

Module IV

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1 Maxwell's equations and EM waves

1.1 Topics to be covered.

1.1.1 Maxwell's equations

*Fundamentals of vector calculus, Divergence and Curl of \mathbf{E} and \mathbf{B} (static), Gauss' divergence theorem and **Stokes'theorem**. Description of laws of electrostatics, Faraday's laws of **EMI**. Current density \mathbf{J} and Equation of Continuity. Displacement current with derivation and Maxwell's equations in **vacuum***

1.1.2 EM Waves

The wave equation in differential form in free space (derivation using Maxwell's equations), Plane EM waves(in vacuum), Transverse Nature and Polarization of EM waves

2 Fundamentals of vector calculus

A *scalar* is a physical quantity with only magnitude.

A *vector* is a physical quantity with both magnitude and direction.

A *unit vector* like \hat{a} has a magnitude of 1

In *Cartesian coordinates*, $\vec{a} = a_1\mathbf{e}_1 + a_2\mathbf{e}_2 + a_3\mathbf{e}_3$ where $\mathbf{e}_1, \mathbf{e}_2$ and \mathbf{e}_3 are unit vectors.

Magnitude $|a| = \sqrt{a_1^2 + a_2^2 + a_3^2}$

2.1 Dot product (scalar product)

$a \cdot b = |a| \cdot |b| \cdot \cos(\theta) = a_1b_1 + a_2b_2 + a_3b_3$ is a scalar

2.2 Cross product (vector product)

$$a \times b = |a||b|\sin(\theta)\hat{n}$$

In terms of components a and b

$$a \times b = \begin{vmatrix} \mathbf{e}_1 & \mathbf{e}_2 & \mathbf{e}_3 \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}$$

or

$$a \times b = ()$$