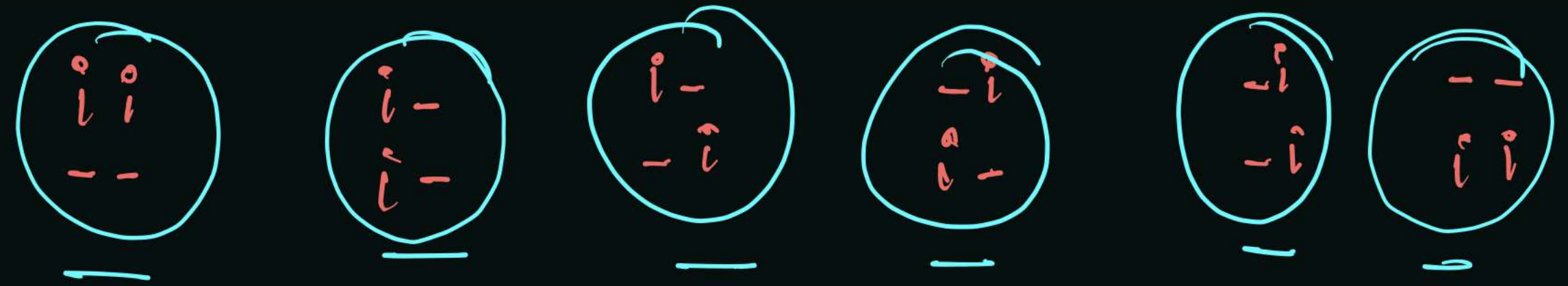


Queens Combinations - 2D as 1D - Queens Chooses

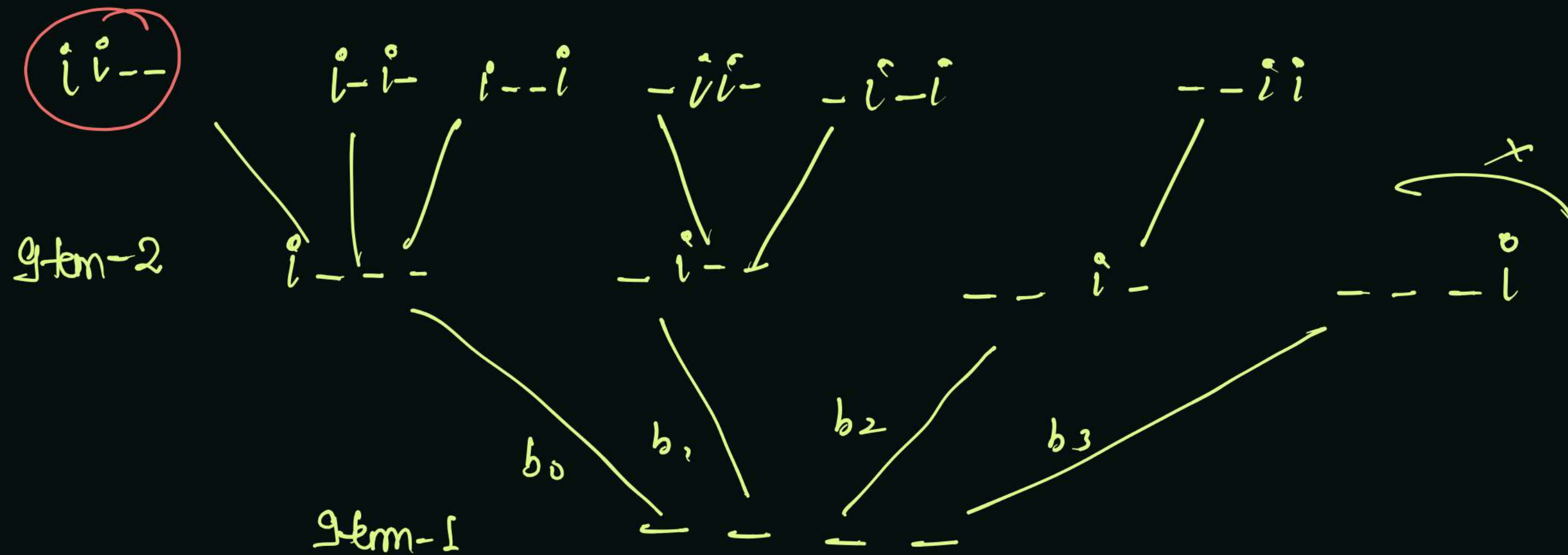
Thursday, 15 July 2021 7:16 PM

level \rightarrow terms

options \rightarrow boxes



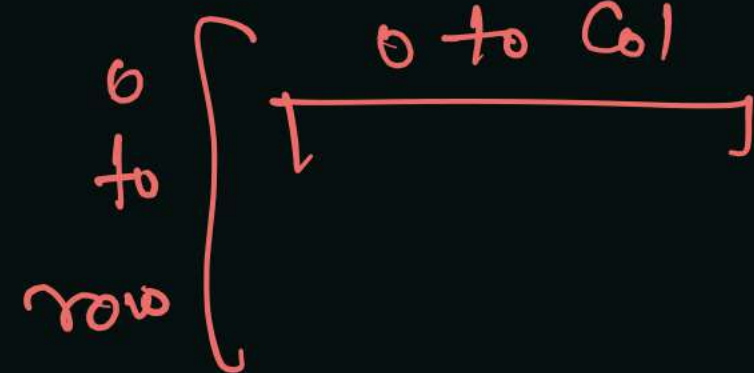
$${}^4C_2 = \frac{4!}{2!2!} = 6$$



	0	1	2	3
0	0	1	2	3
1	4	5	6	7
2	8	9	10	11
3	12	13	14	15

cell → m x n

Traversal in 2D matrix



Conversion from b.no. to row and Col →

$$r = \frac{b.no.}{\text{Total Row}}$$

$$c = b.no. \% \text{Total Col}$$

0 to (m x n - 1)

(2,1)
 9
 row →
 No. cell no.
 m
 Col. → (cell no.) % n
 No.

(0,0) 0	(0,1) 1	(0,2) 2	(0,3) 3
(1,0) 4	(1,1) 5	(1,2) 6	(1,3) 7
(2,0) 8	(2,1) 9	(2,2) 10	(2,3) 11
(3,0) 12	(3,1) 13	(3,2) 14	(3,3) 15

$$\frac{11}{4} = 2$$

$$11 \% 4 = 3$$

→ (2,3)

	0	1
0	0	1
1	2	3

${}^4C_2 \rightarrow$
 $\begin{bmatrix} 9 & 9 \\ - & - \end{bmatrix}$
 $\begin{bmatrix} 9 & - \\ 9 & - \end{bmatrix}$
 $\begin{bmatrix} 9 & - \\ - & 9 \end{bmatrix}$
 $\begin{bmatrix} - & 9 \\ 9 & - \end{bmatrix}$
 $\begin{bmatrix} - & 9 \\ - & 9 \end{bmatrix}$
 $\begin{bmatrix} - & - \\ 9 & 9 \end{bmatrix}$

selected \rightarrow (0,1) (0,2) (0,3) (1,2) (1,3) (2,3)

