

Quick Select

Sunday, 2 May 2021 9:58 AM

find k^{th} smallest?

arr \rightarrow { 80, 10, 20, 90, 70, 60, 40, 30, 50 }

0 1 2 3 4 5 6 7 8

$k=3$

partition Index \rightarrow

quickselect

correct position

pivot = arr[hi] \rightarrow

$pi = \text{partitionIndex}(arr, lo, hi)$ \rightarrow

\swarrow sorted position

$lc \leftarrow lo$ sorted

if ($pi == k$) {
 answer is \rightarrow pivot
} else if ($pi > k$) {
 answer is on left side
} else if ($pi < k$) {
 answer is on Right side
}

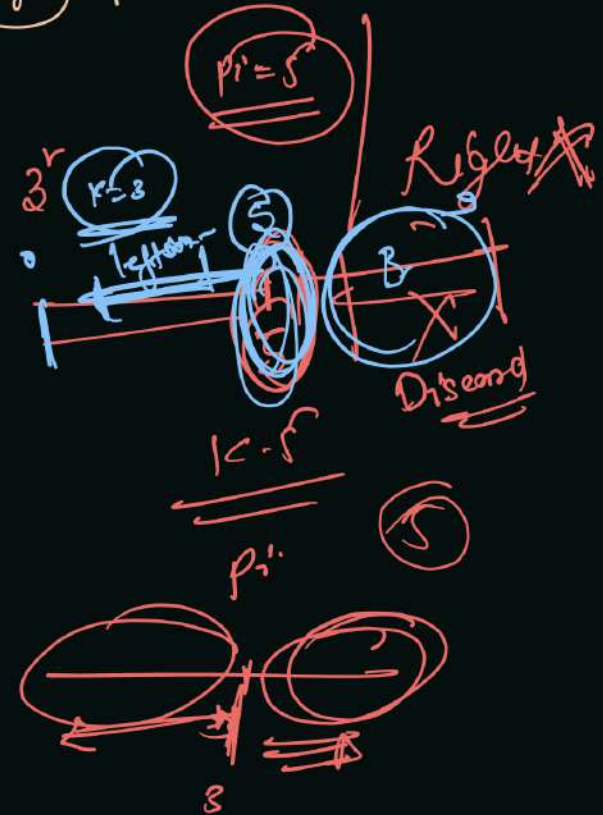
Brute force
 $n \log n$

① Sort Array

10 20 30 40 50 60 70 80 90

think in more optimised Approach.

$n \log k$ heap not allowed X



arr → { 90 20 10 70 50 40 60 30 }

Call from main → lo
quickSelect(arr, lo, hi, k)

Index

hi

```
public static int quickSelect(int[] arr, int lo, int hi, int k) {
    int pivot = arr[hi];
    int pi = partitionIndex(arr, lo, hi, pivot);

    int ans = 0;
    if (pi == k) {
        // found
        ans = pivot;
    } else if (pi > k) {
        // answer is on left side
        ans = quickSelect(arr, lo, pi - 1, k);
    } else {
        // answer is on right side
        ans = quickSelect(arr, pi + 1, hi, k);
    }
    return ans;
}
```

