

# Simulating Supermassive Binary Black Holes

Vikram Manikantan

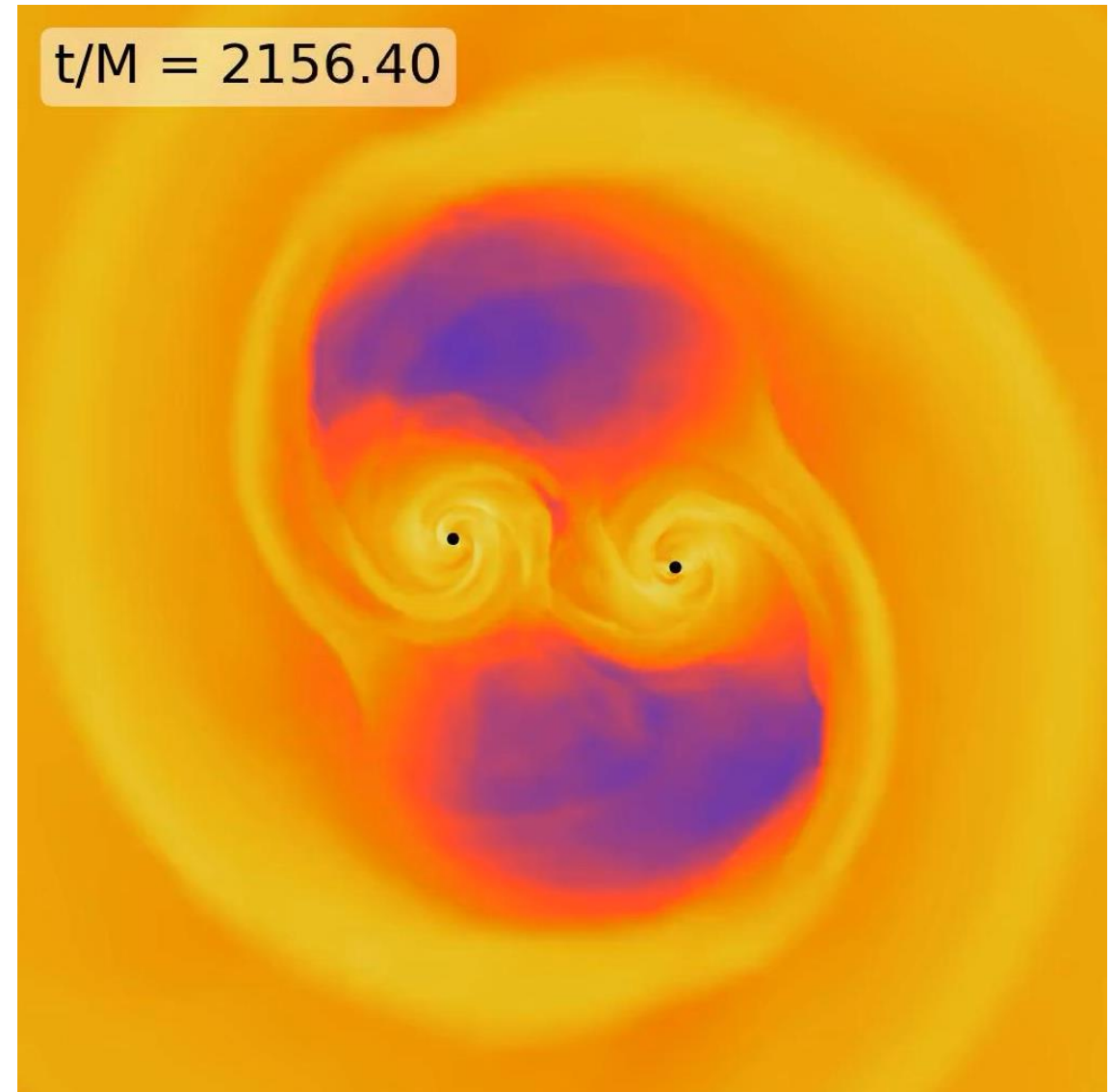


Astronomy  
& Steward Observatory

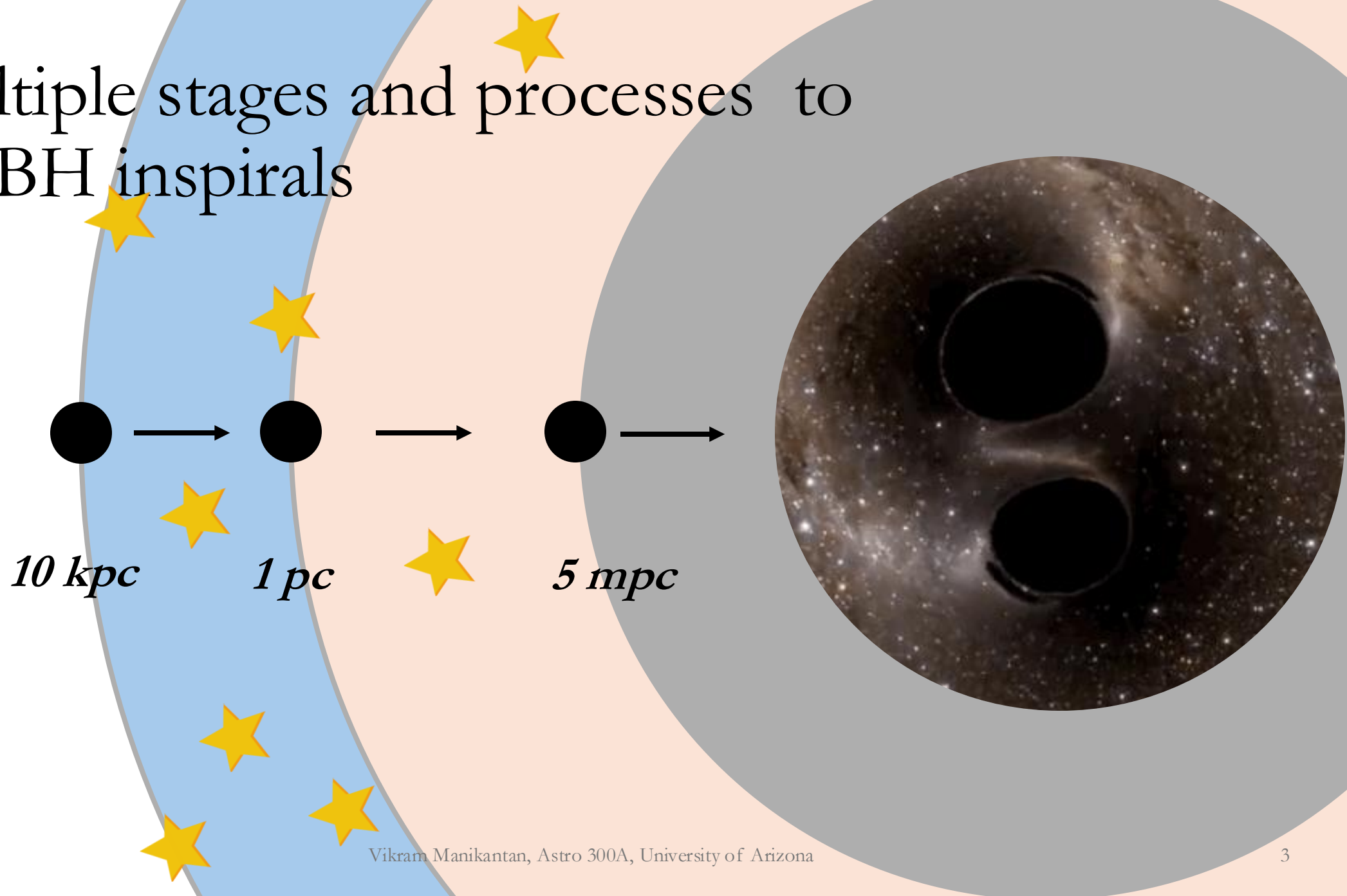


# Today

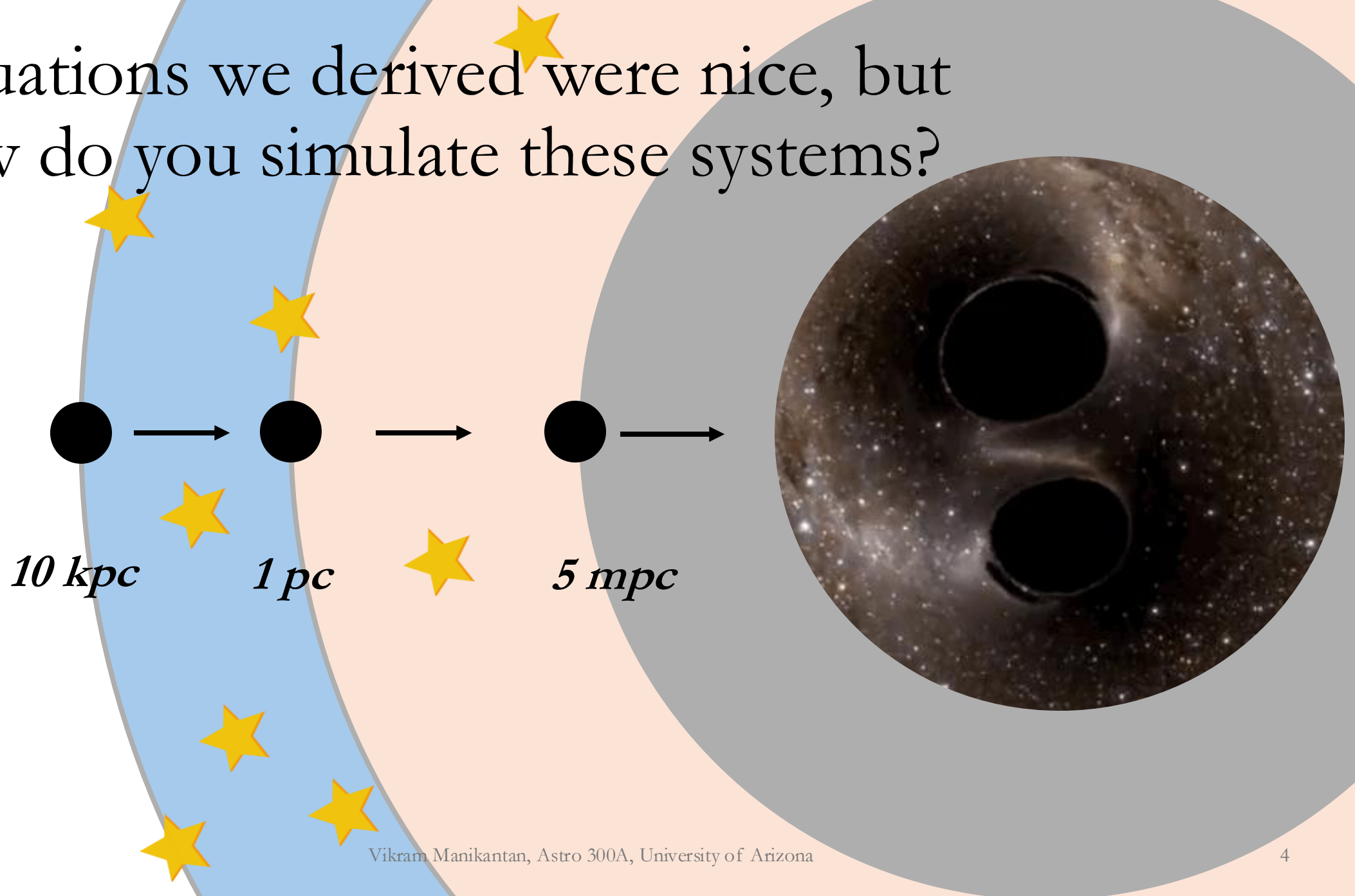
1. Tell you about my research!
