# Lab 05 Matlab Conversion

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This file aims to convert a series of Matlab scripts and data files into a R Markdown file that replicates the Tol (2023) Lab 5 for the economics of climate change. https://github.com/rtol/ClimateEconomics

The Matlab files this replicates are:

- MLIAM01.m
- MLIAM.mat
- init01.m
- MRHparam.m
- MRH.m
- RFparam.m
- RadForc.m
- STparam.m
- ST.m
- init02.m
- Popparam
- Outputparam
- CO2param
- init03.m
- MLIAM03.m
- CobbDouglas.m
- $\bullet$  invest.m
- init04.m
- MLIAM04.m
- init05.m
- init06.m
- init07.m
- impactcc.m
- MLIAM05.m

# Overview - the MLIAM05.m script

```
# init01
# init02
# init03
# init04
# init05
# init06
# init07
#
# for t=StartYear+1:EndYear,
# i = t - StartYear + 1;
# MRHbox(i,:) = MRH(MRHbox(i-1,:),CO2global(i-1),MRHlife,MRHshare,CO2convert);
```

```
#
            CO2conc(i) = sum(MRHbox(i,:));
#
            RF(i) = RadForc(CO2conc(i), RFO, CO2O);
#
            [atmtemp(i) \ oceantemp(i)] = ST(atmtemp(i-1), oceantemp(i-1), RF(i), STpar);
#
            impact(i,:) = impactcc(atmtemp(i), impactpar, 0, 1, 1);
#
            if t > 2010,
#
                    population(i,:) = population(i-1,:).*(1+popgrowth);
#
                    popgrowth= popdecline*popgrowth;
#
                    TFPqrowth= TFPdecline*TFPqrowth;
#
            end
#
            if t > 1960,
#
                    capital(i,:) = invest(capital(i-1,:),output(i-1,:),savings,depreciation);
#
                    TFP(i,:) = TFP(i-1,:).*(1+TFPgrowth);
#
#
            if t >= 1960,
#
                    output(i,:) = max(0.3*population(i,:), CobbDouglas(TFP(i,:), capital(i,:), population(i,:), lambd
#
                    outputpc(i,:) = output(i,:)./population(i,:)*1000;
#
                    consumption(i,:) = (1-savings)*output(i,:);
#
                    impact(i,:) = impactcc(atmtemp(i), impactpar, impelas, outputpc(i,:), outputpc2010);
#
            end
#
#
            %first best tax, period 1
#
            if t == 2015,
#
                    emred(i,1) = 0.0;
#
                    for j = 2:NReg,
#
                             emred(i,j) = emred(i,1)*unitabcost(1)/unitabcost(j)*output(i-1,1)/output(i-1,j)*CO2emit(i-1,j)*O12emit(i-1,j)*O2emit(i-1,j)*O2emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O12emit(i-1,j)*O
#
                    end
#
            end
#
#
            %first best tax, later periods
#
            if t > 2015,
#
                    emred(i,1) = min(0.99, emred(i-1,1)*(1+qlobalDR(i-1)));
#
                    for j = 2:NReq,
                             emred(i,j) = min(0.99, emred(i,1)*unitabcost(1)/unitabcost(j)*output(i-1,1)/output(i-1,j)*
#
#
                    end
#
            en.d.
#
#
            if t > 2010,
#
                    energyint(i,:) = AEEI.*energyint(i-1,:);
#
                    emissint(i,:) = ACEI.*emissint(i-1,:);
#
                    energy(i,:) = energyint(i,:).*output(i,:);
#
                    CO2emitbau(i,:) = emissint(i,:).*energy(i,:);
#
#
                    %permit trade
#
                    %permitprice(i) = 1000*emitalloc(i,:)*CO2emitbau(i,:)'/sum(0.5*CO2emitbau(i,:).^2./unitabcost)
#
                    %emred(i,:) = 0.5*0.001*permitprice(i)*CO2emitbau(i,:)./unitabcost./output(i,:);
#
                    %permittrade(i,:) = (emitalloc(i,:)-emred(i,:)).*CO2emitbau(i,:);
#
#
                    CO2emit(i,:) = CO2emitbau(i,:).*(1-emred(i,:));
#
                    CO2qlobal(i) = CO2qlobal(i-1)*sum(CO2emit(i,:))/sum(CO2emit(i-1,:)) + perturbation(i);
#
#
                    discountrate(i,:) = PRTP + RRA*(consumption(i,:)./consumption(i-1,:)-1);
#
                    globalDR(i) = PRTP + RRA*(sum(consumption(i,:))/sum(consumption(i-1,:))-1);
#
```

