

$T(N) = 2 * T(N/2) + O(N)$

Pr. 10 \Rightarrow Do substitution, expand and find TC

$\Rightarrow TC \Rightarrow O(N \log N)$

$T(N) = 2 * T(N/2) + O(N)$

\rightarrow func N {

func N/2 {

func N/2 {

for (i=0 \rightarrow N-1) {

}

i) logic

ii) write recursive code

iii) write TC relationship

iv) expand & TC

$N \rightarrow N/2 \rightarrow N/4 \rightarrow N/8 \rightarrow N/16 \rightarrow \dots$

$\log N$ times func call

So, each func call has

$O(N)$ for loop.

total TC $\Rightarrow O(N \log N)$

\Rightarrow Space complexity for recursion

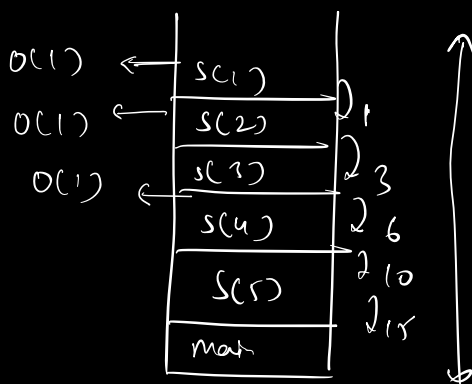
\hookrightarrow sum(N)

sum(5)

max size of call

Stack

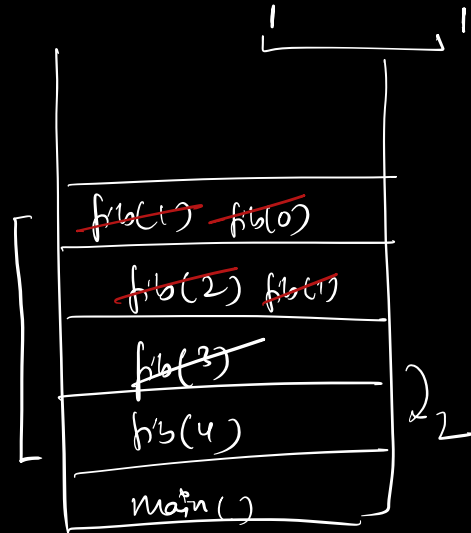
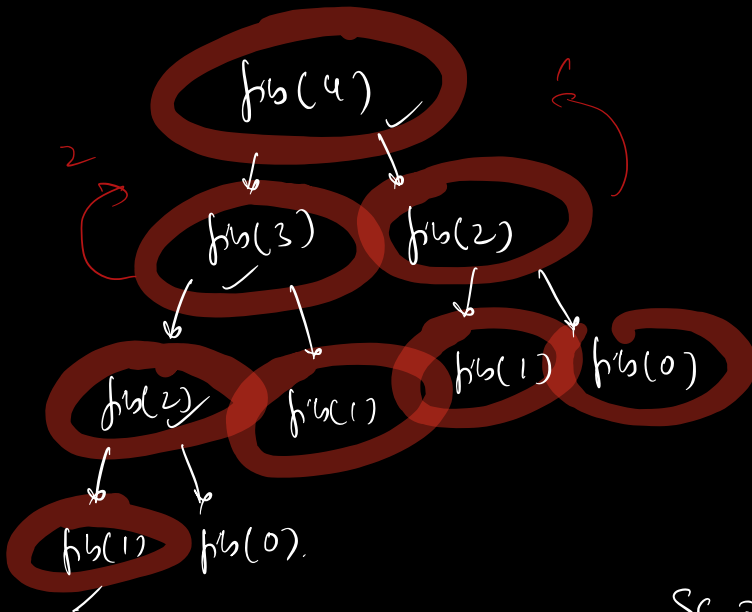
SC $\Rightarrow O(N)$



