

Rigidity transition in biological tissues

**Student discussion group
IMSc, Chennai**

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Upto now

Embryonic development, cancer metastasis, wound healing:

- Early stage: large scale movement \Rightarrow fluid-like rheology
- Later stage: need to support forces and stresses \Rightarrow solid-like rheology

Many biological tissues are close to glass transition

- Caging: MSD and NGP
- Dynamical heterogeneity: Four point correlation function

Models for dense tissues

Active particle models

Active matter models + short-range repulsive/attractive interactions



Glass transition in self-propelled particle models is identical to adhesive colloids

Activity generates an effective adhesion

PRL 112, 220602 (2014)

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week ending
6 JUNE 2014

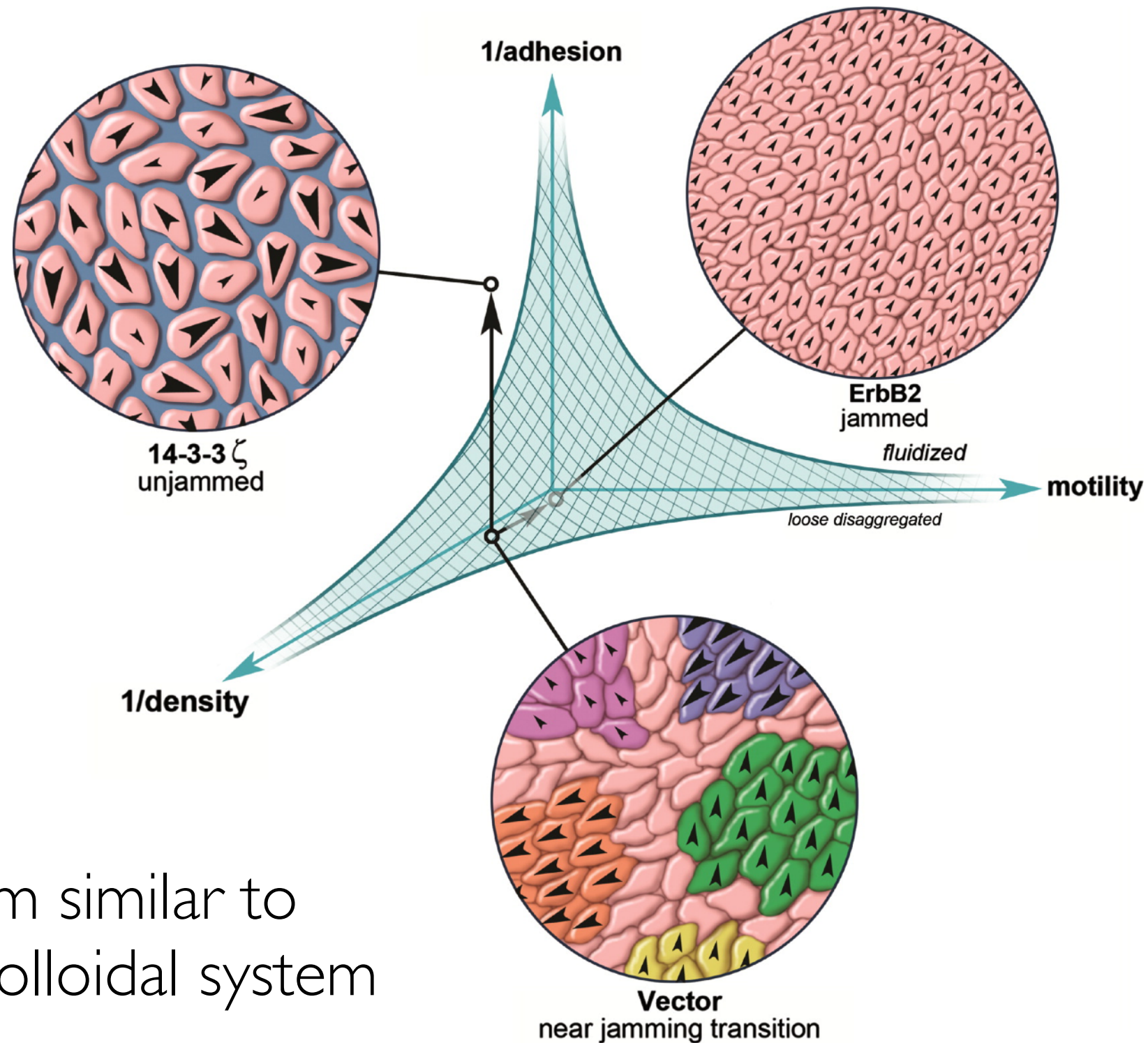
Nonequilibrium Glassy Dynamics of Self-Propelled Hard Disks

Ludovic Berthier

Laboratoire Charles Coulomb, UMR 5221, CNRS and Université Montpellier 2, Montpellier, France

(Received 4 July 2013; revised manuscript received 22 May 2014; published 4 June 2014)

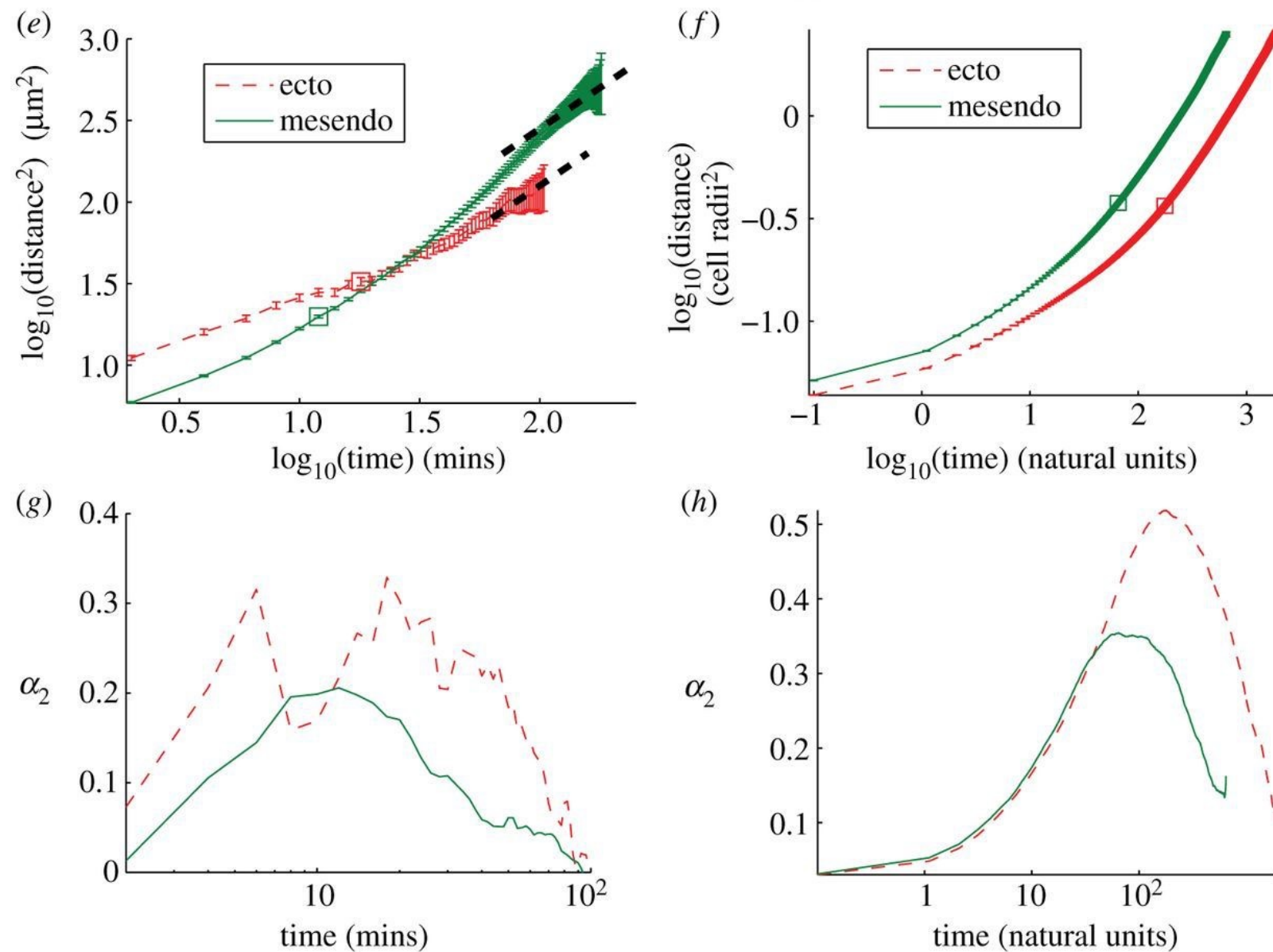
Jamming phase diagram for biological tissue



Cells jam similar to
adhesive colloidal system

Density driven phase transition is
impossible in confluent tissues

Rigidity transition
in confluent tissues?



