

$n \times n \rightarrow$ board, n - identical items } queen.

print all possible ways to place queens in chess board,

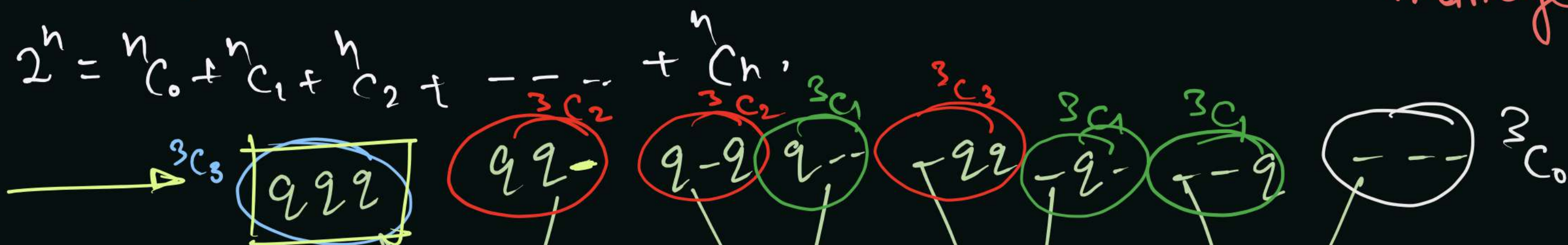
level - Box

option - Yes and No of queen.

"behavior of chess queen is not managed here"

$n=3$

$r=2$



$2^3 = {}^3C_0 + {}^3C_1 + {}^3C_2 + {}^3C_3$ box 2.

q q -

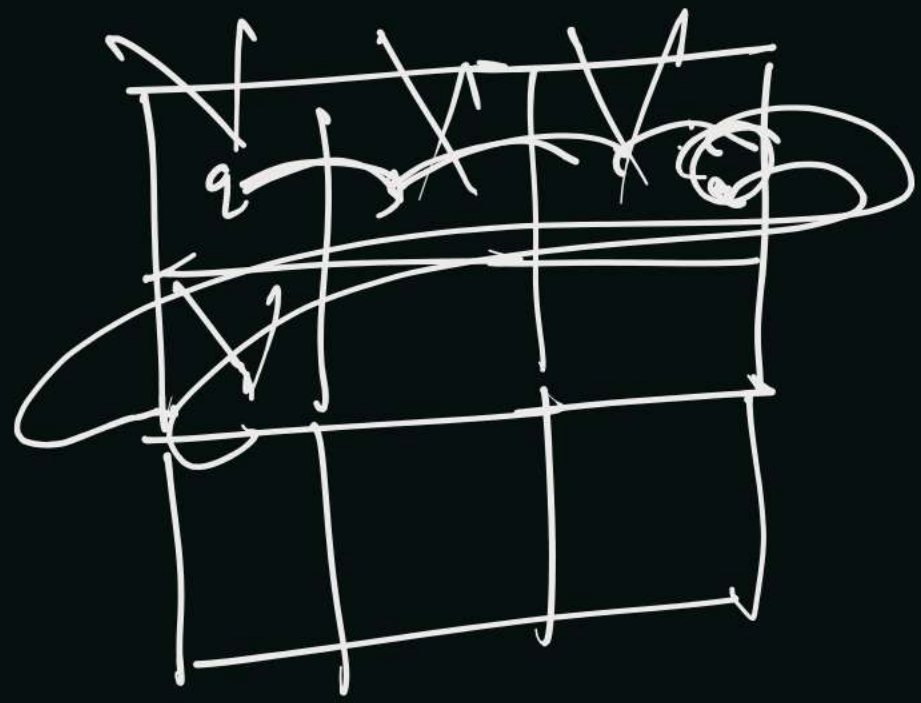
q q

box 1

box - 0

Combination

box no. increment on every call



if col. cross its range.

row - ignore next
col. begin with '0'

99

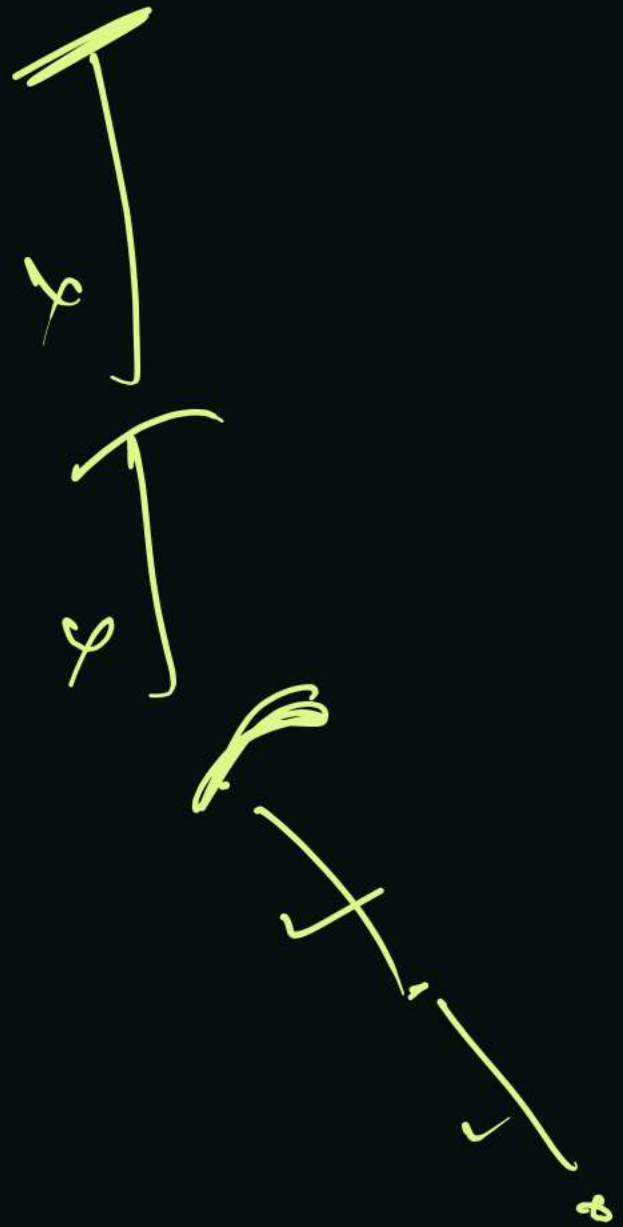
(row == tq)