fibonacci

$$fib(N) = fib(N-1) + fib(N-2)$$

$$// \underline{fib(3) = fib(2) + fib(1)}$$



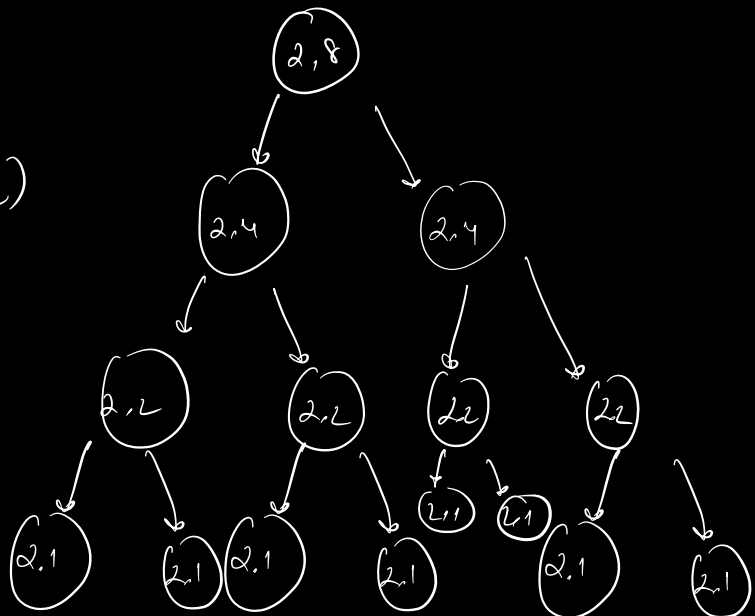
$$Sc \approx \underline{\underline{O(N)}}$$