$n \times n$ All arrangement of n queens in $n \times n$ boxes -

level → greens

option - horses

Identical

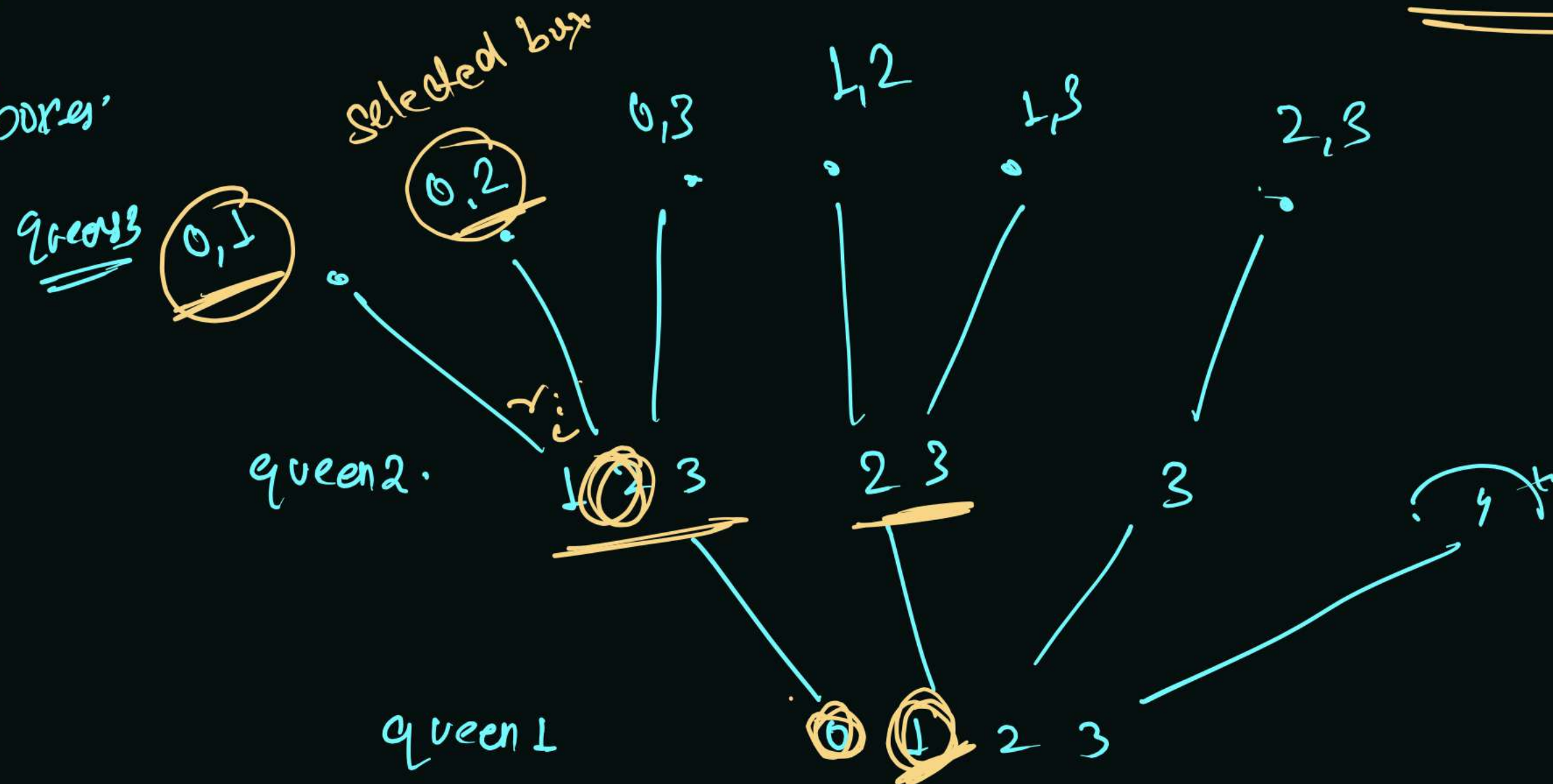
↳ 2D matrix of box

~~4~~ b. no -
~~4~~ current green

✓ total 9 green

$$r = \frac{\text{bno.}}{\text{total Res}}$$

$C = \text{bno } Y, \text{ total Col.}$


$$b = 2b + 1 \quad \text{to} \quad m \times n + 1$$
$$lb = -1$$

argument of Recursion

NQueens Combinations - 2D as 1D - Queens Chooses

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level \rightarrow queen.

option \rightarrow boxes.

box $\rightarrow 4 \times 4$.

queen $\rightarrow 4$

Safety of queen also

place \rightarrow is safe to place

concern of problem.

