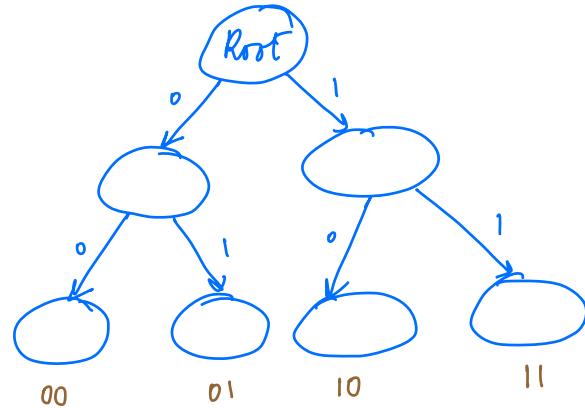


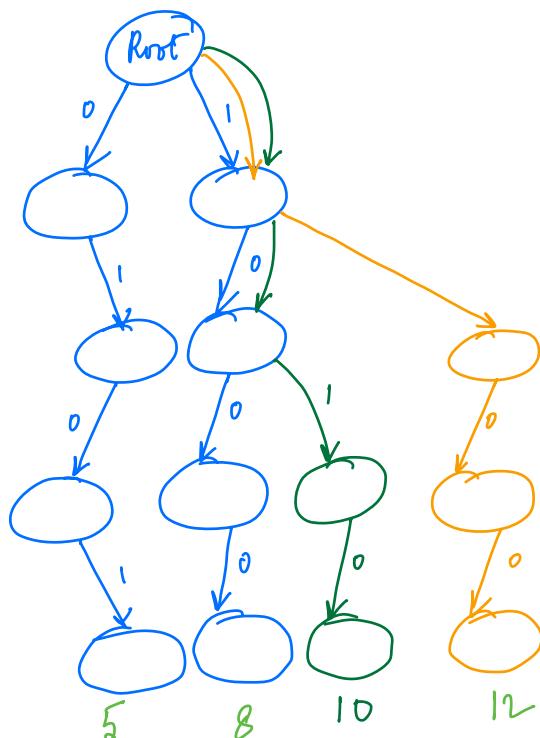
- Trie of Bits
- Maximum XOR Pair
- Maximum XOR Subarray
- Flatten binary tree to linked list
- Find swapped nodes on BST

## Trie of Bits

Binary Tree where each edge denotes a 0/1. Each non-leaf node has 2 children.



5 → MSB 0101 LSB  
8 → 1000  
12 → 1100  
10 → 1010



```
class Node {  
    Node children[];  
    Node() {  
        children = new Node[2];  
    }  
}
```

Q1) Given an integer array  $A[]$ , find the max value of  $(A[i] \wedge A[j])$   
 for all  $i, j$  pairs.

$$A = \{3, 5, 2\}$$

$$\begin{array}{c}
 3 \wedge 5 \\
 \hline
 11 \\
 \wedge 101 \\
 \hline
 110 \rightarrow 6
 \end{array}
 \quad
 \begin{array}{c}
 3 \wedge 2 \\
 \hline
 11 \\
 \wedge 10 \\
 \hline
 1 \rightarrow 1
 \end{array}
 \quad
 \begin{array}{c}
 5 \wedge 2 \\
 \hline
 101 \\
 \wedge 10 \\
 \hline
 111 \rightarrow 7
 \end{array}$$

Brute force  $\rightarrow O(n^2)$  T.C.  
 $O(1)$  S.L.

### Optimization

$$\begin{array}{l}
 \text{4-bit nos.} \rightarrow \\
 \begin{array}{l}
 1000 \rightarrow 2^3 = 8 \\
 0111 \rightarrow 2^2 + 2^1 + 2^0 = 7
 \end{array}
 \end{array}$$

MSB is more powerful than all the bits to its right taken together.

$\rightarrow$  We should try to get a 1 in the MSB (best effort)

$\rightarrow$  " try to get a 1 in the 2<sup>nd</sup> leftmost bit (best effort)