Ectoderm tissues have longer relaxation timescales => closer to glass transition

Need additional parameter to explain mechanical response in confluent tissues

Mechanical forces acting to regulate cell shapes

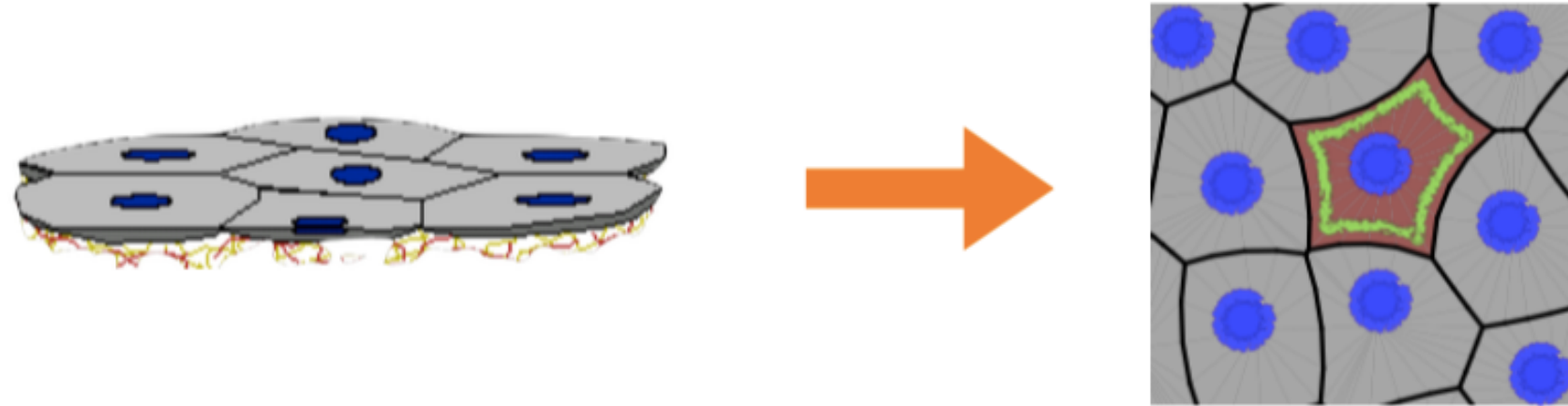
Cell-cell adhesion: cells can stick together

Active cytoskeleton: prevents too much distortion

Fluid filled: volume roughly fixed

Vertex model

How much work is required for a cell to migrate



$$E_{\text{cell}} = k_A (A - A_0)^2 + k_P (P - P_0)^2$$

\mathbf{A} = cross-sectional area
 \mathbf{P} = cross-sectional perimeter

$$= k_A (A - A_0)^2 + k_P (P^2 - 2P_0P + P_0^2)$$

Incompressibility

**actomyosin
contractility**

**Interfacial tension:
adhesion and
cortical tension**

$$\epsilon = \frac{1}{k_A A_0^2} \sum^N E_i = \sum_i [(a_i - 1)^2 + \frac{(p_i - p_0)^2}{r}]$$

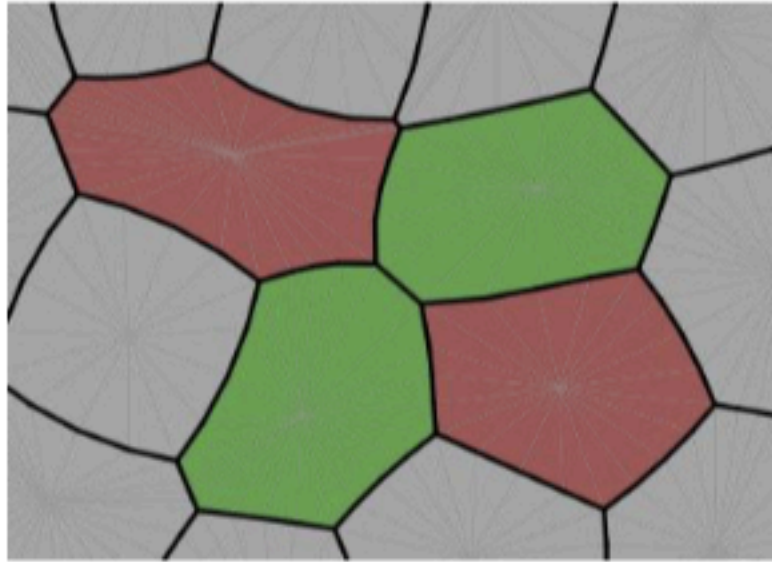
*Non-dimensionalized
energy form*

p_i = rescaled shape function => increases with increasing adhesion

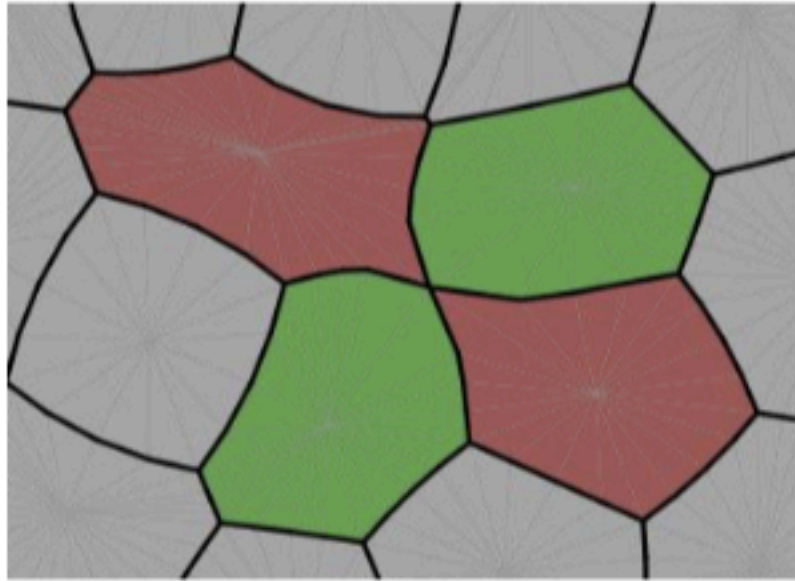
r = ratio between bulk stiffness and interface stiffness

