

Taking the derivative of a function

Let $f(x) = \exp(1 + 1/x^2) + x * \ln(x)$

Next, we will take the derivative $f'_x(x)$:

Step-by-step solution:

$$\begin{aligned} (\exp(1 + 1/x^2) + x * \ln(x))' &= (x * \ln(x))' + (\exp(1 + 1/x^2))' \\ (x * \ln(x))' &= x' * \ln(x) + x * (\ln(x))' \\ \ln' x &= 1/x * x' \\ \exp'(1 + 1/x^2) &= \exp(1 + 1/x^2) * (1 + 1/x^2)' \\ (1 + 1/x^2)' &= (1/x^2)' + 1' \\ (1/(x^2))' &= (1' * (x^2) - 1 * (x^2)') / (x^2)^2 \\ (x^2)' &= x^{2-1} * (2 * x' + x * \ln x * 2') \end{aligned}$$

The derivative is:

$$\exp(1 + 1/x^2) * (0 + ((0 * x^2) - (x^{2-1} * (1 * 2 + x * 0 * \ln(x)) * 1)) / (x^2)^2) + 1 * \ln(x) + 1/x * 1 * x$$

But you can see many unnecessary actions.

Let us make some simplifications:

$$\begin{aligned} &\exp(1 + 1/x^2) * ((0 * x^2) - (x^1 * (1 * 2 + x * 0 * \ln(x)) * 1)) / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * (0 - (x^1 * (2 + x * 0 * \ln(x)) * 1)) / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x^1 * (2 + x * 0 * \ln(x)) * 1 / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x^1 * (2 + x * 0 * \ln(x)) / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x * (2 + x * 0 * \ln(x)) / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x * (2 + x * 0) / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x * (2 + 0) / (x^2)^2 + 1 * \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x * 2 / (x^2)^2 + \ln(x) + 1/x * 1 * x \\ &\exp(1 + 1/x^2) * -1 * x * 2 / (x^2)^2 + \ln(x) + 1/x * x \\ &\exp(1 + 1/x^2) * -1 * x * 2 / (x^2)^2 + \ln(x) + x/x \\ &\exp(1 + 1/x^2) * -1 * x * 2 / (x^2)^2 + \ln(x) + 1 \\ &\exp(1 + 1/x^2) * -1 * x * 2 / (x^2)^2 + \ln(x) + 1 \end{aligned}$$

In this way:

$f'_x(x) = \exp(1 + 1/x^2) * -1 * x * 2 / (x^2)^2 + \ln(x) + 1$

Further simplifications reader can hold their own.