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Characterizing holographic displays via numerical simulations - Report

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Abstract

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Laboratory Report

Tampere University

Master's Degree Programme in Signal Processing

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The abstract is a concise 1-page description of the work: what was the problem, what was done, and what are the results. Do not include charts or tables in the abstract.

These instructions are intended for students of Computer Sciences at the Tampere University. They cover questions of writing a thesis, such as use of the literature, structure of the thesis and style, the external appearance of the thesis and the use of tools. These instructions do not cover the scientific content of the thesis.

Keywords: M.Sc. thesis, layout, writing style.

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1 Introduction

In this report we describe our work with the ‘Characterizing holographic displays via numerical simulations’ exercise, for the Advanced Signal Processing Laboratory Course.

In this project we familiarized ourselves with the basics of holographic display, by implementing a part of a holographics display viewing simulation. We implemented two holographic synthesis methods and a retinal image formation model, by contributing code to a MATLAB codebase given by the course faculty.

1.1 Hologram synthesis

Hologram synthesis describes the method for forming holographic images in 3d space from a given image. In this assignment, instead of using entire 3d space, the analysis can be simplified by considering only a cross section of the 3d space. The hologram is now represented as a 1D array of complex values. This simplification eases the computational load and also makes the process easier to handle.

1.2 Retinal Image Formation

In our exploration of holographic displays and their numerical characterization, Retinal Image Formation is a key part of the analysis. This simulation replicates how the human eye perceives visual information. Through this model, we obtain images on the retina, which can be used to analyze the perceived sharpness of the displayed content.

In these simulation tools, the human eye is considered as a camera, with the lens (the pupil) and the retina (the sensor). This simulation involves three key planes: the display (hologram), the lens, and the sensor. We model the pupil as a thin lens with a specific width, influencing how light passes through it.

2 Methodology

2.1 Implementing Hologram Synthesis

Our implementation of the holographic image viewer included three different methods of holographic image synthesis, one of which was provided in the code base given to us. The ready made synthesis method was holographic stereograph synthesis (HSS), [TODO: explain hss here]. The first synthesis method we implemented was a Fresnel hologram synthesis which is based on the Fresnel diffraction kernel. Using this kernel to define the 1D field $U(x; 0)$ for a single point source at (x_p, z_p) as

$$U(x; 0) = a_p \frac{\exp(jkz_p)}{\sqrt{j\lambda z_p}} \exp(jk \frac{(x - x_p)^2}{2z_p} + \phi_p), \quad (2.1)$$

where a_p is the amplitude of the point source, ϕ_p is the relative phase, λ is the wavelength of the monochromatic light (i.e. the color, if in visible spectrum) and $k = \frac{2\pi}{\lambda}$ is the wave number.

The second method we implemented was Rayleigh-Sommerfeld synthesis (RSS), which uses Rayleigh-Sommerfeld diffraction kernel.

$$U(x; 0) = a_p \frac{z_p}{\sqrt{j\lambda}[(x - x_p)^2 + z_p^2]^{\frac{3}{4}}} \exp[jk \sqrt{(x - x_p)^2 + z_p^2} + \phi_p] \quad (2.2)$$

This formula is similar to the Fresnel but has some differences in calculating the hologram.

2.2 Retinal Image Formation Simulation

To be able to view the synthesized holograms, we had to simulate the viewing process of an eye. This was achieved with a simplified wave propagation model, where human eye is represented by a simple lens and a one-dimensional sensor behind the lens in relation to the viewed hologram.

The transmittance of the lens is described by function 2.3

$$T(s) = \exp\left(\frac{-i\pi}{\lambda f} s^2\right) \quad (2.3)$$

where, f is the focal length of the lens.

The propagation of light from the hologram is modeled with a following field function 2.4

$$U(x; z) = \int \mathcal{F}\{U(\xi; z_0)\}(f_\xi) \exp[-2\pi i(f_\xi x + f_z z)] df_\xi \quad (2.4)$$

where,

$$f_z = \sqrt{\frac{1}{\lambda^2} - f_\xi^2} \quad (2.5)$$

[TODO: Explain these functions]

The simplified eye model differs from a real human eye in multiple cases. Firstly, sensor of the human eye consists, [TODO: Add stuff]

2.2.1 Field propagation implementation

The implementation of the field propagation was provided to us in the code base, in the *propagateField_PWD.m* file. The file starts with defining the basic parameters, which are current location of the eye, distance from lens to sensor, the focal length of the eye and the physical size of the hologram plane.

