

T-TEST

Studying independently the relation b/w input and output.

Select a column and perform T-Test

Steps:

1. State the null & alternate hypothesis.

For slope (β_1)

Null hypothesis (H_0): $\beta_1 = 0$ (no relation b/w x and Target)

Alternate hypothesis (H_1): $\beta_1 \neq 0$ (relation exists)

For intercept

Null hypothesis (H_0): $\beta_0 = 0$ (no relation i.e. line passes through origin)

Alternate hypothesis (H_1): $\beta_0 \neq 0$ (doesn't pass through origin)

② fit the regression & sample coef

$b_0, b_1 \rightarrow$ model coef

③ calculate standard error for b_1 & b_0

$$SE(b_1) = \sqrt{\frac{\sum (y_i - \hat{y}_i)^2}{(n-2) \sum (x_i - \bar{x})^2}}$$

$$SE(b_0) = \sqrt{\frac{\sum (y_i - \hat{y}_i)^2}{(n-2)} \left[\frac{1}{n} + \frac{\bar{x}^2}{\sum (x_i - \bar{x})^2} \right]}$$

④ compute T-stat

$$T_{stat} b_1 = \frac{b_1 - 0}{SE(b_1)}$$

hypothetical value for b_1 which is 0

$$T_{stat} b_0 = \frac{b_0 - 0}{SE(b_0)}$$

To check if the x input is important or not.



calculate P-value for $T_{stat} b_1$ (2 tail)

if P-value is less than 0.05 (significance) then we can reject null hypothesis.

ie the statement $P_1 = 0$ is false. Hence the associate column is important

If there are multiple columns we will perform t-test and even for intercept

CONFIDENCE interval for coef

Provides a interval for coef

Formula

→ calculated using significance level and df

$$CI_{b_0} = b_0 \pm \underline{t\text{-value}} \times SE(b_0)$$

$$CI_{b_1} = b_1 \pm \underline{t\text{-value}} \times SE(b_1)$$

→ calculated using significance level & degree of freedom

Example

$$CI_{b_1} = 0.0450 \pm 3.18 \times (0.001)$$

$$CI_{b_1} = 0.0006$$