Total combination \rightarrow

16

C_4

=

$$\frac{16 \times 15 \times 14 \times 13 \times 12!}{4! \times 12!}$$

	0	1	2	3
0		q ₁		
1				q ₂
2	q ₃			
3			q ₄	

(0,1) \rightarrow (1,3) \rightarrow (2,0) \rightarrow (3,2)

	0	1	2	3
0			q ₁	
1	q ₂			
2				q ₃
3		q ₄		

(0,2) \rightarrow (1,0) \rightarrow (2,3) \rightarrow (3,1)

$$= 14 \times 13 \times 10$$

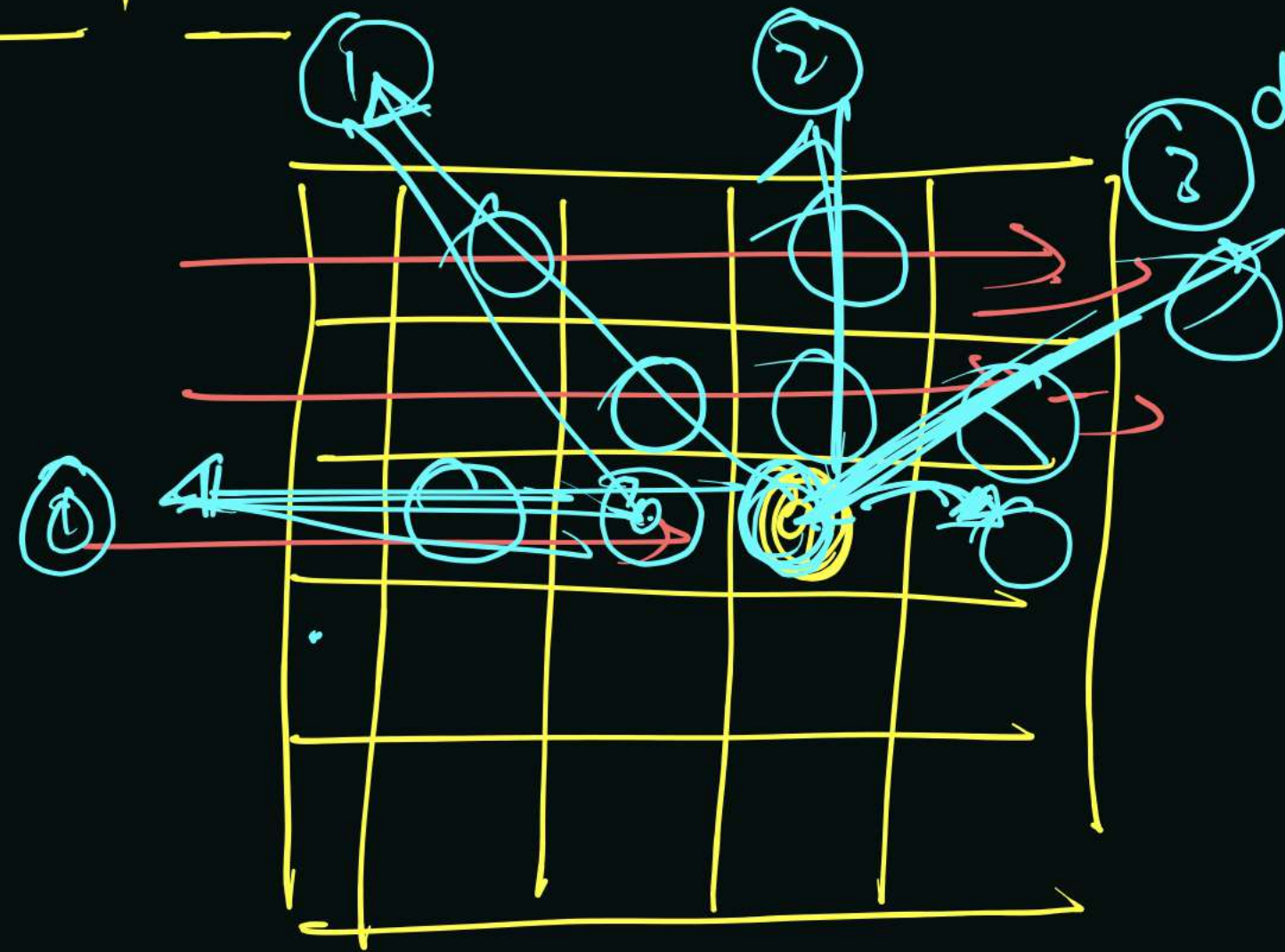
$$= 1820$$

Final Result
with
safety
concern

\hookrightarrow (2)

[NOTE: To find box No \rightarrow $b.no = r * Total Row + C$]

Is safe to place. \rightarrow



direction of checking \rightarrow

Direction \rightarrow 0

$r \rightarrow$ source
 $col \rightarrow$ default until $\rightarrow 0$

Direction \rightarrow 1

$row \rightarrow$ default
 $col \rightarrow$ default } until both are white

Direction \rightarrow 2

$row \rightarrow$ default
 $col \rightarrow$ same } until $\rightarrow 0$

Direction \rightarrow 3

$row \rightarrow$ default } until
 $col \rightarrow$ default } chess length

r, c

NQueens Permutations - 2D as 1D - Queens Chooses

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$${}^3P_2 = \frac{3!}{1!} = 8 \times 2 = 6$$