In the next step the file sets up the more complex parts of the simulation, like size of the sensor, properties of the propagating light and the sampling grid.

Finally the file executes the field propagation simulation, where each of the sections of the synthesized hologram are propagated through the wave field and the results are of the sensor are sampled to produce an image as PSF which is returned from the function.

3 Results

In this section we analyze the images produced by the implemented model.

From the simulation we attained an image consisting of multiple overlaid PSF images depicting the hologram formed on the simulated sensor. From the image 3.1 we can see that from the samples the z_f value of -0.42 produces the sharpest image, since most of the points fall in the origin. This is different from what would be expected, since in ideal situation the sharpest images should form with the same values as the distance to point source, which in our simulation is -0.4 . When the value of z_f moves away from -0.42 we expected the graph to widen, since image formed won't be as sharp and this is reflected in the figure, as the values closer to -0.42 produce higher graphs.

We also repeated this for Rayleigh-Sommerfield synthesis and Holographic stereogram synthesis, as shown in figures 3.2 and 3.3. The result for the Rayleigh-Sommerfield synthesis we basically identical, as the sharpest image, was obtained with the value of -0.42 and further away values produced wider graphs.

As for the holographic stereogram, the results different, in the sense that the sharpest image was produced with a z_f value of -0.44 . Also all the z_f values produced blurrier images as the graphs were wider. This would indicate that the holographic stereogram produces overall blurrier holograms.

3.1 MTF Analysis

With the multiple PSF images we performed MTF analysis to obtain the value of z_f which would provide the sharpest image. By generating multiple PSF images with different z_f values we were able to obtain multiple MTF values in particular spectral frequency. We chose spectral frequency of 15 as suggested in the instructions. We fitted a 7th degree polynomial function to datapoints of MTF values as a function of z_f values. We chose to use 7th degree polynomial function, since after some experimentation, it seemed to visually be the best match for our datapoints. From the fitted function we could more confidently determine the depth at which value of z_f the image would be the sharpest. For the Fresnel and Rayleigh-Sommerfield synthesized holograms the values was -0.4190 and for the stereogram synthesis the value was -0.446 .