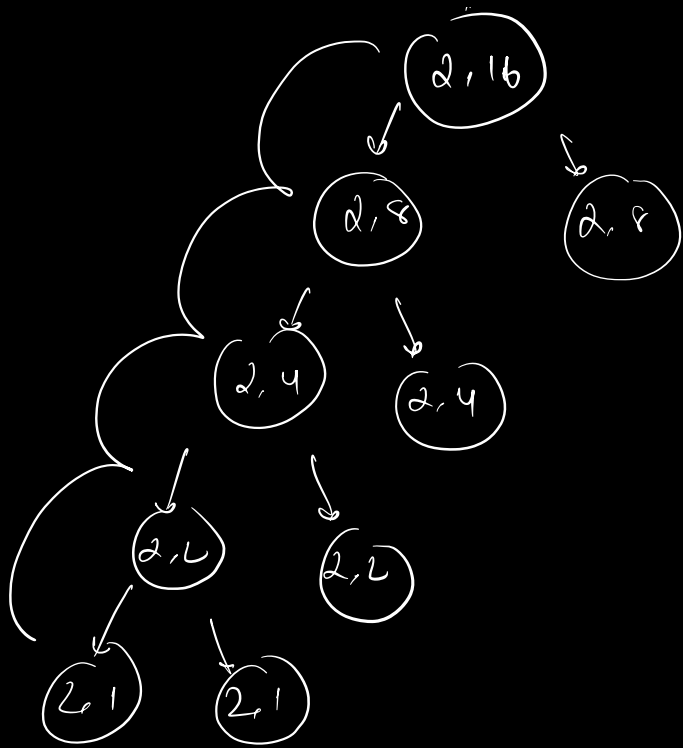
$pow(N) \{$

$$pow(N/2) \times pow(N/2)$$

$\{$

$$Sc \approx \underline{\underline{O(\log N)}}$$





$$\log_2 16 = \boxed{4} + 1$$

LinkedList

Arrays

$O(1)$ accessing any element

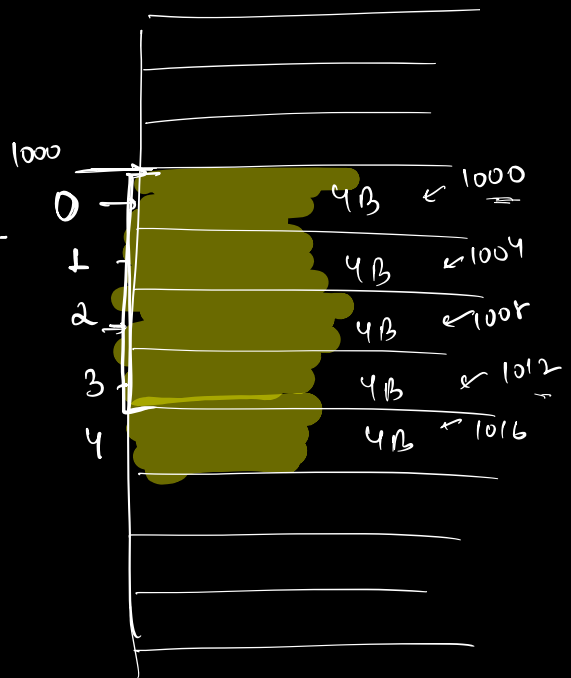
int arr[5] \Rightarrow size is fixed

\downarrow
4B

int arr[5]

\downarrow

stores memory add for 0th idx



* array is defined as contiguous memory.

⇒ working of arraylist

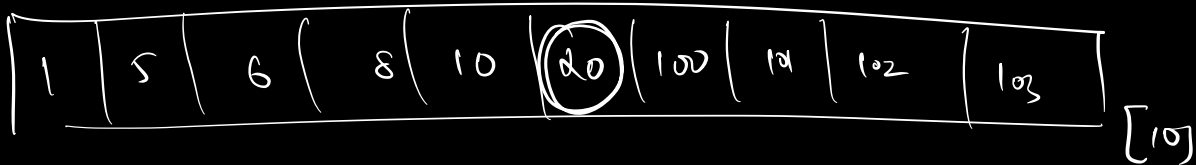
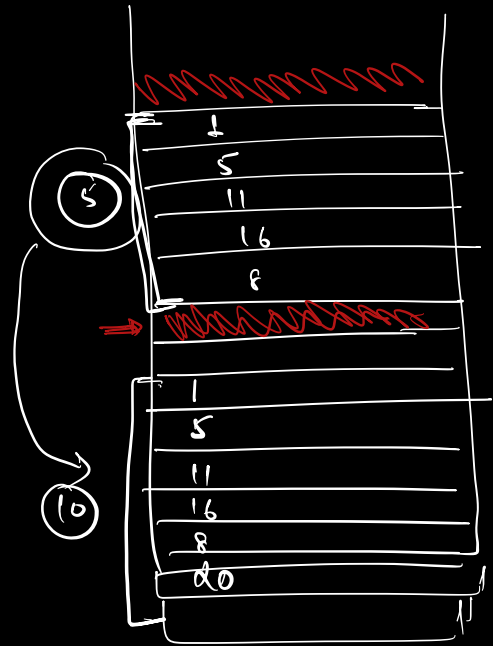
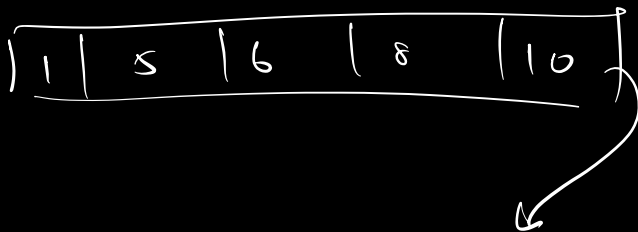
uses an array internally

