

# Computer Networks

## Homework 3

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### Problem 1:

A signal is sampled two times each microsecond, into samples carrying 2 bits of information each. The communication channel has a bandwidth of 20 MHz and a signal to noise ratio of 30 dB.

- a) What data rate does the sampling provide?
- b) What is the maximum data rate of the channel?

$$B = 20 \text{ MHz} = 20 * 10^6 \text{ Hz}$$

$$\text{SNR} = 30 \text{ dB}$$

$$\text{ips (information per sample)} = 2\text{b}$$

$$L = \text{ips}^2 = 4$$

$$\text{a) data rate} = B * \text{ips} = 20 * 10^6 \text{ Hz} * 2\text{b} = 40 \text{ Mbps}$$

**Answer:** The sampling provides the data rate of 40 Mbps.

$$\text{SNR} = 10 * \log_{10}(\text{S/N})$$

$$\log_{10}(\text{S/N}) = \text{SNR} / 10$$

$$\text{S/N} = (\text{SNR} / 10)^{10} = (30 \text{ dB} / 10)^{10} = 59\,049 \text{ dB}$$

$$\text{b) } \text{mdr}_{\text{NY}} (\text{max data rate Nyquist}) = 2 * B * \log_2 L = 2 * 20 * 10^6 \text{ Hz} * \log_2 4 = 80 \text{ Mbps}$$

$$\text{Mdr}_{\text{SH}} (\text{max data rate Shannon}) = B * \log_2(1 + \text{S/N}) = 20 * 10^6 \text{ Hz} * \log_2(59\,050) = 317 \text{ Mbps}$$

$$\text{mdr}_{\text{REAL}} (\text{real max data rate}) \leq \min \{\text{mdr}_{\text{NY}}, \text{mdr}_{\text{SH}}\} = \text{mdr}_{\text{NY}} = 80 \text{ Mbps}$$

**Answer:** The maximum data rate of the channel is lower or equal to 80 Mbps.

## Problem 2:

Given the following bit sequences:

- A: 01101111
- B: 10001111
- FLAG: 01111110
- ESC: 11100000

show the transmitted bit sequence for data = FLAG A B ESC when using:

- byte count,
- flag bytes with byte stuffing,
- flag bytes with bit stuffing.

| data | = 4 B

| data<sub>BCount</sub> | = | data | + 1B = 5B

a) data<sub>BCount</sub> = | data<sub>BCount</sub> | + data =  
00000101 01111110 01101111 10001111 11100000

b) data<sub>BStuffing</sub> = FLAG ESC FLAG A B ESC ESC FLAG =  
01111110 11100000 01111110 01101111 10001111 11100000 11100000  
01111110

c) data<sub>bStuffing</sub> = FLAG FLAG A B ESC FLAG + [0 after every 5 successive 1s] =  
01111110 01111110 10 01101111 10000111 11010000 01111110