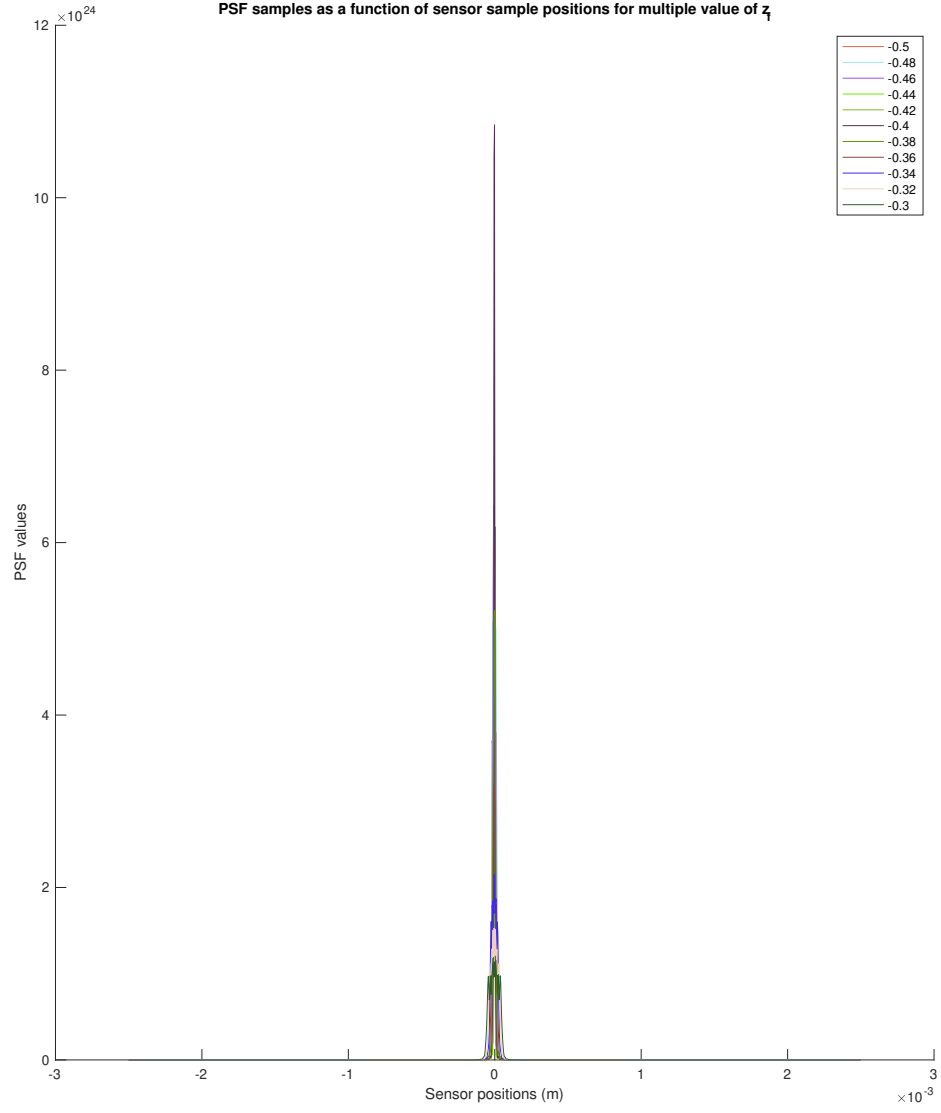


Figure 3.1 PSF results of the simulation with Fresnel synthesis, with multiple z_f values between -0.5 and -0.3

