

13. Magnetic Effects of Electric Current

Ampere's circuital law

- The line integral of magnetic field induction \vec{B} around a closed path in vacuum is equal to μ_0 times the total current I threading it.

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 n I$$

Applications of Ampere's circuital law

- Magnetic field (B) due to a long straight conductor carrying current is given by $B = \frac{\mu_0 I}{2\pi r}$.

Here, r = radius and I = current

Solenoid

- It consists of an insulating long wire closely wound in the form of a helix.
- The magnetic field induction at a point as well as inside a solenoid is given by $B = \mu_0 n I$.
Here, n is the number of turns of the solenoid and I is the current flowing in the solenoid.

Toroid

It is a hollow circular ring on which a large number of turns of wire are closely wound.

The magnetic field (B) due to a toroid is given by $B = \frac{\mu_0 N I}{2\pi r}$.

Here, r = radius, I = current and N = no. of turns of the toroidal coil

Moving Coil Galvanometer

- Its working is based on the fact that when a current carrying coil is placed in a magnetic field, it experiences a torque that deflects the coil connected with the pointer.
- The suspension wire provides the restoring or control torque.
- The relation between deflection θ and current (I) is given by $I = k N B A \theta$.
 - $k N B A = G$ is the galvanometer constant.
 - Current sensitivity $= \frac{1}{k N B A}$
 - Voltage sensitivity $= \frac{1}{k N B A R}$
- Conversion of a Galvanometer into an Ammeter**
 - It can be converted into an ammeter by introducing a shunt resistance (r_s) of small value in parallel with it.
- Conversion of a Galvanometer into a Voltmeter**

- It can be converted into a voltmeter by introducing a series resistance of large value in series with it.
- **Advantages of a Moving Coil Galvanometer**
 - It is not affected by the Earth's magnetic field.
 - It has a high value of torque-weight ratio.
 - It is highly accurate and reliable.
 - Its scales are uniform.
- Sensitivity of moving coil galvanometer is given by $S = \frac{NBA}{C}$.

Here,

N = number of turns in the coil

B = magnetic field

A = area of the rectangular coil

C = twist constant of the suspension wire

- Fractional error in a galvanometer is given by $\frac{\Delta I}{I} = \frac{\Delta \theta}{\theta}$.

Motion of a charged particle in a uniform magnetic field

- In a uniform magnetic field B , a charge q executes a circular orbit in a plane normal to B .
- The magnetic force acts as the centripetal force.
- $q(\vec{v} \times \vec{B}) = \frac{mv^2}{r}$

If \vec{v} and \vec{B} are at right angles, then radius of the circular orbit, $r = \frac{mv}{Bq}$

- Time period (T), $T = \frac{2\pi m}{Bq}$
- Frequency of rotation, $\omega = \frac{Bq}{m}$

Motion of a charged particle in combined electric and magnetic field

- Generally, a charged particle moves in a spiral path when the magnetic and electric field are combined.
- **Velocity selector**
 - The magnetic and the electric field are perpendicular to each other.
 - At a certain velocity at which the net force due to the magnetic and the electric field is zero, we have:

$$qvB = qE \text{ or } v = \frac{E}{B}$$

Cyclotron

- It works on the principle that the frequency of revolution of a charged particle is not dependent on the energy.
- The electric and the magnetic field are used in combination to increase the energy.
- **Cyclotron frequency:**

$$v = Bqm$$

Limitations of Cyclotron

- It cannot accelerate uncharged particles like neutrons.
- There is a limit of speed beyond which a charged particle cannot be accelerated by a cyclotron.
- It cannot produce highly energetic particles with energy of the order of 500 MeV.