# Step 1 - load the MLIAM.mat file

```
library(R.matlab)
## R.matlab v3.7.0 (2022-08-25 21:52:34 UTC) successfully loaded. See ?R.matlab for help.
## Attaching package: 'R.matlab'
## The following objects are masked from 'package:base':
##
##
       getOption, isOpen
#MLIAM <- readMat("../TolMatlabFiles/MLIAM.mat")</pre>
MLIAM <- readMat("./MLIAM.mat")</pre>
ls.str()
## MLIAM : List of 11
## $ CO2global : num [1:551, 1] 0 3 3 3 3 3 3 3 3 3 ...
## $ CO2emit
                 : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 ...
## $ CO2concobs : num [1:689, 1:2] 2006 2005 2004 2003 2002 ...
## $ population : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
## $ output
                 : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
## $ atmtempobs : num [1:551, 1] 0 0 0 0 0 0 0 0 0 0 ...
## $ oceantempobs: num [1:551, 1] 0 0 0 0 0 0 0 0 0 0 ...
## $ CO2emitobs : num [1:551, 1] 0 3 3 3 3 3 3 3 3 3 ...
## $ outputobs : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
## $ energy
                 : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
## $ NReg
                  : num [1, 1] 3
CO2global <- MLIAM$CO2global
                                    # should we use this?
CO2emit <- MLIAM$CO2emit
# CO2concobs <- MLIAM$CO2concobs
population <- MLIAM$population
# output <- MLIAM$output</pre>
# atmtempobs <- MLIAM$atmtempobs
# oceantempobs <- MLIAM$oceantempobs</pre>
# CO2emitobs <- MLIAM$CO2emitobs
                                  # should we use this?
outputobs <- MLIAM$outputobs
energy <- MLIAM$energy
NReg <- MLIAM$NReg
```

## Step 2 - run init01.m script, MRHparam, RFparam, STparam

```
climsens = 4.260547;
EndYear = 2300;
StartYear = 1750;
```

```
year = StartYear:EndYear
NYear = length(year)
# %MRHparam
MRHlife \leftarrow c(0, 1-exp(-1/363), 1-exp(-1/74), 1-exp(-1/17), 1-exp(-1/2))
MRH1750 \leftarrow c(275, 0, 0, 0, 0);
MRHshare \leftarrow c(0.13, 0.20, 0.32, 0.25, 0.10);
CO2convert = 1/2.13/1000;
MRHbox = matrix(0, NYear, 5); # "five boxes" for each year
MRHbox[1,] = MRH1750;
CO2conc = matrix(0, NYear, 1);
CO20 = sum(MRH1750);
CO2conc[1] = CO20;
# %RFparam
### RadForc
RadForc <-function(CO2,RF0,CO20) RF0*log(CO2/CO20);</pre>
RF0 = 5.35;
RF = matrix(0, NYear, 1);
RF[1] = RadForc(CO20, RFO, CO20) #Needs the RadForc function
# %STparam
atmtemp0 = 0;
oceantemp0 = 0;
atmtemp = matrix(0, NYear, 1);
oceantemp = matrix(0, NYear, 1);
atmtemp[(1)] = atmtemp0;
oceantemp[(1)] = oceantemp0;
STpar \leftarrow c(climsens/RF0/log(2), 0.0256, 0.00738, 0.00568)
```

