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Tutorial - 4
   T(n) = 3T (n/2) + n2
                           , f(n) = n2
         nlog b = n log 3
        comparing n log 2 and n2
                   n log 3 < n2 (case 3)
      ... according to masur's theorem
                   T(M) = 8 (M2)
         T(n) = 4T (1/2) + n2
            a=4, b=2
            nlog b = nlog 2 = n2 = f(n) (case 2)
  · · · according to masters theorem T(n) = O(n2 log n)
     T(n) = T(1/2) + 27
3
         a=1,6=2
         n log 2 = no = 1
                  1 < 27 (case 3)
 ... according to masters theorem T(n) = g(24)
    T(n) = 2 + T(n/2) + nn
   .. Master's trussem is not applicable as a is
           function of n.
      T(n) = 16 T (n/4) + n
(5)
           a = 16, b = 4, f(n) = n

n \log b = n \log 4 = n^2
                        n2 > f(n) € case 1)
                          · T(4) 2 ( 12)
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(a)
$$T(u) = 2T(u) + n \log n$$
 $a = 2$, $b = 2$, $f(u) = n \log n$
 $n \log 6 = n \log 2 = n$
 $n \log 6 = n \log 2 = n$
 $n \log 6 = n \log 2 = n$

Now, $f(u) > n$

... According to master's $T(u) = 0 (n \log n)$
 $T(u) = 2T(\frac{n}{2}) + \frac{n}{\log n}$
 $a = 2$, $b = 2$, $f(u) = \frac{n}{\log n}$
 $n \log 6 = n \log 2 = n$
 $n > f(u)$

... According to master's theorem $T(u) = g(u)$

8 $T(u) = 2T(\frac{n}{4}) + n^{0.51}$
 $a = 2$, $b = 4$, $f(u) = n^{0.51}$
 $n \log 6 = n \log 4 = n^{0.51}$
 $n^{0.5} < f(u)$

... According to masters theorem $T(u) = 0 (n^{0.5})$

9 $T(u) = 0.5T(u) + \frac{1}{n}$

... Masters not applicable as $a < 1$
 $T(u) = 16T(u) + n!$
 $a = 16$, $b = u$, $f(u) > n!$
 $n \log 6 = n \log 4 = n^2$
 $n^2 < n!$

.: According to masters, T(n) = & (n!)

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T(n) = 4T (1/2) + log n
      a=4, b=2, f(n)=log n
    n logg = n logg = n2
             n2 >f(n)
  -. According to master's , T(n) = Q(n2)
(12) T(n) = squt (n) + (n/2) + log n
  :. Master's not applicable as a is not constant
(13) T(n) = 3T (4/2) + n
       a=3, b=2, f(n)=n
    nlogo = nlog 23 = n1.58
                n1.58 > f(n)
  - According to master's theorem, T(n) = O(n log23)
     T(n) = 8T (n/3) + Nn
(14)
        a=3, b=3, f(n)=Nn
          n log 6 = nlog 3 = n
                  ハフがり
 .. According to masters theorem, T(u) = Q(u)
       T(n12 4T(n/2) + Cn
(15)
          a=4, b=2, f(n) 2 c*n
            nlogo = nlog = n2
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· · According to masters theorem, T(4) = Q(42)

n2 > c x n

T(1)= 3T(4/4) + n log n a=3, b=4, fcm) = n log n nlog b = nlog 4 = n0.79 no.79 < n log n According to masters theorem, T(4) = O(4 log 4) T(n) = 3T(M/3) + M/2 f(n) = 1 a=3,5=3 nlogs = nlog3 = n Q(n) = Q(1/2) .. According to masters measure T(11) = O(n log n) T(n)= 6T (M/3) + n2 log n (18) 6=3, f(n1= n2 log n a=6, = n log 3 = n 1.63 n log b n 1.63 < n2 log n .. According to masters theorem T(n) 2 0 (n2 log n) T(112 4T(112) + 1/20g n (19) > f(n) = 1/ lug n a=4, b=2 nlog 6 = nlog 2 = n2 n2 > n/log n ... According to masters theosem

T(n) = O(n2)

- (20) $T(n) = 64T(9/8) n^2 log 9$ Masters theorem is not applicable as f(n) is not increasing function.
- (21) $T(n) = 7T(9/3) + n^2$ a = 7, b = 3, $f(n) = n^2$ n = 1.7 $n = 1.7 < n^2$
 - ": According to mesters, $T(n) = O(n^2)$
- T(n) = $T(n_{12}) + n(2-\cos n)$ Master's theosem isn't applicable since segularity condition is isolated in case 3.