

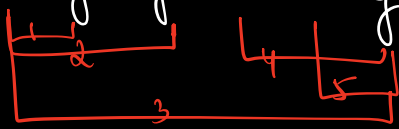
Q1. Given a char^[], calculate the no. of pairs $[i, j]$, such that $i < j$, && $s[i] == 'a'$, && $s[j] == 'g'$, all characters are lowercase alphabets $[a\ b\ c\ d\ \dots]$.


ex \Rightarrow arr \Rightarrow b a a g d c a g
 0 1 2 3 4 5 6 7

pair : $\langle 1, 3 \rangle$ $\langle 2, 3 \rangle$ $\langle 6, 7 \rangle$
 $\langle 1, 7 \rangle$ $\langle 2, 7 \rangle$

~~$\langle 3, 6 \rangle$~~ \rightarrow not valid.
 ↓ ↓
 g a

$Q_p = 5$.

ex \Rightarrow arr \Rightarrow b c a g g a a g

 $Q_p = 5$.

ex \Rightarrow arr \Rightarrow a c g d g a g

 $Q_p = 4$.

Bruteforce

** check for all possible pairs:-

c=0

for(i=0; i<N; i++) {

for(j=i+1; j<N; j++) {

if (arr[i] == 'a' &&
arr[j] == 'g')

c++

}

} print(c);



** If S[i] != 'a', then second loop is not required:-

c=0

for(i=0; i<N; i++) {

if(arr[i] == 'a') {

for(j=i+1; j<N; j++) {

if(arr[j] == 'g')

c++

}

}

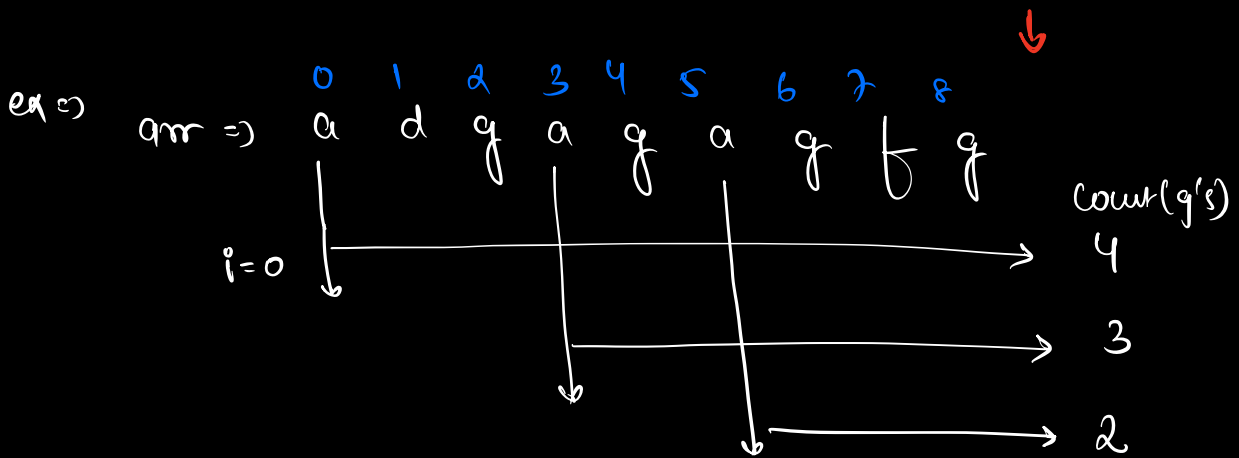
print(c);