→ initial size → 5

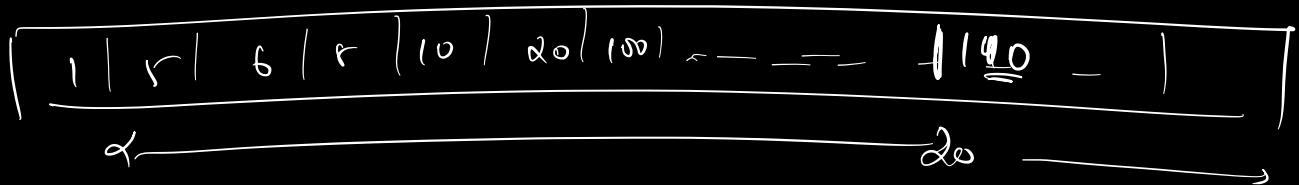
→ load factor → 1 ←

doubles

`ArrayList<Integer> = new ArrayList<>()`



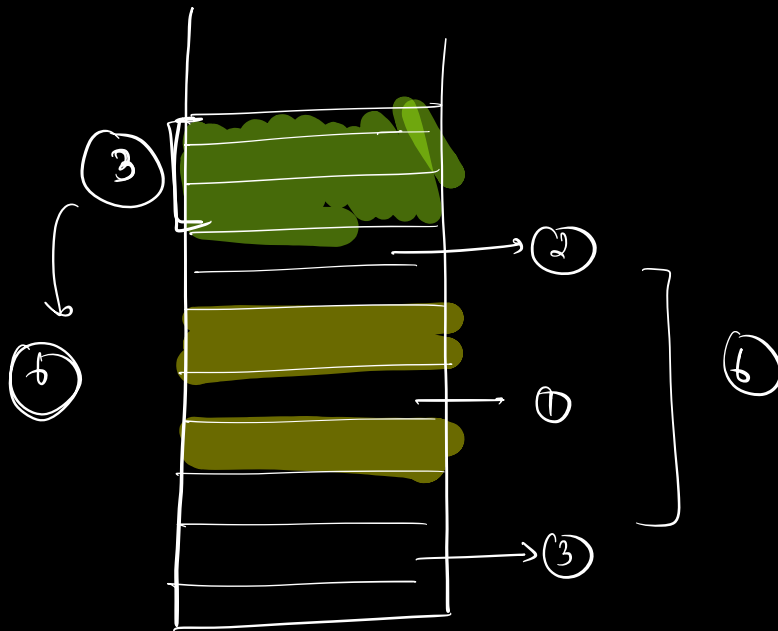
$O(N)$ ← worst case
insertion



ArrayList → $\left. \begin{array}{l} \text{insert} \\ \text{read} \\ \text{update} \end{array} \right\} O(1) \text{ [amortised]}$

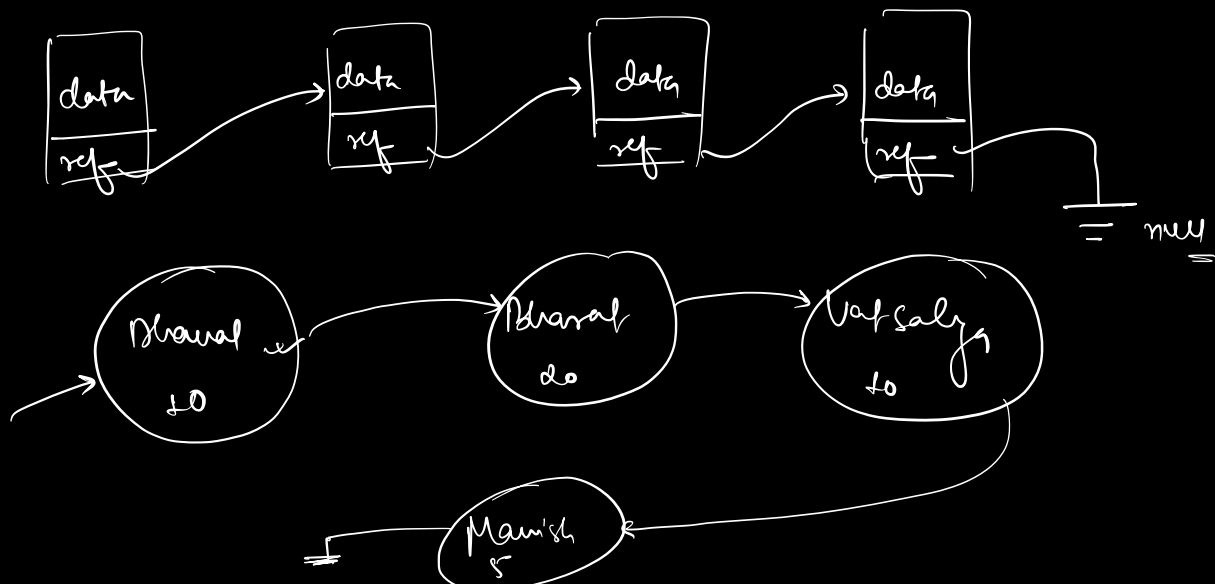
plastic cans \rightarrow 20 l \rightarrow 100 l