Rearrangement and migration via T1 transition

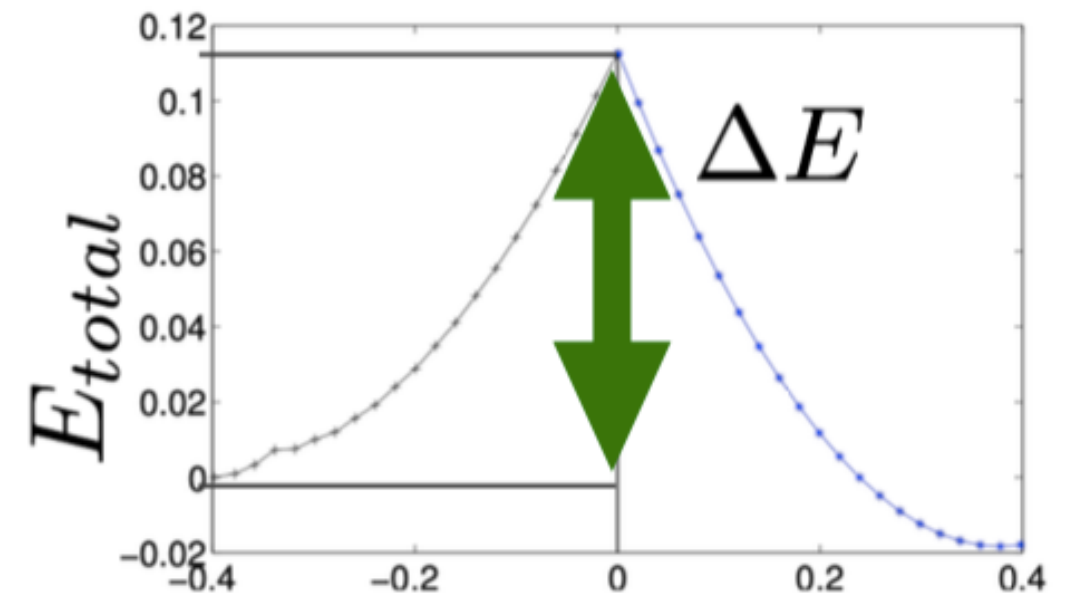
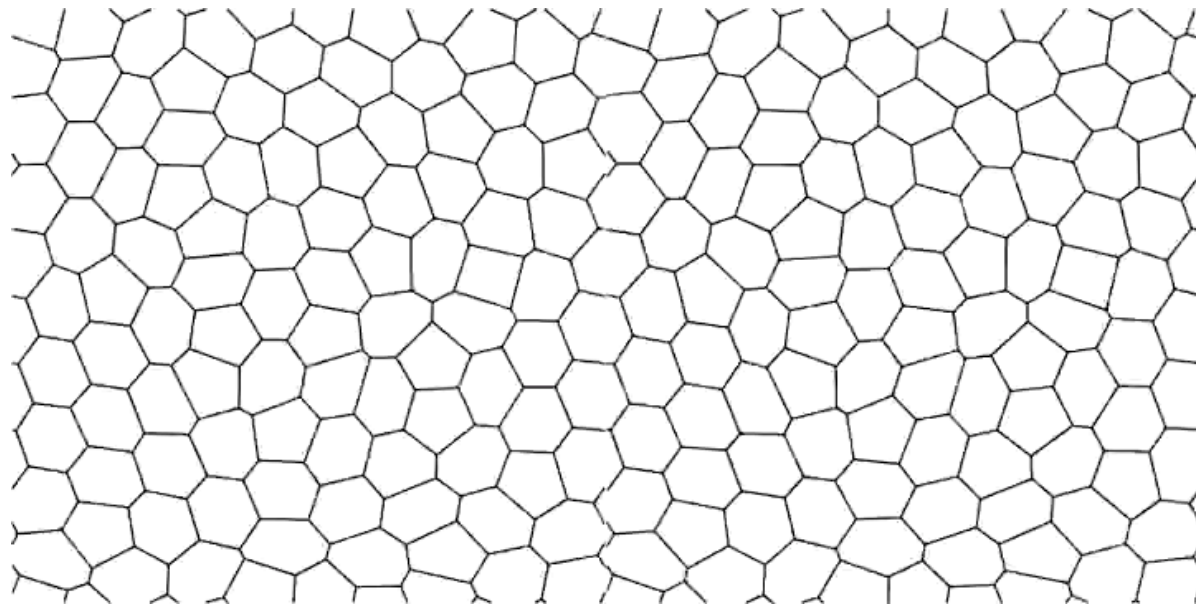
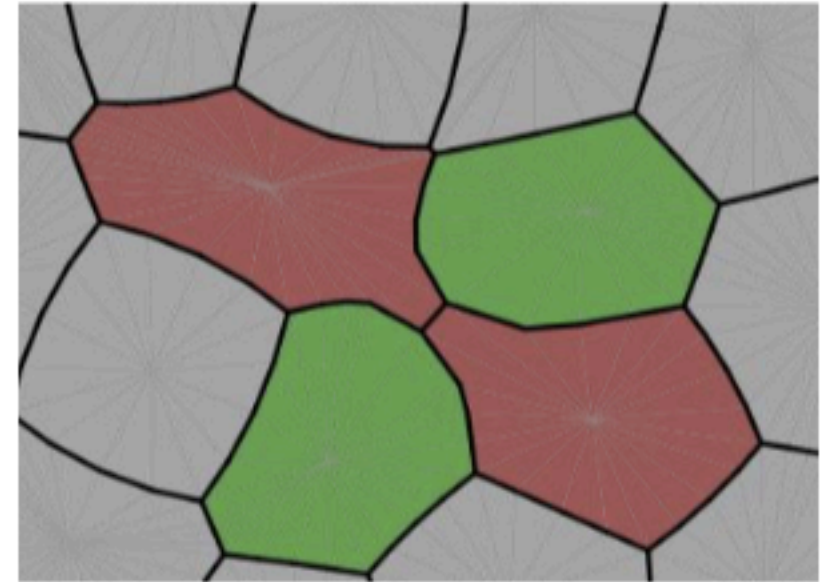
Shrink edge before T-1