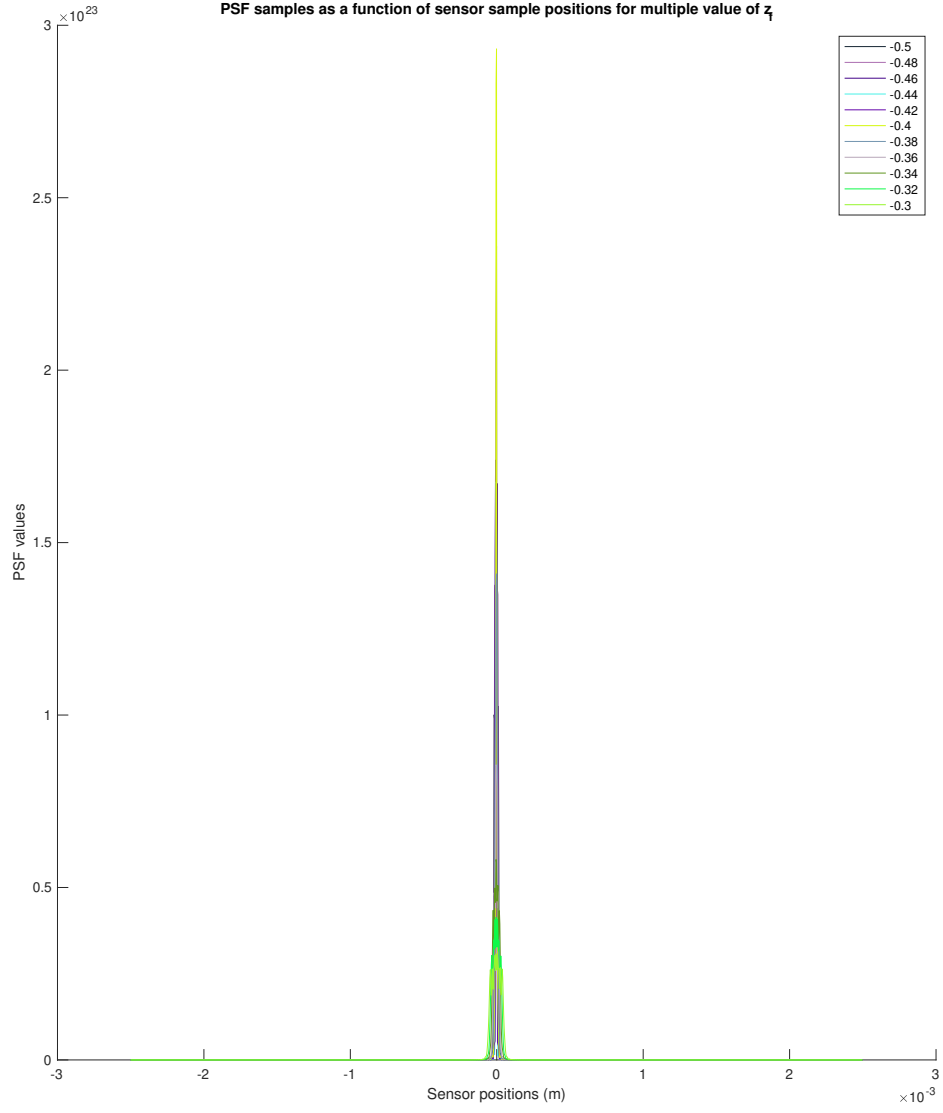


Figure 3.2 PSF results of the simulation with Rayleigh-Sommerfield synthesis, with multiple z_f values between -0.5 and -0.3