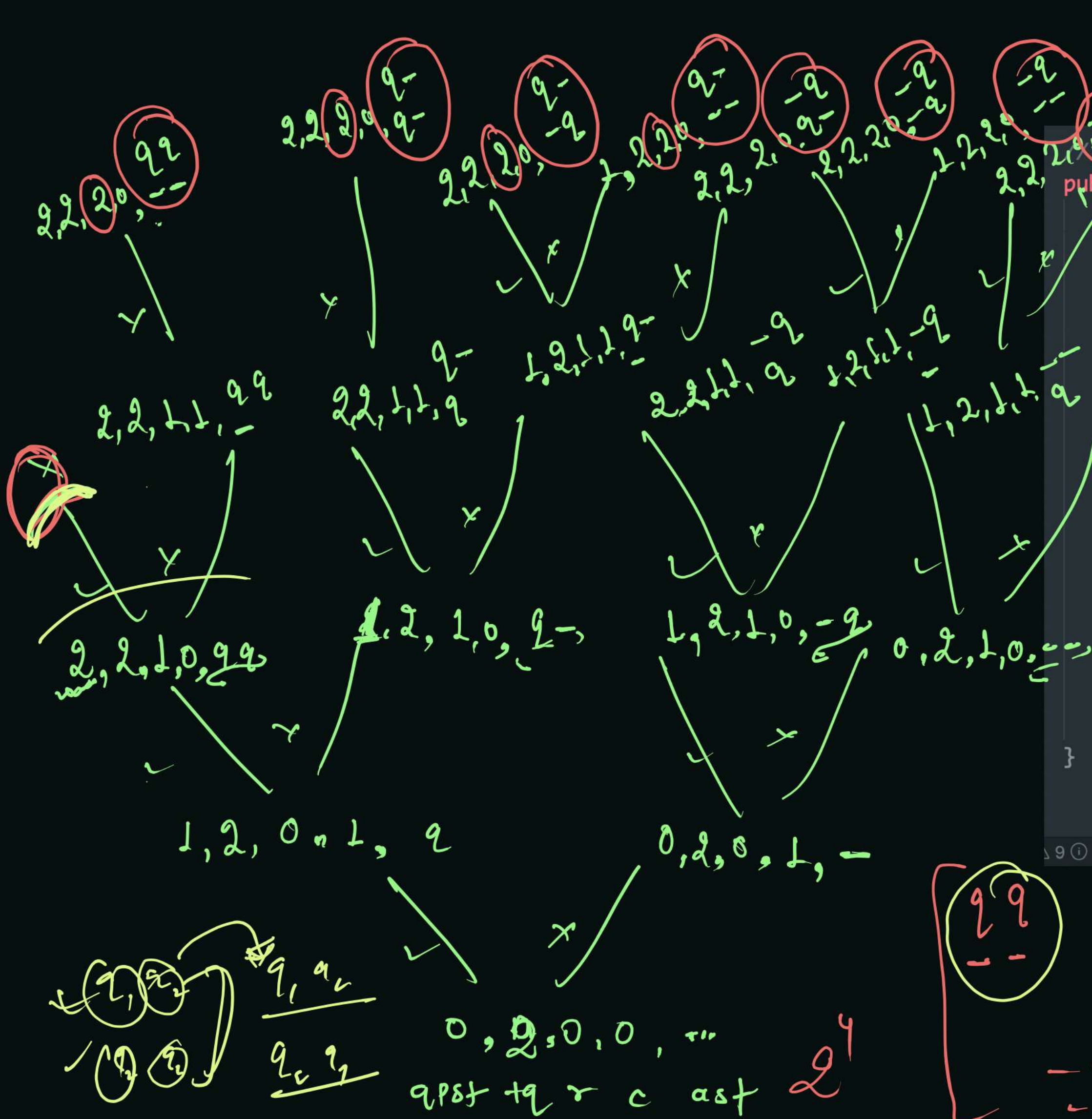
99

0	9	9
1	9	9

99

row == tq



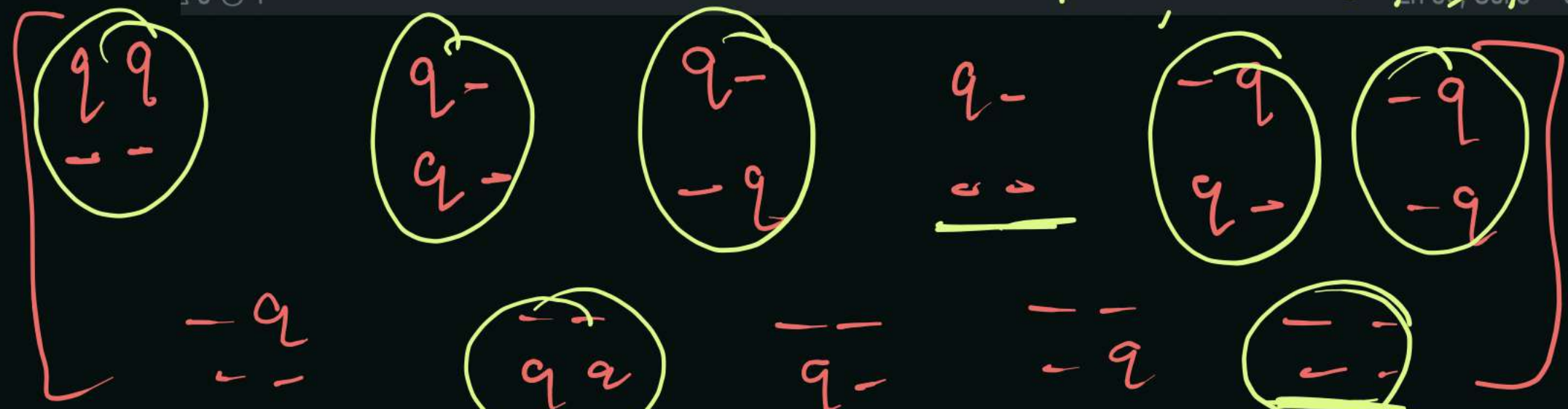


```

// qpsf -> queens placed so far, tq -> total queen, asf -> answer so far
public static void queensCombinations(int qpsf, int tq, int row, int col, String asf) {
    if (row == tq) {
        if (qpsf == tq) {
            System.out.println(asf);
        }
        return;
    }
    if (col + 1 < tq) {
        // yes call
        queensCombinations(qpsf + 1, tq, row, col + 1, asf + "q");
        // no call
        queensCombinations(qpsf, tq, row, col + 1, asf + "-");
    }
    else {
        // yes call