2. In-class activity: working with simulated gravitational waveforms



# Multiple stages and processes to SMBH inspirals

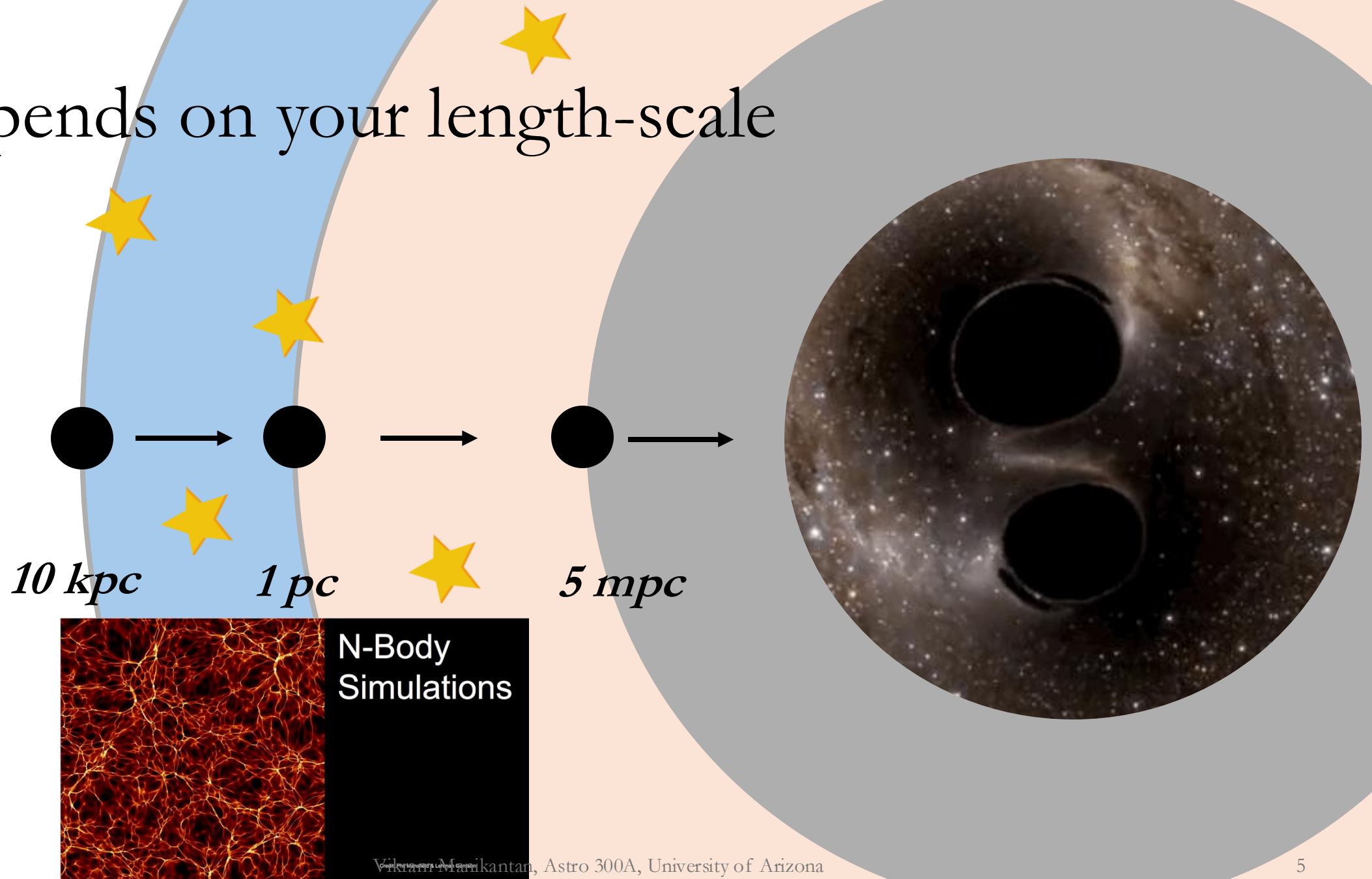


Equations we derived were nice, but  
how do you simulate these systems?