# Step 3 - run init02.m script, Popparam, Outparam, and CO2param

```
consumption <- matrix(0, nrow = NYear, ncol = NReg)

# %Popparam
popgrowth <- population[2010 - StartYear + 1, ] / population[2009 - StartYear + 1, ] - 1
popdecline <- 0.95
popgrowth <- popdecline * popgrowth

# %Outputparam
capital <- matrix(0, nrow = NYear, ncol = NReg)
TFP <- matrix(0, nrow = NYear, ncol = NReg)
output <- matrix(0, nrow = NYear, ncol = NReg)
output <- matrix(0, nrow = NYear, ncol = NReg)
outputpc <- matrix(0, nrow = NYear, ncol = NReg)</pre>
```

```
TFPgrowth <- c(0.0206, 0.0260, 0.0236)
TFPdecline <- 0.99
outputpc2010 \leftarrow c(33498, 3170, 954)
lambda <- 0.2
savings <- 0.2
depreciation <- 0.1
A0 <- (outputobs[1960 - StartYear + 1, ] / population[1960 - StartYear + 1, ])^(1 - lambda)
AO <- AO * (depreciation / savings) lambda
KO <- (AO ^ (1 / (1 - lambda))) * population[1960 - StartYear + 1, ]</pre>
KO <- (savings / depreciation)^(1 / (1 - lambda)) * KO</pre>
capital[1960 - StartYear + 1, ] <- KO</pre>
TFP[1960 - StartYear + 1, ] <- A0
# %CO2param
CO2emitbau <- CO2emit
energyint <- energy / outputobs</pre>
emissint <- CO2emit / energy
AEEI <- energyint[(2010 - StartYear + 1), ] / energyint[(1960 - StartYear + 1), ]
AEEI <- AEEI ^ (1 / 50)
ACEI <- emissint[(2010 - StartYear + 1), ] / emissint[(1960 - StartYear + 1), ]
ACEI <- ACEI ^ (1 / 50)
AEEI \leftarrow c(0.98926539, 0.98782002, 0.99025746)
ACEI <- c(0.99594960, 1.00029674, 1.00979371)
```

## Step 4 - define MRH, ST, Cobb-Douglas and invest functions

```
### MRH - Maier-Reimer Hasselmann model
MRH <- function(CO2concold, CO2emit, CO2life, CO2share, CO2convert) {
 CO2concnew = (1-CO2life)*CO2concold + CO2convert*CO2share*CO2emit
  CO2concnew
}
### Schneider-Thompson model of Ocean and Atm Temps
# updates the temperature of the atmosphere and the ocean using the Schneider-Thompson model
ST <- function(atmtempold,oceantempold,radforc,STpar) {</pre>
atmtempnew = atmtempold
    STpar[2]*(STpar[1]*radforc-atmtempold) +
    STpar[3]*(oceantempold-atmtempold)
oceantempnew = oceantempold +
 STpar[4]*(atmtempold-oceantempold)
temps <- c(atmtempnew, oceantempnew)</pre>
names(temps) <- c("atm", "ocean")</pre>
temps
}
### Cobb-Douglas function
CobbDouglas <- function(A, K, L, lambda) {</pre>
Y \leftarrow A * (K^{lambda}) * (L^{(1 - lambda)})
```

```
return(Y)
}

### invest function
invest <- function(oldK, Y, s, d) {
  newK <- (1 - d) * oldK + s * Y
  return(newK)
}</pre>
```

#### Step 5 - run init03 and init04

```
## init03
unitabcost <- c(0.1, 0.1, 0.1)
emred <- matrix(0, nrow = NYear, ncol = NReg)
relabcost <- matrix(0, nrow = NYear, ncol = NReg)
totabcost <- matrix(0, nrow = NYear, ncol = NReg)
margabcost <- matrix(0, nrow = NYear, ncol = NReg)

PRTP <- 0.03
RRA <- 1

discountrate <- matrix(0, nrow = NYear, ncol = NReg)
globalDR <- matrix(0, nrow = NYear, ncol = 1)

## init04
emitalloc <- matrix(0, nrow = NYear, ncol = NReg)
emitalloc[266:NYear, ] <- emitalloc[266:NYear, ] + 0.05
permittrade <- matrix(0, nrow = NYear, ncol = NReg)
permitprice <- matrix(0, nrow = NYear, ncol = 1)</pre>
```

