Lab 03 Matlab Conversion

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2025-04-15

This file aims to convert a series of Matlab scripts and data files into a R Markdown file that replicates the Tol (2023) Lab 3 for the economics of climate change. https://github.com/rtol/ClimateEconomics

The Matlab files this replicates are:

- MLIAM01.m
- MLIAM.mat
- init01.m
- MRHparam.m
- MRH.m
- RFparam.m
- RadForc.m
- STparam.m
- ST.m
- init02.m
- Popparam
- Outputparam
- CO2param
- init03.m
- MLIAM03.m

Overview - the MLIAM03.m script

```
# clear all
# load MLIAM
# init01
# init02
# init03
#
# for t=StartYear+1:EndYear,
#     i = t - StartYear + 1;
#     MRHbox(i,:) = MRH(MRHbox(i-1,:),CO2global(i-1),MRHlife,MRHshare,CO2convert);
#     CO2conc(i) = sum(MRHbox(i,:));
#     RF(i) = RadForc(CO2conc(i),RF0,CO20);
#     [atmtemp(i) oceantemp(i)] = ST(atmtemp(i-1),oceantemp(i-1),RF(i),STpar);
#     if t > 2010,
#         population(i,:) = population(i-1,:).*(1+popgrowth);
#         popgrowth= popdecline*popgrowth;
#         TFPgrowth= TFPdecline*TFPgrowth;
#     end
#     if t > 1960,
#         capital(i,:) = invest(capital(i-1,:),output(i-1,:),savings,depreciation);
#         TFP(i,:) = TFP(i-1,:).*(1+TFPgrowth);
```

```
#     end
#     if t >= 1960,
#         output(i,:) = CobbDouglas(TFP(i,:),capital(i,:),population(i,:),lambda).*(1-relabcost(i-1,:))
#         consumption(i,:) = (1-savings)*output(i,:);
#     end
#
#     if t == 2015,
#         emred(i,1) = 0.05;
#         for j = 2:NReg,
#             emred(i,j) = emred(i,1)*unitabcost(1)/unitabcost(j)*output(i-1,1)/output(i-1,j)*CO2emit(i
#         end
#     end
#
#     if t > 2015,
#         emred(i,1) = min(0.99,emred(i-1,1)*(1+globalDR(i-1)));
#         for j = 2:NReg,
#             emred(i,j) = min(0.99,emred(i,1)*unitabcost(1)/unitabcost(j)*output(i-1,1)/output(i-1,j)*
#         end
#     end
#
#     if t > 2010,
#         energyint(i,:) = AEEI.*energyint(i-1,:);
#         emissint(i,:) = ACEI.*emissint(i-1,:);
#         energy(i,:) = energyint(i,:).*output(i,:);
#         CO2emit(i,:) = emissint(i,:).*energy(i,:).*(1-emred(i,:));
#         CO2global(i) = CO2global(i-1)*sum(CO2emit(i,:))/sum(CO2emit(i-1,:));
#
#         discountrate(i,:) = PRTP + RRA*(consumption(i,:)./consumption(i-1,:)-1);
#         globalDR(i) = PRTP + RRA*(sum(consumption(i,:))/sum(consumption(i-1,:))-1);
#     end
#
#     if t > 2015
#         relabcost(i,:) = unitabcost.*emred(i,:).^2;
#         totabcost(i,:) = relabcost(i,:).*output(i,:);
#         margabcost(i,:) = 2*unitabcost.*emred(i,:).*output(i,:)./CO2emit(i,:)*1000;
#     end
# end
```

Step 1 - load the MLIAM.mat file

```
library(R.matlab)
```

```
## R.matlab v3.7.0 (2022-08-25 21:52:34 UTC) successfully loaded. See ?R.matlab for help.
```

```
##
## Attaching package: 'R.matlab'
```

```
## The following objects are masked from 'package:base':
##
##     getOption, isOpen
```

```
#MLIAM <- readMat("../TolMatlabFiles/MLIAM.mat")
MLIAM <- readMat("./MLIAM.mat")
ls.str()
```

```
## MLIAM : List of 11
##  $ CO2global   : num [1:551, 1] 0 3 3 3 3 3 3 3 3 3 ...
##  $ CO2emit     : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
##  $ CO2concobs  : num [1:689, 1:2] 2006 2005 2004 2003 2002 ...
##  $ population  : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
##  $ output      : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
##  $ atmtempobs  : num [1:551, 1] 0 0 0 0 0 0 0 0 0 0 ...
##  $ oceantempobs: num [1:551, 1] 0 0 0 0 0 0 0 0 0 0 ...
##  $ CO2emitobs  : num [1:551, 1] 0 3 3 3 3 3 3 3 3 3 ...
##  $ outputobs   : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
##  $ energy      : num [1:551, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
##  $ NReg        : num [1, 1] 3
```

```
CO2global <- MLIAM$CO2global        # should we use this?
CO2emit <- MLIAM$CO2emit
# CO2concobs  <- MLIAM$CO2concobs
population  <- MLIAM$population
# output  <- MLIAM$output
# atmtempobs  <- MLIAM$atmtempobs
# oceantempobs  <- MLIAM$oceantempobs
# CO2emitobs  <- MLIAM$CO2emitobs    # should we use this?
outputobs  <- MLIAM$outputobs
energy  <- MLIAM$energy
NReg  <- MLIAM$NReg
```