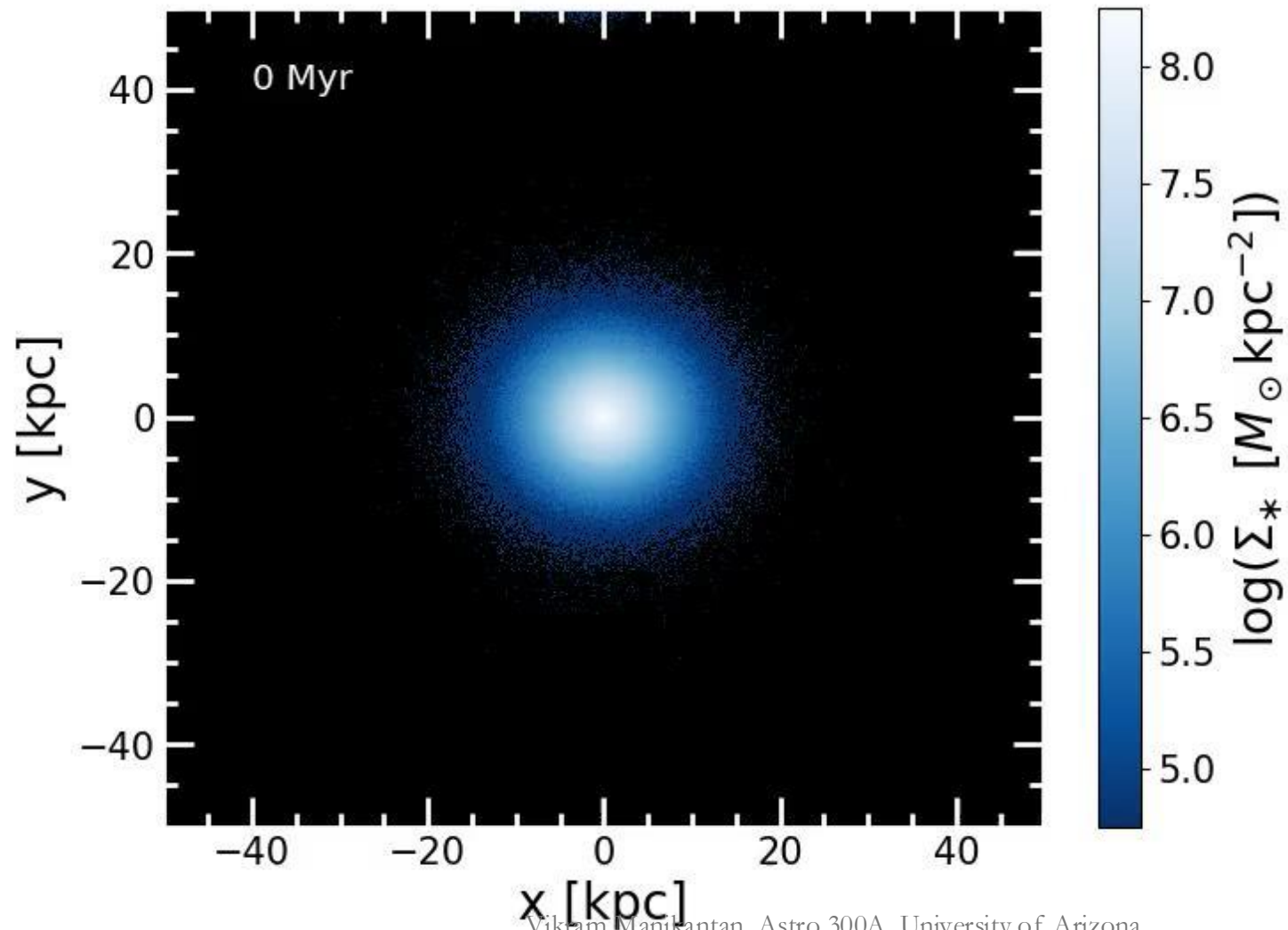




# Depends on your length-scale

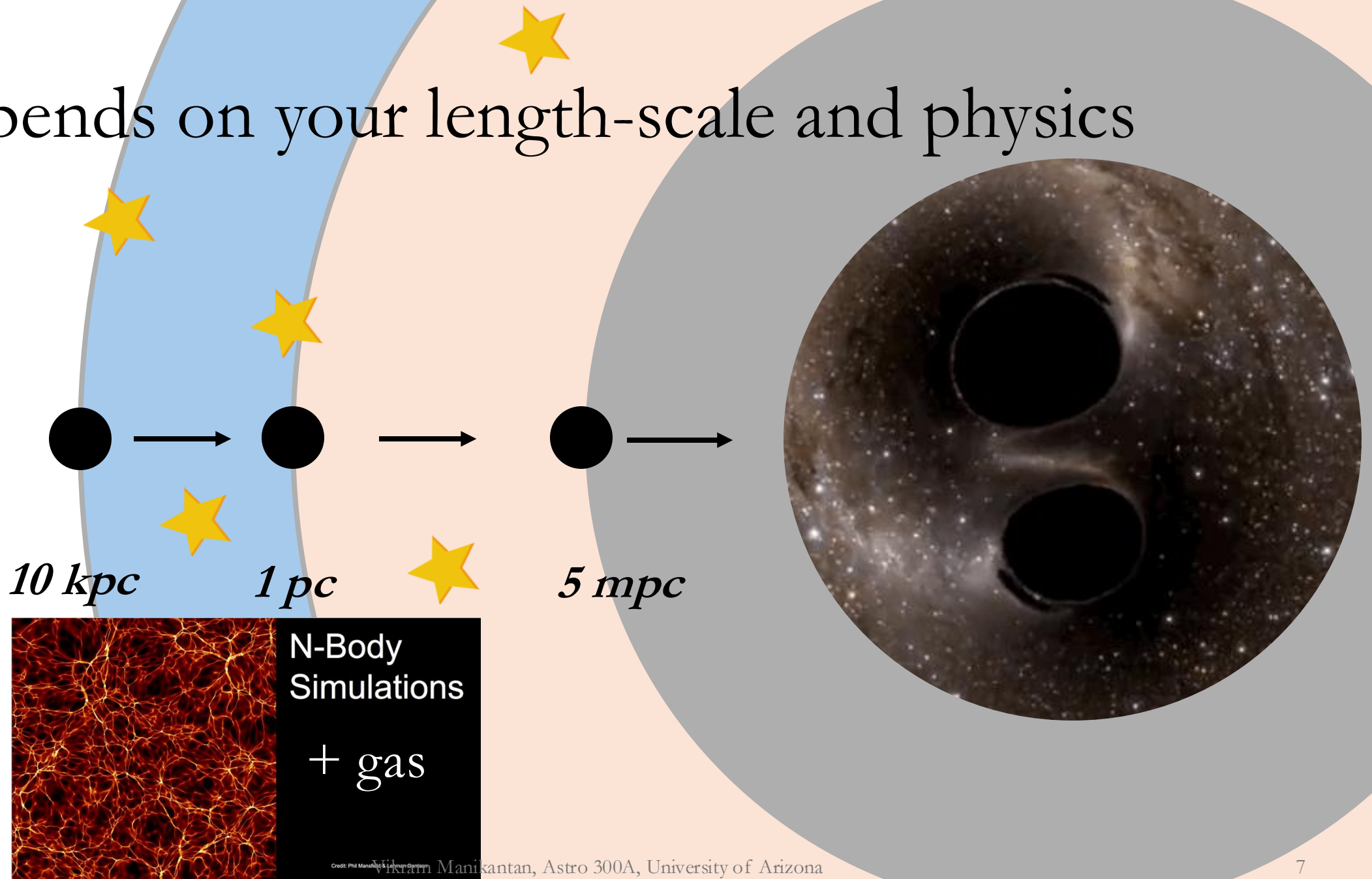


# N-body galaxy merger simulations



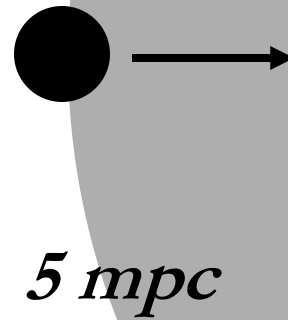
From Himansh Rathore,  
3<sup>rd</sup> year graduate student  
working with Prof.  
Gurtina Besla

# Depends on your length-scale and physics



# Sub 5mpc, we called the GW-driven regime

- This is where  $t_0$  was less than the Hubble time
- In other words, the effects of gravitational waves were **significant**
- So, we need to consider general relativity (rather than Newtonian gravity)





# More than GR, there are also fluids

- This is where  $t_0$  was less than the Hubble time
- In other words, the effects of gravitational waves were **significant**
- So, we need to consider general relativity
- But, there is also lots of material hanging around we have to model



*5 mpc*



# Suddenly, it is more complex

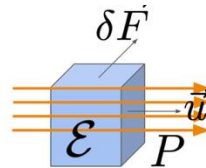
- We need general relativity:

$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

- And, we also need fluid dynamics!

$\rho$  – density  
 $\vec{u}$  – bulk motion  
 $P$  – pressure  
 $\mathcal{E}$  – internal energy density ( $n, T$ )

Fluid dynamics



$$\frac{\partial \rho}{\partial t} = -\vec{\nabla} \cdot (\rho \vec{u})$$

$$\frac{\partial \tilde{E}}{\partial t} = -\vec{\nabla} \cdot [\vec{u} (\tilde{E} + P)] + \rho \vec{u} \cdot \vec{g} + \Gamma - \Lambda$$

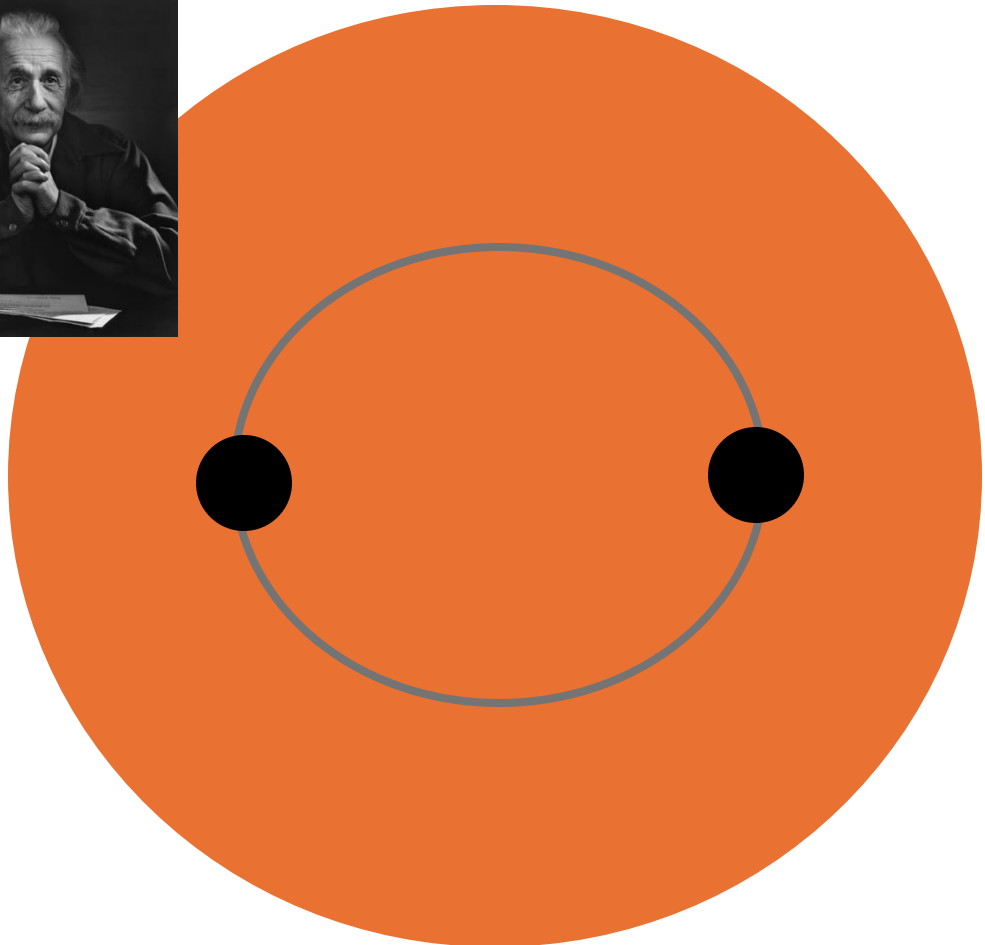
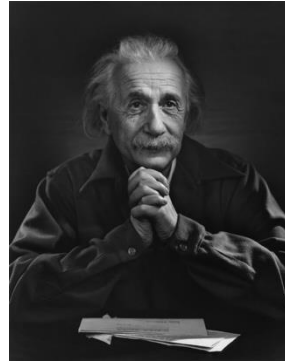
$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \vec{\nabla} \vec{u} = -\frac{\vec{\nabla} P}{\rho} - \vec{\nabla} \Phi$$

