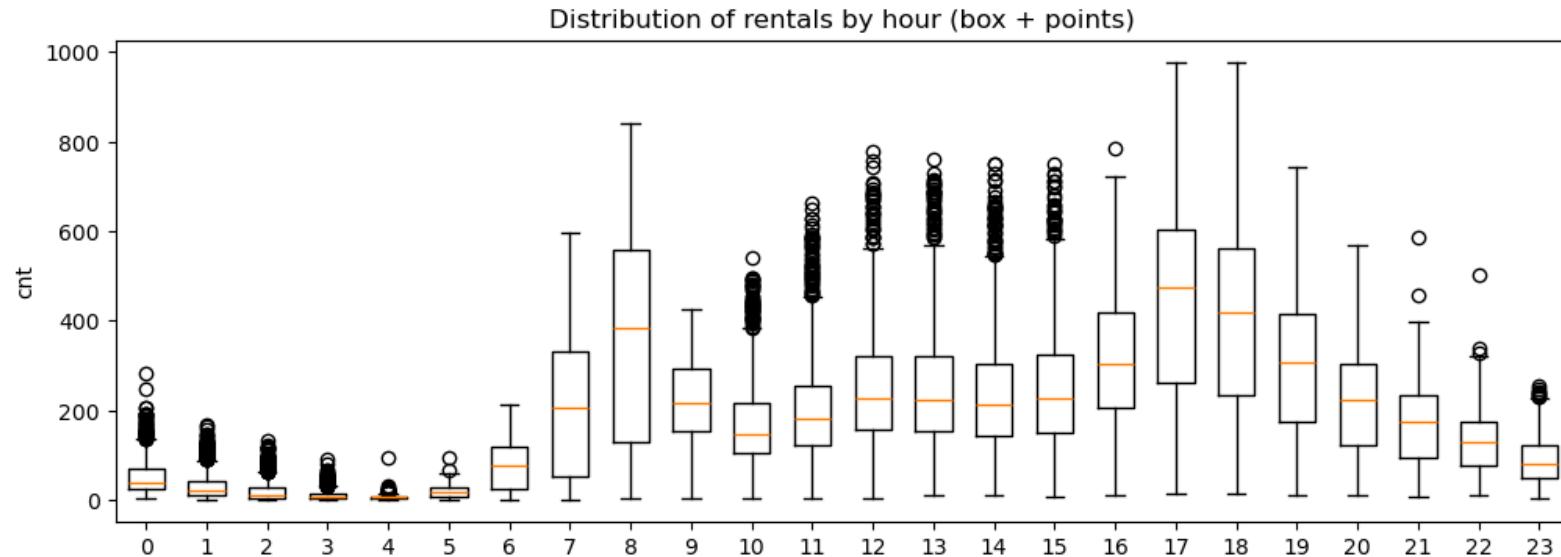


Pearson Correlation Matrix

- Pearson correlation matrix is used to observe the linear relationship between the number of hourly rentals and different parameters.
- Our only parameter of concern in temperature to analyze the data.
- We see that correlation appears to be 0.40 with the temperature which signifies a linear relationship between the hourly rentals and temperature.
 - If temperature increases (summers) the number of rentals are also increased.



Boxplot of rentals Per Day for Whole Data

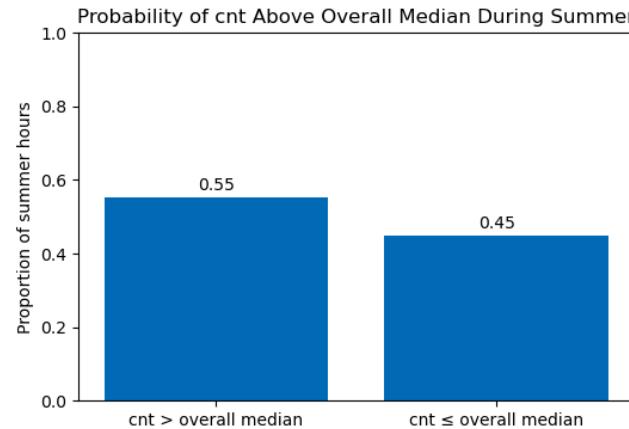


Probability of Rentals above overall median during Summers

- It is an Empirical probability
 - Because we are observing the real data and not the theoretical model.
 - Probability that rentals are above overall median given that it is summer.
 - Total number of hours in summer are 4409.
 - 2435 hrs the rentals are above overall median.
 - $P(\text{cnt} > \text{overall median} \mid \text{summer}) = 0.5523 \ (55.23\%)$