At T-1

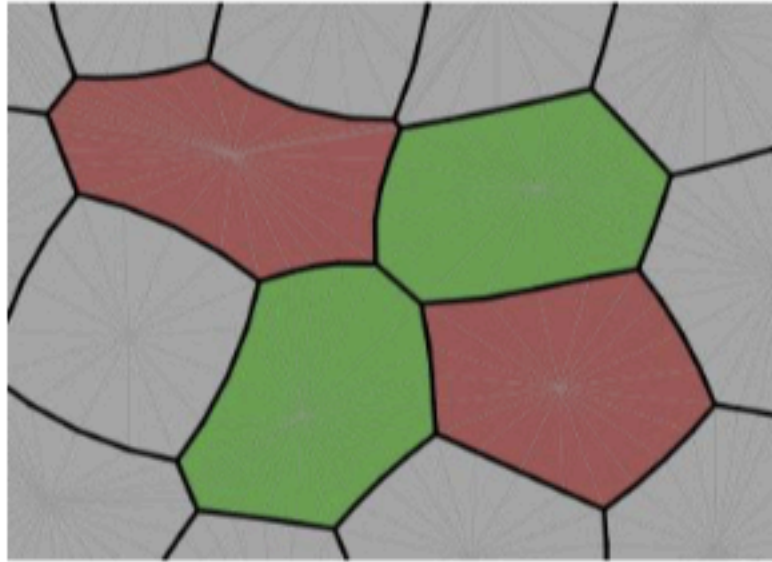


Grow edge after T-1

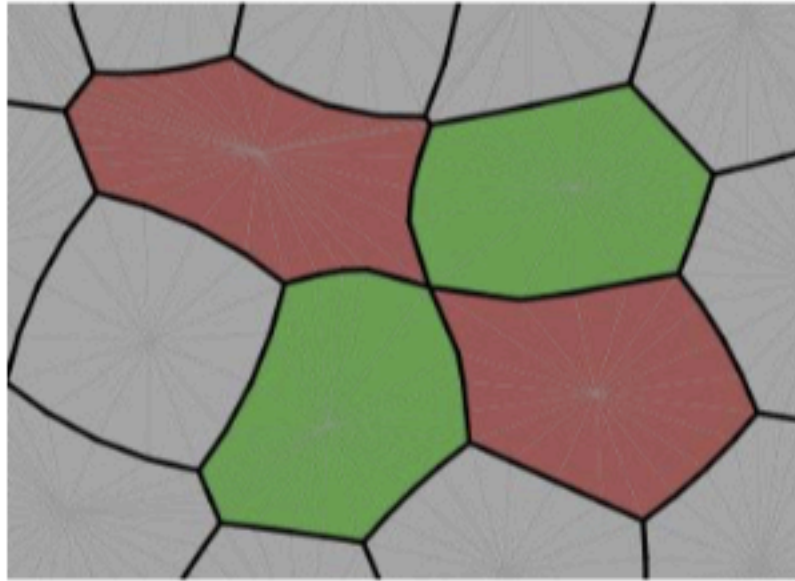


Rearrangement and migration via T1 transition

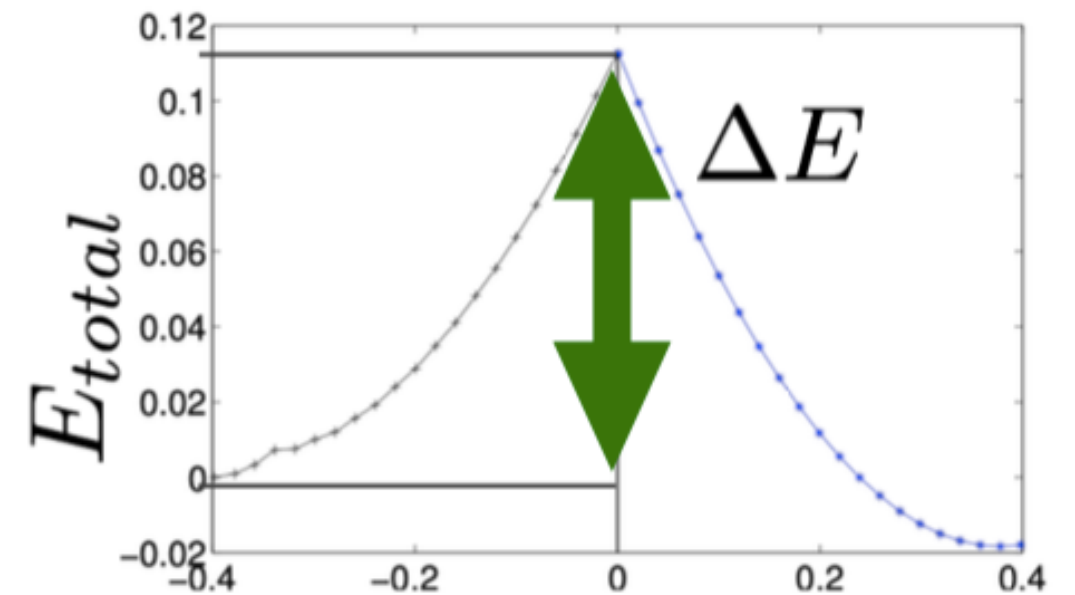
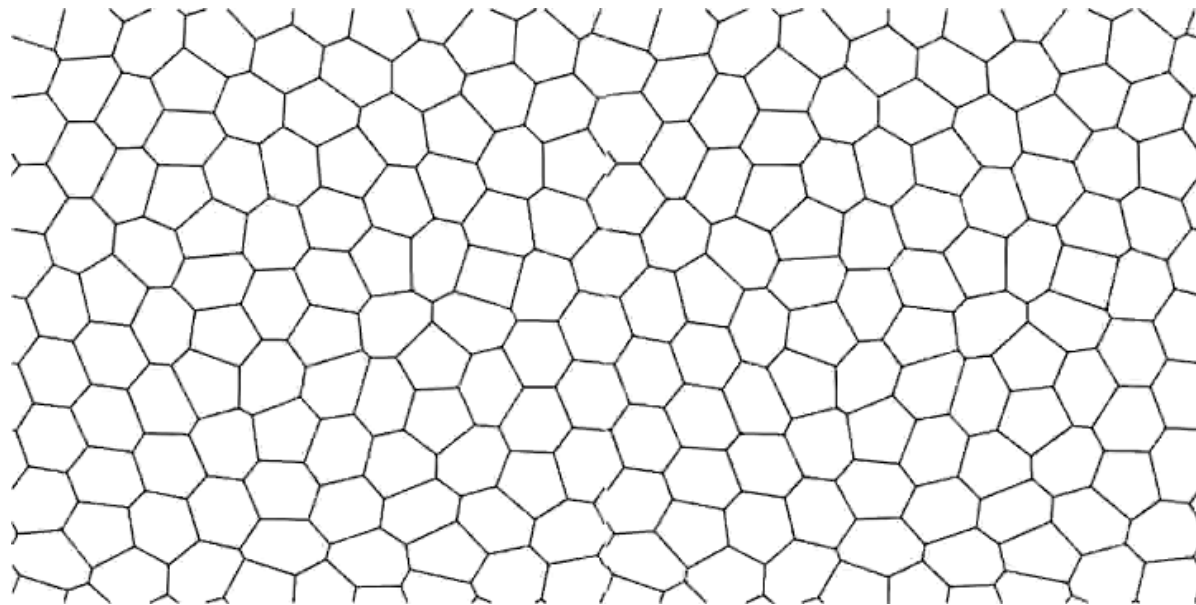
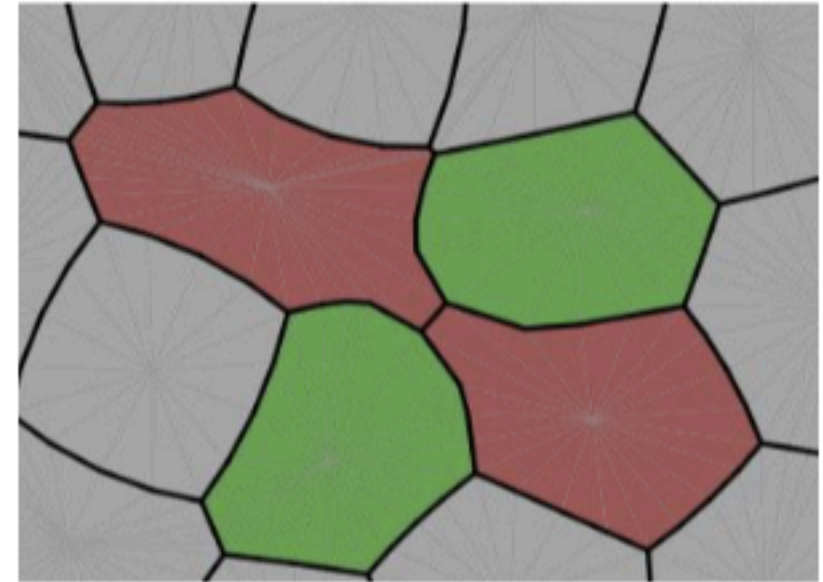
Shrink edge before T-1



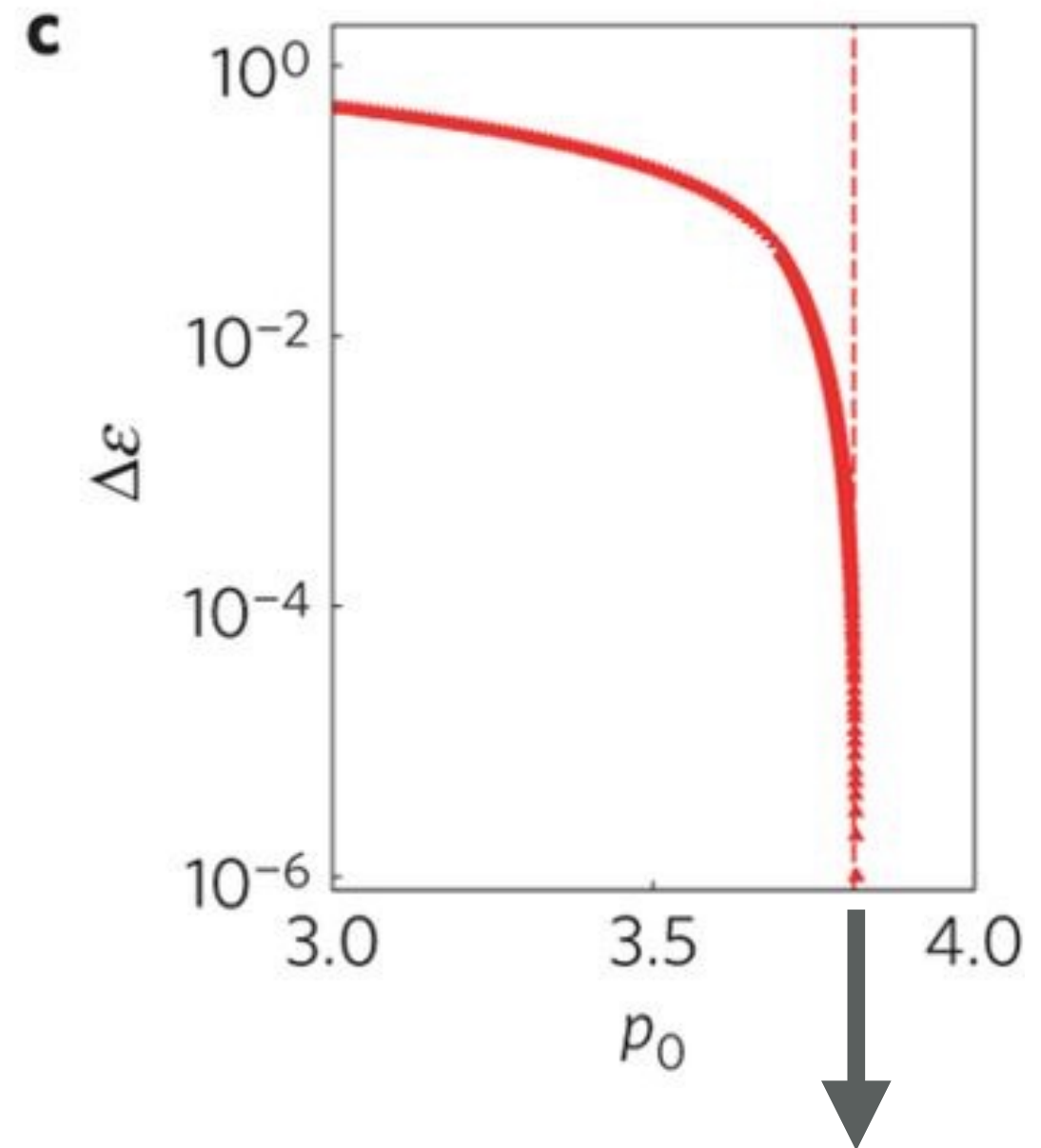
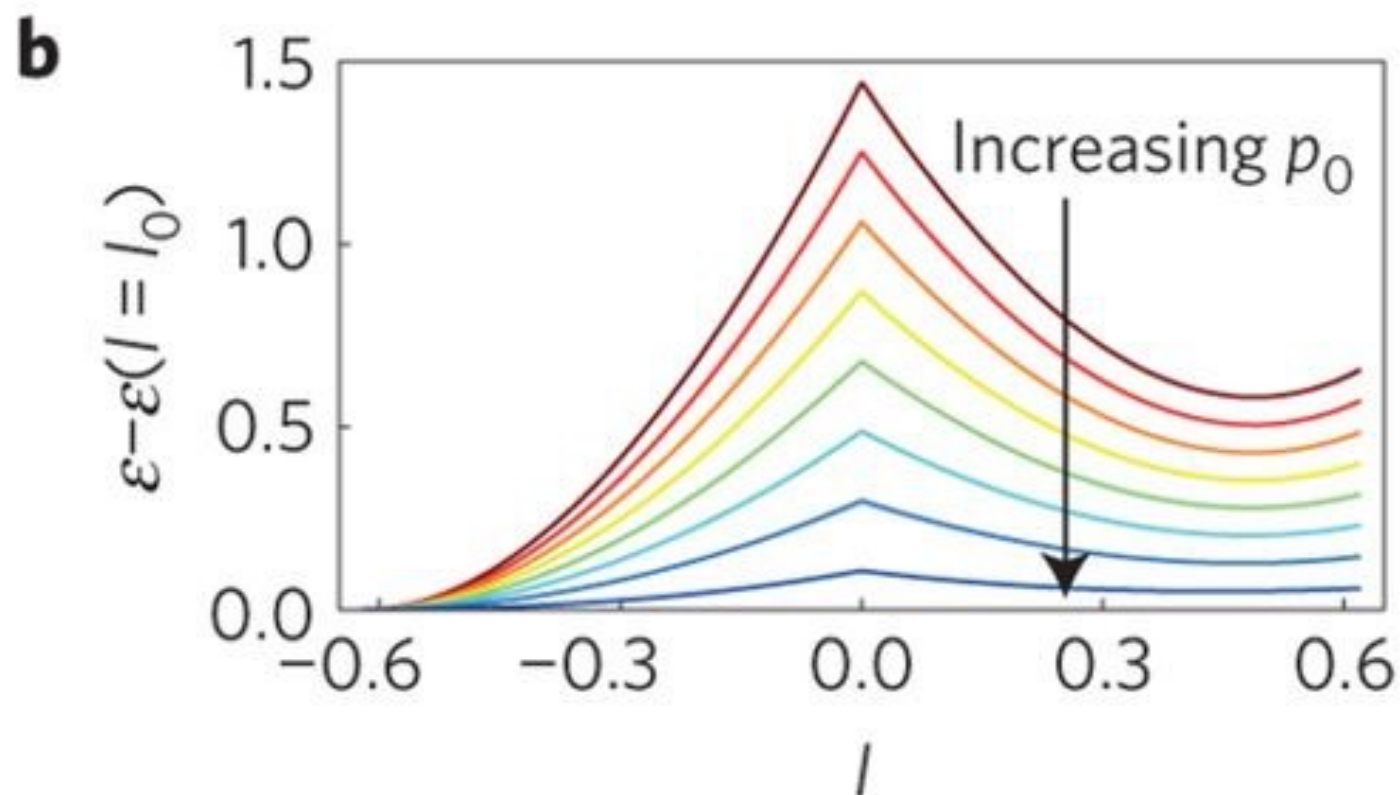
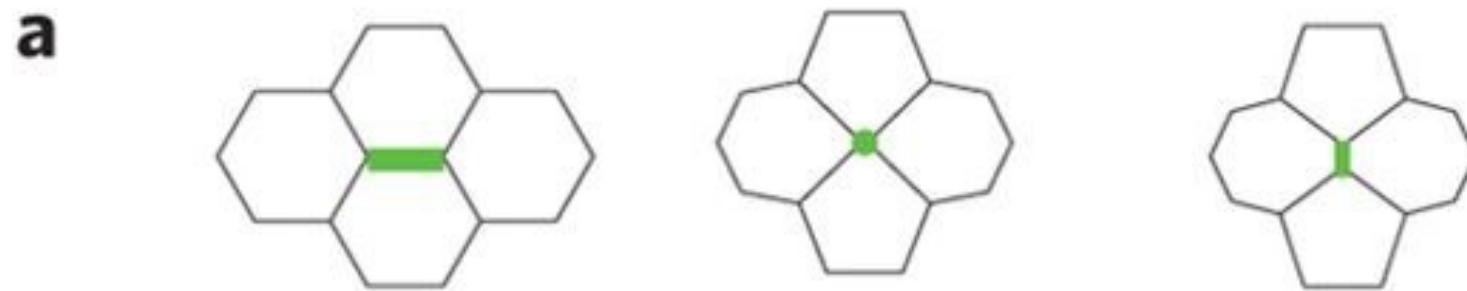
At T-1