3 place

2 item

level → items

options → boxes

$n \times n \rightarrow$ box
 $n \rightarrow$ items

16 → box
4 → queen

$n \times n$ P_n

$${}^{16}P_4 = \frac{16 \times 15 \times 14 \times 13}{1}$$

is Queen Safe

valid answer

✓ 1 2 0

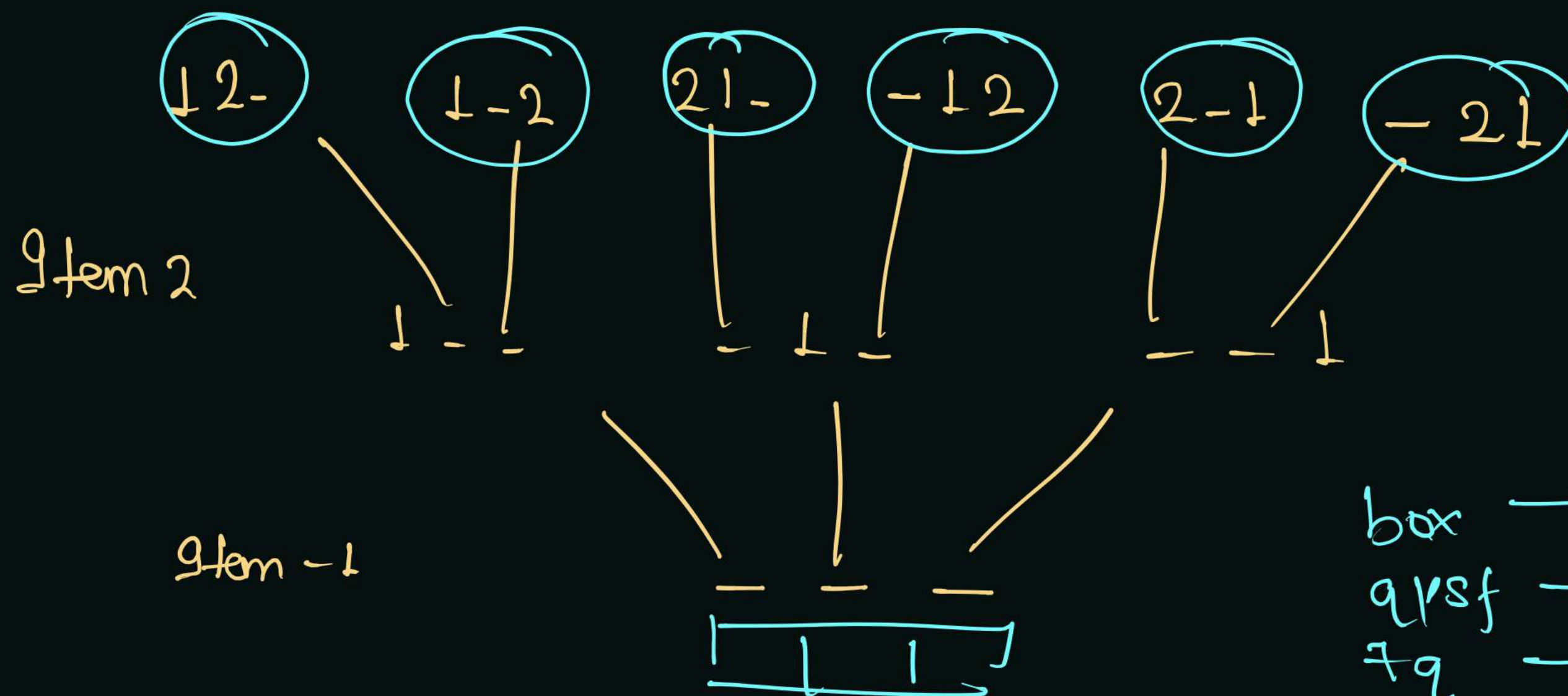
✓ 1 0 2

✓ 2 1 0

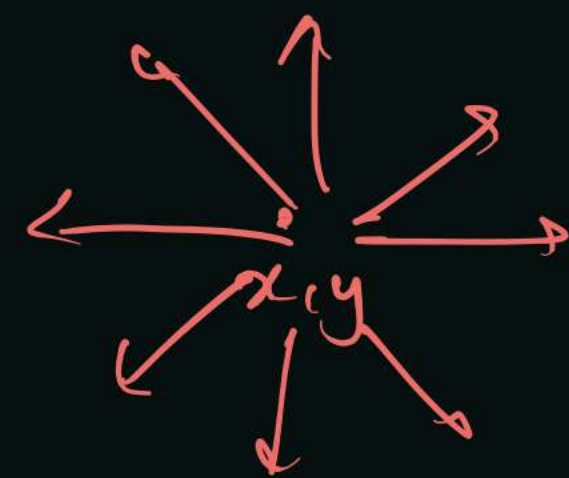