~~pi = 30~~ 60

pi = 5

pi < k

if

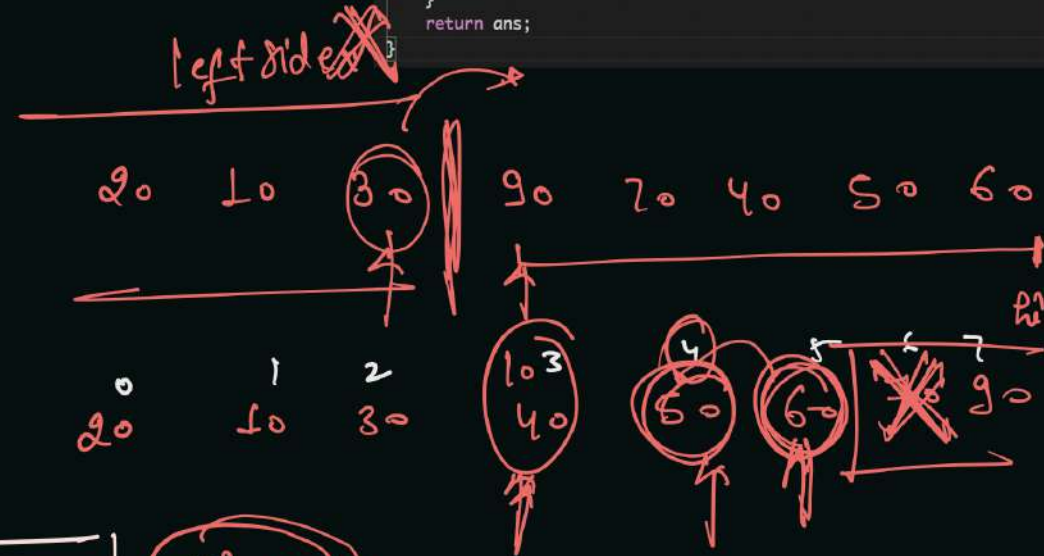
pi = 5

pi > k

pi == k

complexity →

$O(n)$ Best



Complexity Analysis \rightarrow (Assumption for quick select/quick sort), $p_i = \underline{\text{mid}}$

overall \rightarrow $T(n) = n + T(n/2) + k$ \rightarrow (1)

$n \rightarrow n/2$

$T(n/2) = n/2 + T(n/4) + k \rightarrow$ (2)

$n \rightarrow n/2$

$T(n/4) = n/4 + T(n/8) + k \rightarrow$ (3)

$n \rightarrow n/2$

$T(n/8) = n/8 + T(n/16) + k$

x times

$T(n/2^{x-1}) = n/2^{x-1} + T(n/2^x) + k$

Assumption

$T(1) = 1$

Base case

$\frac{n}{2^x} = 1$

$n = 2^x$

$\log_2 n = \log_2 2^x$

$x = \log_2 n$

Add all eq \rightarrow

$T(n) = T(1) + n + \frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \dots$

$\frac{n}{2^{x-1}} + kx$

$= 1 + n \left[1 + \frac{1}{2} + \frac{1}{4} + \dots + \frac{1}{2^{x-1}} \right] + kx$

$$a=1, r=\frac{1}{2}, n \geq x$$

$$= 1 + n \left[\frac{1 - \left(\frac{1}{2}\right)^x}{\frac{1}{2}} \right]$$

$$= 1 + 2n \left[1 - 2^{-\log_2 n} \right] + kx$$

$$= 1 + 2n \left[1 - \frac{1}{n} \right] + k \log n$$

$$= 1 + 2n - 2 + \frac{2}{n} + k \log n$$

$$T(n) = 2n + k \log n + \text{constant}$$

Order =

$$O(n)$$

$$(2^{-1})^2 = 2^{-2} \left(\frac{1}{2}\right)^2 = \frac{1}{4}$$

$$a, ar, ar^2, ar^3, \dots, ar^{n-1}$$

Sum of
G.P.

$$ar^{n-1}$$

$$= \frac{a(r^n - 1)}{r - 1} = \frac{a(1 - r^n)}{1 - r}$$

$$a^{c \log_a b} = a^{\log_a b^c} = b^c$$

$$x = \log_2 n$$

$$\frac{a}{1-r}$$

Infinite

G.P.

$$a=2, b=n, c=-1$$

$$\left(\frac{1}{2}\right)^x = 2^{-x}$$

$$= 2^{-\log_2 n}$$

$$\log_2 n = n^{-1} = \frac{1}{n}$$

$$a \log_c b^a$$

Target Sum Pair

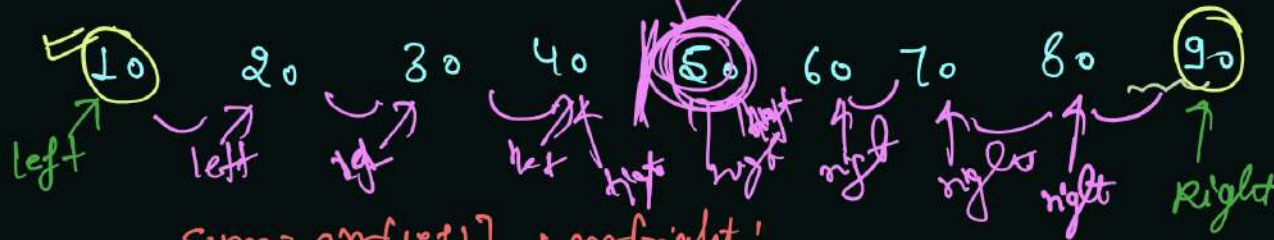
Sunday, 2 May 2021 9:58 AM

arr \rightarrow {90, 60, 70, 50, 40, 10, 30, 20, 80}
 target = 100
 print all possible pair.

allowed complexity $O(n \log n)$

② Optimisation

Sort the array.



sum = arr[left] + arr[right];

if (sum == target) {
 print (arr[left] + " " + arr[right]);
 left++;
 right--;

} else if (sum > target) {
 right--;

} else if (sum < target) {
 left++;