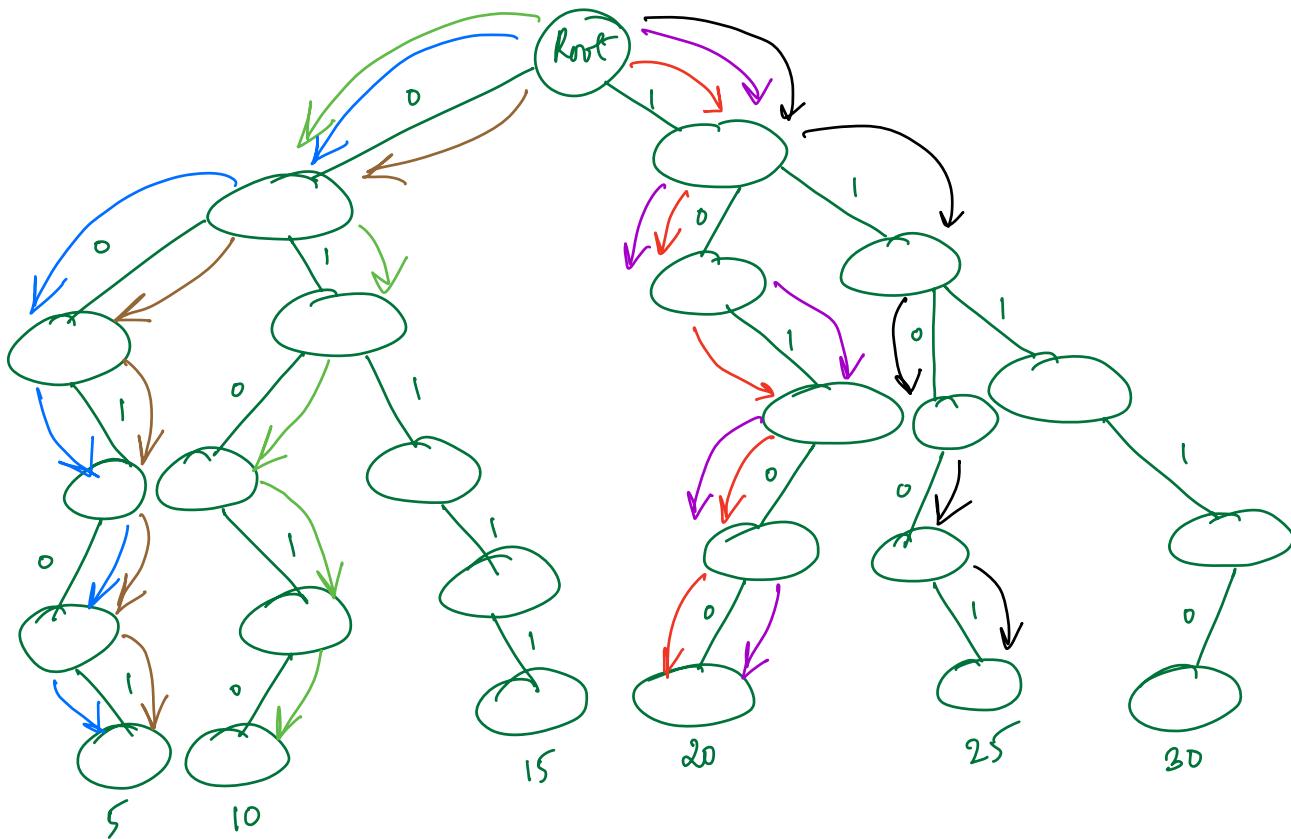
⋮

$$A[] \rightarrow \{20, 30, 15, 25, 10, 5\}$$

$$\hookrightarrow \# \text{ bits} = 5.$$

$$\begin{array}{l} 20 \rightarrow 10100 \xrightarrow{\text{XOR}} 11110 \rightarrow 30 \\ 30 \rightarrow 11110 \xrightarrow{\text{XOR}} 11011 \rightarrow 27 \\ 15 \rightarrow 01111 \xrightarrow{\text{XOR}} 11011 \rightarrow 27 \\ 25 \rightarrow 11001 \xrightarrow{\text{XOR}} 11100 \rightarrow 28 \\ 10 \rightarrow 01010 \xrightarrow{\text{XOR}} 11110 \rightarrow 30 \\ 5 \rightarrow 00101 \xrightarrow{\text{XOR}} 11100 \rightarrow 28 \end{array} \left. \begin{array}{l} \text{mod} \\ = 30. \end{array} \right\}$$

$$\begin{array}{l} 20 \rightarrow 10100 \xrightarrow{\text{XOR}} 11110 \\ \text{Best Partner} \rightarrow 01010 \xrightarrow{\text{XOR}} 11110 \\ \downarrow \\ 30 \end{array}$$



$$\begin{array}{l} 20 \rightarrow 10100 \\ \downarrow \downarrow \downarrow \downarrow \downarrow \\ 01010 \\ \hline 11110 \\ 30 \end{array}$$