        queensCombinations(qpsf + 1, tq, row + 1, 0, asf + "q\n");
        // no call
        queensCombinations(qpsf, tq, row + 1, 0, asf + "\n");
    }
}

```

$$C_2 = \frac{4!}{2! \times 2!} = 6$$



$n \times n$ chessboard, n - non identical queens
print all possible arrangement

level = queen / gkms

option → box

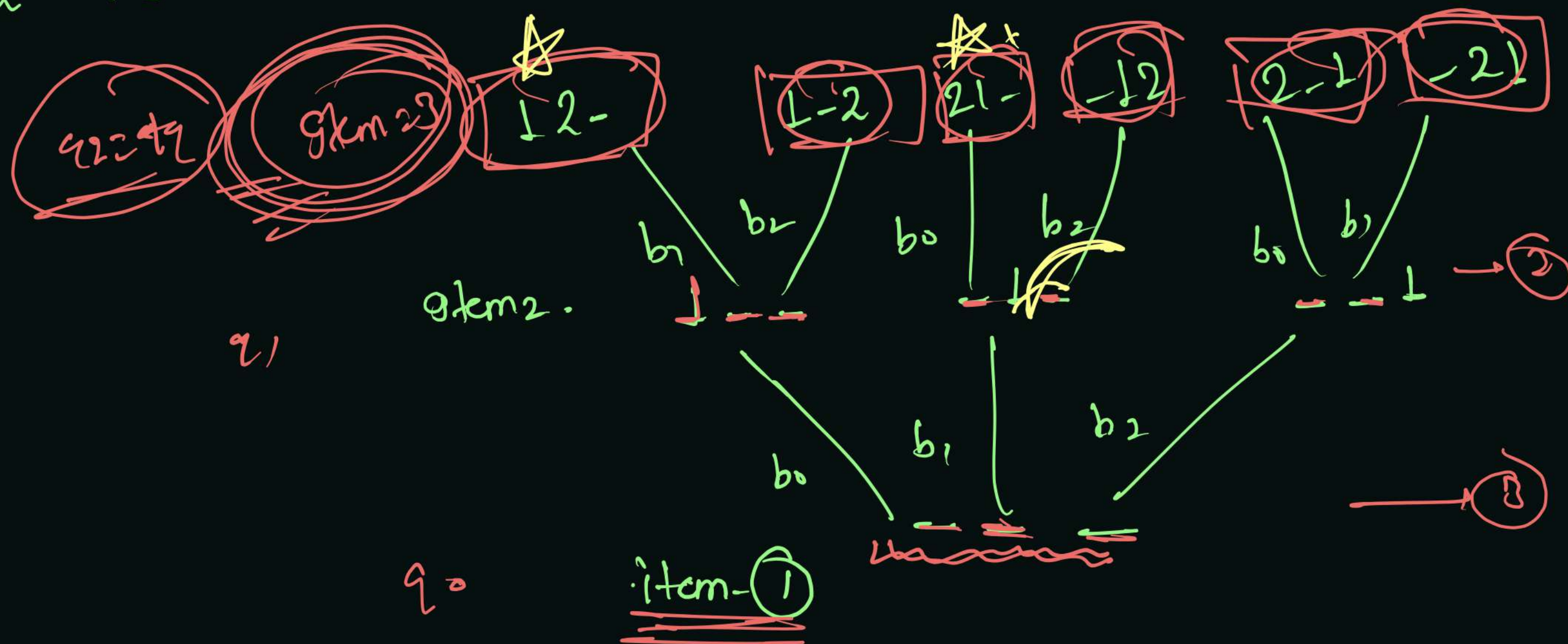
$n=3 \rightarrow$ boxes

$r=2 \rightarrow$ gkms

$n \times (n-1) \times (n-2) \times \dots \times (n-(r-1))$

$$\hookrightarrow \frac{n!}{(n-r)!} = {}^n P_r$$

$${}^3 P_2 = \frac{3!}{1!} = \frac{3 \times 2 \times 1}{1} = 6 \quad (C)$$



12-

1-2

21-

-12

2-1

-21

if (qpsf == tq)