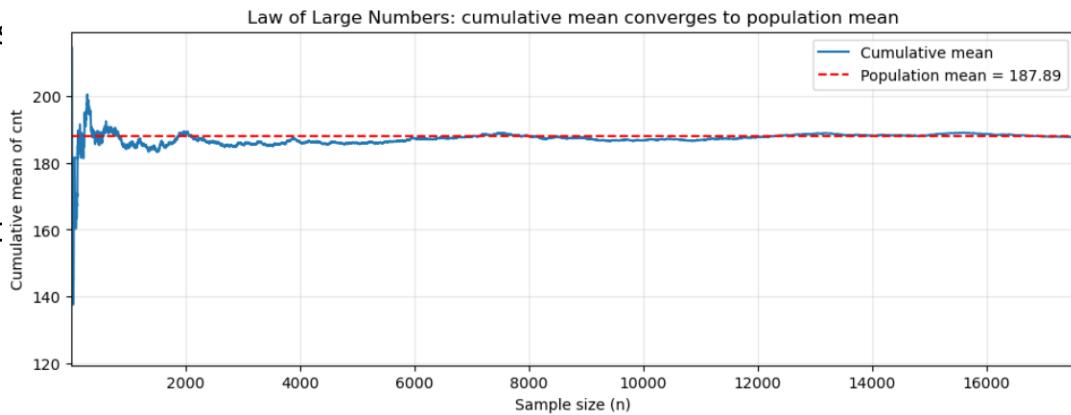
Overall median cnt = 140.0
Number of summer hours = 4409
Number of summer hours above overall median = 2435

Empirical probability:
 $P(\text{cnt} > \text{overall median} \mid \text{summer}) = 0.5523 \ (55.23\%)$



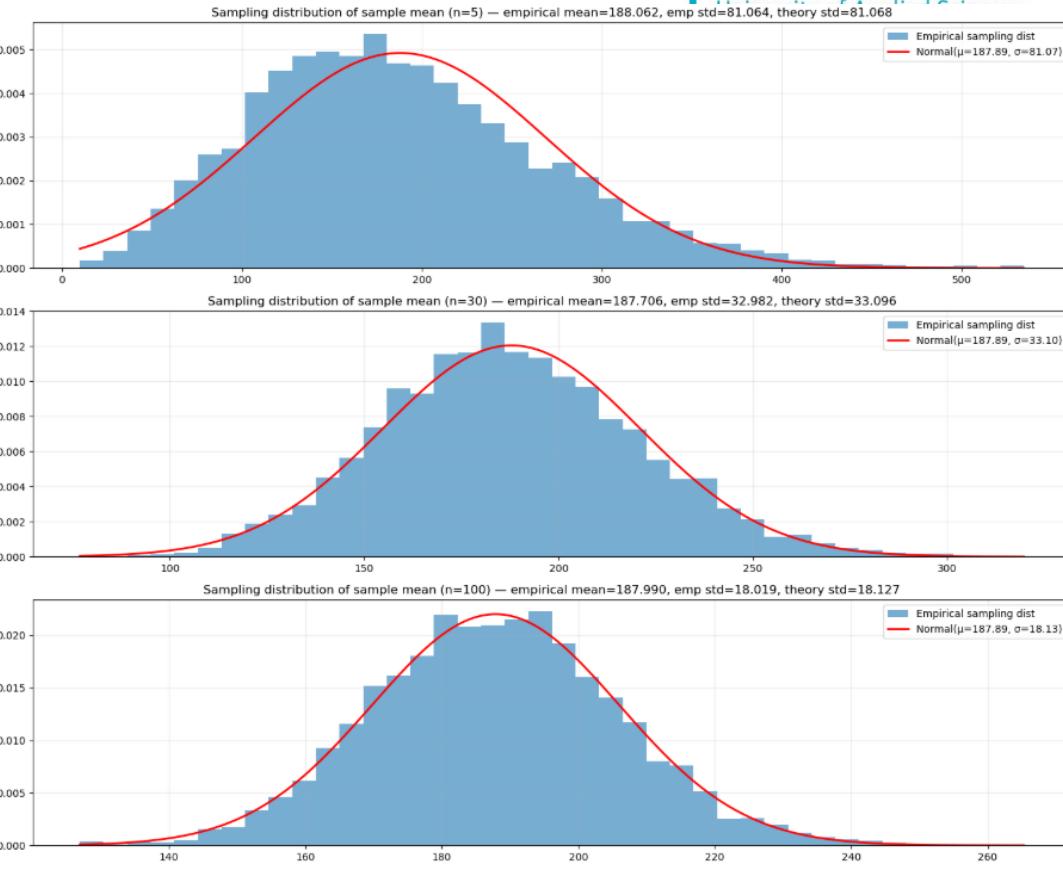
Law of Large Numbers

- As the number of observations increases, sample averages converge to the true population value.
- Cumulative probability of high-demand hours stabilizes as more hourly observations are included.
- Temporal dependence in hourly data slows convergence compared to independent samples but convergence is still observable.
- LLN justifies using long-term averages and empirical probabilities for stable demand estimation.