machine \rightarrow 10k



& even though
we have
memory, we
are not able
to use it.

\Rightarrow How LL works?

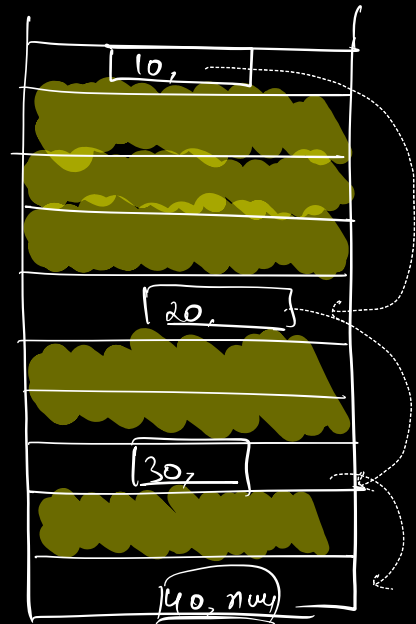


4 integers [10, 20, 30, 40]

array?

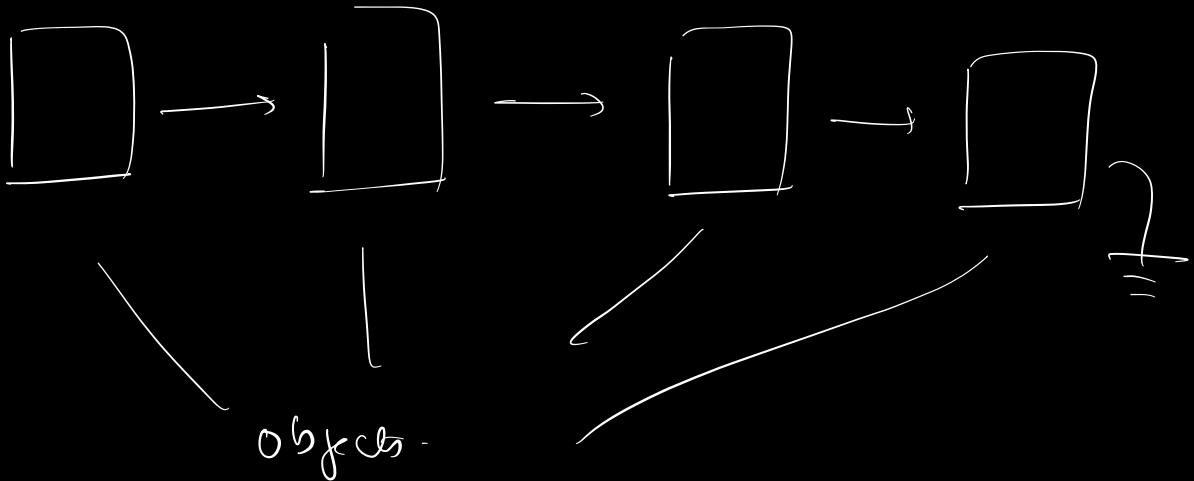
arraylist?