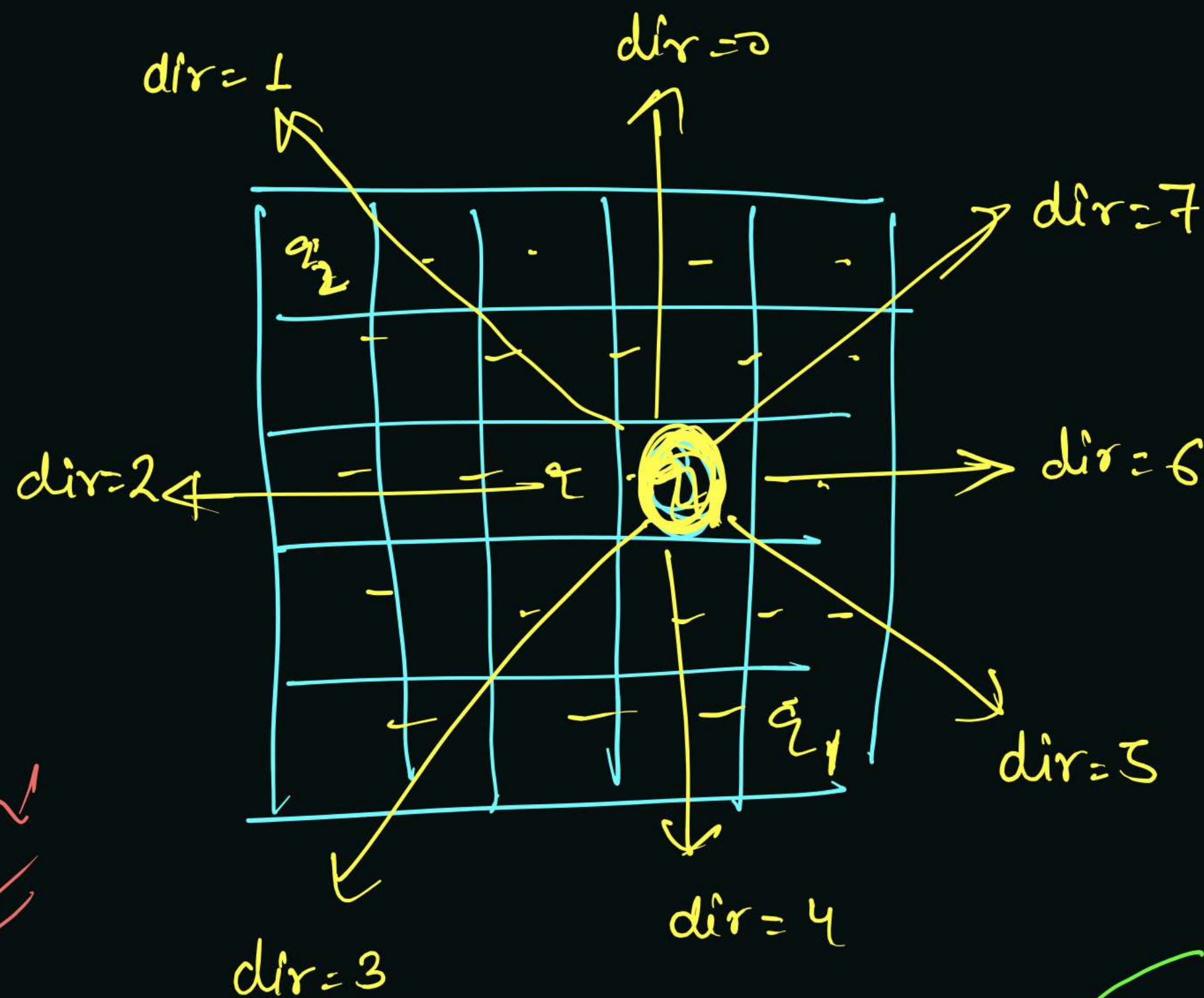
✓ 2 0 1

✓ 0 1 2

✓ 0 2 1



Direction of
checking
the
safety
of queen



check safety of
queen in
all directions

why? → we are
finding permutation.

On Every call, we are
starting loop from
beginning position.

8x8

K		K		K		K	
	K		K		K		K
K		K		K		K	
	K		K		K		K
K		K		K		K	
	K		K		K		K
K		K		K		K	
	K		K		K		K

{ Max. knights we can
place on chess board }

NKnights Combination- 2D as 1D - Knights Chooses

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$n \times n \rightarrow$ chessboard, n - identical knights,
print all possible arrangements to place n - knights.