Navier-Stokes Equations

Continuity  
 Momentum  
 Energy

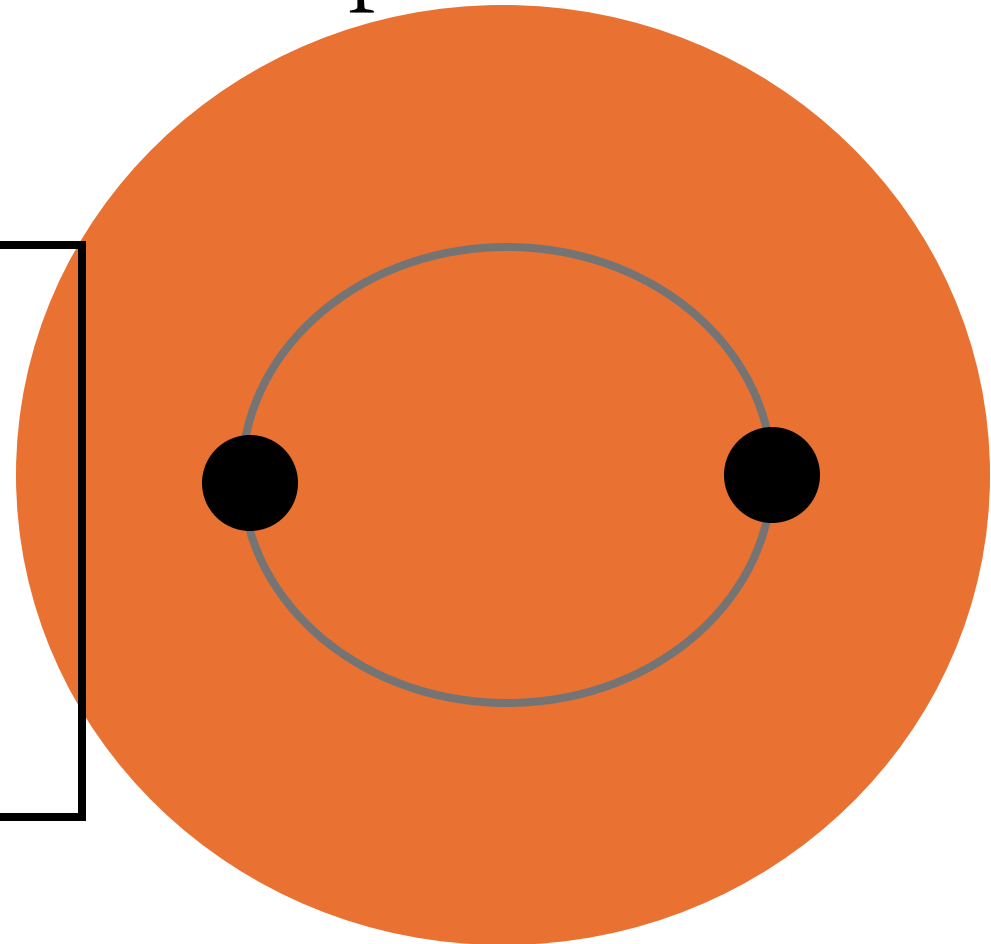
$$\mathcal{E} = \frac{3}{2}P$$

$$\tilde{E} = \frac{1}{2}\rho u^2 + \mathcal{E}$$



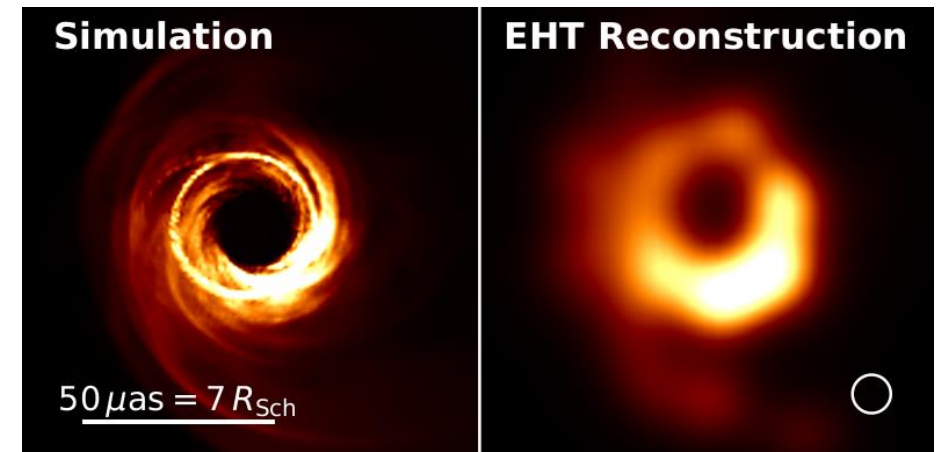
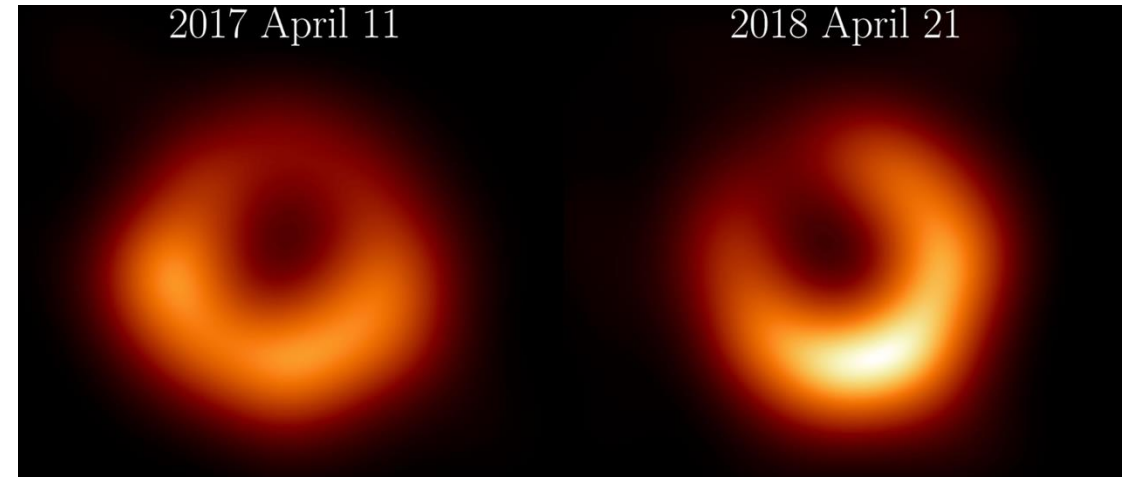
# In fact, the picture is so much more complicated!