LinkedList



Node

[data] → int, String, char, Map, Map, Array
ref



```

class Node {
    int data;
    Node next;
}

```

data

ref. variable to next node.

Java

```
Node head = new Node();
```

↓

```
head.data = 0 / null;
```

```
head.next = - - - -
```

Constructor

```

public Node(int a) {
    data = a;
    next = null;
}

```

```
Node head = new Node(10);
```

↓

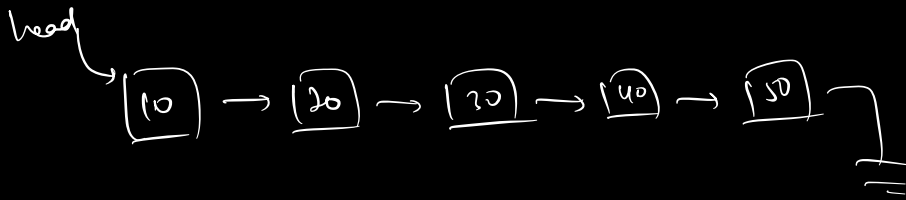
```

[
    head.data = 10;
    head.next = null;
]

```

Q 1. Find length of a LL, given LL

i/p ⇒ head



Op \Rightarrow 5

```

int getlength (Node head) {
    int len = 0; Node temp = head;
    while (temp != null) {
        len++;
        temp = temp->next;
    }
    return len;
}

```

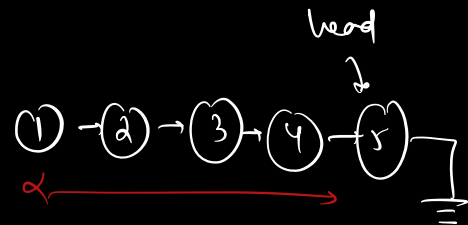
TC $\Rightarrow O(N)$
 SC $\Rightarrow O(1)$

Op = 5

```

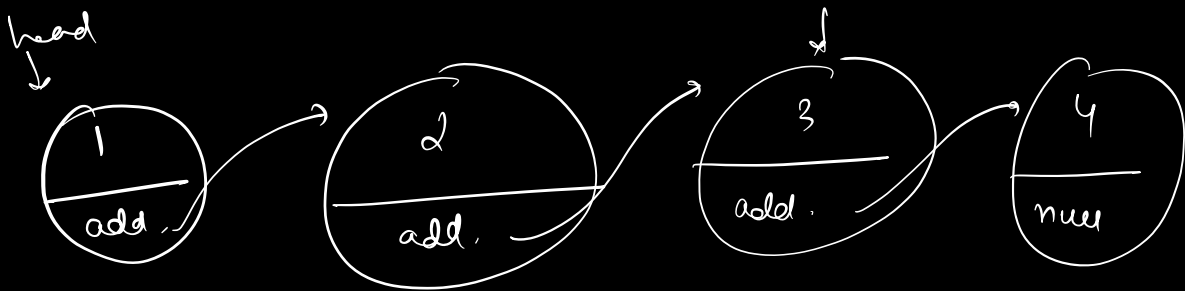
int getlength (Node head) {
    int len = 0;
    while (head->next != null) {
        len++;
        head = head->next;
    }
    return len;
}