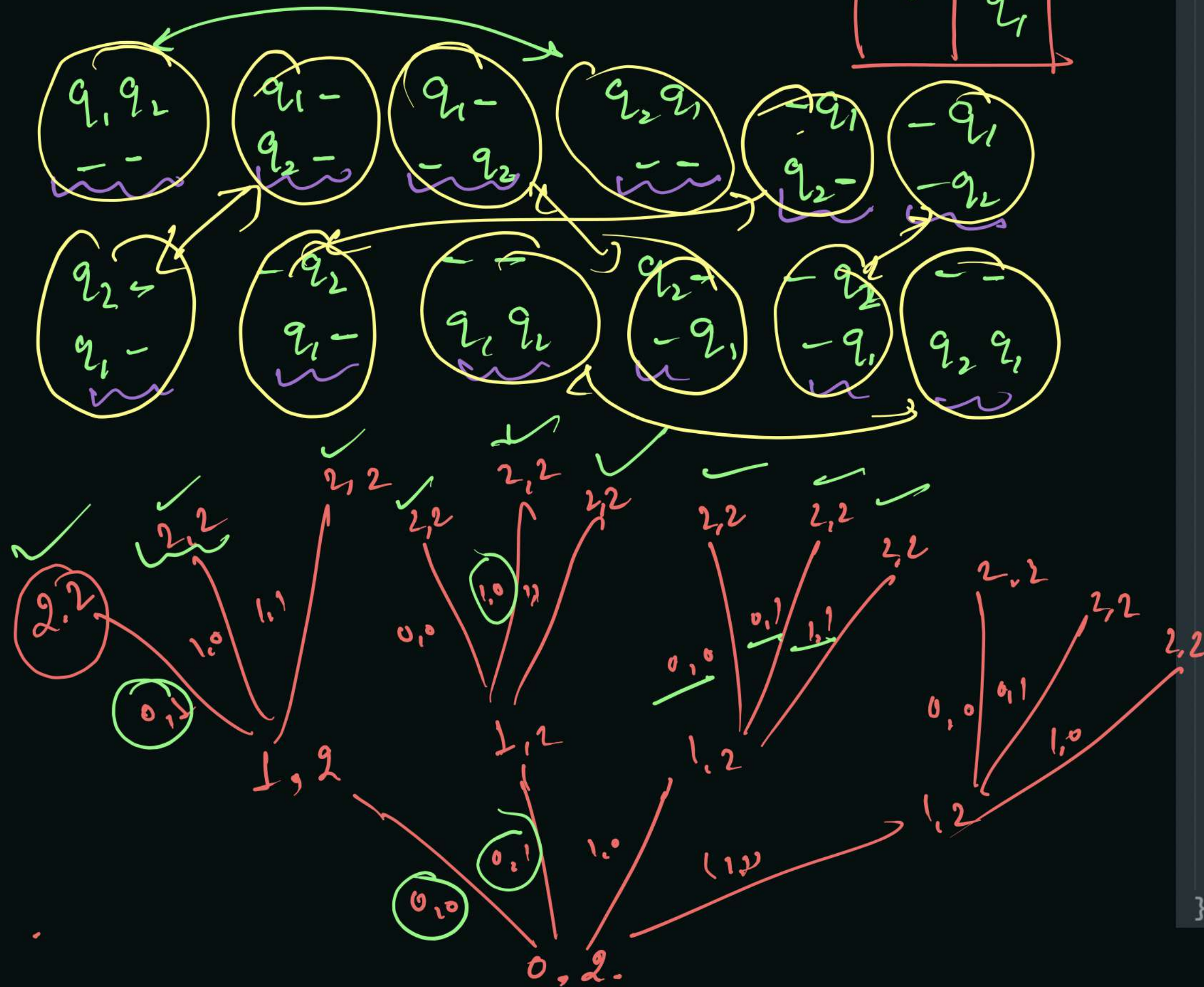
print result

}

level $\rightarrow 2$

option \rightarrow boxes

:	:
.	q ₁



```
public static void queensPermutations(int qpsf, int tq, int[][] chess){
    if(qpsf == tq) {
        // print result
        for(int i = 0; i < chess.length; i++) {
            for(int j = 0; j < chess[0].length; j++) {
                if(chess[i][j] != 0) {
                    System.out.print("q" + chess[i][j] + "\t");
                } else {
                    System.out.print("-\t");
                }
            }
            System.out.println();
        }
        System.out.println();
        return;
    }

    for(int i = 0; i < chess.length; i++) {
        for(int j = 0; j < chess[0].length; j++) {
            if(chess[i][j] == 0) {
                // place queen
                chess[i][j] = qpsf + 1;
                queensPermutations(qpsf + 1, tq, chess);
                // unplace queen
                chess[i][j] = 0;
            }
        }
    }
}
```

$$\begin{pmatrix} i_1 & i_2 \\ 0 & 0 \end{pmatrix} \quad \begin{pmatrix} i_2 & i_1 \\ 0 & 0 \end{pmatrix}$$

$n \times n$ - chessboard,

n -queens, (non identical) print

level \rightarrow Boxes

option \rightarrow queen.

all possible

ways to

arrange

these queens.