- Self-gravitating N-body simulations
  - Dynamical friction
- Fluid Dynamics
  - Accretion, viscosity, winds
- General relativity
  - Gravitational waves, jets
- Magnetic fields
  - Jets would come from here, viscosity, winds
- Radiation?
  - Photons everywhere! Accretion disks, jets, winds



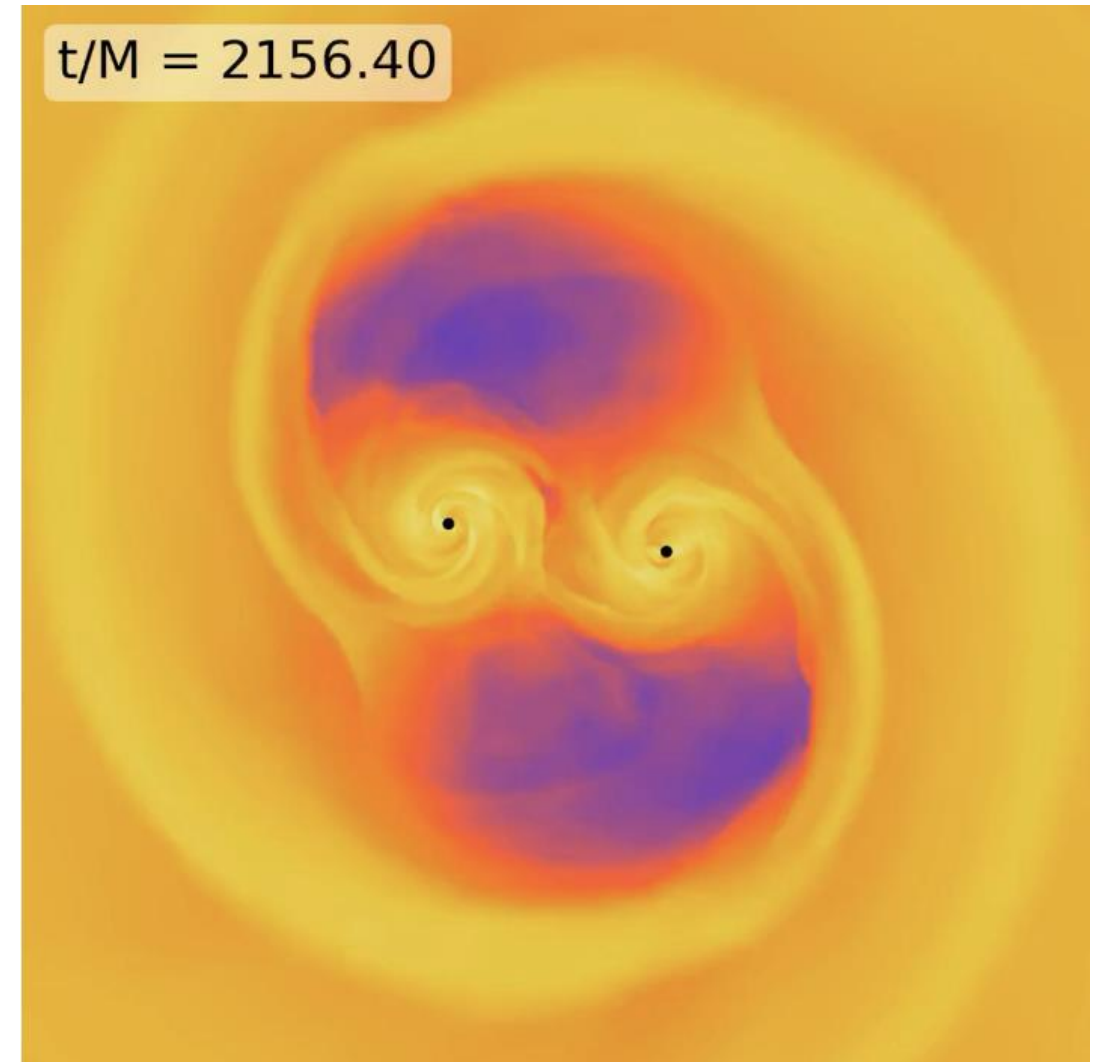
# Simulations can be confirmed and tested now

- By modeling GR and fluid dynamics around black holes, we can predict what they will look like
- Simulations reasonably predict the EHT images!
- We can test our simulations and understanding directly



# GRMHD Simulations

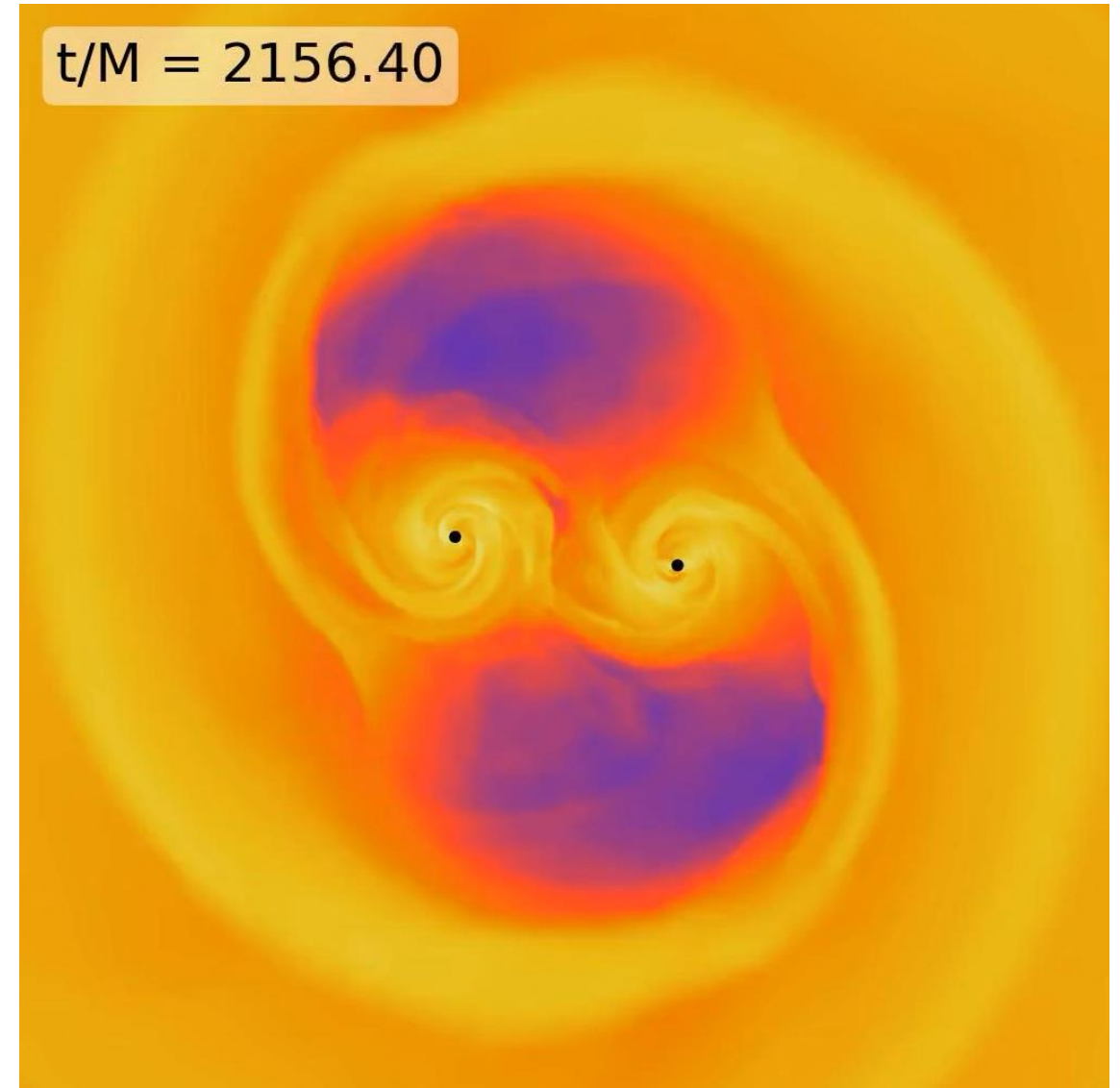
- We do general-relativistic (GR) magnetohydrodynamic (MHD) simulations of binary black holes
- Very expensive – these simulations take months to run on high-performance computing!





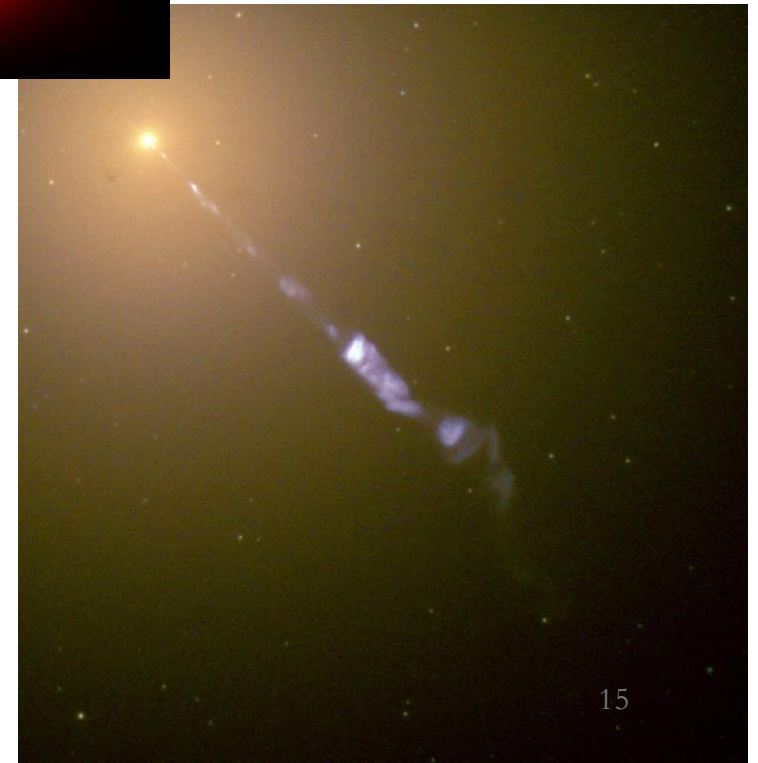
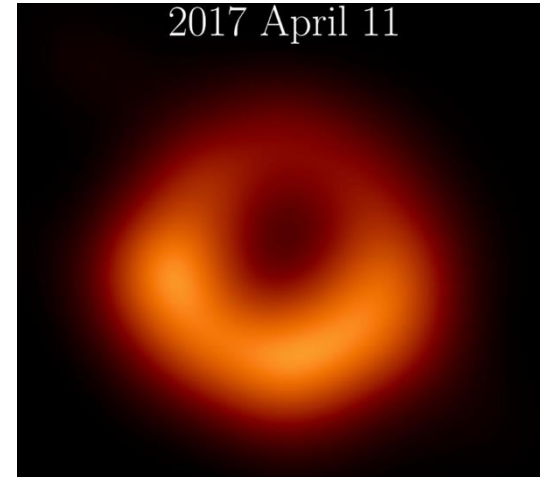
# GRMHD Simulations