Step 2 - run init01.m script, MRHparam, RFparam, STparam

```
climsens = 4.260547;
EndYear = 2300;
StartYear = 1750;
year = StartYear:EndYear
NYear = length(year)

# %MRHparam
MRHlife <- c(0, 1-exp(-1/363), 1-exp(-1/74), 1-exp(-1/17), 1-exp(-1/2))
#
MRH1750 <- c(275, 0, 0, 0, 0);
#
MRHshare <- c(0.13, 0.20, 0.32, 0.25, 0.10);
#
CO2convert = 1/2.13/1000;
#
MRHbox = matrix(0, NYear, 5); # "five boxes" for each year
MRHbox[1, ] = MRH1750;
CO2conc = matrix(0, NYear, 1);
CO20 = sum(MRH1750);
CO2conc[1] = CO20;

# %RFparam
### RadForc
RadForc <-function(CO2,RF0,CO20) RF0*log(CO2/CO20);
#
RF0 = 5.35;
RF = matrix(0, NYear, 1);
```

```
RF[1] = RadForc(CO20, RF0, CO20) #Needs the RadForc function

# %STparam
atmtemp0 = 0;
oceantemp0 = 0;

atmtemp = matrix(0, NYear, 1);
oceantemp = matrix(0, NYear, 1);

atmtemp[(1)] = atmtemp0;
oceantemp[(1)] = oceantemp0;

STpar <- c(climsens/RF0/log(2), 0.0256, 0.00738, 0.00568)
```

Step 3 - run init02.m script, Popparam, Outparam, and CO2param

```
consumption <- matrix(0, nrow = NYear, ncol = NReg)

# %Popparam
popgrowth <- population[2010 - StartYear + 1, ] / population[2009 - StartYear + 1, ] - 1
popdecline <- 0.95
popgrowth <- popdecline * popgrowth

# %Outputparam
capital <- matrix(0, nrow = NYear, ncol = NReg)
TFP <- matrix(0, nrow = NYear, ncol = NReg)
output <- matrix(0, nrow = NYear, ncol = NReg)
outputpc <- matrix(0, nrow = NYear, ncol = NReg)

TFPgrowth <- c(0.0206, 0.0260, 0.0236)
TFPdecline <- 0.99
outputpc2010 <- c(33498, 3170, 954)

lambda <- 0.2
savings <- 0.2
depreciation <- 0.1

A0 <- (outputobs[1960 - StartYear + 1, ] / population[1960 - StartYear + 1, ])^(1 - lambda)
A0 <- A0 * (depreciation / savings)^lambda
K0 <- (A0 ^ (1 / (1 - lambda))) * population[1960 - StartYear + 1, ]
K0 <- (savings / depreciation)^(1 / (1 - lambda)) * K0

capital[1960 - StartYear + 1, ] <- K0
TFP[1960 - StartYear + 1, ] <- A0

# %CO2param
CO2emitbau <- CO2emit
energyint <- energy / outputobs
emissint <- CO2emit / energy

AEEI <- energyint[(2010 - StartYear + 1), ] / energyint[(1960 - StartYear + 1), ]
AEEI <- AEEI ^ (1 / 50)
ACEI <- emissint[(2010 - StartYear + 1), ] / emissint[(1960 - StartYear + 1), ]
```

```
ACEI <- ACEI ^ (1 / 50)

AEEI <- c(0.98926539, 0.98782002, 0.99025746)
ACEI <- c(0.99594960, 1.00029674, 1.00979371)
```