#### Step 6 - run init05.m, init06.m, init07.m

```
## init05
partol <- matrix(c(5.88, -2.31, 0, 3.57, -1.70, 0, 1.96, -1.26, 0), nrow = 3, ncol = 3)
parweitzman <- matrix(c(0, 0.5563, -0.0113, 0, 0.2561, -0.0106, 0, 0.0655, -0.0101), nrow = 3, ncol = 3
impactpar <- partol
impelas <- 0
impact <- matrix(0, nrow = NYear, ncol = NReg)

## init06
# set peturb to 0 for now
perturb <- 0
perturbation <- matrix(perturb, nrow = NYear, ncol = 1)

## init07
impelas <- -0.25</pre>
```

#### Step 6 - define impactcc function

```
impactcc <- function(temp, impar, impelas, inccap, inccap0) {
  imp <- impar[1,] * temp + impar[2,] * temp^2 + impar[3,] * temp^6
  imp <- imp * (inccap / inccap0)^impelas</pre>
```

```
return(imp)
}
```

### Step 7 - the main script, MLIAM05

```
for (t in (StartYear+1):EndYear) {
        i <- t - StartYear + 1
        MRHbox[i,] <- MRH(MRHbox[i-1,], CO2global[i-1], MRHlife, MRHshare, CO2convert)
        CO2conc[i] <- sum(MRHbox[i,])</pre>
        RF[i] <- RadForc(CO2conc[i], RFO, CO20)</pre>
        atmtemp[i] <- ST(atmtemp[i-1], oceantemp[i-1], RF[i], STpar)[[1]]</pre>
        oceantemp[i] <- ST(atmtemp[i-1], oceantemp[i-1], RF[i], STpar)[[2]]
        impact[i,] <- impactcc(atmtemp[i], impactpar, 0, 1, 1)</pre>
        if (t > 2010) {
                population[i,] <- population[i-1,] * (1 + popgrowth)</pre>
                popgrowth <- popdecline * popgrowth</pre>
                TFPgrowth <- TFPdecline * TFPgrowth
        if (t > 1960) {
                capital[i,] <- invest(capital[i-1,], output[i-1,], savings, depreciation)</pre>
                TFP[i,] <- TFP[i-1,] * (1 + TFPgrowth)</pre>
        if (t >= 1960) {
                output[i,] <- pmax(0.3 * population[i,], CobbDouglas(TFP[i,], capital[i,], population[i,], lamb
                outputpc[i,] <- output[i,] / population[i,] * 1000</pre>
                consumption[i,] <- (1 - savings) * output[i,]</pre>
                impact[i,] <- impactcc(atmtemp[i], impactpar, impelas, outputpc[i,], outputpc2010)</pre>
        if (t == 2015) {
                emred[i,1] <- 0.0
                for (j in 2:NReg) {
                         emred[i,j] <- emred[i,1] * unitabcost[1] / unitabcost[j] * output[i-1,1] / output[i-1,j] * output[i-1,j] 
        }
        if (t > 2015) {
                emred[i,1] <- pmin(0.99, emred[i-1,1] * (1 + globalDR[i-1]))</pre>
                for (j in 2:NReg) {
                         emred[i,j] <- pmin(0.99, emred[i,1] * unitabcost[1] / unitabcost[j] * output[i-1,1] / outpu</pre>
                }
        }
        if (t > 2010) {
                energyint[i,] <- AEEI * energyint[i-1,]</pre>
                emissint[i,] <- ACEI * emissint[i-1,]</pre>
                energy[i,] <- energyint[i,] * output[i,]</pre>
                CO2emitbau[i,] <- emissint[i,] * energy[i,]</pre>
                CO2emit[i,] <- CO2emitbau[i,] * (1 - emred[i,])
                CO2global[i] <- CO2global[i-1] * sum(CO2emit[i,]) / sum(CO2emit[i-1,]) + perturbation[i]
                discountrate[i,] <- PRTP + RRA * (consumption[i,] / consumption[i-1,] - 1)</pre>
                globalDR[i] <- PRTP + RRA * (sum(consumption[i,]) / sum(consumption[i-1,]) - 1)</pre>
        }
        if (t > 2015) {
                relabcost[i,] <- unitabcost * emred[i,]^2 + 0.001 * permitprice[i] * permittrade[i,] / output[i
                totabcost[i,] <- relabcost[i,] * output[i,]</pre>
```

```
margabcost[i,] <- 2 * unitabcost * emred[i,] * output[i,] / CO2emit[i,] * 1000
}</pre>
```