- We do general-relativistic (GR) magnetohydrodynamic (MHD) simulations of binary black holes
- Very expensive – these simulations take months to run on high-performance computing!
- These are from ‘first-principles’ (very few assumptions)



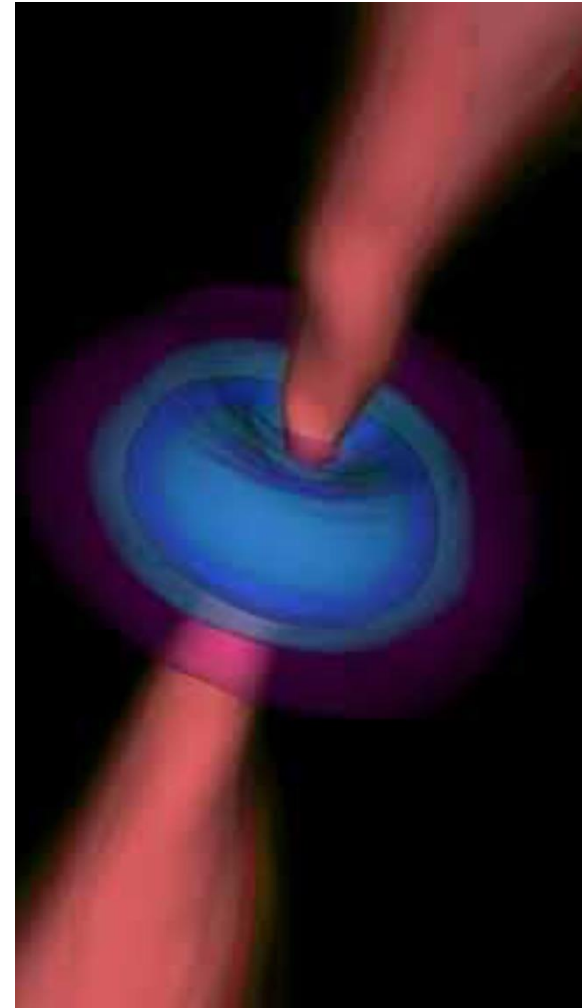
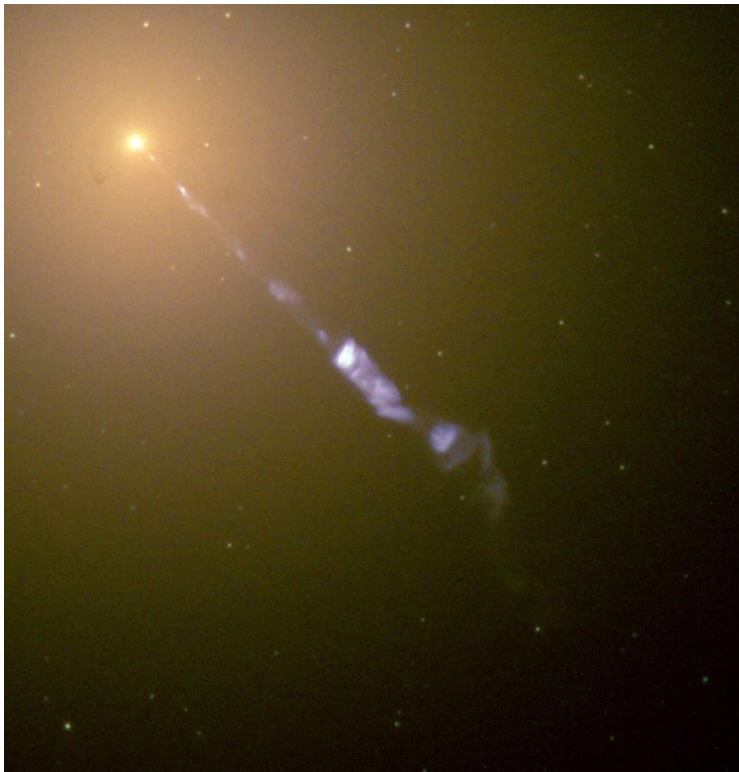
# These BHs also launch jets

- Sometimes known as blazars, quasars, or active galactic nuclei
- These are galactic-scale jets (many kpc) that are powered by black holes (maybe few AU)
- How do they create these outflows?



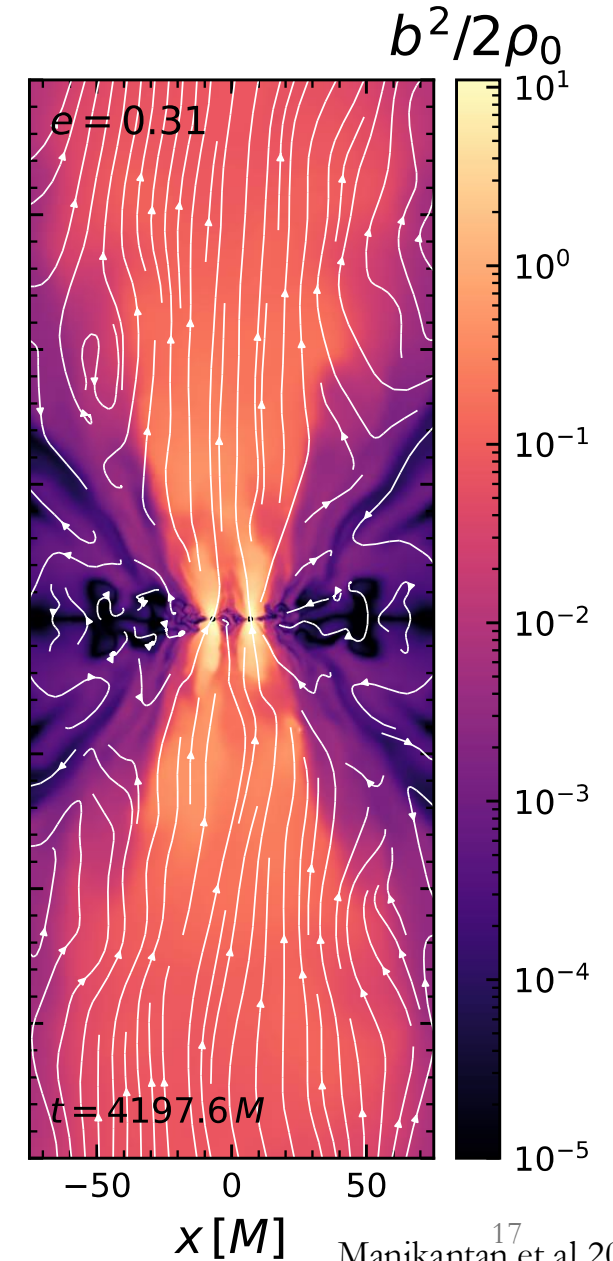
# BHs + magnetic fields launch jets!

- When you combine BHs and magnetic fields, they launch jets!



