

Roosa Kuusivaara & Väinö-Waltteri Granat

Characterizing holographic displays via numerical simulations - Report

Abstract

Roosa Kuusivaara & Väinö-Waltteri Granat: Characterizing holographic displays via numerical simulations - Report
Laboratory Report
Tampere University
Master's Degree Programme in Signal Processing
September 2023

The abstract is a concise 1-page description of the work: what was the problem, what was done, and what are the results. Do not include charts or tables in the abstract.

These instructions are intended for students of Computer Sciences at the Tampere University. They cover questions of writing a thesis, such as use of the literature, structure of the thesis and style, the external appearance of the thesis and the use of tools. These instructions do not cover the scientific content of the thesis.

Keywords: M.Sc. thesis, layout, writing style.

Contents

1	Introduction	1
	1.1 Hologram synthesis	1
	1.2 Retinal Image Formation	1
2	Methodology	2
	2.1 Implementing Hologram Synthesis	2
	2.2 Retinal Image Formation Simulation	
	2.2.1 Field propagation implementation	3
3	Results	4
	3.1 PSF analysis	4
	3.2 MTF Analysis	4
4	Conclusions	13
Re	eferences	14
ΑI	PPENDIX A. Something extra	14

1 Introduction

In this report we describe our work with the 'Characterizing holographic displays via numerical simulations' exercise, for the Advanced Signal Processing Laboratory Course.

In this project we familiarized ourselves with the basics of holographic display, by implementing a part of a holograpics display viewing simulation. We implemented two holographic synthesis methods and a retinal image formation model, by contributing code to a MATLAB codebase given by the course faculty.

1.1 Hologram synthesis

Hologram synthesis describes the method for forming holographic images in 3d space from a given image. In this assignment, instead of using entire 3d space, the analysis can be simplified by considering only a cross section of the 3d space. The hologram is now represented as a 1D array of complex values. This simplification eases the computational load and also makes the process easier to handle.

1.2 Retinal Image Formation

In our exploration of holographic displays and their numerical characterization, Retinal Image Formation is a key part of the analysis. This simulation replicates how the human eye perceives visual information. Through this model, we obtain images on the retina, which can be used to analyze the perceived sharpness of the displayed content.

In these simulation tools, the human eye is considered as a camera, with the lens (the pupil) and the retina (the sensor). This simulation involves three key planes: the display (hologram), the lens, and the sensor. We model the pupil as a thin lens with a specific width, influencing how light passes through it.

2 Methodology

2.1 Implementing Hologram Synthesis

Our implementation of the holographic image viewer included three different methods of holographic image synthesis, one of which was provided in the code base given to us. The ready made synthesis method was holographic stereograph synthesis (HSS), [TODO: explain has here]. The first synthesis method we implemented was a Fresnel hologram synthesis which is based on the Fresnel diffraction kernel. Using this kernel to define the 1D field U(x;0) for a single point source at (x_p, z_p) as

$$U(x;0) = a_p \frac{exp(jkz_p)}{\sqrt{j\lambda z_p}} exp(jk\frac{(x-x_p)^2}{2z_p} + \phi_p), \qquad (2.1)$$

where a_p is the amplitude of the point source, ϕ_p is the relative phase, λ is the wavelength of the monochromatic light (i.e. the color, if in visible spectrum) and $k = \frac{2\pi}{\lambda}$ is the wave number.

The second method we implemented was Rayleigh-Sommerfeld synthesis (RSS), which uses Rayleigh-Sommerfeld diffraction kernel.

$$U(x;0) = a_p \frac{z_p}{\sqrt{j\lambda}[(x-x_p)^2 + z_p^2]^{\frac{3}{4}}} exp[jk\sqrt{(x-x_p)^2 + z_p^2} + \phi_p]$$
 (2.2)

This formula is similar to the Fresnel but has some differences in calculating the hologram.

2.2 Retinal Image Formation Simulation

To be able to view the synthezised holograms, we had to simulate the viewing process of an eye. This was achieved with a simplified wave propagation model, where human eye is represented by a simple lens and a one-dimensional sensor behind the lens in relation to the viewed hologram.

The transmittance of the lens is described by function 2.3

$$T(s) = exp(\frac{-i\pi}{\lambda f}s^2)$$
 (2.3)

where, f is the focal length of the lens.