Grow edge after T-1



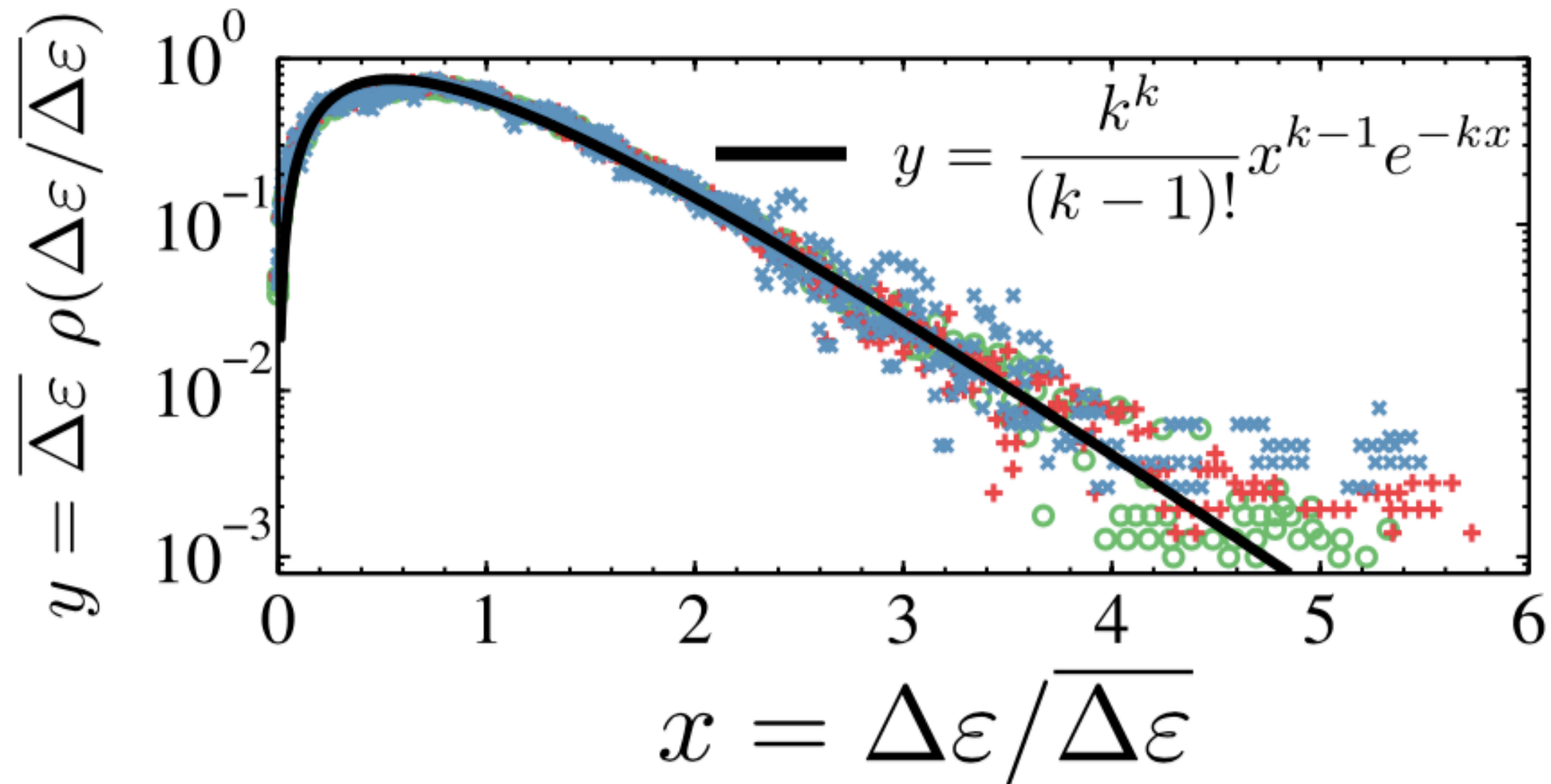
Four-cell model



p_0 is the only control parameter here

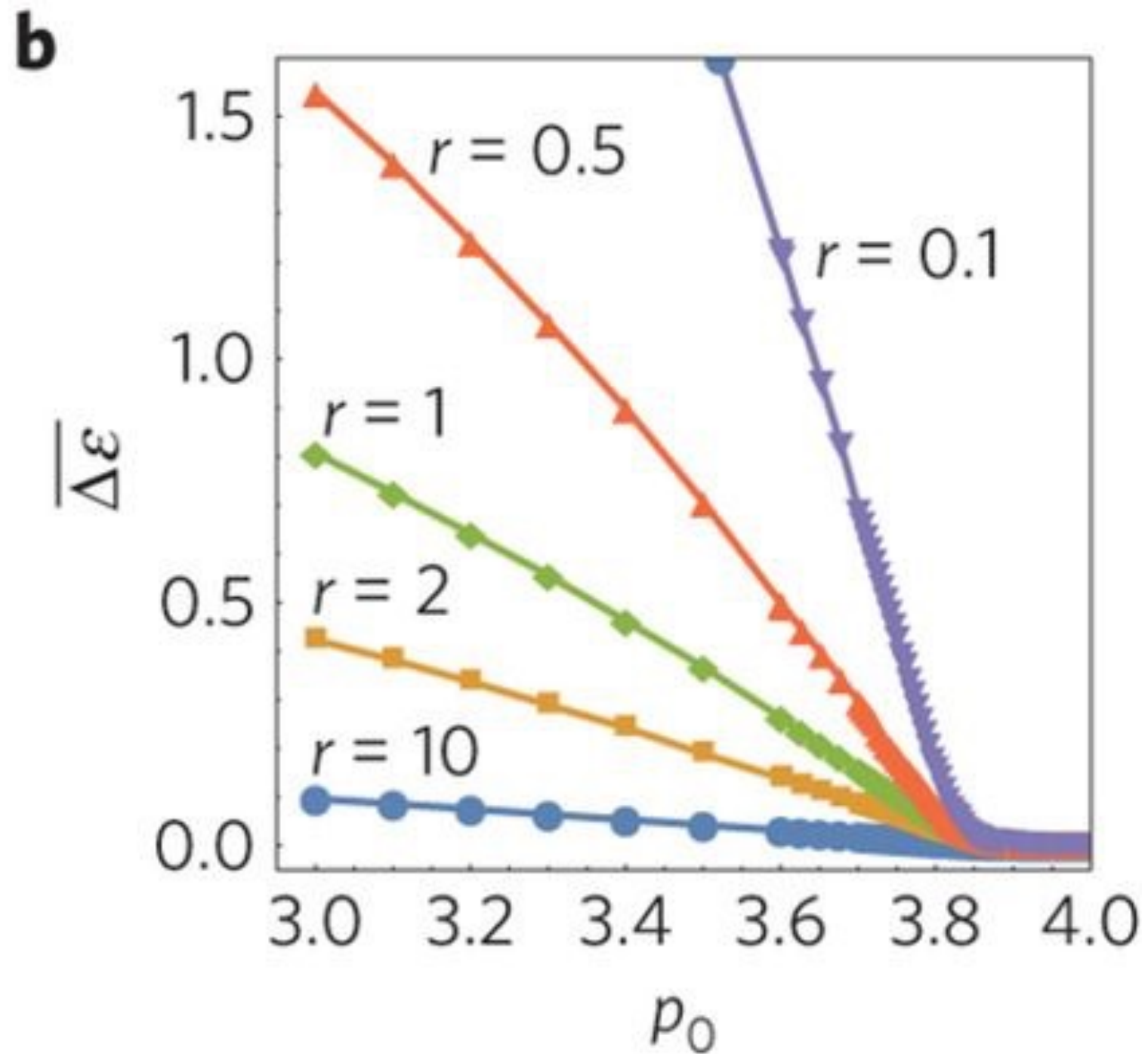
Transition point $p_0^* = 3.813$
 = perimeter of regular
 pentagon with unit area

