

Ex. given a collection  $\mathcal{F}$  of sets with  $|\mathcal{F}|=n$  show that the algebra generated by  $\mathcal{F}$  has at most  $2^n$  sets.

Bertrand's postulate:  $\exists$  a prime between  $n$  and  $2n$ . See proof by THE BOOK

Reading: Memorize proof of bertrand's postulate <sup>Ch 2</sup> from pTB. Also Ch 3.

Think about:  $(a+b)^n \rightsquigarrow \binom{n}{k}$ .  $(a+b)^x \rightsquigarrow ?$

other things:  $n! \leftarrow \Gamma(x)$   $\rightarrow$  connected  
fractional derivative?

or look @ book

google: multinomial coefficients in multivariable calculus/taylor series.  
 $\rightarrow$  MathSciNet

Ex. play w/ diagonals of Pascal Triangle & maybe find a formula for sums of first  $n$  elements in  $k^{\text{th}}$  diagonal.

Ex. Show that integers have unique representation in terms of fibonacci base (if you don't use adjacent #s)

Given  $a_n \uparrow \infty$ ,  $a_n \in \mathbb{N}$ , Do you expect  $(a_n)$  to be a "good" base (say, like 10 or 2).

Ex. fix solution to "unique powers of 3" problem.

Ex. Show that  $2^n$  is "slowest" with which you can still do well.

Ex. show that  $\lim_{p \rightarrow \infty} d_p = d_\infty$ .

exercises from Ch 3: 2.5.(2,3,4) 3.8.(8,9,12)