

Polynomials over F : $F[X] \cong F_0^\infty$.
 is a Vector Space endowed with commutative multiplication. ^{and associative}
 no inverses so $F[X]$ not a field

$F[X]$ is a commutative algebra

$$\deg: F[X] \setminus \{0\} \rightarrow \mathbb{N} \cup \{0\} \quad (\text{or } \deg 0 = -\infty)$$

$$\deg(P+Q) \leq \max\{\deg P, \deg Q\}$$

$$\deg(PQ) = \deg P + \deg Q$$

$$P, Q \neq 0 \Rightarrow PQ \neq 0. \quad (\text{Ring w/o zero divisors})$$