The propagation of light from the hologram is modeled with a following field function 2.4

$$U(x;z) = \int \mathscr{F}\{U(\xi;z_0)\}(f_{\xi})exp[-2\pi i(f_{\xi}x + f_z z)]df_{\xi}$$
 (2.4)

where,

$$f_z = \sqrt{\frac{1}{\lambda^2} - f_\xi^2} \tag{2.5}$$

[TODO: Explain these functions]

The simplified eye model differs from a real human eye in multiple cases. Firstly, sensor of the human eye consists, [TODO: Add stuff]

2.2.1 Field propagation implementation

The implementation of the field progation was provided to us in the code base, in the propagateField_PWD.m file. The file starts with defining the basic parameters, which are current location of the eye, distance from lens to sensor, the focal length of the eye and the physical size of the hologram plane.

In the next step the file sets up the more complex parts of the simulation, like size of the sensor, properties of the propagating light and the sampling grid.

Finally the file executes the field propagation simulation, where each of the sections of the synthezied hologram are propagated trough the wave field and the results are of the sensor are sampled to produces an image as PSF which is returned from the function.

3 Results

In this section we analyze the images produced by the implemented model.

The wave propagation function produces a PSF images of the given hologram. These images were plotted as a function of the sensor positions. In the most optimal case allthe values would be in a single pile at the zero coordinated of the sensor, i.e. the center of the sensor. This would mean that all the pixels were percieved at the the best focus. The figures 3.1 and 3.2 so the plots for Fresnel synthesizied hologram and Rayleigh-Sommerfield synthesized hologram. The PSF plots of both of these methods were very similar, with tighlty packed values close to 0. This indicated that these methods, with this given focal length, provides fairly sharp images. The holographic stereogram synthesized hologram produced as significantly less packed PSF plot, as shown in figure 3.3.

3.1 PSF analysis

From the simulation we attained an image consisting of multiple overlayed PSF images depicting the hologram formed on the simulated sensor. From the image 3.4 we can see that from the samples the z_f value of -0.42 produces the sharpest image, since most of the points fall in the origin. This is different from what would be expected, since in ideal situation the sharpest images should form with the same values as the distance to point source, which in our simulation is -0.4. When the value of z_f moves away from -0.42 we expected the graph to widen, since image formed won't be as sharp and this is reflected in the figure, as the values closer to -0.42 produce higher graphs.

We also repeated this for Rayleigh-Sommerfield synthesis and Holographic stereogram synthesis, as shown in figures 3.5 and 3.6. The result for the Rayleigh-Sommerfield synthesis we basically identical, as the sharpest image, was obtained with the value of -0.42 and further away values produced wider graphs.

As for the holographic stereogram, the results different, in the sense that the sharpest image was produced with a z_f value of -0.44. Also all the z_f values produced blurrier images as the graphs were wider. This would indicate that the holographic stereogram produces overall blurrier holograms.

3.2 MTF Analysis

With the multiple PSF images we performed MTF analysis to obtain the value of z_f which would provide the sharpest image. By generating multiple PSF images with different z_f values we were able to obtain multiple MTF values in particular spectral

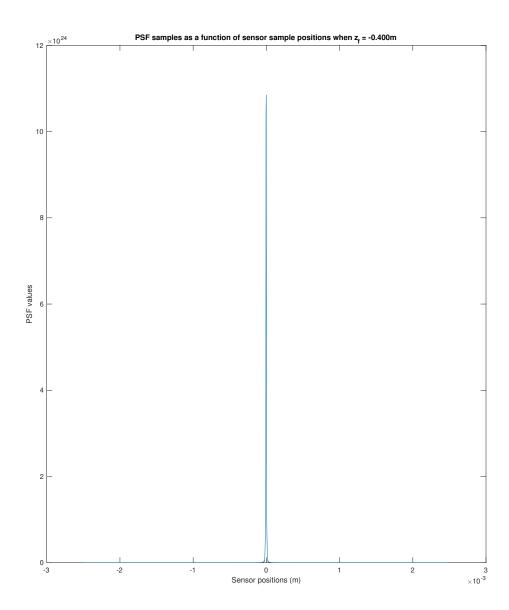


Figure 3.1 PSF results of the simulation with Fresnel synthesis

frequency. We chose spectral frequency of 15 as suggested in the instructions.

We fitted a 7th degree polynomial function to datapoints of MTF values as a function of z_f values. We chose to use 7th degree polynomial function, since after some experimentation, it seemed to visually be the best match for our datapoints. From the fitted function we could more confidentally determine the depth at which value of z_f the image would be the sharpest. For the Fresnel and Rayleigh-Sommerield synthezied holograms the values was -0.4190 and for the stereogram synthesis the value was -0.446, as can be seen from figures 3.7, 3.8 and 3.9.

