Obtimal number of knots

