

# EE5609 Assignment 3

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**Abstract**—This assignment involves finding the determinant of the given matrix.

The python solution code for this problem can be downloaded from

[https://github.com/vimalkb007/EE5609/blob/master/Assignment\\_4/codes/assignment4\\_solution.py](https://github.com/vimalkb007/EE5609/blob/master/Assignment_4/codes/assignment4_solution.py)

$$\begin{aligned} & (-\sin^2 \alpha - \cos^2 \alpha)(-\sin^2 \beta - \cos^2 \beta) \\ \Rightarrow & (\sin^2 \alpha + \cos^2 \alpha)(\sin^2 \beta + \cos^2 \beta) = 1 \quad (2.0.3) \end{aligned}$$

Therefore, the determinant of the matrix is 1.

## 1 PROBLEM STATEMENT

Evaluate 
$$\begin{vmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta & -\sin \alpha \\ -\sin \beta & \cos \beta & 0 \\ \sin \alpha \cos \beta & \sin \alpha \sin \beta & \cos \alpha \end{vmatrix}.$$

## 2 SOLUTION

We first multiply either the rows or the columns, and then try taking the common element out.

$$\begin{vmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta & -\sin \alpha \\ -\sin \beta & \cos \beta & 0 \\ \sin \alpha \cos \beta & \sin \alpha \sin \beta & \cos \alpha \end{vmatrix} \begin{matrix} C_3 \leftarrow (\cos \alpha)C_3 \\ \longleftrightarrow \\ C_3 \leftarrow (\sin \alpha)C_3 \end{matrix}$$

$$\left( \frac{1}{\sin \alpha \cos \alpha} \right) \begin{vmatrix} \cos \alpha \cos \beta & \cos \alpha \sin \beta & -\sin^2 \alpha \cos \alpha \\ -\sin \beta & \cos \beta & 0 \\ \sin \alpha \cos \beta & \sin \alpha \sin \beta & \cos^2 \alpha \sin \alpha \end{vmatrix} \quad (2.0.1)$$

From (2.0.1)  $R_1$  we take out common element  $\cos \alpha$ . And from row  $R_2$  we take out common element  $\sin \alpha$

$$\begin{vmatrix} \cos \beta & \sin \beta & -\sin^2 \alpha \\ -\sin \beta & \cos \beta & 0 \\ \cos \beta & \sin \beta & \cos^2 \alpha \end{vmatrix} \xrightarrow{R_1 \leftarrow R_1 - R_3} \begin{vmatrix} 0 & 0 & -\sin^2 \alpha - \cos^2 \alpha \\ -\sin \beta & \cos \beta & 0 \\ \cos \beta & \sin \beta & \cos^2 \alpha \end{vmatrix} \quad (2.0.2)$$

Now, we can expand the determinant from row 1 in (2.0.2), and we get