

A system is composed of two harmonic oscillators, each of natural frequency  $\omega_0$ , and having permissible energies  $(n + 1/2)\hbar\omega_0$ , where  $n$  is any non-negative integer. The total energy of the system is  $E' = n'\hbar\omega_0$ , where  $n'$  is a positive integer.

- For a given energy, how many microstates are available to the system ? What is \* the entropy of the system ?
- A second system is also composed of two harmonic oscillators, each of natural frequency  $2\omega_0$ . The total energy of this system is  $E'' = n''\hbar\omega_0$ , where  $n''$  is an even integer.
  - How many microstate are available to this system ?
  - What is the entropy of a system composed of the two preceeding subsystems (separated and enclosed by a totally restrictive wall) ? Express the entropy as a function of  $E'$  and  $E''$ .

We are now asked to estimate the probability of  $E - \langle E \rangle = 10^{-6} \langle E \rangle$  for a system of  $N = 10^{21}$ .

Take an ideal gas  $\langle E \rangle = \frac{3}{2} N k_B T$ ,  $C_V = \frac{3}{2} N k_B$

(Note  $(E - \langle E \rangle)^2 \sim N^2$ ,  $C_V \sim N$  only, so the standard deviation  $\sim \frac{1}{N}$ )

$$\Rightarrow \frac{p(E)}{p(\langle E \rangle)} \sim e^{-10^9}$$

This is for a monatomic ideal gas. People may use different models.