Energy barrier statistics



Distribution of normalized energy barrier height for a large range of parameters; universal shape with k-gamma distribution

Mean energy barrier completely specifies the distribution and mechanical response



Average energy barrier height vanishes at $p_0^* \sim 3.813$

We know: Jamming in inert matter

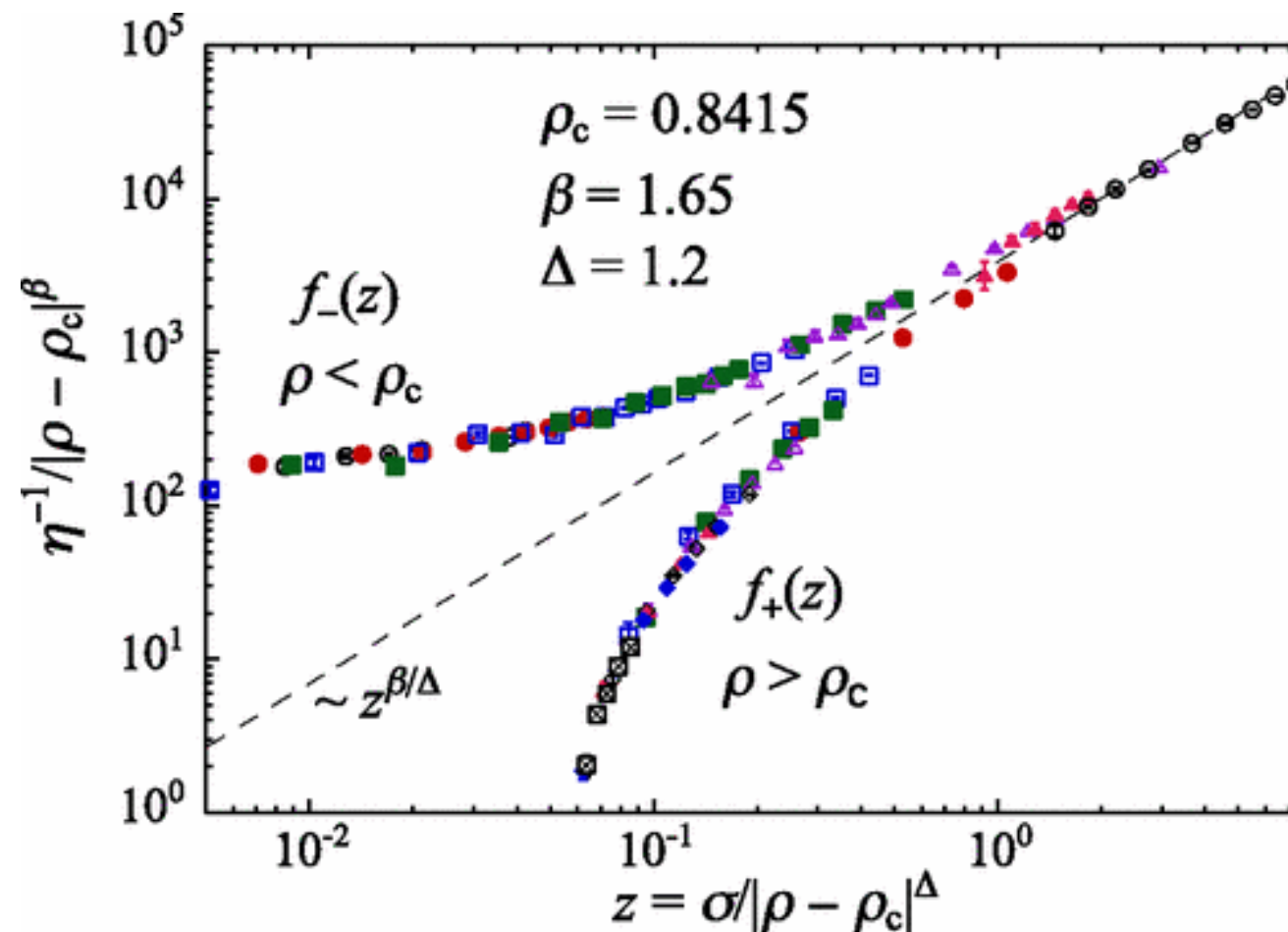
PRL **99**, 178001 (2007)