Level \rightarrow Knights

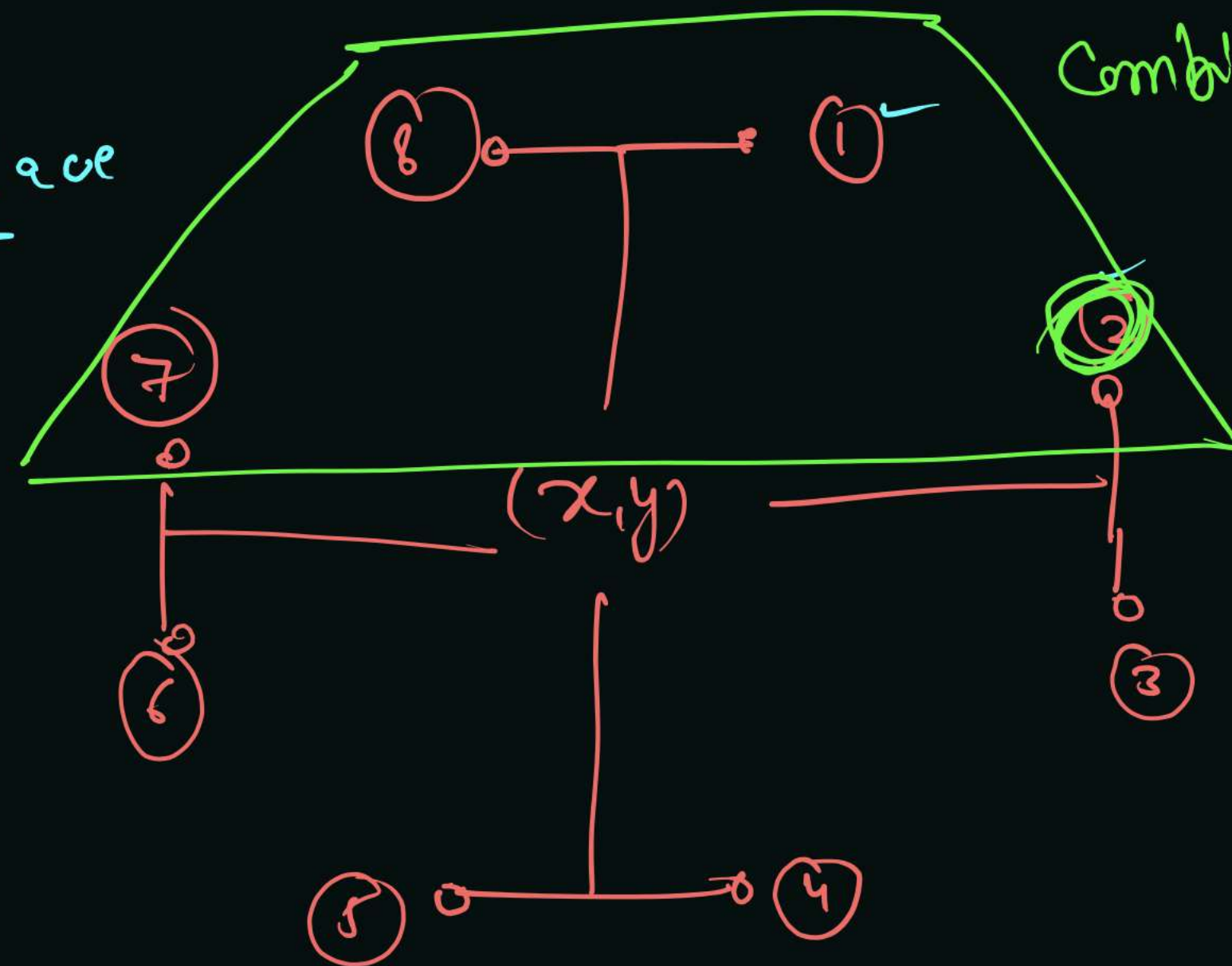
option \rightarrow box

is safe to place

for Comb's \rightarrow

$\left[\begin{array}{l} x-2, y+1 \\ x-1, y+2 \\ x-1, y-2 \\ x-2, y-1 \end{array} \right]$

last box } combination / k



Combinations

- ① $x-2, y+1$ ✓
- ② $x-1, y+2$ ✓
- ③ $x+1, y+2$
- ④ $x+2, y+1$
- ⑤ $x+2, y-1$
- ⑥ $x+1, y-2$
- ⑦ $x-1, y-2$ ✓
- ⑧ $x-2, y-1$ ✓