

Thm  $X \in R[x]$  is irreducible iff  $R$  is indecomposable.

eg  $X = (2x+3)(3x+2)$  in  $\mathbb{Z}_6[x]$ ,  $\mathbb{Z}_6 = \mathbb{Z}_3 \oplus \mathbb{Z}_2$

$X \in \mathbb{Z}_4[x]$  is irreducible but not prime ( $\mathbb{Z}_4[x]/(X) \cong \mathbb{Z}_4$ ).