TC $\Rightarrow O(N^2)$

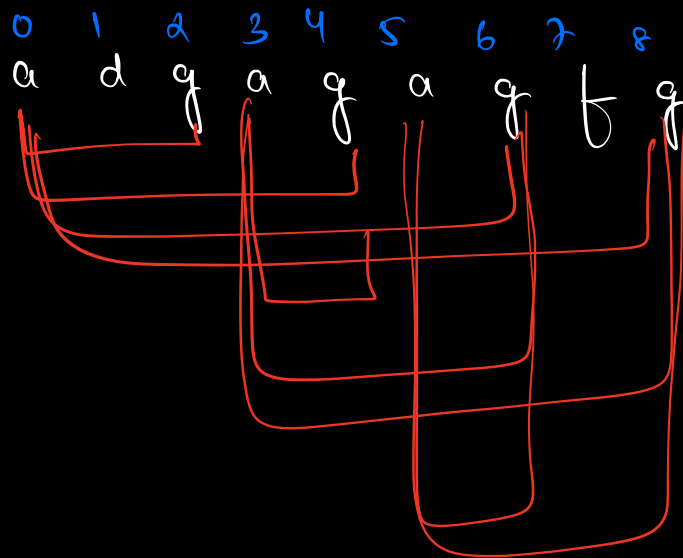
SC $\Rightarrow O(1)$

TC $\Rightarrow O(N^2)$

SC $\Rightarrow O(1)$



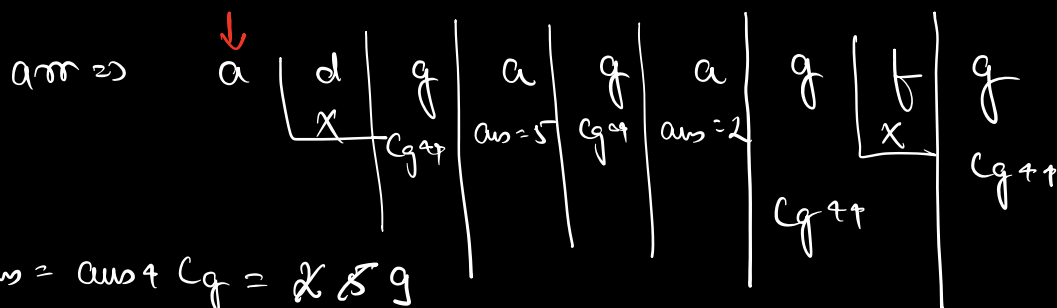
$$Op = g (4+3+2)$$



\Rightarrow new approach:-

$$ans = 0$$

$$C_g = 0$$



$$ans = ans + C_g = 2 + 3 = 5$$

$$C_g = 0 + 1 + 1 + 1 = 3$$

$$\Rightarrow Op = \underline{\underline{g}}$$

TC $\Rightarrow O(N)$
 SC $\Rightarrow O(1)$.

\Rightarrow Carry forward technique

pseudo

```
ans = 0  cg = 0
for (i = N-1; i >= 0; i--) {
    if (arr[i] == 'g') {
        cg++;
    }
    else if (arr[i] == 'a') {
        ans = ans + cg;
    }
}
print(ans)
```

Qn-2

For every 'g' calculate 'a' to the left of 'g'.

Carry \rightarrow Ca, ans
 (left to right)
 $i=0 \rightarrow i=N-1$.

Q2. Leaders in an array:

Given an $arr[N]$, you have to find all leaders in arr , an element is known as a leader, if it is strictly greater than all elements on its right side.

Note: $arr[N-1]$ is always a leader.

ex $\Rightarrow arr[] \Rightarrow$ 15 -1 7 2 5 4 2 3
Qp = 5
↓
✓ X ✓ X ✓ ✓ X ✓

ex $\Rightarrow arr[] \Rightarrow$ 8 -2 4 7 6 5 1
Qp = 5
↓
✓ X X ✓ ✓ ✓ ✓

ex $\Rightarrow arr[] \Rightarrow$ 10 7 9 3 2 4 5
Qp = 3
↓
✓ X ✓ X X X ✓

ex $\Rightarrow arr[] \Rightarrow$ 10 8 8
Qp \Rightarrow 2
↓
✓ X ✓

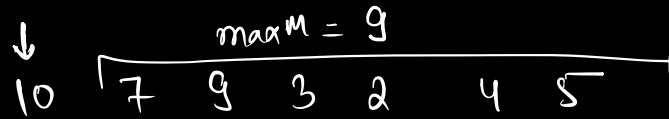
Bruteforce

take each element, and iterate till end, and check if its greater than all elements.

TC $\Rightarrow O(N^2)$
SC $\Rightarrow ?$

How \Rightarrow pseudo code for bruteforce.

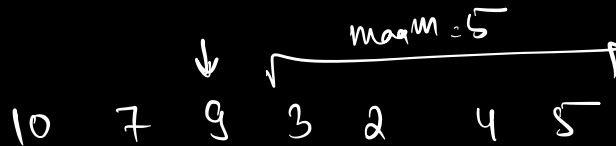
Optimise



$10 > 9 \rightarrow 10$ is leader, ans++



$7 < 9 \rightarrow 7$ is not a leader.



$9 > 5 \rightarrow 9$ is a leader, ans++

Ans: if for index i , max is the largest element on right of i [$i+1$ to $N-1$], and if

$\text{arr}[i] > \text{max} \Rightarrow \text{ans}++$
leader.

ans = 2, 3
max = 9, 10

10 7 9 3 2 4 5

↑

Q1 = 3

pseudo

$c = 1, \text{max} = \text{arr}[N-1]$

for($i = N-2; i \geq 0; i--$) {

if($\text{arr}[i] > \text{max}$) {

$c++$;

$\text{max} = \text{arr}[i]$

}

}

print(c).