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26 OCTOBER 2007

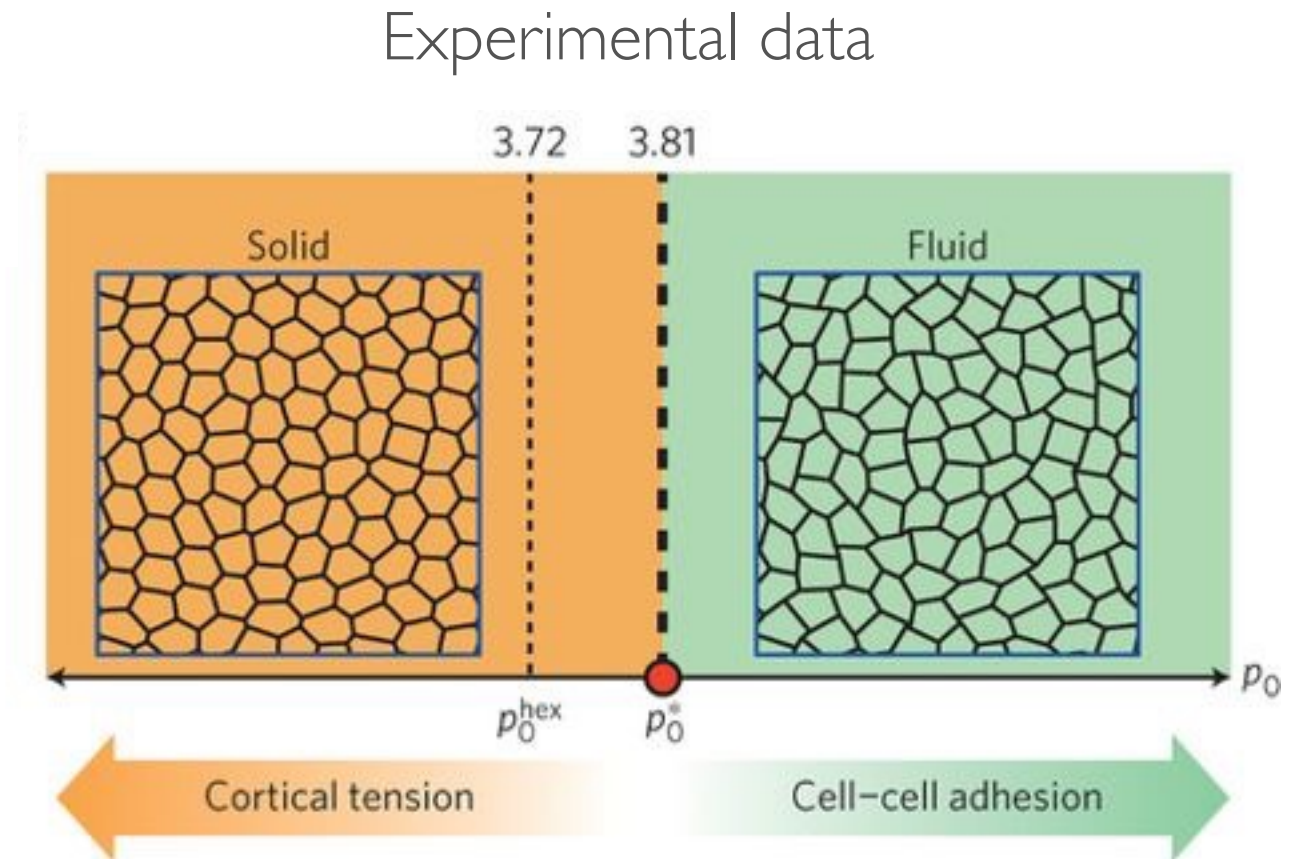
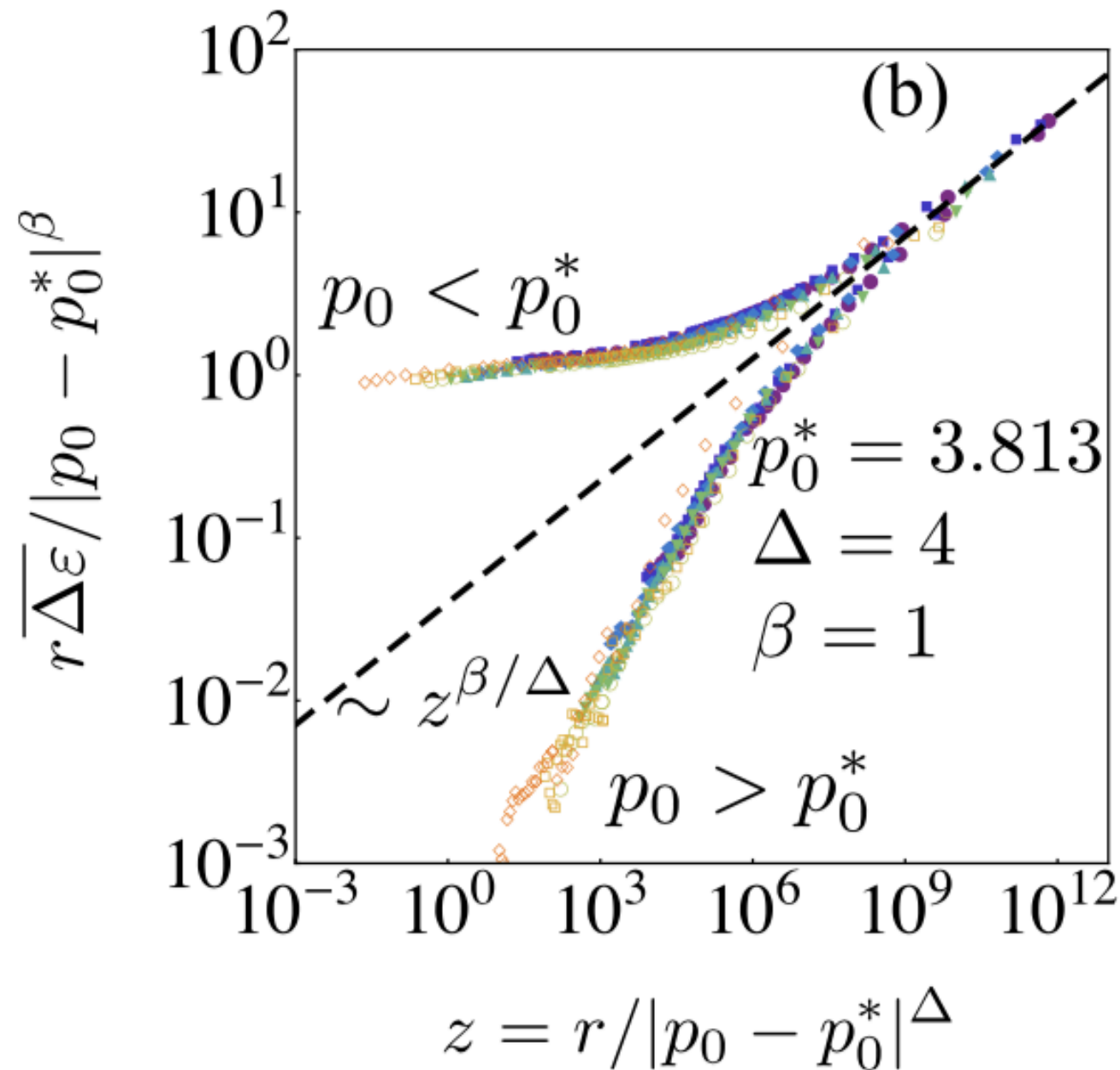
Critical Scaling of Shear Viscosity at the Jamming Transition