$$\begin{array}{l} 30 \rightarrow 11110 \\ 00001 \\ \hline 11011 \\ 27 \end{array}$$

$$\begin{array}{l} 15 \rightarrow 01111 \\ 10000 \\ \hline 11011 \\ 27 \end{array}$$

$$\begin{array}{l} 25 \rightarrow 11001 \\ 00110 \\ \hline 11100 \\ 28 \end{array}$$

$$\begin{array}{r}
 10 \rightarrow 01010 \\
 10101 \\
 \text{p} \\
 \hline
 11110 \\
 \hline
 30
 \end{array}$$

$$\begin{array}{r}
 5 \rightarrow 00101 \\
 11010 \\
 \text{p} \\
 \hline
 11100 \\
 \hline
 28
 \end{array}$$

$$\text{Ans} \rightarrow \underline{30}.$$

class Node {

Node children [ ];

Node () {

children = new Node [2];

}

} int findMaxXor (root, x) {

cur = root; num = 0

for (i=30; i >= 0; i--) {

bit = ((x >> i) & 1);

t = (1 & bit);

if (cur. children [t] != null) {

cur = cur. children [t]; num |= ((1 << i) \* t);

}

else {

cur = cur. children [bit]; num |= ((1 << i) \* bit);

}

} return (x & num);

}

mx = 0;

fn(i=0; i < n; i++) {

y = findMaxXor (root, A[i]);

mx = max(mx, y);

}

T.C.  $\rightarrow n * \# \text{bits}$

$= n * 31$

$= O(n)$

$\underline{\underline{SC}} \rightarrow O(n)$ .

$t = 1 \rightarrow \overset{i}{10000 \dots 0} \xrightarrow{\text{OR}} \boxed{\dots | 1 \dots}$

$t = 0 \rightarrow 00000 \dots 0 \xrightarrow{\text{OR}} \boxed{\dots \dots}$

$$x = 20$$

$$\begin{smallmatrix} 5 & 4 & 3 & 2 & 1 & 0 \\ | & 0 & 1 & 0 & 0 \end{smallmatrix}$$

$$\boxed{0 \ 0 \ 1 \ 0 \ 1 0 0} \xrightarrow{\text{pink}}$$

$$i = 5$$

$$\begin{aligned} (x \gg i) \& 1 = (20 \gg 5) \& 1 \\ &= (00) \& 1 = 0 \end{aligned}$$

$$i = 2$$

$$(x \gg 2) \& 1 = \underbrace{(101)}_2 \& 1 = 1.$$

$$\boxed{10100} \xrightarrow{\text{blue}}$$

Q2) Find the maximum XOR of subarray, out of all subarrays.

$\boxed{4 \ 6 \ 1}$

4

6

1

$$4 \wedge 6 = 2$$

$$4 \wedge 6 \wedge 1 = 3$$

$$\boxed{6 \wedge 1 = 7} \quad \text{Best} =$$

$\text{pxor} \rightarrow \boxed{4 \ 2 \ 3}$

$\downarrow \text{xor}$

$7 \rightarrow \text{Best}$ .

```
int Pxor[] = new int[n+1];
Pxor[0] = 0;
for (i=0; i<n; i++) {
    Pxor[i+1] = Pxor[i]  $\wedge$  A[i];
}
```

// Find the max xor pair in pxor array.

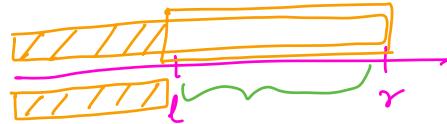
..

$O(n)$  T.C

$O(n)$  S.C.

$$\text{sum}(A[l \dots r]) = \text{Psum}[r] - \text{Psum}[l-1]$$

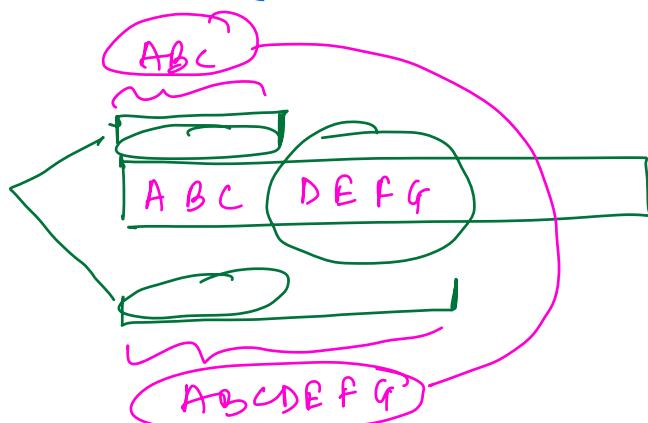
$$\text{xor}(A[l \dots r]) = \text{Pxor}[r] \wedge \text{Pxor}[l-1]$$



$[i, j] \rightarrow \text{Pxor}[j] \wedge \text{Pxor}[i-1]$ ,  
if  $i > 0$ .