$T.C \Rightarrow O(N)$

$S.C \Rightarrow O(1)$

: Subarrays :- [basics]

* Continuous part of an array is called subarray.

i) a single element is a subarray

ii) entire array is a subarray

iii) empty can't be a subarray

ex $\Rightarrow \text{arr}[9] \Rightarrow$

-3	4	6	2	8	7	14	9	21
0	1	2	3	4	5	6	7	8

idx $\Rightarrow [2 \ 3 \ 4 \ 5] \Rightarrow \text{Yes} \rightarrow [2-5]$

idx $\Rightarrow [3 \ 4 \ 6 \ 7 \ 8] \Rightarrow \text{No} \rightarrow \text{S.B skipped}$

idx \Rightarrow [1-3] \Rightarrow Yes.

idx \Rightarrow [4] \Rightarrow Yes

idx \Rightarrow [0-8] \Rightarrow Yes.

[1] \Rightarrow No

ex \Rightarrow subarray [3-7] \Rightarrow $\underbrace{3 \ 4 \ 5 \ 6 \ 7}_{\substack{7-3+1 \\ = 5}} \quad \underline{5 \text{ elements}}$

sub [s-e] \Rightarrow e-s+1

predefined func:

\rightarrow min(a,b) \rightarrow returns min of a & b.

TC $\Rightarrow O(1)$

\rightarrow max(a,b) \rightarrow returns max of a & b

TC $\Rightarrow O(1)$

\rightarrow sort(arr) \rightarrow arrange the elements in asc order by default.

TC $\Rightarrow O(N \log N)$

% always maintain TC of inbuilt func. in your overall TC

Q 3. Closest min max

Given an array find the length of smallest subarray which contains both min & max of array?

ex) arr \Rightarrow

	0	1	2	3	4	5	6	7	8	9
	1	2	3	1	3	4	6	4	6	3

min = 1
max = 6

$\{ \begin{aligned} \text{id}_X &\Rightarrow [0 \ 8] \Rightarrow \text{len} = 9 \\ &[3 \ 8] \Rightarrow \text{len} = 6 \\ &[3 \ 6] \Rightarrow \text{len} = 4, \rightarrow \text{minimum.} \end{aligned}$

$$Q_1 = 4$$

ex) arr[] \Rightarrow

2	2	6	4	5	1	5	2	6	4	1
0	1	2	3	4	5	6	7	8	9	10

$$\min \geq 1$$
$$\text{mod} = 6$$

idea of [17] is 7.

$$\text{id}_X \Rightarrow [2 \ 5] \Rightarrow 4$$

IdA 27 $[8 \ 10] \Rightarrow 3 \rightarrow \min^m$

$$Q_P = \underline{\underline{3}}$$

ex ⇒ qm ⇒

8 8 8 8 8 8

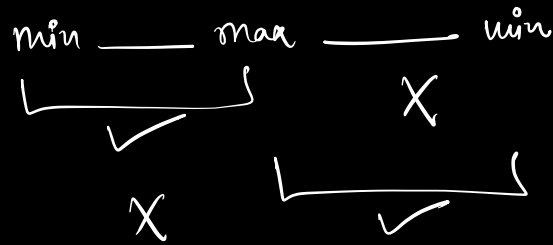
$$\min = 8$$

max = 8

Sub \Rightarrow 1. (870)

Observation

i)



Shortest subarray will contain only 1 min & 1 max

ii)



min & max would always be at boundaries.

[two ends of subarray]

iii) combining i & ii;

Case 1 →

min ——— max

↓

if I am

standing at min, find next max at right

Case 2 →

max ——— min

↓

if I am

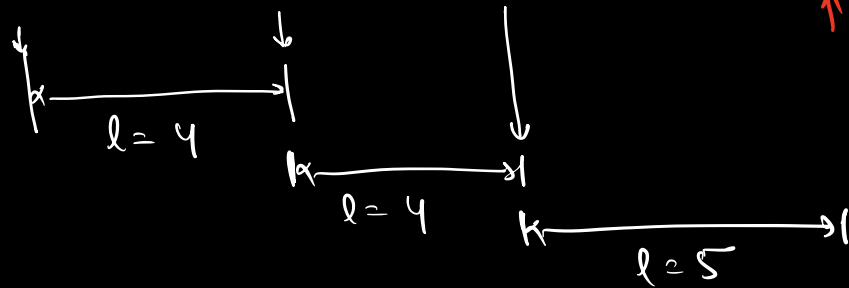
standing at max, find next min at right

ex \Rightarrow

0	1	2	3	4	5	6	7	8	9	10	11	12
2	2	6	4	5	1	5	2	6	4	3	4	1

min = 1

max = 6



Qp = min len \Rightarrow 4.