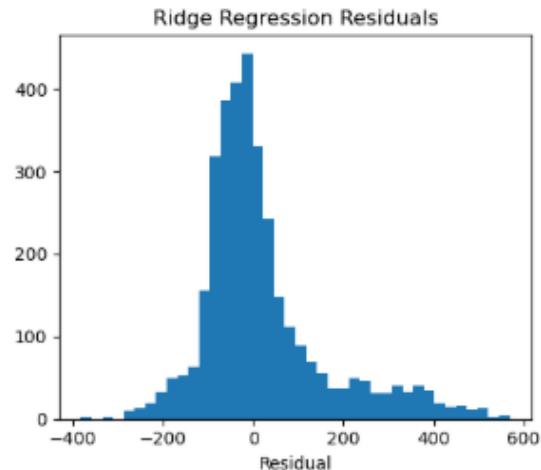
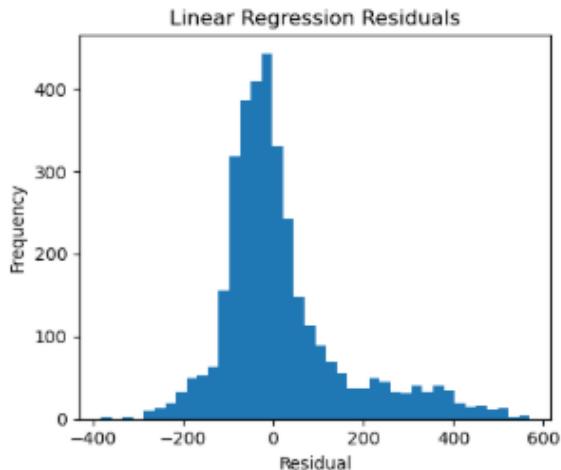
Central Limit Theorem

- The distribution of sample means approaches a normal distribution as sample size increases.
- Sampling distributions of mean hourly rentals become more symmetric and concentrated with larger sample sizes.
- Larger samples reduce variability of the sample mean, improving stability and reliability of estimates.



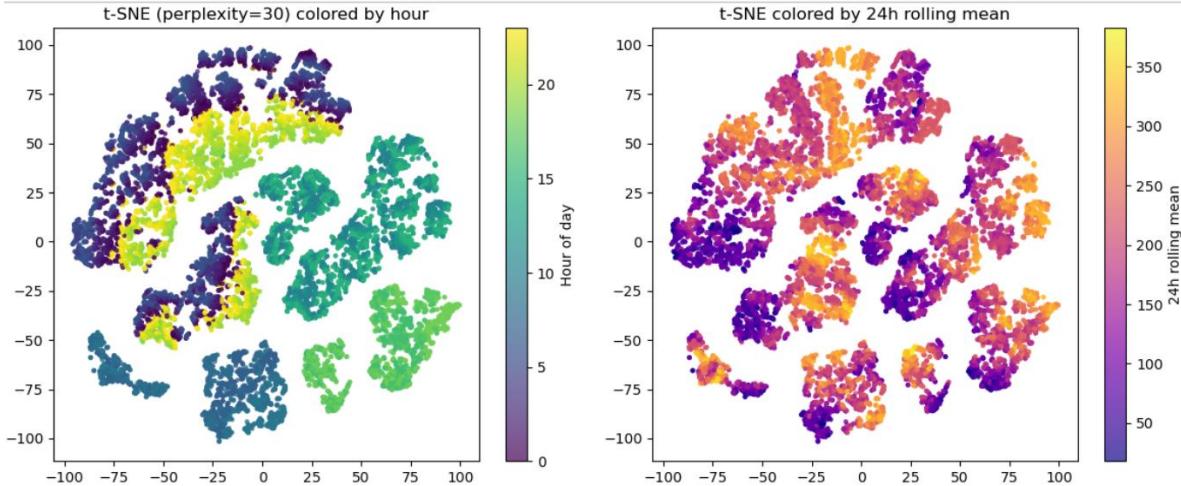
Residual Analysis

- Residuals are centered around zero, indicating no strong systematic bias.
- Most prediction errors are small, showing that the model performs well for typical demand level
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t-SNE