$\text{Pxor}[j]$  if  $i = 0$ .

$$\downarrow \\ (\text{Pxor}[j] \wedge 0)$$

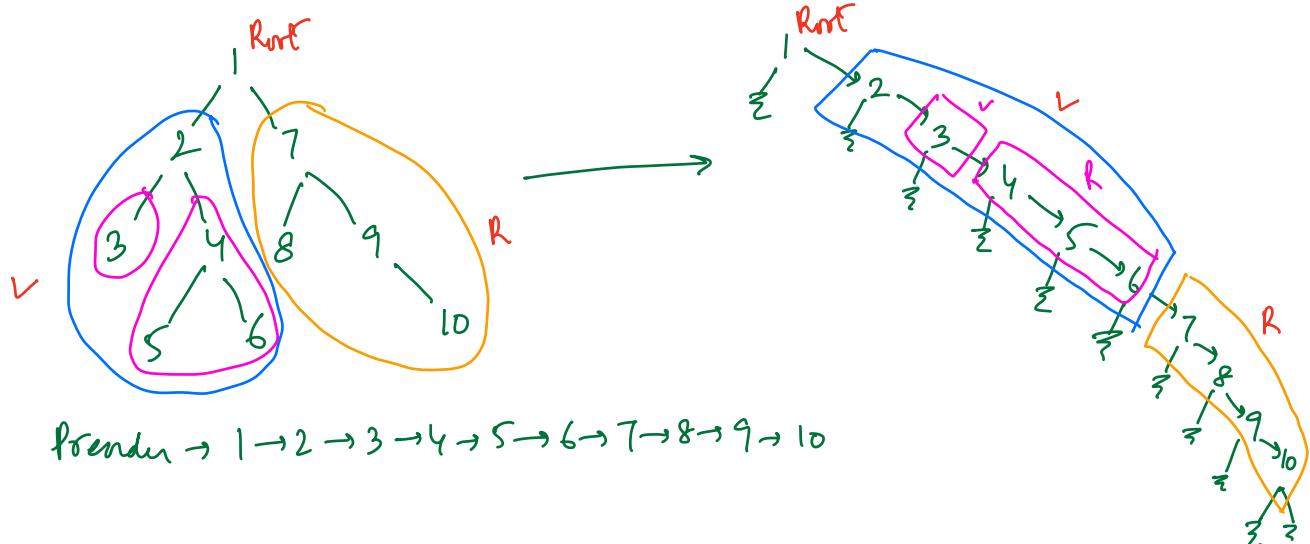


$$(A \wedge B \wedge C) \wedge (A \wedge B \wedge D \wedge E \wedge F \wedge G)$$



[Break till 10:45 PM]

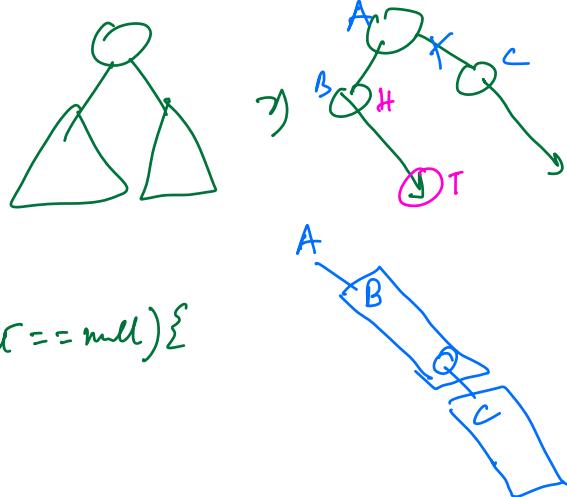
Q3) Flatten the given binary tree in Preorder manner such that right child will become the next node and left child of all nodes is null.



```

Pair flatten(TreeNode* root) {
    if (root == null)
        return {null, null};
    L = flatten(root.left);
    R = flatten(root.right);
    if (root.left == null && root.right == null)
        return {root, root};
    if (root.right == null) {
        root.right = root.left;
        root.left = null;
        return {root, L.tail};
    }
    else if (root.left == null)
        return {root, R.tail};
}