Yes or No

$${}^n C_r = \frac{n!}{(n-r)! r!}$$

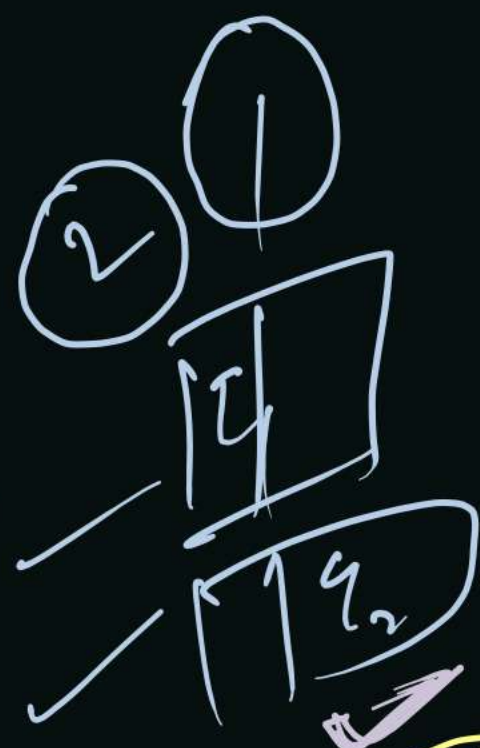
$${}^n P_r = \frac{n!}{(n-r)!}$$

$${}^n P_r = {}^n C_r \times r!$$

$n=3$

$3P_2$

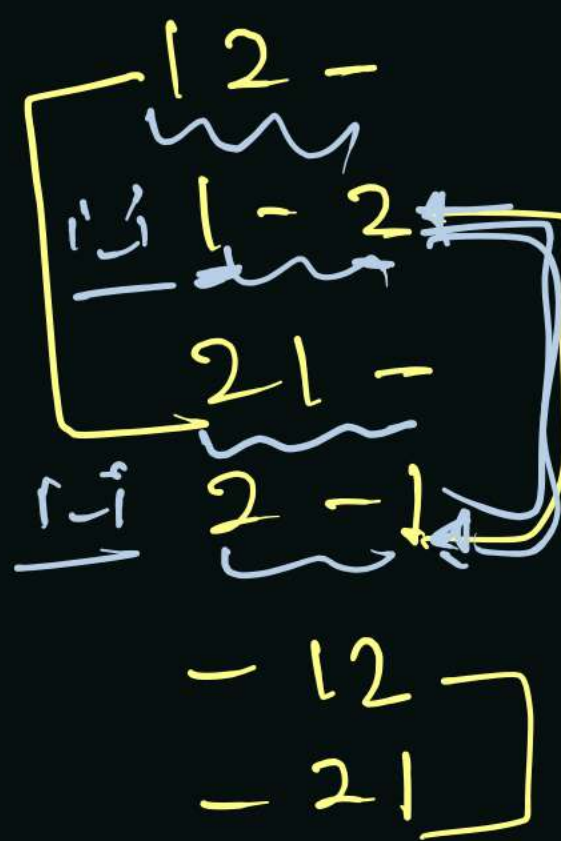
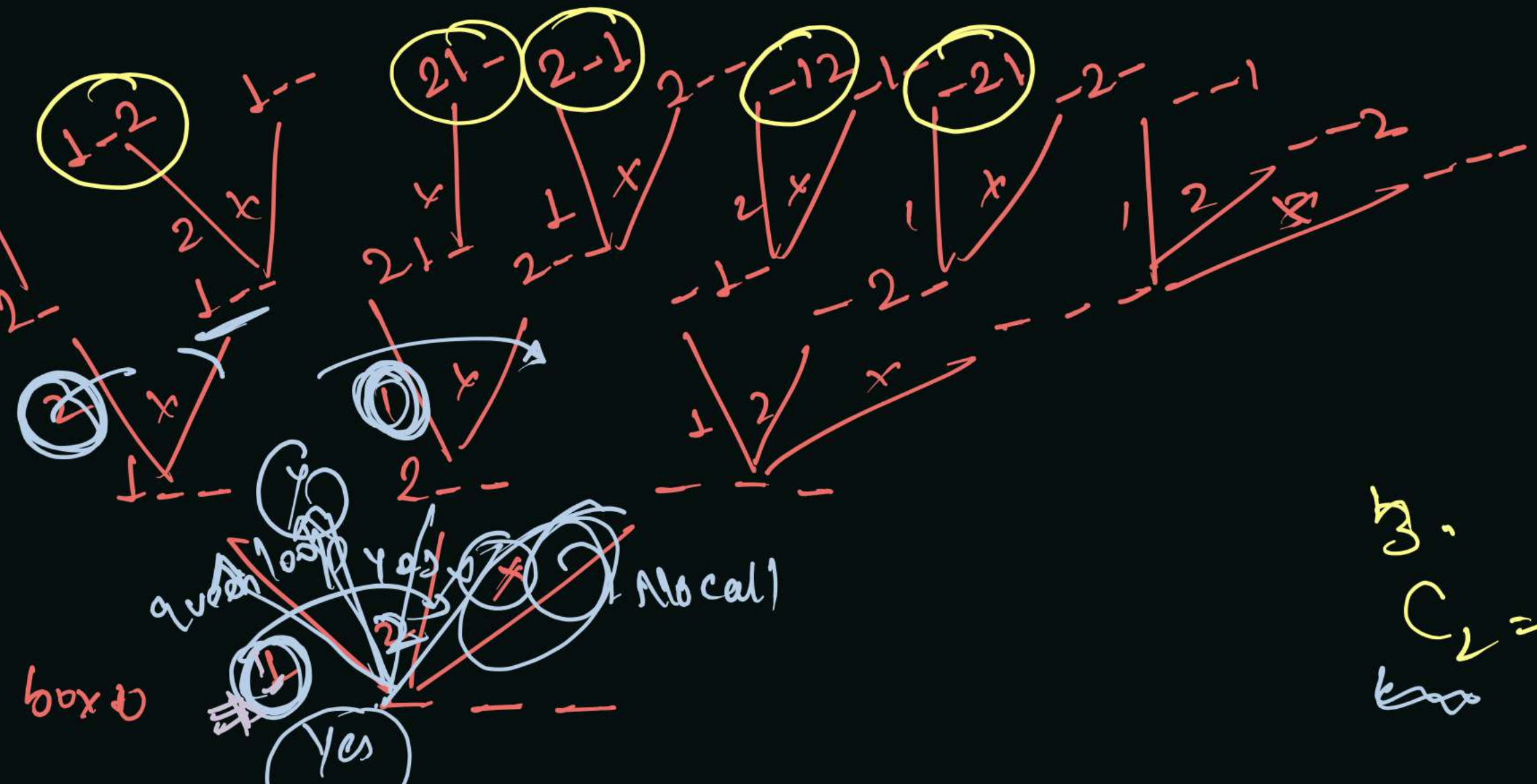
$3P_2$



box 2.