The results where closely in line with the observations we made from the over-

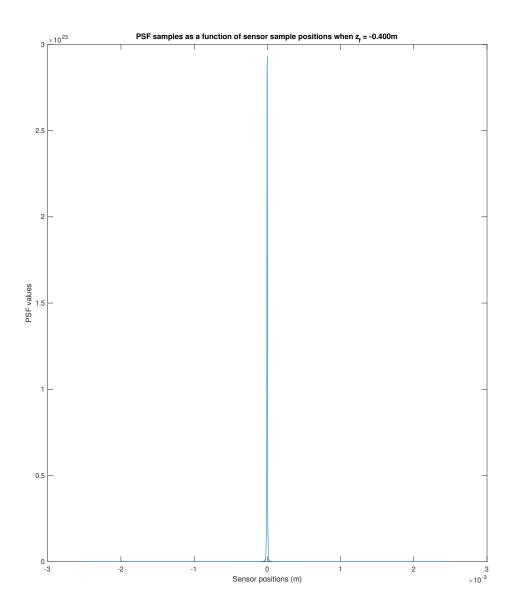
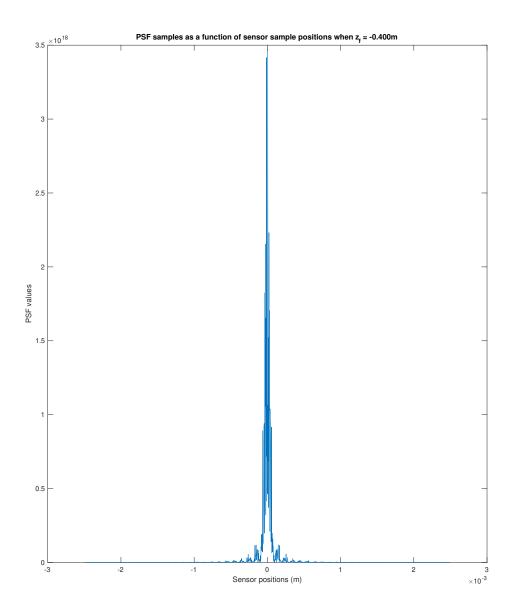


Figure 3.2 PSF results of the simulation with Rayleigh-Sommerfield synthesis

layed PSF images. The value optimal z_f value in our system is slightly offset from the expected optimal value of -0.4, which corresponds to the point source of the hologarm. This offset might be caused by bad approximations in the hologram synthesis or bad assumptions during the wave field propagation. Our fitting function might not be optimal for this case.



 $\textbf{\textit{Figure}} \quad \textbf{\textit{3.3} PSF results of the simulation with Holgraphic Stereopgram synthesis}$

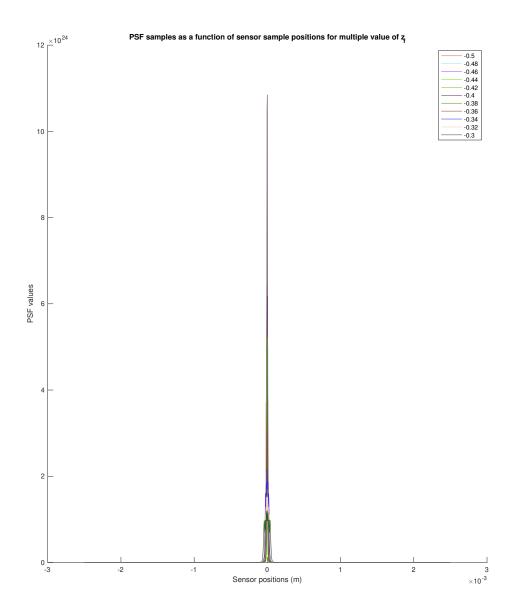


Figure 3.4 PSF results of the simulation with Fresnel synthesis, with multiple z_f values between -0.5 and -0.3