```



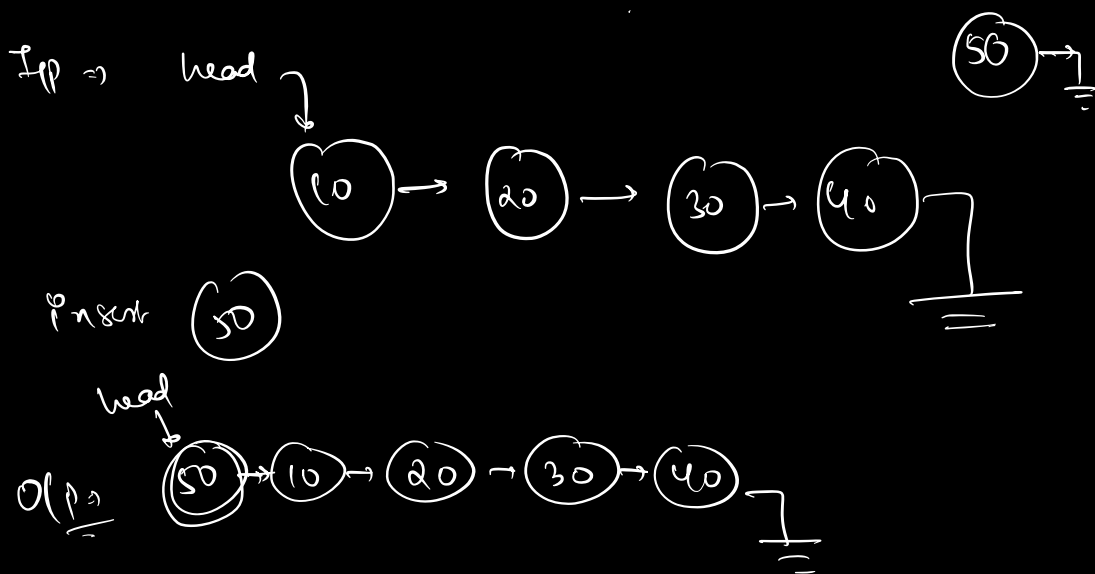
$l = \cancel{0} \cancel{1} \cancel{2} \cancel{3} 4$

Op = 4



* access randomly \rightarrow LL is not a good option

Q2, Given a LL, add data in front of LL



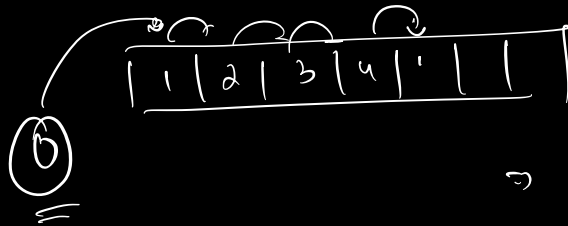
Node newNode = new Node(50); \leftarrow

data = 50
next = null

newNode.next = head;

head = newNode

adding element at front \Rightarrow LL $\Rightarrow O(1)$



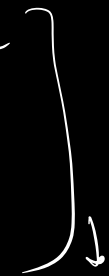
\Rightarrow array $\Rightarrow O(N)$

\Rightarrow use case

Flash search

BBT

Lucene



Special

types of LL

[Skip list]

iphone	doc1	doc2	doc3	doc10
Samung	doc4	doc5	doc6	
phone	doc1	doc2	doc3	
	doc4	doc5	doc6	

Indexed Index

Q 3. Given a LL add data at end of LL.

Tip \Rightarrow head \downarrow



Insert \rightarrow 0 at end

O/p \Rightarrow head \downarrow



Node newNode = new Node(0)

temp = head

while (temp.next != null) {

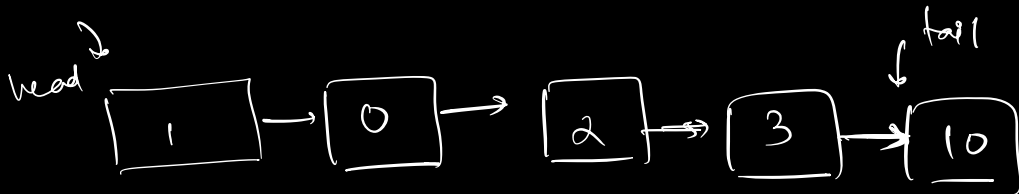
temp = temp.next;

}

temp.next = newNode;