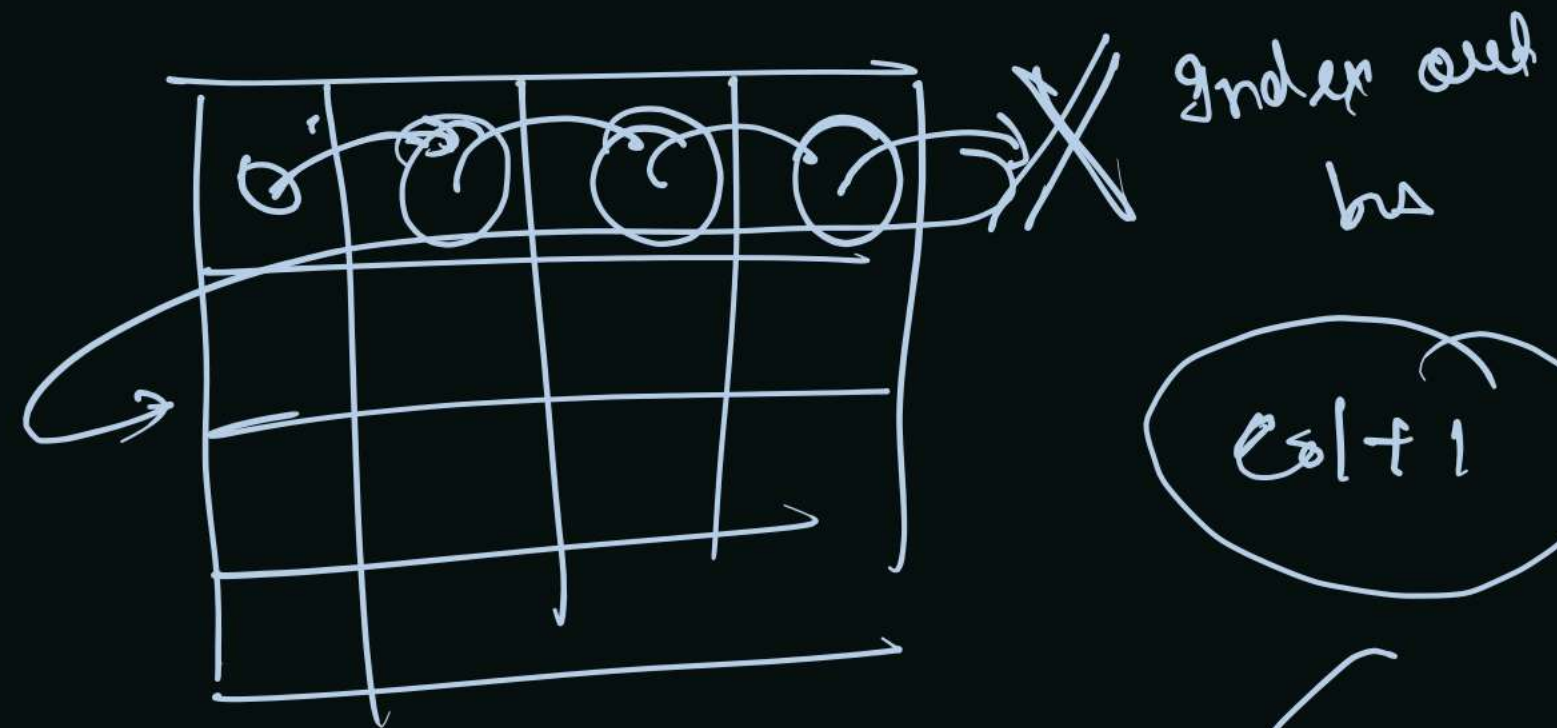
box 1

box 0



$${}^3 C_2 = \frac{3!}{1! 2!} = 3$$

$$3 \times 2! = 6$$



$col + 1$ out of bounds

$row + 1, col = 0$

$-1/n$
 $-q_1$
 q_1, q_2

String,
arr

row, col,
 $\downarrow \downarrow$
 box
 for current
 level

green array
 \downarrow
 to figure out

which
 item / green
 has already
 placed in
part

$n \times n$ - chess board,

n - queens (identical)