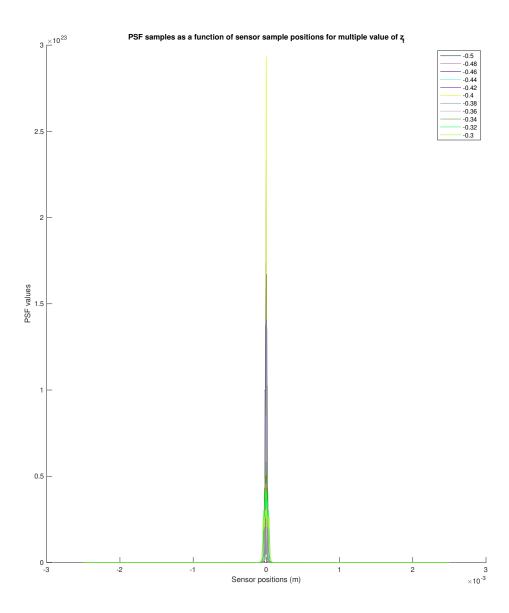


Figure 3.5 PSF results of the simulation with Rayleigh-Sommerfield synthesis, with multiple z_f values between -0.5 and -0.3

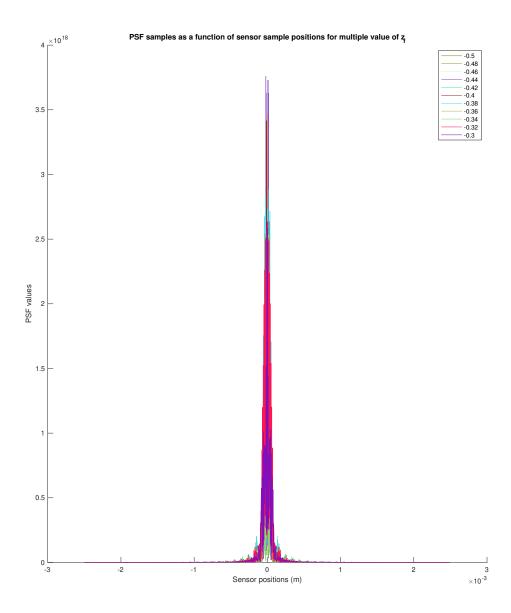
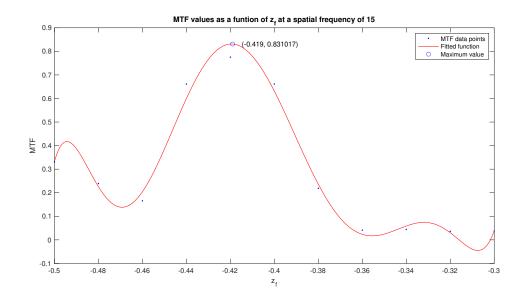
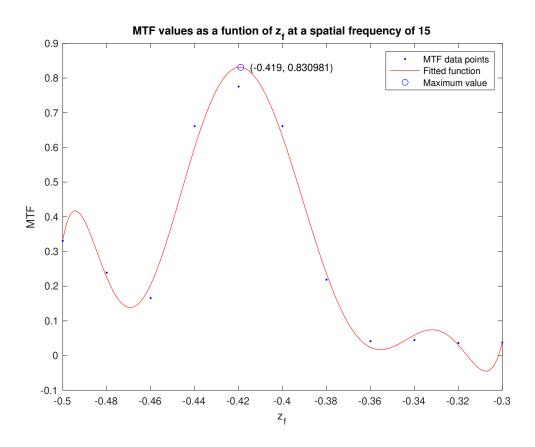


Figure 3.6 PSF results of the simulation with holograpic stereograph synthesis, with multiple z_f values between -0.5 and -0.3



 $\textbf{\textit{Figure}} \quad \textbf{\textit{3.7} MTF analysis results for Fresnel synthesis}$



 $\textbf{\textit{Figure}} \quad \textbf{\textit{3.8}} \ \textit{MTF analysis results for Rayleigh-Sommerfield synthesis}$

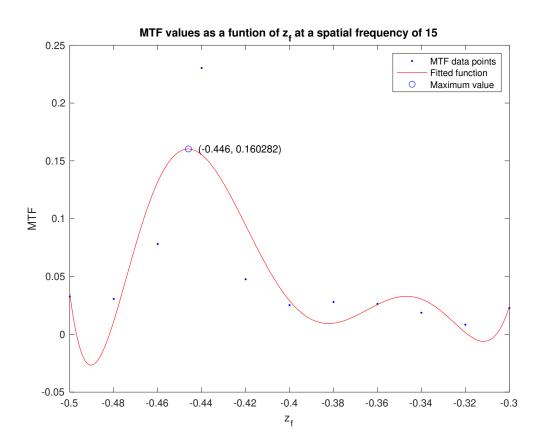


Figure 3.9 MTF analysis results for Holographic stereograph synthesis

4 Conclusions

APPENDIX A. Something extra

Appendices are purely optional. All appendices must be referred to in the body text