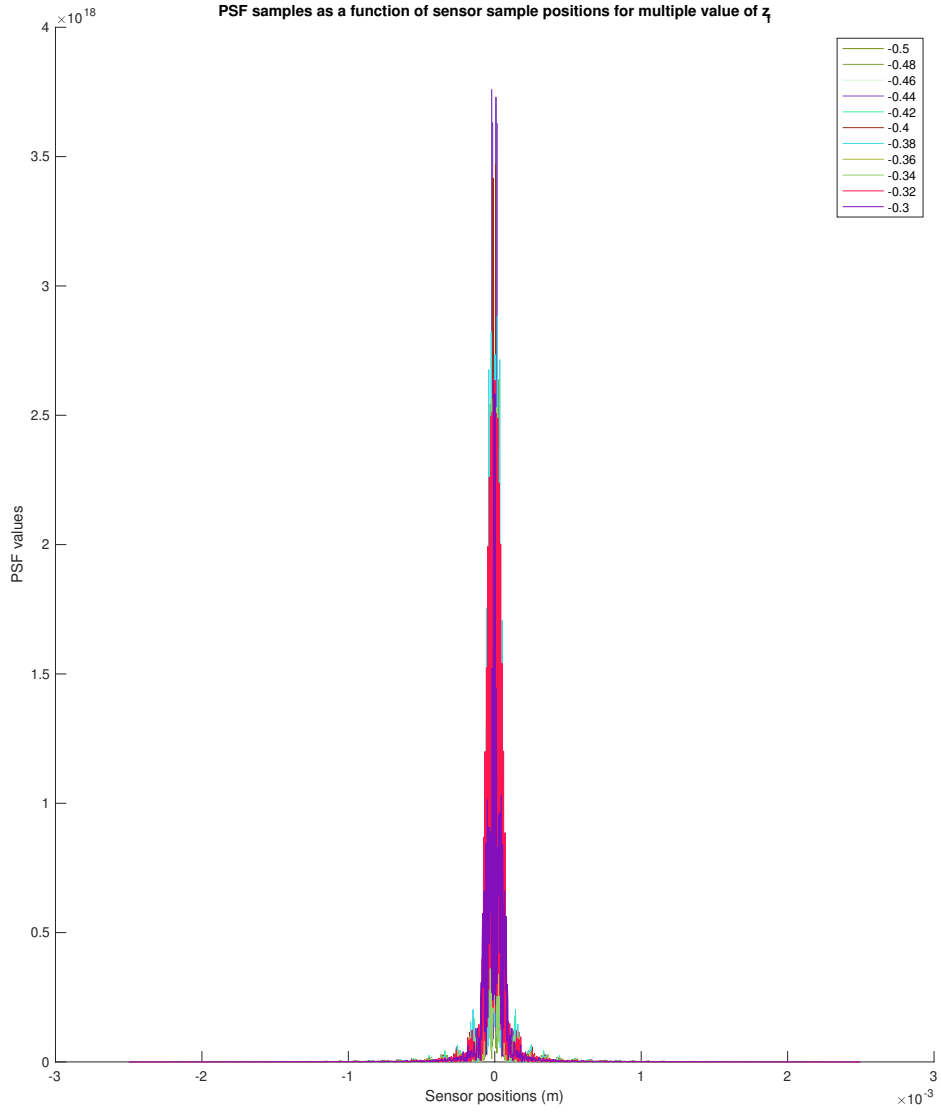


Figure 3.3 PSF results of the simulation with holographic stereograph synthesis, with multiple z_f values between -0.5 and -0.3