}

Brute force \rightarrow

val1 = 90
 val2 \rightarrow 100
 val1 + val2 = target - val1
 90 10
 60 40
 70 30

left = 10
 right = 90

while (left < right)

10 80
 20 70
 30 60
 40 50

Pivot in Sorted Rotated Array

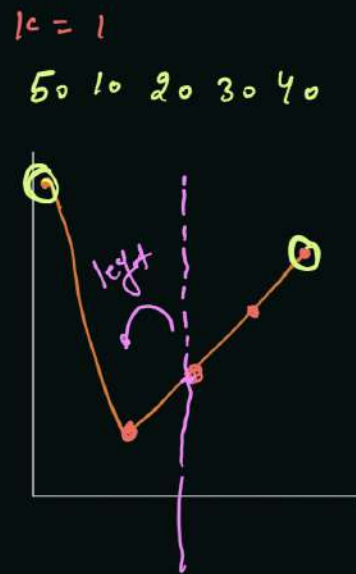
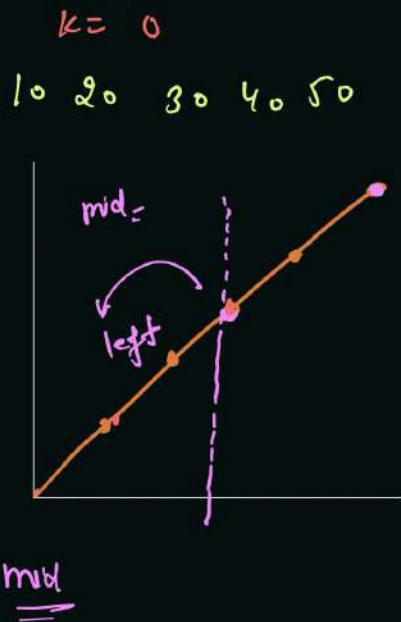
Sunday, 2 May 2021 9:59 AM

arr \rightarrow 30 40 50 10 20
 pivot \rightarrow smallest element

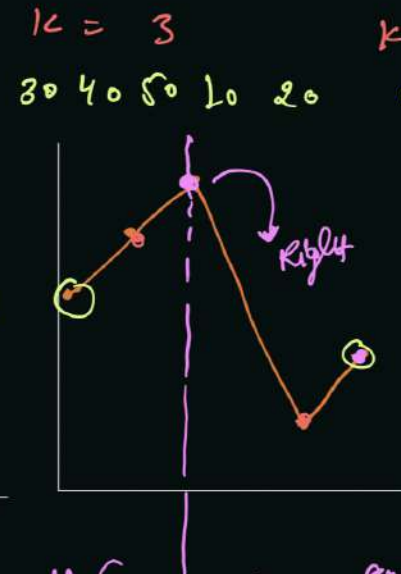
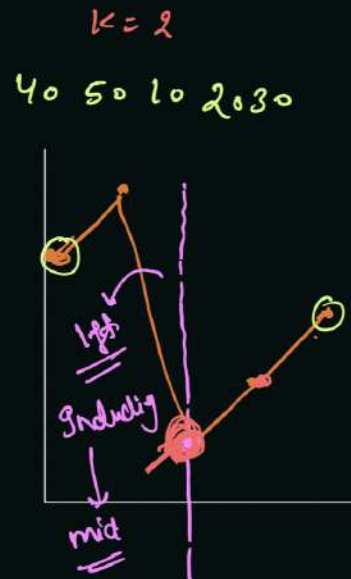
$k=3$

sorted
 arr \rightarrow 10 20 30 40 50

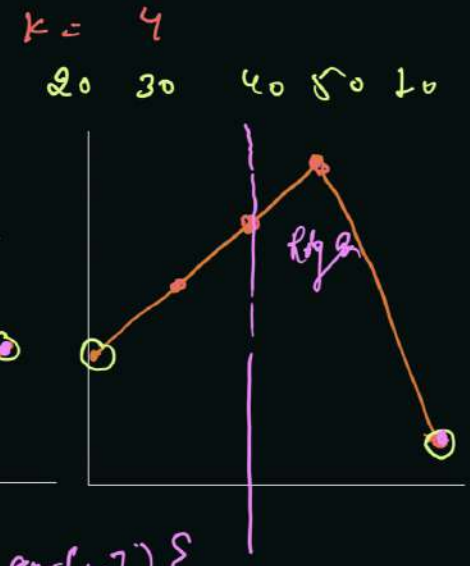
① Bruteforce \rightarrow travel final min $\rightarrow O(n)$
 allowed complexity $\rightarrow O(\log n)$