Step 4 - define MRH, ST, Cobb-Douglas and invest functions

```
### MRH - Maier-Reimer Hasselmann model
MRH <- function(CO2concold, CO2emit, CO2life, CO2share, CO2convert) {
  CO2concnew = (1-CO2life)*CO2concold + CO2convert*CO2share*CO2emit
  CO2concnew
}

### Schneider-Thompson model of Ocean and Atm Temps
# updates the temperature of the atmosphere and the ocean using the Schneider-Thompson model
ST <- function(atmtempold,oceantempold,radforc,STpar) {
atmtempnew   = atmtempold   +
    STpar[2]*(STpar[1]*radforc-atmtempold) +
    STpar[3]*(oceantempold-atmtempold)
oceantempnew = oceantempold +
  STpar[4]*(atmtempold-oceantempold)
temps <- c(atmtempnew, oceantempnew)
names(temps) <- c("atm", "ocean")
temps
}

### Cobb-Douglas function
CobbDouglas <- function(A, K, L, lambda) {
  Y <- A * (K^lambda) * (L^(1 - lambda))
  return(Y)
}

### invest function
invest <- function(oldK, Y, s, d) {
  newK <- (1 - d) * oldK + s * Y
  return(newK)
}
```

Step 5 - run init03

```
unitabcost <- c(0.1, 0.1, 0.1)
emred <- matrix(0, nrow = NYear, ncol = NReg)
relabcost <- matrix(0, nrow = NYear, ncol = NReg)
totabcost <- matrix(0, nrow = NYear, ncol = NReg)
margabcost <- matrix(0, nrow = NYear, ncol = NReg)

PRTP <- 0.03
RRA <- 1

discountrate <- matrix(0, nrow = NYear, ncol = NReg)
globalDR <- matrix(0, nrow = NYear, ncol = 1)
```

Step 6 - the main script, MLIAM03

```
for (t in (StartYear + 1):EndYear) {
  i <- t - StartYear + 1
  MRHbox[i, ] <- MRH(MRHbox[i - 1, ], CO2global[i - 1], MRHlife, MRHshare, CO2convert)
  CO2conc[i] <- sum(MRHbox[i, ])
  RF[i] <- RadForc(CO2conc[i], RF0, CO20)
  temp <- ST(atmtemp[i - 1], oceantemp[i - 1], RF[i], STpar)
  atmtemp[i] <- temp[1]
  oceantemp[i] <- temp[2]

  if (t > 2010) {
    population[i, ] <- population[i - 1, ] * (1 + popgrowth)
    popgrowth <- popdecline * popgrowth
    TFPgrowth <- TFPdecline * TFPgrowth
  }

  if (t > 1960) {
    capital[i, ] <- invest(capital[i - 1, ], output[i - 1, ], savings, depreciation)
    TFP[i, ] <- TFP[i - 1, ] * (1 + TFPgrowth)
  }

  if (t >= 1960) {
    output[i, ] <- CobbDouglas(TFP[i, ], capital[i, ], population[i, ], lambda) * (1 - relabcost[i - 1,
    consumption[i, ] <- (1 - savings) * output[i, ]
  }

  if (t == 2015) {
    emred[i, 1] <- 0.05
    for (j in 2:NReg) {
      emred[i, j] <- emred[i, 1] * unitabcost[1] / unitabcost[j] * output[i - 1, 1] / output[i - 1, j] *
    }
  }

  if (t > 2015) {
    emred[i, 1] <- min(0.99, emred[i - 1, 1] * (1 + globalDR[i - 1]))
    for (j in 2:NReg) {
      emred[i, j] <- min(0.99, emred[i, 1] * unitabcost[1] / unitabcost[j] * output[i - 1, 1] / output[
    }
  }

  if (t > 2010) {
    energyint[i, ] <- AEEI * energyint[i - 1, ]
    emissint[i, ] <- ACEI * emissint[i - 1, ]
    energy[i, ] <- energyint[i, ] * output[i, ]
    CO2emit[i, ] <- emissint[i, ] * energy[i, ] * (1 - emred[i, ])
    CO2global[i] <- CO2global[i - 1] * sum(CO2emit[i, ]) / sum(CO2emit[i - 1, ])
    discountrate[i, ] <- PRTP + RRA * (consumption[i, ] / consumption[i - 1, ] - 1)
    globalDR[i] <- PRTP + RRA * (sum(consumption[i, ]) / sum(consumption[i - 1, ]) - 1)
  }

  if (t > 2015) {
    relabcost[i, ] <- unitabcost * emred[i, ]^2
    totabcost[i, ] <- relabcost[i, ] * output[i, ]
```

```
    margabcost[i, ] <- 2 * unitabcost * emred[i, ] * output[i, ] / CO2emit[i, ] * 1000
  }
}
```