```



```

class Pair {
    Node head;
    Node tail;
}

```

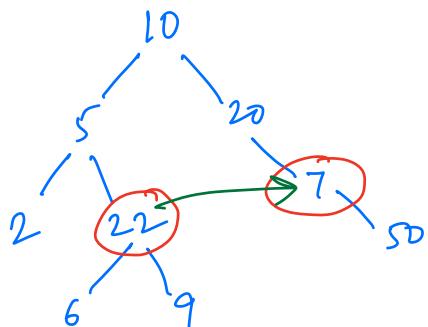
$O(n) T.C$   
 $O(h) S.C.$

```

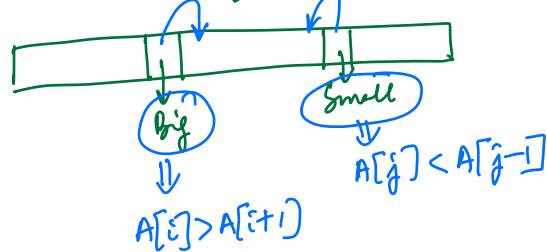
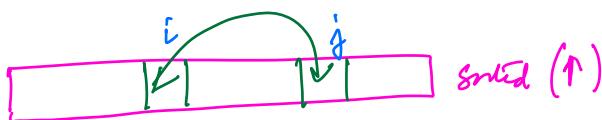
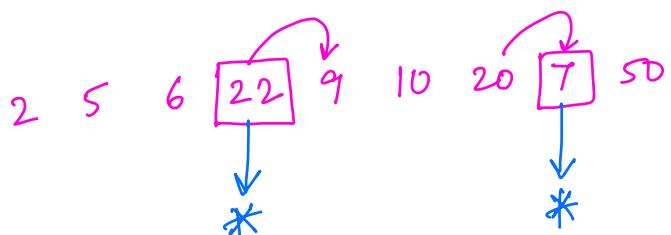
else{
    root.right = L.head;
    L.tail.right = R.head;
    root.left = null;
    return {root, R.tail};
}
}

```

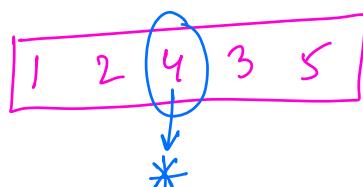
Q4) Given a BST, where 2 nodes have been swapped, find the values of the 2 nodes. (All the values in BST are distinct)



Inorder of given Tree  $\rightarrow$  UNSORTED.



1 2 3 4 5



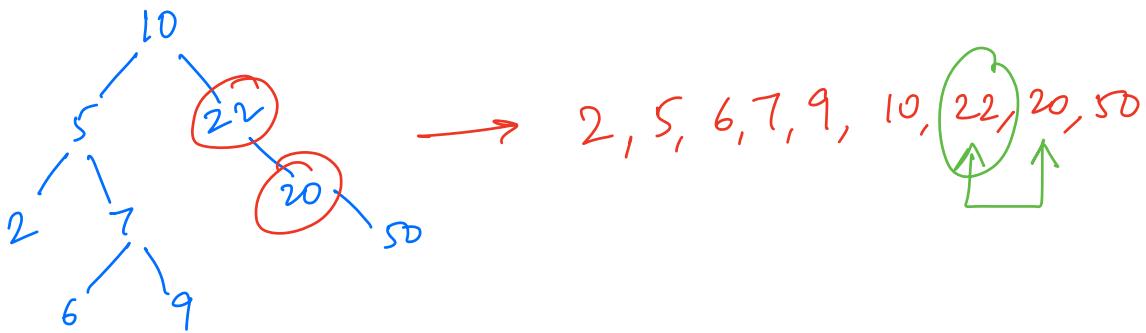
Find out no. of areas of wrong order

2

$\rightarrow$  bigger element of 1st area  
 $\rightarrow$  smaller element of next area

1

$\rightarrow$  bigger element  
 $\rightarrow$  next element.



$O(n)$  T.C  
 $O(h)$  S.C.  $\longrightarrow O(1)$  S.C.

```

last = null      next = 0
ans1 = 0
ans2 = 0
void inoder ( Node root ) {
    if ( root == null )
        return;
    inoder ( root . left )
    if ( last != null && root . data < last . data ) {
        if ( ans1 == 0 )
            ans1 = last . data , next = root . data
        else
            ans2 = root . data
    }
    last = root ;
    inoder ( root . right );
}

```

```

main ( ) {
    ;
    inoder ( root );
    if ( ans2 != 0 )
        print ( ans1, ans2 )
    else
        print ( ans1, next )
}

```