if (arr[mid] < arr[l])
 left side } including mid



if (arr[mid] > arr[l])
 right side
 }



{ 4₀ 5₁ 6₂ 7₃ 8₄ 9₅ 10₆ 2₇ 3₈ }

right
↑
mid = 5
5, 6

left

mid = 6
5, 8

right

mid = 4
0, 8

(lo == hi)

ans = arr[lo],

ans = arr[hi],

```
public static int pivotInSortedRotated(int[] arr, int lo, int hi) {
    int mid = lo + (hi - lo) / 2;

    int res = 0;

    if(arr[mid] < arr[hi]) {
        // left side -> including mid
        res = pivotInSortedRotated(arr, lo, mid);
    } else {
        // right side
        res = pivotInSortedRotated(arr, mid + 1, hi);
    }

    return res;
}
```

Binary Search

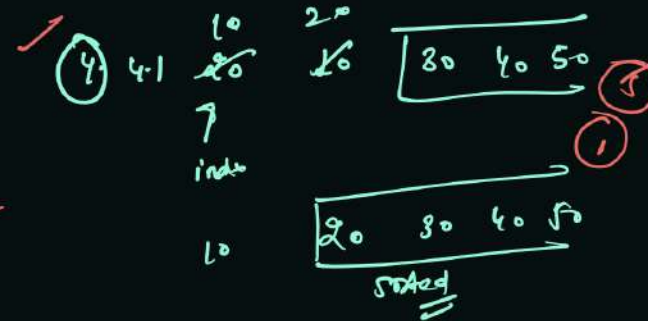
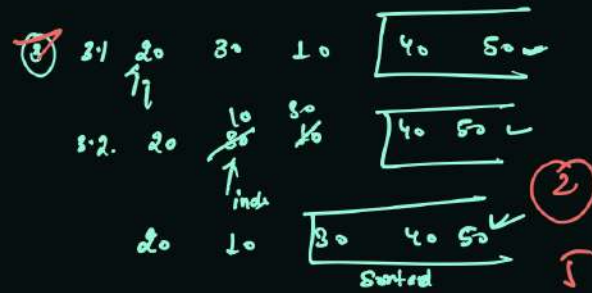
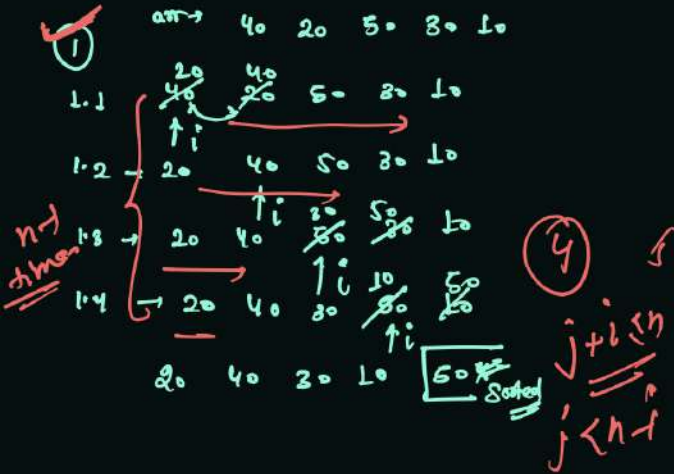
ans lo == hi
distinct
Definitely
ans / 1

Bubble Sort

Sunday, 2 May 2021 9:58 AM

arr → 40 20 50 30 10

final array = 10 20 30 40 50
after sorting.



Outer loop: $i=0$
Inner loop: $j=0; arr.length-1-i; j++$

$i < arr.length$

$< n-1$

0, 1, 2, 3 < 4

Selection Sort

Sunday, 2 May 2021 9:58 AM

arr → 40 20 50 30 10

① → 0.0 10 20 50 30 40 minIndex = 0
 0.1 40 20 50 30 50 minIndex = 1
 0.2 40 20 50 30 10 minIndex = 1
 0.3 40 20 50 30 10 minIndex = 1
 0.4 40 20 50 30 10 minIndex = 4

swap(arr, i, minIndex);

10 20 50 30 40
 Sorted

outer loop ②
 $i = 0 \rightarrow n-1$
 minIndex

10 20 30 50 40
 Sorted 1
 30 50 40
 30 40

③

10 20 30 40 50
 Sorted

① 1.0 10 20 50 30 40 min = 1
 1.1 10 20 50 30 40 min = 1
 1.2 10 20 50 30 40 min = 1
 1.3 10 20 50 30 40 min = 1
 swap(arr, i, min);
 10 20 50 30 40
 Sorted

Random → // quick sort
 pivot
 arr