

# EE5609 Assignment 5

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**Abstract**—This assignment involves proving the equivalence of 2 lines that are formed inside an isosceles triangle because of certain given conditions via vector representation.

Download all latex-tikz codes from

[https://github.com/vimalkb007/EE5609/tree/master/Assignment\\_5](https://github.com/vimalkb007/EE5609/tree/master/Assignment_5)

## 1 PROBLEM STATEMENT

In an isosceles  $\triangle ABC$  with  $AB = AC$ ,  $D$  and  $E$  are points on  $BC$  such that  $BE = CD$ . Show that  $AD = AE$ .

## 2 SOLUTION

In the given  $\triangle ABC$ , let  $D$  and  $E$  be any arbitrary points on the side  $BC$  such that  $BE = CD$ .

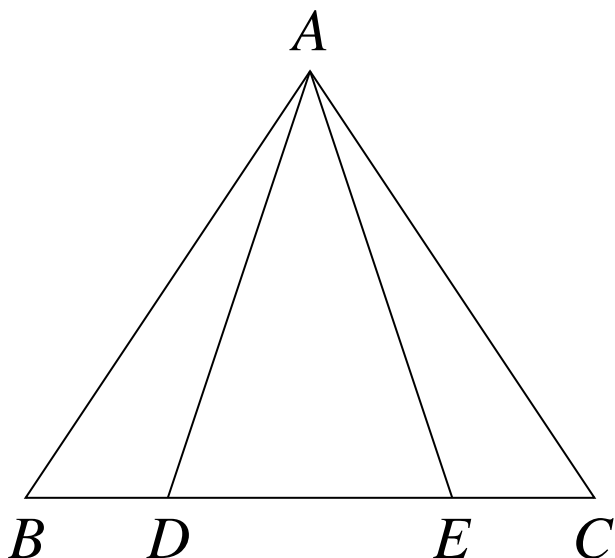


Fig. 1: Isosceles Triangle with sides  $AB = AC$

We are given that the sides  $AB = AC$ , and  $BE = CD$ . These two can be represented as

$$\|B - A\| = \|C - A\| \quad (2.0.1)$$

$$\|B - E\| = \|D - C\| \quad (2.0.2)$$

Since the given triangle is an isosceles triangle, the angles formed by  $AB$  and  $AC$  on  $BC$  will be the same. That is

$$\angle ABC = \angle ACB = \alpha \quad (2.0.3)$$

The side  $AD$  can be represented as

$$(D - A) = (B - A) - (B - D) \quad (2.0.4)$$

Squaring both the sides we get

$$\|D - A\|^2 = \|B - A\|^2 + \|B - D\|^2 - 2 \|B - A\| \|B - D\| \cos \alpha \quad (2.0.5)$$

The side  $AE$  can be represented as

$$(A - E) = (C - A) - (C - E) \quad (2.0.6)$$

Squaring both the sides we get

$$\|A - E\|^2 = \|C - A\|^2 + \|C - E\|^2 - 2 \|C - A\| \|C - E\| \cos \alpha \quad (2.0.7)$$

From (2.0.2), we can further write it as

$$\|E - B\| = \|B - D\| + \|E - D\| \quad (2.0.8)$$

$$\|C - D\| = \|C - E\| + \|E - D\| \quad (2.0.9)$$

From equations (2.0.2), (2.0.8) and (2.0.9) we can equate the L.H.S and get

$$\|B - D\| = \|C - E\| \quad (2.0.10)$$

Using equations (2.0.1), (2.0.10), we apply them in the equation (2.0.5), (2.0.7). After applying it we see that the R.H.S components are getting equated to each other, then we can equate the L.H.S as well. We get

$$\begin{aligned} \|D - A\|^2 &= \|A - E\|^2 \\ \|D - A\| &= \|A - E\| \end{aligned} \quad (2.0.11)$$

Therefore, we can say that  $AD = AE$ .