Peter Olsson¹ and S. Teitel²



Jamming is controlled by: $\rho - \rho_c$

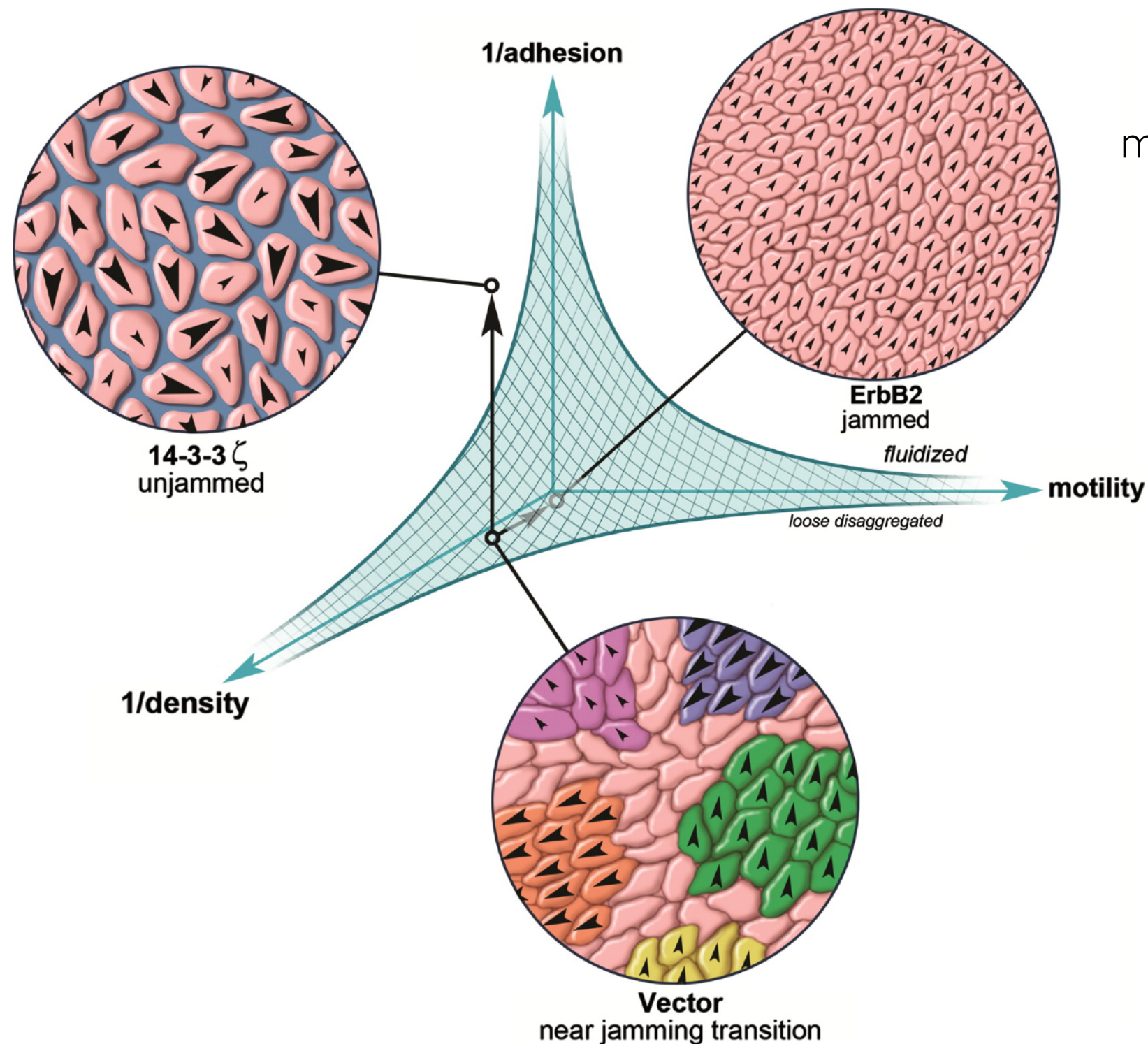
Rigidity transition controlled by p_0



Equivalence

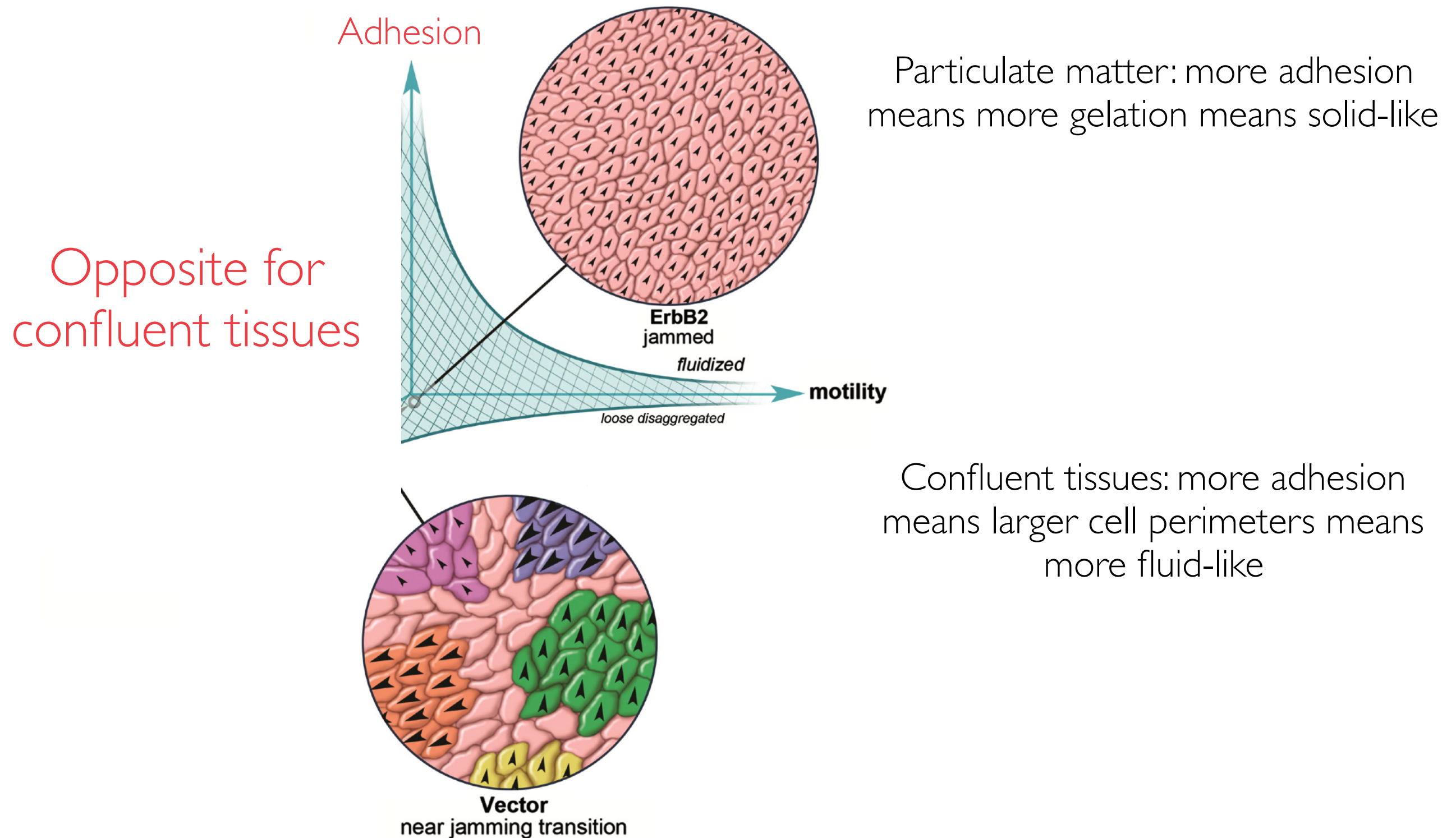
Inert matter	Biological tissues
Yield stress	Average energy barrier height
Strain rate	Inverse perimeter modulus r
Density	Preferred perimeter p_0

Modified Jamming phase diagram for biological tissue

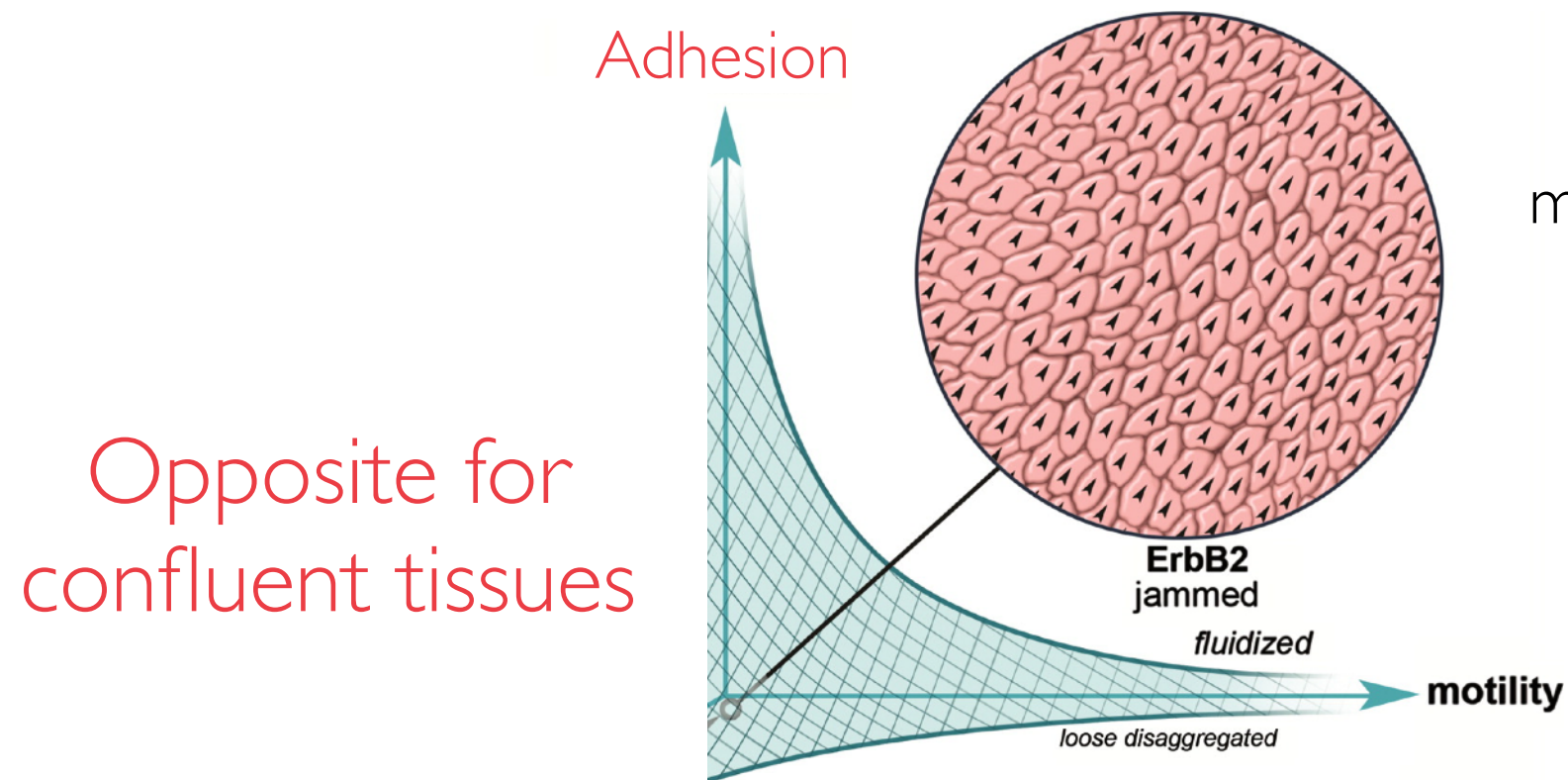


Particulate matter: more adhesion means more gelation means solid-like

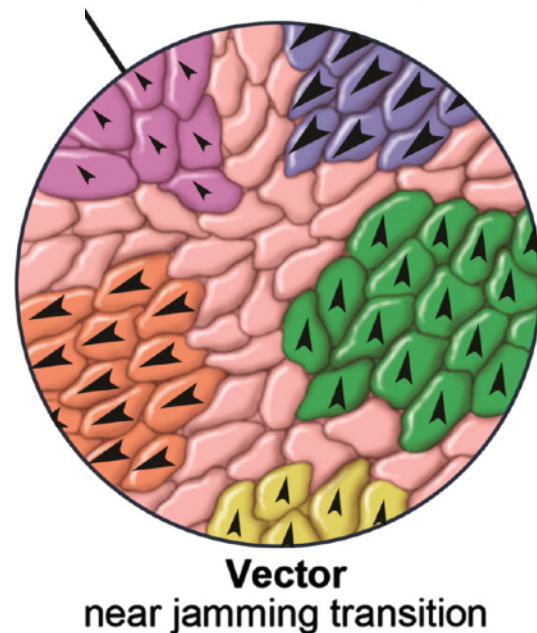
Modified Jamming phase diagram for biological tissue



Modified Jamming phase diagram for biological tissue



Particulate matter: more adhesion means more gelation means solid-like



Confluent tissues: more adhesion means larger cell perimeters means more fluid-like

More adhesion can lead to unjamming in tissues

Confluent tissues with motility?

Confluent tissues with mitosis
and apoptosis?

Confluent tissues with motility?

Confluent tissues with mitosis
and apoptosis?

Active vertex model