

$$\alpha_p = 3 \text{ dB} \quad \alpha_s = 10 \text{ dB}$$

$$\omega_c = 2 \times \pi \times 1000 = 2000\pi \text{ rad/sec}$$

$$\omega_s = 2 \times \pi \times 350 = 700\pi \text{ rad/sec}$$

$$T = \frac{1}{f} = \frac{1}{5000} = 2 \times 10^{-4} \text{ sec}$$

$$\omega_p = \frac{2}{T} \tan \frac{\omega_p T}{2} = \frac{2}{2 \times 10^{-4}} \tan \left(\frac{2000\pi \times 2 \times 10^{-4}}{2} \right)$$

$$= 7265 \text{ rad/sec}$$

$$\omega_s = \frac{2}{T} \tan \frac{\omega_s T}{2} = \frac{2}{2 \times 10^{-4}} \tan \left(\frac{700\pi \times 2 \times 10^{-4}}{2} \right)$$

$$= 0.2235 \text{ rad/sec}$$

Order of Filter

$$N = \frac{\log \sqrt{\frac{10^{0.1 \alpha_p} - 1}{10^{0.1 \alpha_s} - 1}}}{\log \frac{\omega_s}{\omega_p}} = \frac{\log 3}{\log 3.25}$$

$$= 0.932$$

$$\omega_c = 1 \text{ rad/sec} \rightarrow H(s) = \frac{1}{1+s}$$

$$\therefore \omega_c = \omega_p = 7265 \text{ rad/sec}$$

$$\delta = \frac{\omega_c}{\omega_p} \quad \text{or } \delta \rightarrow \frac{7265}{\omega}$$

$$H(s) = \frac{1}{s+1}$$

$$\frac{1}{s+7265}$$

Apply Bilinear Transform:

$$H(z) = H(s) \Big|_{s = \frac{2}{T} \left(\frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$= \frac{1}{s+7265} \Big|_{s = \frac{2}{2 \times 10^{-4}} \left(\frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$= \frac{1}{\frac{10000}{1} \left(\frac{1-z^{-1}}{1+z^{-1}} \right) + 7265}$$

$$= \frac{10000 \left(\frac{1-z^{-1}}{1+z^{-1}} \right) + 7265}{10000 \left(\frac{1-z^{-1}}{1+z^{-1}} \right) + 7265}$$

$$= \frac{0.5722 (1-z^{-1})}{1 - 0.1584 z^{-1}}$$

$$1 - 0.1584 z^{-1}$$