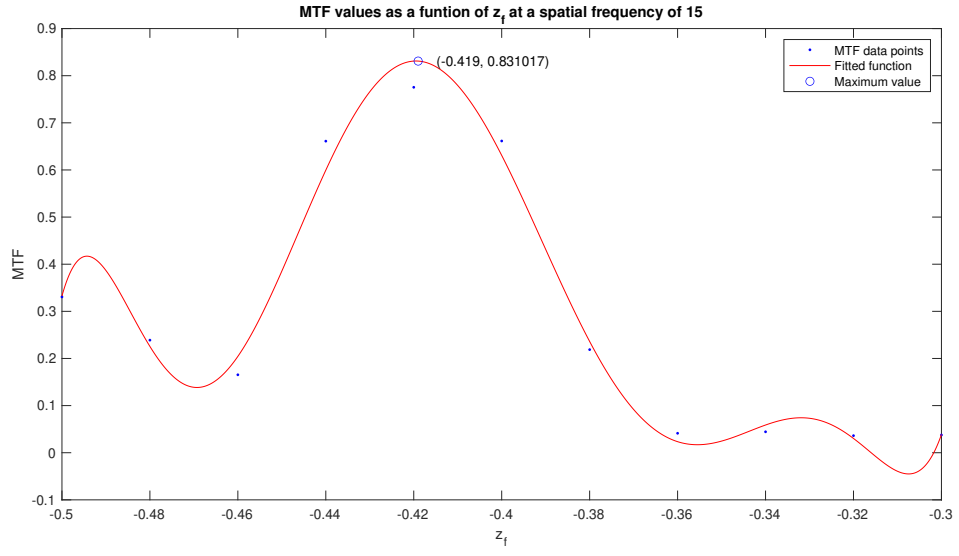


Figure 3.4 MTF analysis results for Fresnel synthesis

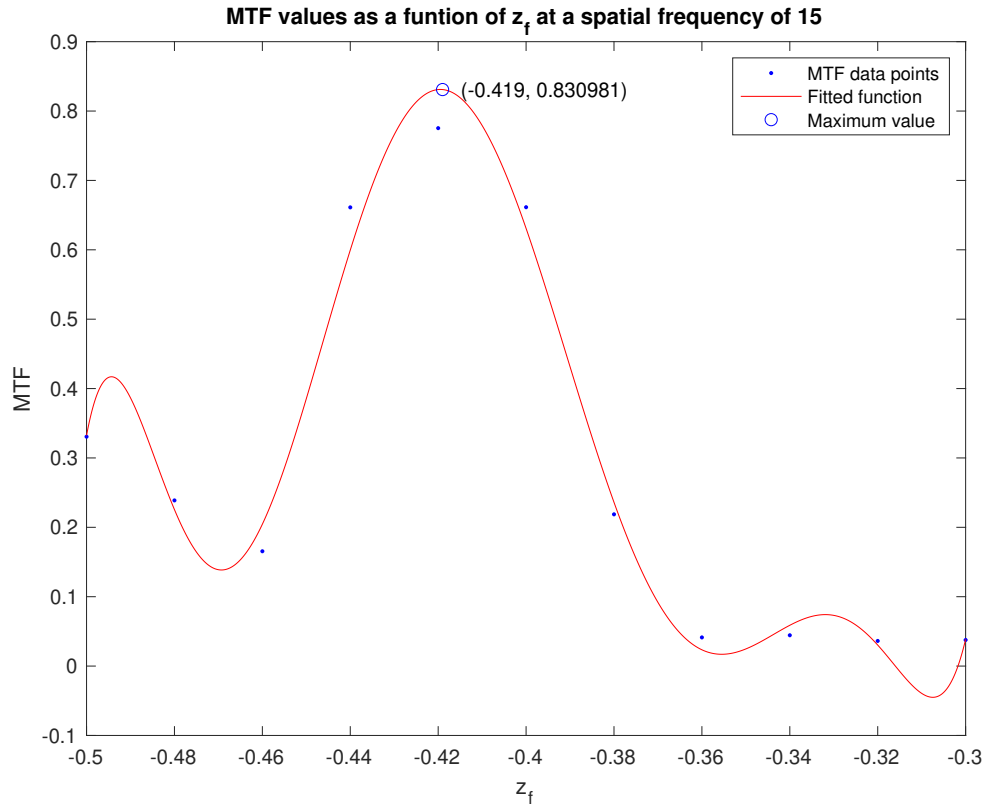


Figure 3.5 MTF analysis results for Rayleigh-Sommerfield synthesis

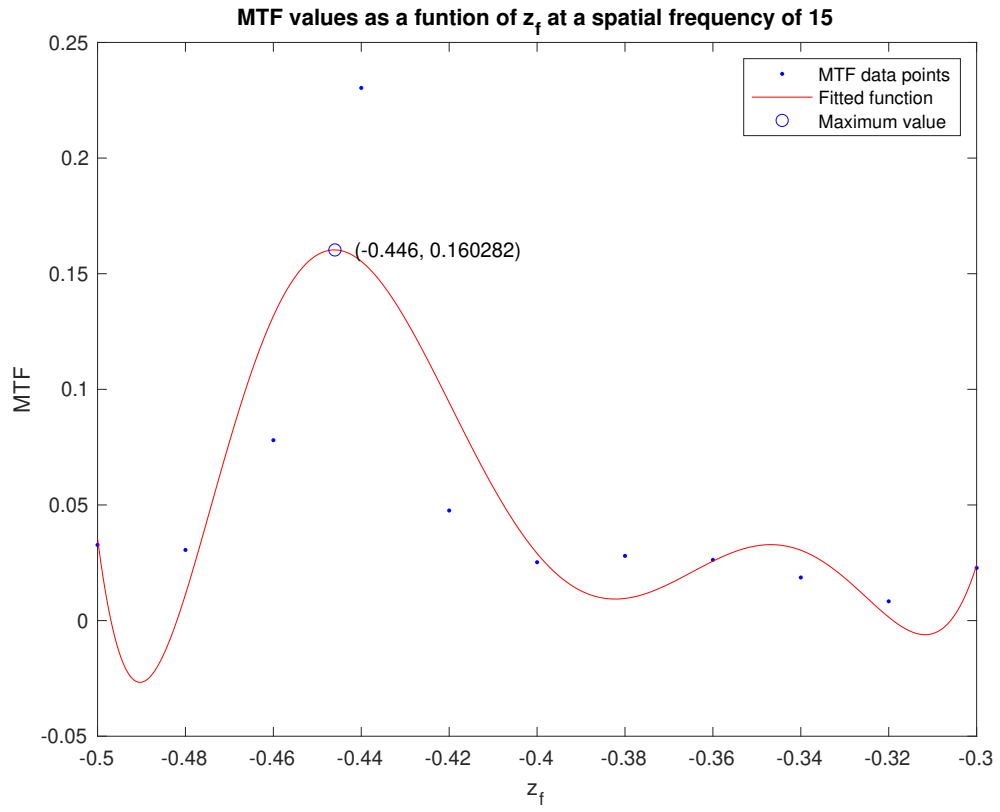


Figure 3.6 MTF analysis results for Holographic stereograph synthesis

4 Conclusions

APPENDIX A. Something extra

Appendices are purely optional. All appendices must be referred to in the body text