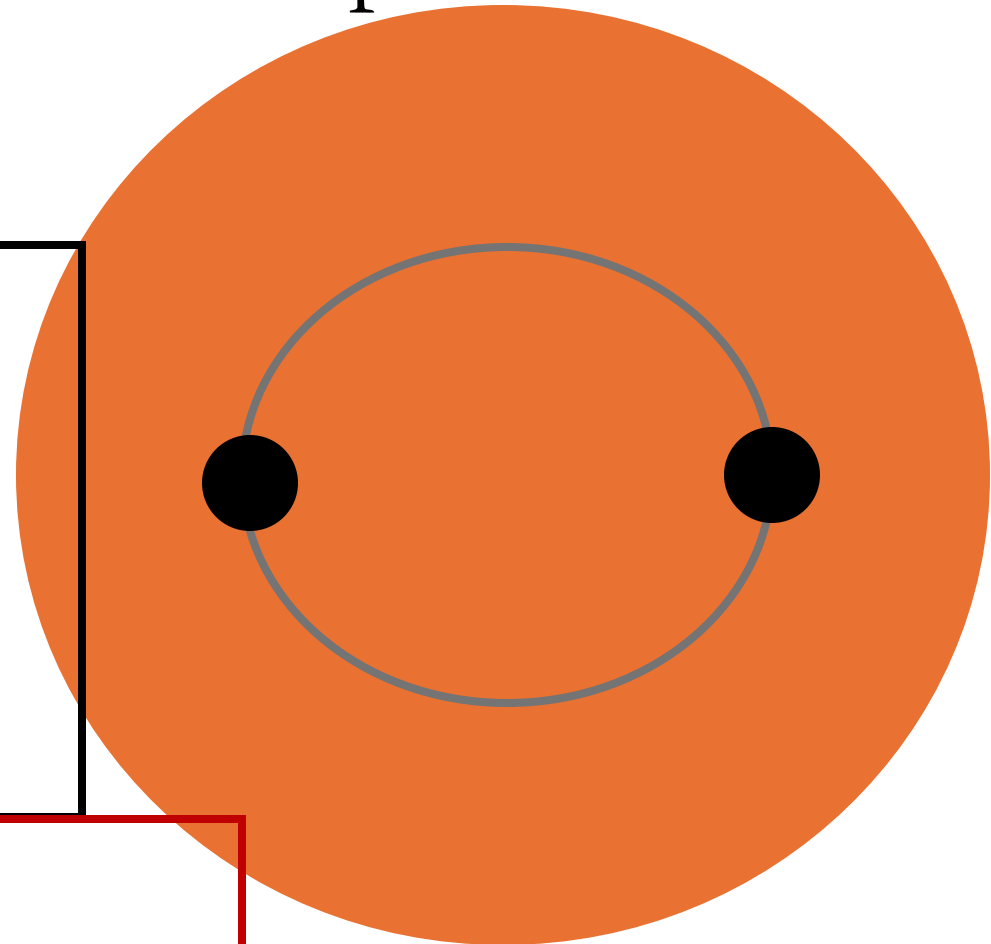
# BBHs + magnetic fields launch jets

- And so do our binary black hole simulations!
- Magnetic fields are very strong near the black hole
- And these help launch relativistic outflows



# In fact, the picture is so much more complicated!

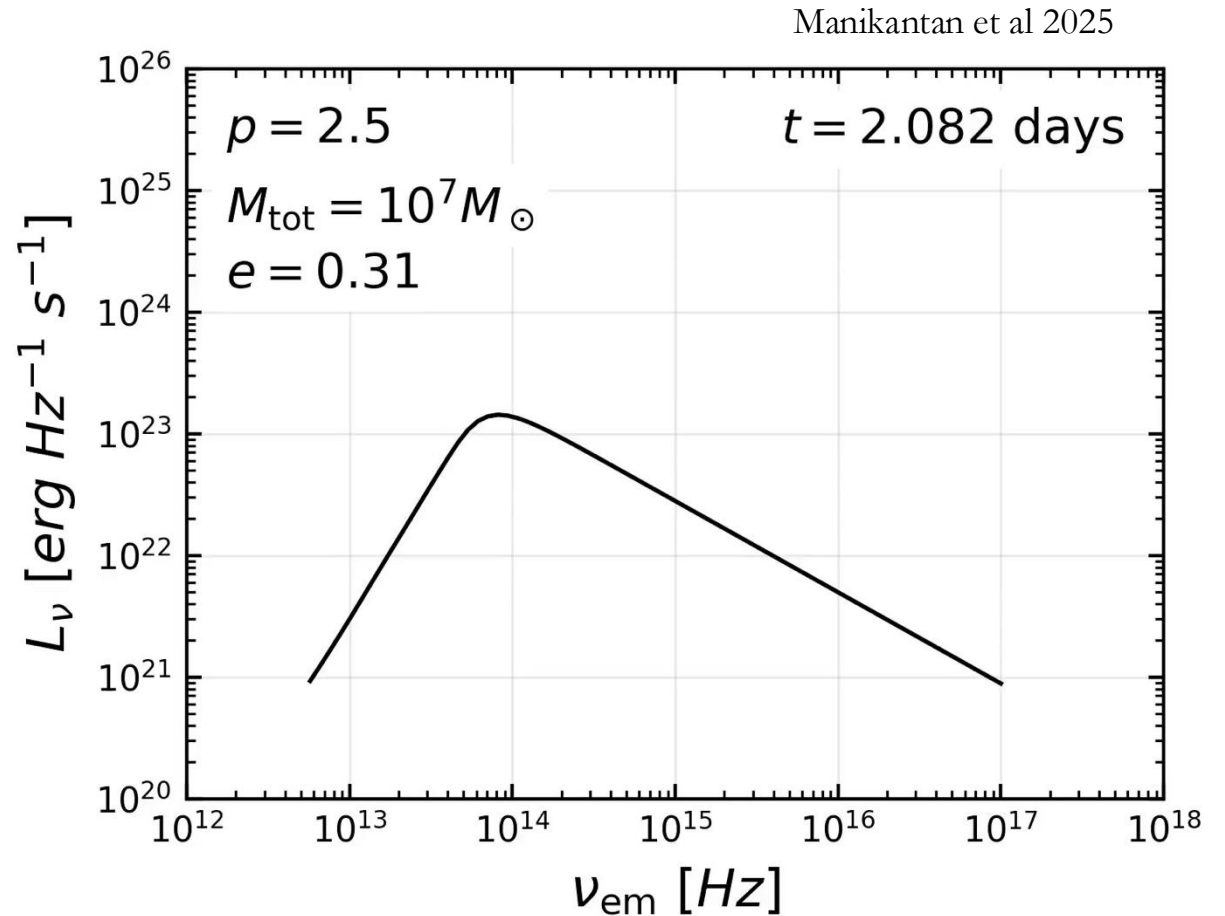
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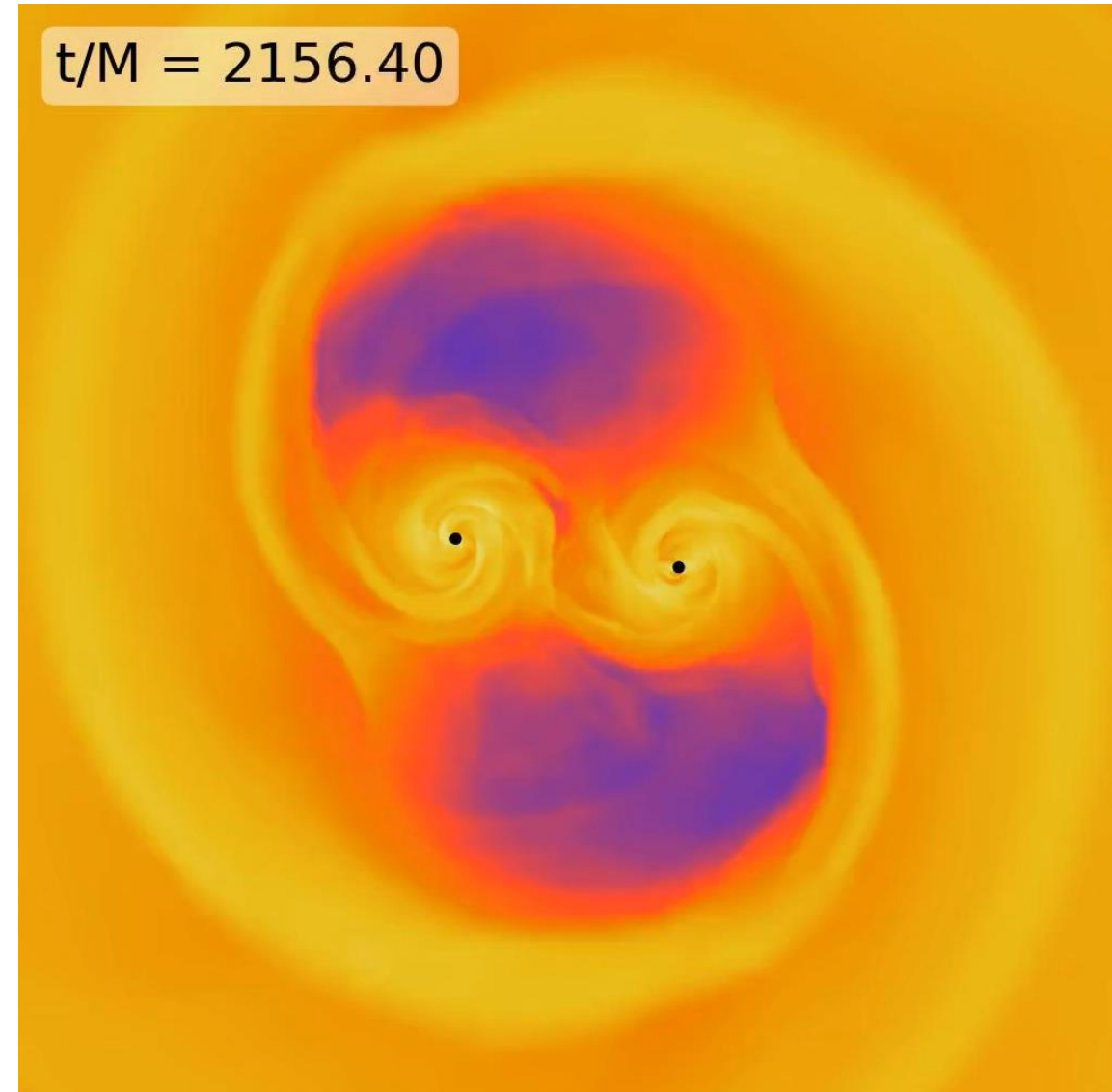
# Predicting electromagnetic emission