pseudo

ans = N.

iterate, get min & max] if (min == max) return 1.

for ($i=0; i < N; i++$) {

if (arr[i] == min) { // find nearest max

for ($j=i+1; j < N; j++$) {

if (arr[j] == max) {

ans = min(ans, j - i + 1);

break;

}

}

}

else if (arr[i] == max) { // find nearest min

for ($j=i+1; j < N; j++$) {

if (arr[j] == min) {

ans = min(ans, j - i + 1);

break;

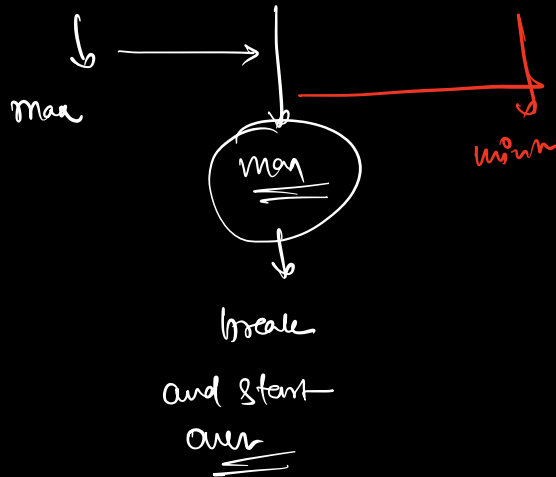
}

}

ex \Rightarrow

	0	1	2	3	4	5	6	7	
	8	3	8	7	3	1	2	8	

$\min = 1$
 $\max = 8$



$i = 0$
 $\max \rightarrow \min$

 $j = 2$ [max]
 $i = 2$ $\rightarrow \min$

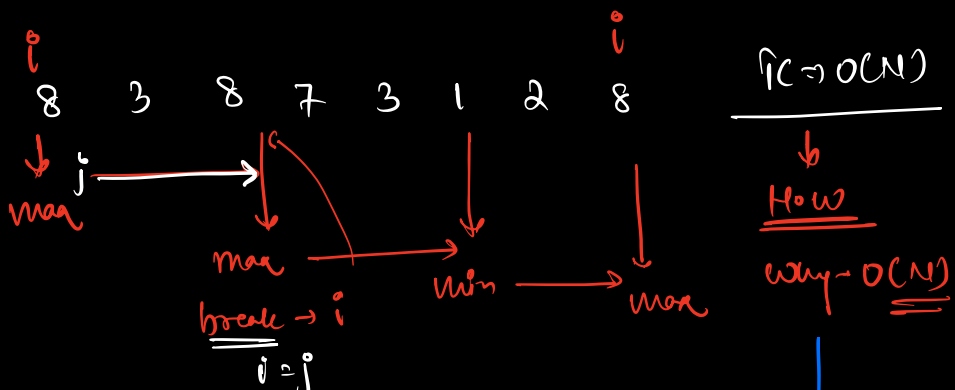
 $j = 5$ $i = 5$

So, if you are at max, finding min but got another
 $\max \Rightarrow$ break

So, if you are at min, finding max but got another
 $\min \Rightarrow$ break

TC \Rightarrow $O(N^2)$

SC \Rightarrow $O(1)$



Start

⇒ carry forward

min = 1, max = 6

Ans = N
min l = -1
max l = -1

0	1	2	3	4	5	6	7	8	9	10	11	12
1	6	4	6	5	1	5	2	6	4	4	2	1
↑		X		X		X	X		X	X	X	
min l = 0 max l = 1 l = 2	min l = 5 max l = 1 l = 5		min l = 5 max l = 3 l = 3		min l = 5 max l = 8 l = 4			max l = 8 min l = 12 l = 5				min l = 12 max l = -1

ans = ~~13~~ ~~5~~ ~~4~~ ~~3~~ 2

Op = 2

TC = O(N)
SC = O(1)

pseudo

ans = N

min1 = -1

max1 = -1

1) iterate \Rightarrow find min & max

for (i = N-1; i >= 0; i--) {

if (arr[i] == min) {

min1 = i;

l = abs(min1 - max1) + 1

ans = min(ans, l)

}

else if (arr[i] == max) {

max1 = i;

l = abs(min1 - max1) + 1

ans = min(ans, l)

}

}

}

print(ans)

check
if max1 $\neq -1$

check
if min1 $\neq -1$