- The hour-of-day coloring transitions smoothly inside and across clusters, indicating that time of day is a major organizing factor.
- Each island groups hours with similar feature patterns.
- The rolling-mean coloring shows that clusters also separate by baseline demand intensity (low vs. high average usage)

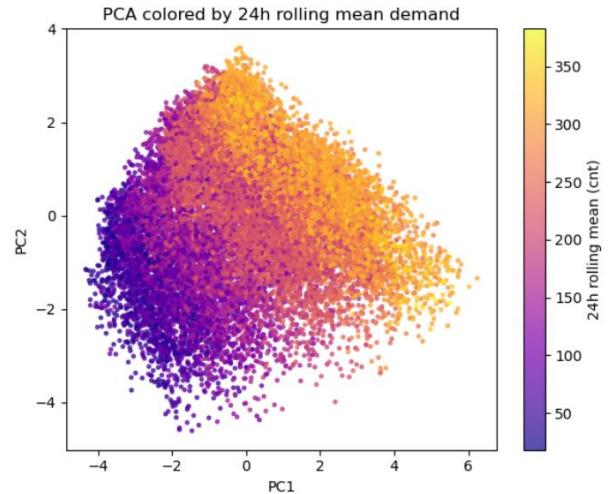
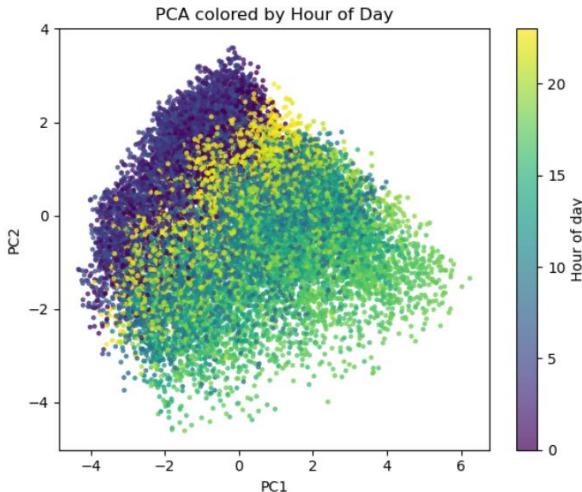


PC1 x PC2

PC plot shows the data projected onto the first two principal components, which capture the largest sources of variance in the dataset.

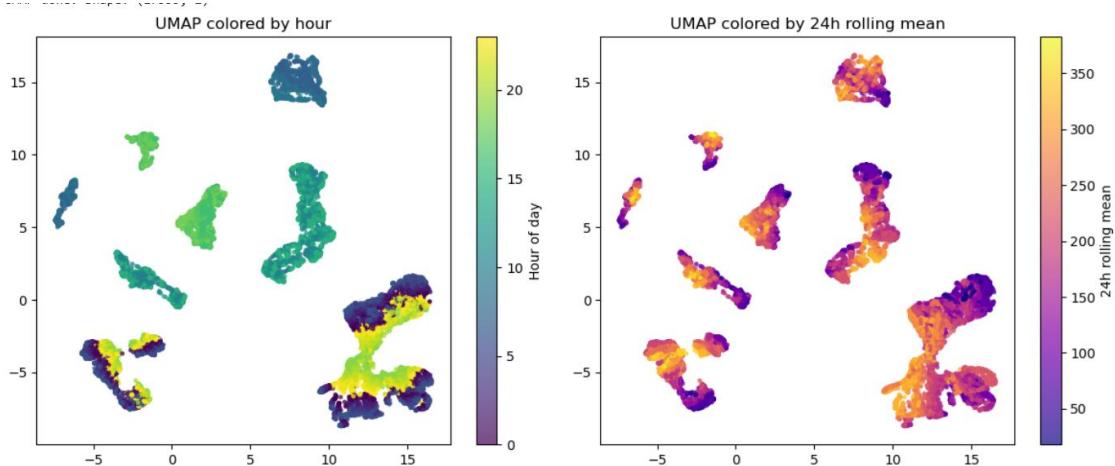
coloring by hour of day shows a smooth gradient, indicating that daily usage cycles are a major contributor to variance.

coloring by the 24-hour rolling mean demand shows an even clearer separation along PC1, suggesting that PC1 represents baseline demand intensity.



U-MAP

- UMAP produces clearer, more separated islands that preserve both local clusters and some global relationships
- UMAP produces distinct islands that correspond to groups of hours with similar features.
- Rolling-mean coloring clusters together regions of similar baseline demand — islands with warmer colors correspond to consistently higher-demand regimes



Q&A