- Using radiative transfer, I can predict what photons will be emitted and reabsorbed
- Calculate this for the entire simulation
- Predict how luminous our system is



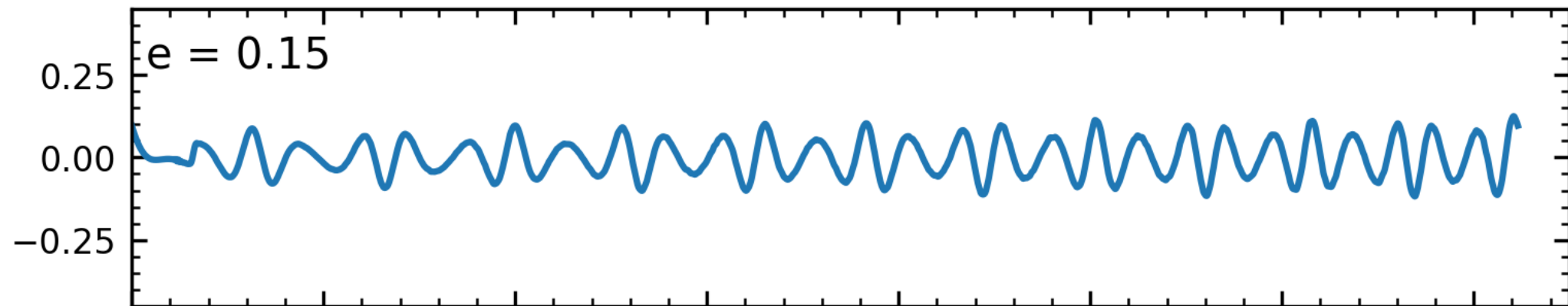
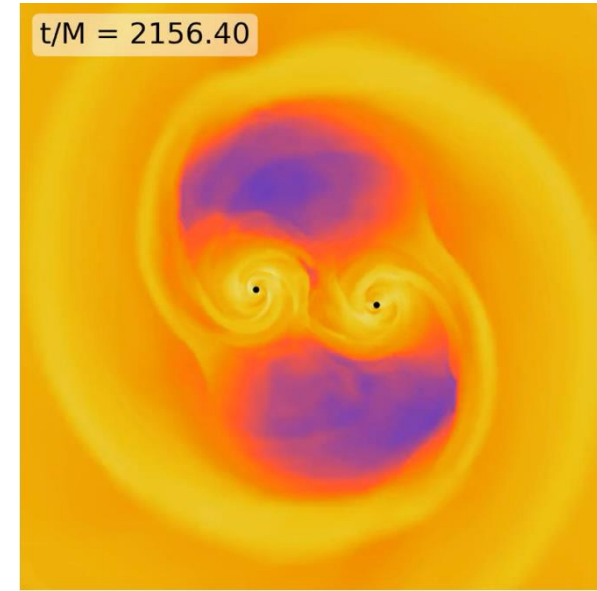
# Research summary

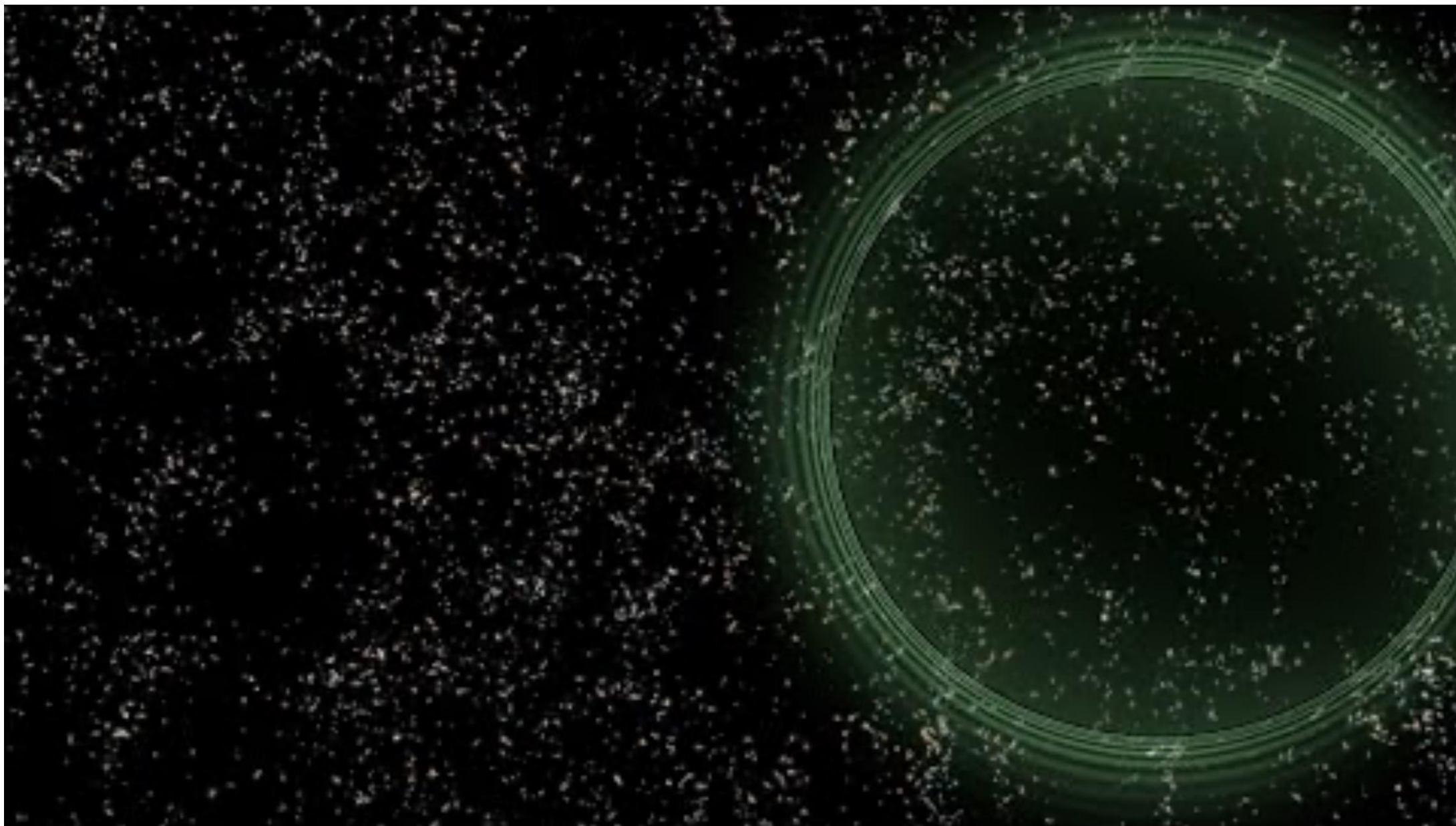
- Use GR and MHD simulations to predict the accretion flow around binary black holes
- Accretion produces emission in the X-ray and UV
- Jets can produce emission in radio, infrared, optical, X-ray and Gamma-ray



# Gravitational Waves

- Our simulations also produce gravitational waves!
- Because we solve for Einstein's equations of general relativity

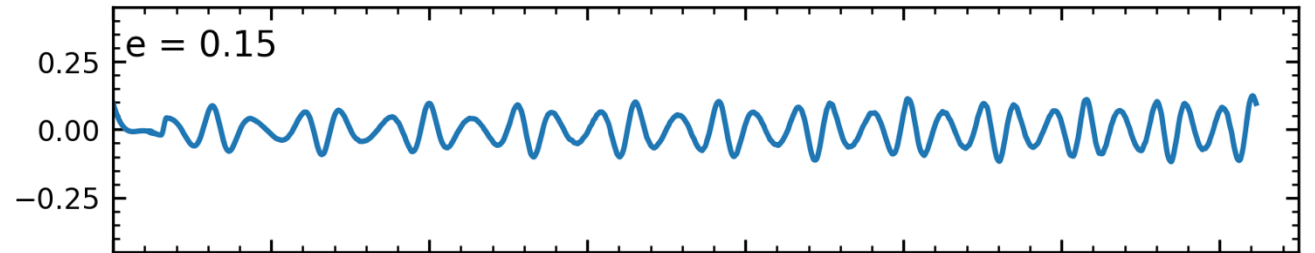




# In-class Assignment: Gravitational Waves

- Let's play with some gravitational wave data!
- All the instructions should be in the d2L
- Let me show you the code we will be using...

$$t_0 = \frac{5}{256} \frac{c^5}{\mu M_1 M_2 G^3} a_0^4$$



Question: What is the actual merger timescale?