

HYPERPARAMETERS

① Weight → 'uniform' or 'distance'.

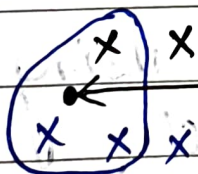
- uniform → each node has same value. Mukesh ambani & Umayak node are considered "same".

- distance → The neighbors which are close will be assigned more weight.

- generally → $W = \frac{1}{\text{distance}}$.

Ex1 →

- When weight is uniform



Query, and $k=3$

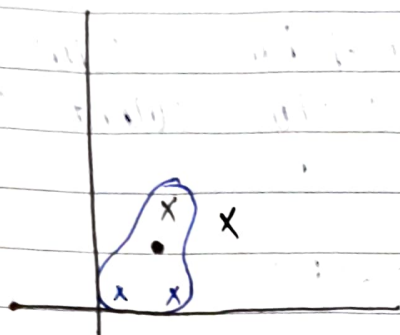
majority count

no of blue	2
no of black	1

- Since blue count is more for $k=3$, new query will be assigned to blue.

Ex2

When $w = \text{'distance'}$



pt	distance	w
X	0.1	$\frac{1}{0.1}$
X	0.9	$\frac{1}{0.9}$
X	0.8	$\frac{1}{0.8}$

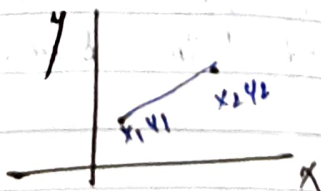
$$\left(\frac{1}{0.1} > \frac{1}{0.9} + \frac{1}{0.8} \right)$$

- Since Black weightage is more than of blue pts the query pt will be assigned to black.

② Types of Distances

- Distance we were using was euclidian distance.
- There are other types of distances too.

a) Euclidian distance: shortest distance between 2 points



dis = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

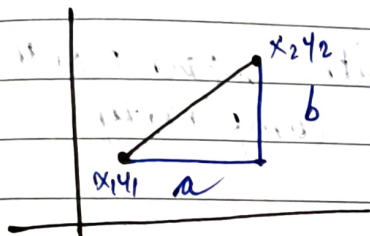
for 3 dimensions $\rightarrow \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$

for n dimension $\rightarrow \left(\sum_{i=1}^d |x_{2i} - x_{1i}|^2 \right)^{\frac{1}{2}}$

$d \rightarrow$ no of dimensions

Also called L2 norm.

b) Manhattan distance



- $a + b =$ manhattan distance.
- also called taxi cab distance
- L1 Norm

$m = \sum_{i=1}^d |x_{2i} - x_{1i}| \rightarrow$ for n dimensions

for 2 pts \rightarrow dim $\Rightarrow |x_2 - x_1| + |y_2 - y_1|$

c) Minkowski \rightarrow custom Norm

$p=2 \Rightarrow$ Eucl $\rightarrow \sum_{i=1}^d \left(|x_{2i} - x_{1i}|^2 \right)^{\frac{1}{2}}$

$p=1 \Rightarrow$ Manhattan $\rightarrow \sum_{i=1}^d \left(|x_{2i} - x_{1i}|^1 \right)^{\frac{1}{1}}$

$p=3 \Rightarrow$ L3 Norm $\rightarrow \sum_{i=1}^d \left(|x_{2i} - x_{1i}|^3 \right)^{\frac{1}{3}}$

$p \Rightarrow p \rightarrow \sum_{i=1}^d \left(|x_{2i} - x_{1i}|^p \right)^{\frac{1}{p}}$