print all possible arrangement

level \rightarrow queens

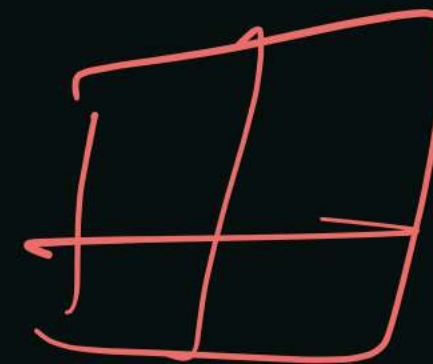
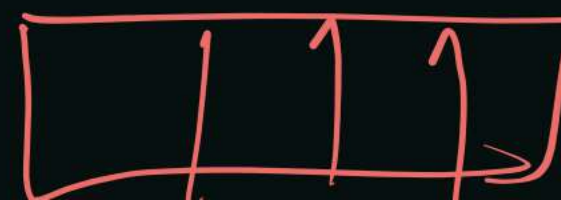
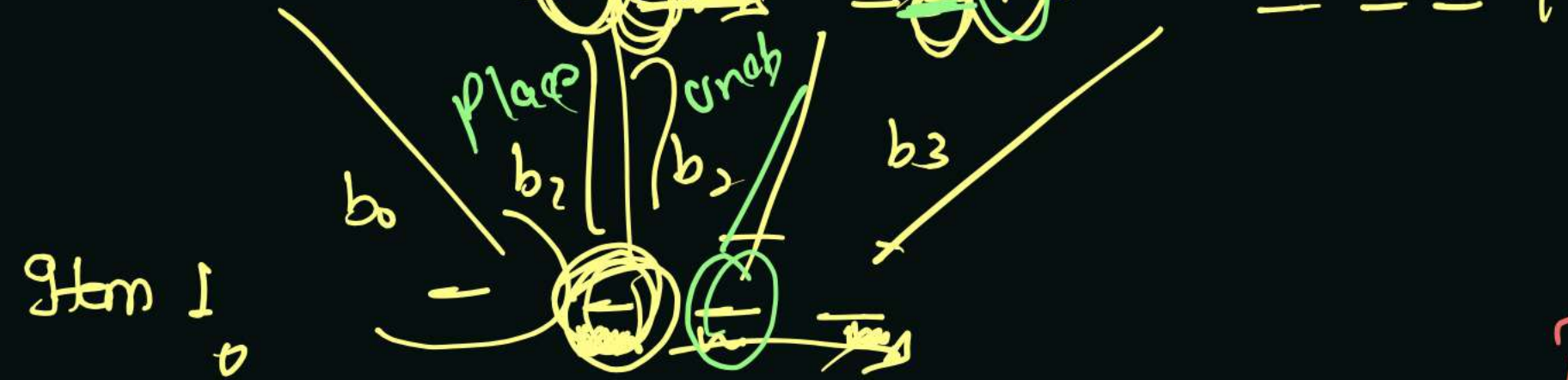
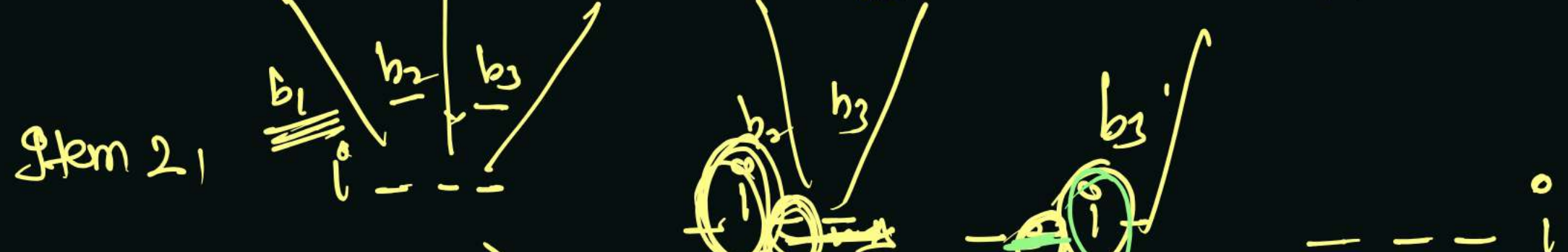
option \rightarrow boxes