$TC \Rightarrow O(N)$
 $SC \Rightarrow O(1)$

Optimise [TO-DO] \rightarrow google



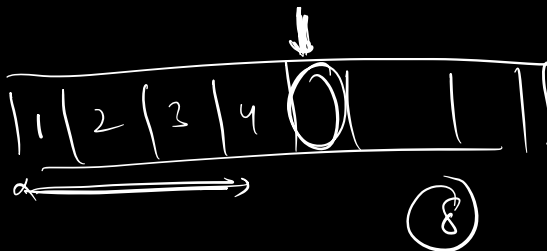
Node newNode = new Node(x);

tail.next = newNode

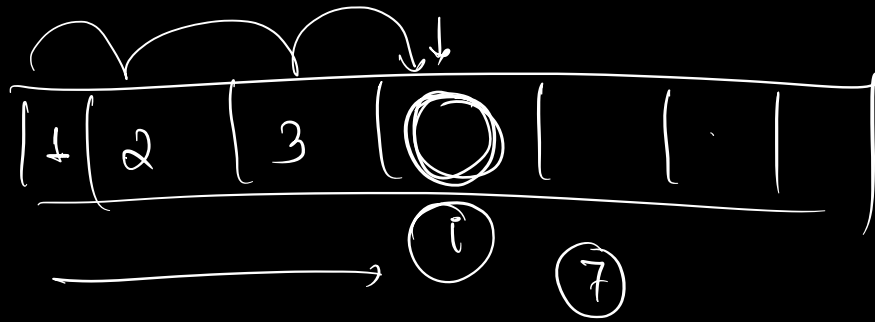
tail = newNode

$TC \Rightarrow O(1)$
 $SC \Rightarrow O(1)$

array $\Rightarrow O(N)$
LL $\Rightarrow O(1)$



$$ans[N-1] \rightarrow \underline{\underline{O(1)}}$$

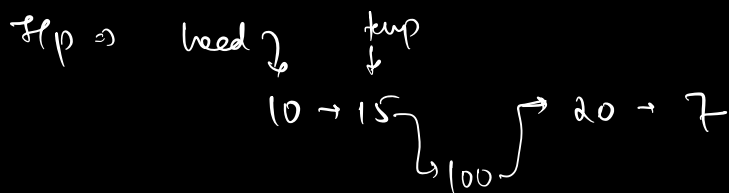


* insertion at edges [start or end]

$$LL \rightarrow O(1)$$

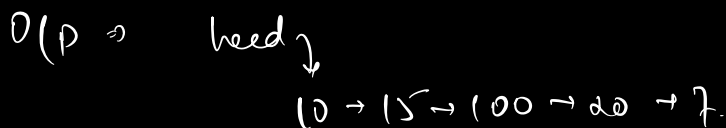
$$Array \rightarrow O(N)$$

Q 4. Given a LL, insert a node at k^{th} position



$$k = 2$$

$$\underline{\underline{100}}$$



$C = 0$

$temp = head;$

$while (C < k-1) \{$

$C++$

$temp = temp->next;$

$\}$

$newNode->next = temp->next$

$temp->next = newNode$

$\}$

$temp$
 $10 \rightarrow 15$

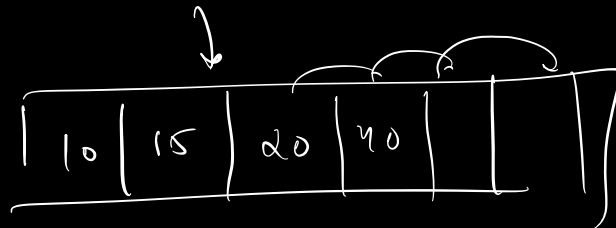
\hookrightarrow

(100)

$20 \rightarrow 7$

at k^{th} position

LL } $O(N)$
array }



11.10 $\left[\begin{array}{l} \underline{Q\ 1.} \text{ Delete a node from beginning} \\ \underline{Q\ 2.} \text{ Delete a node from end.} \end{array} \right]$