Perception and Logistic Regnession ear find a hyperplane that reparates the data if the data is linearly separables. Then why SVM? -> SVM Jinds the hyperplane with Lest separability (largest margin) and thus gives better GENERALIZATION performance. we want to find a line that not only separates 2 knods of data but also maximizes the margin. W'x + b = 0 for $x \in \mathbb{R}^2$ $w_1 \times 1 + w_2 \times 2 + b = 0$ X2 2 (- W) X1 - (b) Hus form

Intercept. û = 33 11311, ₹ = ₹'-₹" — ① let r = rû - 1 will - * $\frac{11712}{1171} = 0. \quad \text{with } = 0.$ $\frac{11712}{1171} = 0.$ นาน = เมาะเมา = (Jw/+1/02) = 110112

 $\overrightarrow{Y} = \overrightarrow{X}' - \overrightarrow{X} - \overrightarrow{A}) \overrightarrow{Y} = \overrightarrow{X} \overrightarrow{A} - (b)$ WTZ = WTZ'-WTX w (xw) =1-6)-(6) Y WW = 1 1/10/1=1< $\omega^T\omega = \omega_1^2 + \omega_2^2$ = ([[[] 2]] 2 = 1112112 since margin = $2\gamma' = \frac{2}{\|\omega\|}$ We noant to learn w, b such that for all points for all points X; for which y: =-1, wTx; +6 <0)
and $\frac{2}{\|w\|}$ is as large as possible Xi for which Yiz 2 wTxi+670. How to Jind w and b for the boundary? Goal: Maximoze margin while incurring to baining error. Maximige 2 with 0 1944. Menenize 1/w/1 with 0 logg Min with o lopp

Ophinization Formulation

Minimize. $\frac{\|\omega\|^2}{2}$

N= 12,...N subject to yn(wTxn+6) ≥1 This is an optenization problem with N linear Inequality constraint.

Let's truy the constrained ophnization problem to unconstained.

Approach

(1) Add Lagrangian Constant

2) solve Dual Ophrnization problem as in this case result voll be equal to primal optimization problem as (a) function is convex lagrangian.

(b) constraints are affine (linear)

 $d^* = \max_{\omega} \sum_{\omega} L(\omega, \alpha, \beta)$

a = inequality B= equality

KKT conditions should be true

minimise $L(\omega, b, \alpha) = \frac{\|\omega\|^2}{2} + \sum_{x=1}^{N} x_x \left\{1 - y_x(\omega^T x_n + b)\right\}$ solving Dual

Setting $\frac{\partial}{\partial w} L(w_1b, x) = 0$ Setting $\frac{\partial}{\partial w} L(w_1b, x) = 0$

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Let x_1^*, x_2^* . x_n^* be the solution of QP problem $w = \sum_{n=1}^{N} x_n y_n x_n$. Get we from here $b = 1 - w^{-n}$ We can get B using KKT condition #5 $\sum_{n=1}^{\infty} \alpha_n \left(y_n \{ \omega^T x_n + b \} - 1 \right) = 0 \quad \text{and} \quad \alpha_n \geq 0$ Either on or (yn zwtxn+b-1) chould be o of and then yngwxn+b}-1 woulded. i.e. x_n is on the margin i.e. points are away from margin and thus these points will not participate at when we compute "w" only toaning points which are on the margin participate $\left| W = \sum_{n=2}^{\infty} \alpha_n y_n x_n \right|$ Only training examples that lie on the reagain are relevant. These are called Support Vectors we only save value of non-zero a and b For a test point x*

V = W x + b. No need to compute w. we shreatly use values of a & b. v = (\(\int \) \(\gamma_n \) \(\gamma_n \) \(\gamma_n \)

What if data is not linearly separable? we relax the constraint yn(w1xn+6) ≥ 1- gn +n=1...N En is called slack variable Optimization Problem for Non-separable case. Maximise f(w, 6) = 11w11 + C \(\sigma_{n21} \sigma_n \) euliet to yn(WTXn+b) ≥ 1-8n. 3n≥0 n=1...N C controls the Impact of margin & margin even Now support vectors are not just points which are on the margin but also those which are on the wrong side of the margin 1. Points on the margin (\$n=0) 2. Inside the margin but on correct side (0 < 3, < 1)3. On the wrong side of the hyperplane (3n ≥ 1) support vectors will be more in number.