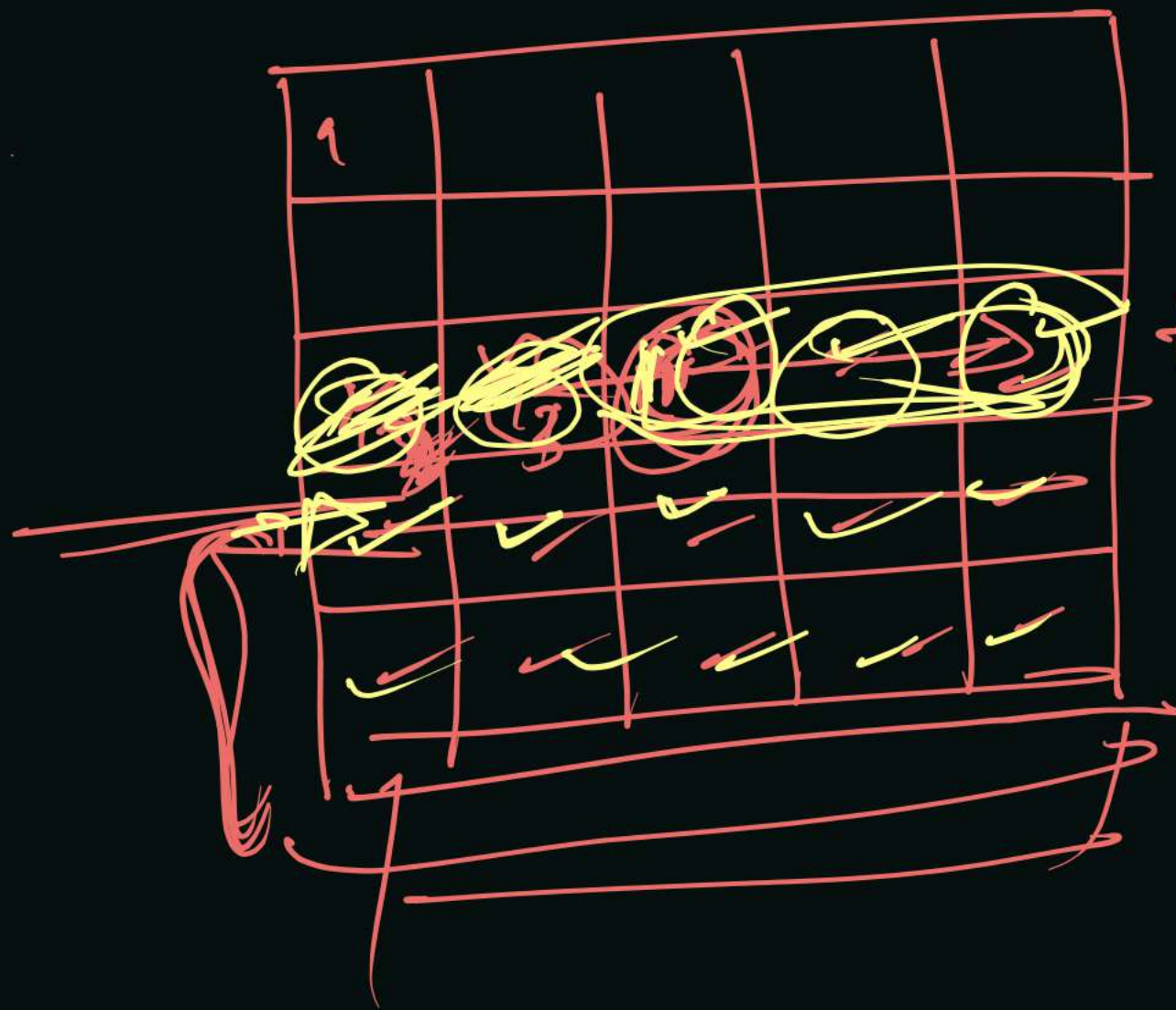
4 \rightarrow boxes

3 - items



$${}^4C_3 = \frac{4!}{3!1!} = 4$$





treat as option

c_9, t_9

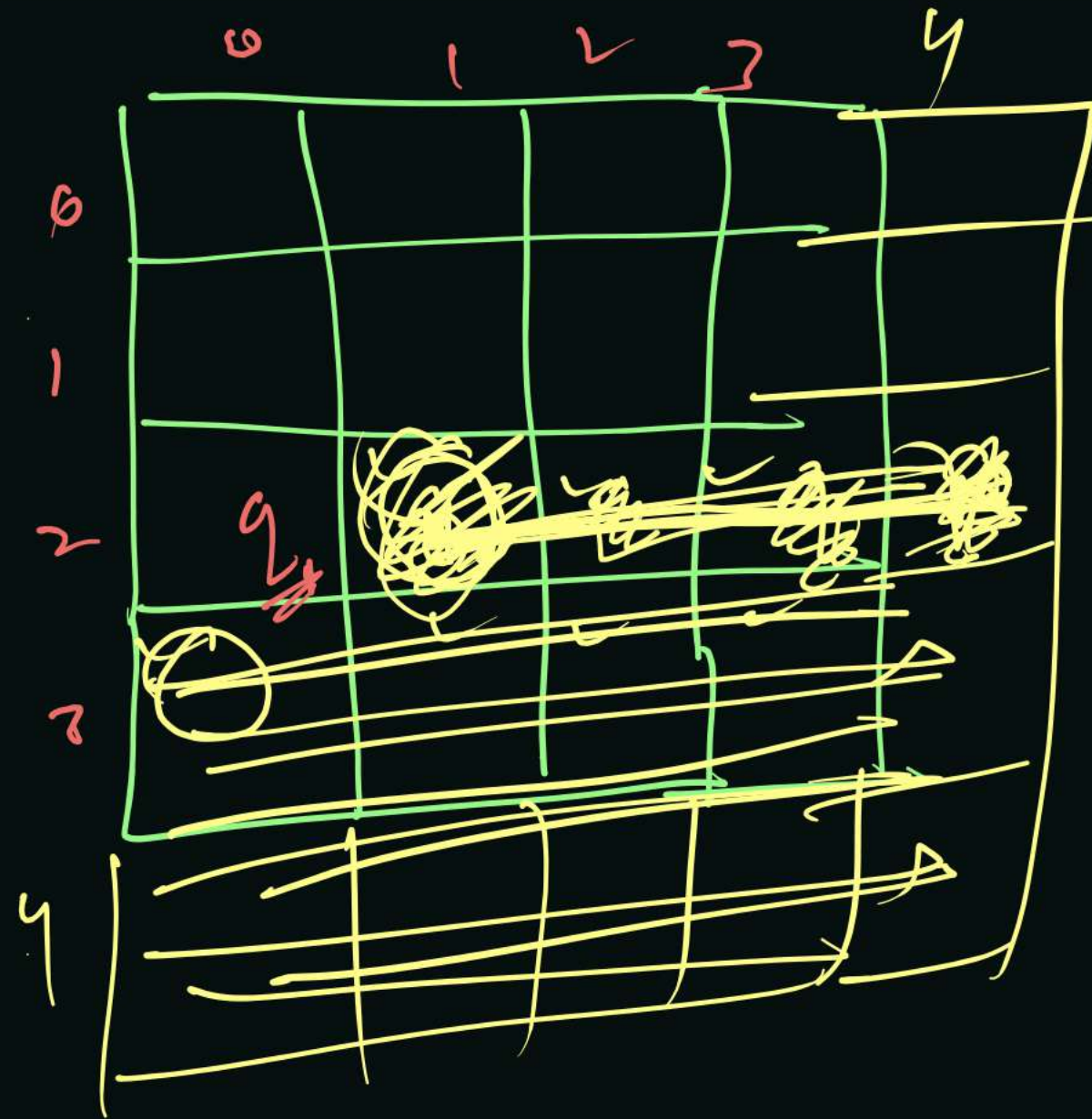
row, col

String

Booleans

in a current row
remaining
col.

remaining row \times col



remaining col
 (4, 2, 0, chess)

```
// travel in remaining columns in current row
for(int c = j + 1; c < chess[0].length; c++) {
    int r = i;
    // place
    chess[r][c] = true;
    queensCombinations(qpsf + 1, tq, chess, r, c);
    // unplace
    chess[r][c] = false;
}
```

```
// travel in remaining rows and columns
for(int r = i + 1; r < chess.length; r++) {
    for(int c = 0; c < chess[0].length; c++) {
        // place
        chess[r][c] = true;
        queensCombinations(qpsf + 1, tq, chess, r, c);
        // unplace
        chess[r][c] = false;
    }
}
```